# Overflow-Master

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5

6

for (int i = 0; i < n - 1; ++i) {

for (int j = 0; j < n; ++j) {

## 1 Template

#### 1.1 C++ Template

```
#include <bits/stdc++.h>
   using namespace std;
   #define L(i, j, n) for (int i = (j); i < (int)n; i++)
   #define LI(i, j, n) for (int i = (j); i \le (int)n; i++)
   #define R(i, j, n) for (int i = (j); i > (int)n; i--)
   #define RI(i, j, n) for (int i = (j); i \ge (int)n; i--)
   #define SZ(x) int((x).size())
   #define ALL(x) begin(x), end(x)
   #define vec vector
   #define pb push_back
11
   using ll = long long;
12
   using ld = long double;
   using pii = pair<int, int>;
   using pll = pair<ll, ll>;
16
   const int MOD = (int)1e9 + 7;
   const int oo = (int)1e9;
18
19
   void solve() {}
21
   int main() {
22
       ios::sync_with_stdio(false);
23
       cin.tie(nullptr);
^{24}
       freopen("input.txt", "r", stdin);
^{25}
       freopen("output.txt", "w", stdout);
26
       int TT = 1;
27
       // cin >> TT;
28
       while (TT--) {
29
           solve();
30
       }
31
       return 0;
32
33 | }
```

#### 1.2 Policy Based

```
#include <ext/pb_ds/assoc_container.hpp>
using namespace __gnu_pbds;
template <typename Key, typename Val = null_type>
```

```
using indexed_set =
       tree<Key, Val, less<Key>, rb_tree_tag,
           tree_order_statistics_node_update>;
  // indexed_set<char> s;
  // char val = *s.find_by_order(0); // access por indice
  // int idx = s.order_of_key('a'); // busca indice del valor
   template <class Key, class Val = null_type>
   using htable = gp_hash_table<Key, Val>;
11 // como unordered_map (o unordered_set si Val es vacio), pero sin metodo
        count
                                    Graph
                              2.1 Dijkstra
vec<pll> G[N];
   vec<ll> dijk(ll s) {
       vec<ll> dist(N, oo);
       dist[s] = 0;
       priority_queue<pll, vec<pll>, greater<pll>> pq;
       pq.push({011, s});
6
       while (!q.empty()) {
           auto [d, u] = pq.top();
           pq.pop();
           if (d != dist[u]) continue;
           for (auto [v, w] : G[u]) {
11
               if (dist[v] > d + w) {
                   dist[v] = d + w;
13
                   pq.push({dist[v], v});
15
           }
16
       }
17
       return dist;
18
19 }
                                 Bellman-Ford
1 | void bellmanFord(int n, int source, vec<vec<pii>>> &g, vec<int>> &d) {
       d.assign(n, INT_MAX);
       d[source] = 0;
3
4
```

```
for (auto &[a, c] : g[j]) {
7
                   if (d[j] != INT_MAX && d[a] > d[j] + c) {
8
                       d[a] = d[j] + c;
9
10
               }
11
12
13
14 }
                          2.3 Floyd-Warshall
  const int N = 10;
   int G[N][N];
   L(k, 0, n)
3
      L(i, 0, n)
4
           L(j, 0, n)
5
               G[i][j] = min(G[i][j], G[i][k] + G[k][j]);
6
                           2.4 Disjoint Sets
  struct UFDS {
       vi p, size;
2
       int numSets, n;
       UFDS(int n) : p(n), size(n, 1), n(n) {
           for (int i = 0; i < n; i++) p[i] = i;
5
           numSets = n;
6
7
       int find(int i) { return (p[i] == i) ? i : (p[i] = find(p[i])); }
8
       void join(int i, int j) {
           int a = find(i), b = find(j);
10
           if (a != b) {
11
               if (size(b) && size(a)) swap(a, b);
12
               p[b] = a;
13
               size[a] += size[b];
14
               numSets--;
15
           }
16
17
18 | };
                               2.5 Kruskal
1 | struct Edge {
2
       int w, u, v;
       Edge(int wx, int ux, int vx) { w = wx, u = ux, v = vx; }
3
```

```
bool operator<(const Edge &other) const { return w < other.w; }</pre>
   };
5
 6
   int main() {
       int V, E;
       cin >> V >> E;
       vector<Edge> EL(E);
       for (int i = 0; i < E; i++) {
           int u, v, w;
12
           cin >> u >> v >> w;
           EL[i] = Edge(w, u, v);
14
15
       sort(EL.begin(), EL.end());
16
       int mst_cost = 0, num_taken = 0;
       UFDS UF(V);
18
       for (auto &[w, u, v] : EL) {
           if (UF.isSameSet(u, v)) continue;
20
           mst_cost += w;
21
           UF.unionSet(u, v);
22
           ++num_taken;
           if (num_taken == V - 1) break;
24
       }
25
26
       return 0;
27
28 }
                                 2.6 Prim
 #include <bits/stdc++.h>
   using namespace std;
3
   typedef pair<int, int> pii;
   vector<vector<pii>>> AL;
   vector<int> taken;
   priority_queue<pii, vector<pii>, greater<pii>> pq;
   void process(int u) {
       taken[u] = 1;
10
       for (auto &[v, w] : AL[u]) {
11
```

if (!taken[v]) {

}

}

pq.emplace(w, v);

12

13

14

15

13

```
16 }
                                                                                                   dfs_low[u] = min(dfs_low[u], dfs_low[v]);
                                                                                   14
                                                                                                   if (dfs_low[v] > dfs_num[u]) {
17
                                                                                   15
                                                                                                       // Bridge from u -> v
   int main() {
18
                                                                                    16
       int V, E;
                                                                                                        cout << "Bridge_" << u << "_->_" << v << "\n";
19
                                                                                   17
                                                                                                   }
       cin >> V >> E;
20
                                                                                    18
       AL.assign(V, vector<pii>());
                                                                                                   if (dfs_low[v] >= dfs_num[u]) {
21
                                                                                    19
       for (int i = 0; i < E; i++) {
                                                                                                       // u is AP
^{22}
                                                                                   20
                                                                                                        ap[u] = 1;
           int u, v, w;
23
                                                                                   21
           cin >> u >> v >> w;
                                                                                                   }
^{24}
                                                                                   22
           AL[u].emplace_back(v, w);
                                                                                               } else
25
                                                                                   23
           AL[v].emplace_back(u, w);
                                                                                                   dfs_low[u] = min(dfs_low[u], dfs_num[v]);
26
                                                                                   24
       }
                                                                                           }
27
                                                                                   25
       taken.assign(V, 0);
                                                                                           if (u == root) {
28
                                                                                   26
       process(0);
                                                                                               ap[u] = child > 1;
                                                                                   27
29
       int mst_cost = 0, num_taken = 0;
                                                                                           }
                                                                                   28
30
       while (!pq.empty()) {
                                                                                    29 }
31
           auto [w, u] = pq.top();
32
                                                                                                                     2.8 SCC
           pq.pop();
33
           if (taken[u]) continue:
34
           mst_cost += w;
                                                                                    1 struct SCC {
35
           process(u);
36
                                                                                           int n;
           ++num_taken;
37
                                                                                           vec<vec<int>> G, G2;
                                                                                    3
           if (num_taken == V - 1) break;
38
                                                                                           vec<int> order, sccId, vi;
                                                                                    4
39
                                                                                           vec<vec<int>> components;
                                                                                    5
       cout << "MST_cost:" << mst_cost << endl;</pre>
                                                                                           int sccCount;
40
                                                                                    6
       return 0;
41
                                                                                    7
42 }
                                                                                           SCC(int n) : n(n) {
                                                                                    8
                                                                                               G.assign(n, vec<int>());
                                                                                    9
                                      Tarjan
                                2.7
                                                                                               G2.assign(n, vec<int>());
                                                                                    10
                                                                                               sccId.assign(n, -1);
                                                                                   11
   vector<int> G[N];
                                                                                               sccCount = 0;
                                                                                   12
   vector<int> dfs_low(N, -1), dfs_num(N, -1),
                                                                                           }
2
                                                                                   13
       ap(N, 0); // ap for Articulation Points
                                                                                   14
   int dfs_count = 0;
                                                                                           void addEdge(int u, int v) {
                                                                                   15
   int root = -1; // For AP
                                                                                               G[u].pb(v);
                                                                                   16
   void dfs(int u, int p = -1) {
                                                                                               G2[v].pb(u);
                                                                                   17
6
                                                                                           }
       dfs_low[u] = dfs_num[u] = dfs_count++;
                                                                                   18
       int child = 0:
8
                                                                                   19
       for (int v : G[u]) {
                                                                                           void dfs1(int u) {
                                                                                   20
9
           if (v == p) continue;
                                                                                               vi[u] = 1;
                                                                                   21
10
           if (dfs_num[v] == -1) {
                                                                                               for (int v : G[u]) {
11
                                                                                   22
                child++;
                                                                                                   if (!vi[v]) dfs1(v);
                                                                                   23
12
                dfs(v, u);
                                                                                               }
```

24

```
order.pb(u);
25
       }
                                                                                                   }
26
                                                                                   69
                                                                                              }
27
                                                                                   70
       void dfs2(int u, int id) {
                                                                                              return sccGraph;
                                                                                   71
28
           vi[u] = 1;
                                                                                          }
                                                                                   72
29
           sccId[u] = id;
30
                                                                                   73
           components[id].pb(u);
                                                                                          int getSCCId(int u) { return sccId[u]; }
                                                                                   74
31
           for (int v : G2[u]) {
                                                                                          vec<int> getSCC(int i) { return components[i]; }
                                                                                   75
32
                                                                                          int getCount() { return sccCount; }
               if (!vi[v]) dfs2(v, id);
33
                                                                                   76
                                                                                   77 | };
34
       }
35
                                                                                                                 2.9 Euler-Tour
36
       void findSCC() {
37
           vi.assign(n, 0);
                                                                                    1 struct edge {
38
           order.clear();
39
                                                                                          int y;
           L(i, 0, n) {
40
               if (!vi[i]) dfs1(i);
41
           }
                                                                                          edge(int y) : y(y) {}
42
                                                                                   4
                                                                                      };
43
                                                                                    5
           vi.assign(n, 0);
44
           sccCount = 0;
                                                                                      list<edge> g[N];
45
           components.clear();
46
                                                                                      void add_edge(int a, int b) {
47
           reverse(ALL(order));
                                                                                          g[a].push_front(edge(b));
48
                                                                                   10
           for (int u : order) {
                                                                                          auto ia = g[a].begin();  // NO DIRIGIDOS
49
                                                                                   11
               if (!vi[u]) {
                                                                                          g[b].push_front(edge(a)); // NO DIRIGIDOS
50
                                                                                   12
                    components.pb(vec<int>());
                                                                                          auto ib = g[b].begin();  // NO DIRIGIDOS
51
                                                                                   13
                   dfs2(u, sccCount++);
                                                                                          ia->rev = ib;
                                                                                                                      // NO DIRIGIDOS
52
                                                                                   14
               }
                                                                                          ib->rev = ia;
                                                                                                                      // NO DIRIGIDOS
53
                                                                                   15
           }
                                                                                      }
54
                                                                                   16
       }
55
                                                                                   17
56
                                                                                      vec<int> p;
                                                                                   18
       vec<vec<int>> getCondensedGraph() {
57
                                                                                   19
           vec<vec<int>> sccGraph(sccCount);
                                                                                      void go(int x) {
58
                                                                                   20
           set<pii> edges;
                                                                                          while (SZ(g[x])) {
59
                                                                                   21
                                                                                              int y = g[x].front().y;
60
                                                                                   22
           L(u, 0, n) {
                                                                                              g[y].erase(g[x].front().rev); // NO DIRIGIDOS: eliminar
61
                                                                                   23
               for (int v : G[u]) {
                                                                                              g[x].pop_front();
62
                                                                                   24
                   int fromScc = sccId[u], toScc = sccId[v];
                                                                                              go(y);
63
                                                                                   25
                   if (fromScc != toScc &&
                                                                                          }
64
                                                                                   26
                        edges.find({fromScc, toScc}) == edges.end()) {
65
                                                                                   27
                                                                                          p.pb(x);
                       sccGraph[fromScc].pb(toScc);
                                                                                   28 }
66
                        edges.insert({fromScc, toScc});
67
                                                                                   29
```

```
}
68
       list<edge>::iterator rev; // NO DIRIGIDOS: iterador para arista
```

```
vec<int> get_path(int x) {
       p.clear();
31
       go(x);
32
       reverse(ALL(p));
33
       return p;
34
35
36
   void solve() {
37
       int n, m;
38
       cin >> n >> m;
39
40
       // vec<int> inDeg(n, 0), outDeg(n, 0); // DIRIGIDOS
41
       vec<int> deg(n, 0); // NO DIRIGIDOS
42
43
       L(i, 0, m) {
44
           int a, b;
45
           cin >> a >> b;
46
           a--;
47
           b--;
48
           add_edge(a, b);
49
           // inDeg[b]++; // DIRIGIDOS
50
           // outDeg[a]++; // DIRIGIDOS
51
           deg[a]++; // NO DIRIGIDOS
52
           deg[b]++; // NO DIRIGIDOS
53
       }
54
55
       // DIRIGIDOS (camino euleriano):
56
       // Nodo 0: outDeg[0] = inDeg[0] + 1 (nodo inicial)
57
       // Nodo n-1: inDeg[n-1] = outDeg[n-1] + 1 (nodo final)
58
       // Resto: inDeg[i] = outDeg[i]
59
       // L(i, 1, n - 1) {
60
              if (inDeg[i] != outDeg[i]) {
61
                   cout << "IMPOSSIBLE\n";</pre>
62
       //
                   return:
63
       //
             }
64
65
       // if (outDeg[0] != inDeg[0] + 1 || inDeg[n - 1] != outDeg[n - 1] +
66
           1) {
              cout << "IMPOSSIBLE\n";</pre>
67
       //
               return;
68
       // }
69
70
       // NO DIRIGIDOS: verificar que todos los grados sean pares
71
```

```
L(i, 0, n) {
72
            if (deg[i] % 2) {
73
                 cout << "IMPOSSIBLE\n";</pre>
74
                 return;
75
            }
76
        }
78
        vec<int> path = get_path(0);
80
        if (SZ(path) != m + 1) {
81
            cout << "IMPOSSIBLE\n";</pre>
82
        } else {
83
            for (auto x : path) {
84
                 cout << x + 1 << "";
            }
86
            cout << "\n";
87
       }
88
89 }
```

## 3 Dynamic Programming

#### 3.1 Knapsack

```
void solve() {
        vec<int> prices(n);
        vec<int> pages(n);
        \text{vec}<\text{vec}<\text{int}>> dp(n + 1, \text{vec}<\text{int}>(x + 1, 0));
        for (int i = 0; i < n; i++) {
5
            for (int j = 0; j \le x; j++) {
6
                 if (prices[i] <= j) {</pre>
7
                      dp[i + 1][j] = max(dp[i][j], pages[i] + dp[i][j - prices
8
                          [i]]);
                 } else {
                      dp[i + 1][j] = dp[i][j];
                 }
            }
12
        }
13
14 }
```

#### 3.2 LIS

```
int lis(vector<int>& arr) {
  int n = arr.size();
```

```
vector<int> lis(n, 1);
                                                                                                   }
3
                                                                                   17
                                                                                              }
       for (int i = 1; i < n; i++) {
                                                                                   18
4
           for (int prev = 0; prev < i; prev++) {</pre>
                                                                                          }
                                                                                   19
5
               if (arr[i] > arr[prev] && lis[i] < lis[prev] + 1) {</pre>
                                                                                          return dp[n][m];
                                                                                   20
6
                   lis[i] = lis[prev] + 1;
                                                                                   21 }
8
                                                                                                                   4 Search
           }
9
       }
10
       return *max_element(lis.begin(), lis.end());
                                                                                                               4.1 Binary Search
11
12 | }
                                                                                    int binSearch(int arr[], int low, int high, int x) {
                                 3.3 LCS
                                                                                          while (low <= high) {</pre>
                                                                                               int mid = low + (high - low) / 2;
                                                                                   3
   int lcs(string &S1, string &S2) {
                                                                                               if (arr[mid] == x) return mid;
       \text{vec}<\text{vec}<\text{int}>> dp(m + 1, \text{vec}<\text{int}>(n + 1, 0));
2
                                                                                               if (arr[mid] < x)</pre>
       for (int i = 1; i <= m; ++i) {
3
                                                                                                   low = mid + 1;
                                                                                    6
           for (int j = 1; j \le n; ++j) {
4
                                                                                    7
               if (S1[i - 1] == S2[i - 1])
                                                                                                   high = mid - 1;
                                                                                    8
                    dp[i][j] = dp[i - 1][j - 1] + 1;
                                                                                          }
                                                                                    9
               else
                                                                                          return -1;
                                                                                   10
                    dp[i][j] = max(dp[i-1][j], dp[i][j-1]);
                                                                                   11 }
           }
9
       }
10
                                                                                                              4.2 Sliding Window
       return dp[m][n];
11
12 }
                                                                                    int main() {
                            3.4 Edit Distance
                                                                                          int cant = 0, start = 0, end = 0, sum = 0;
                                                                                          while (end < n) {
                                                                                   3
  int editDistance(string& s1, string& s2) {
                                                                                               while (end < n && sum < x) {
                                                                                    4
                                                                                                   sum += arr[end];
       int n = s1.length(), m = s2.length();
2
                                                                                   5
       vector<vector<int>> dp(n + 1, vector<int>(m + 1));
                                                                                                   end++;
3
                                                                                    6
                                                                                    7
4
       // Base cases
                                                                                               while (start <= end && sum > x) {
5
       for (int i = 0; i \le n; i++) dp[i][0] = i;
                                                                                                   sum -= arr[start];
6
       for (int j = 0; j \le m; j++) dp[0][j] = j;
                                                                                                   start++;
                                                                                   10
8
                                                                                   11
       for (int i = 1; i <= n; i++) {
                                                                                               if (sum == x) {
                                                                                   12
9
           for (int j = 1; j \le m; j++) {
                                                                                                   cant++;
                                                                                   13
10
               if (s1[i - 1] == s2[i - 1]) {
                                                                                                   sum -= arr[start]:
11
                                                                                   14
                    dp[i][j] = dp[i - 1][j - 1];
                                                                                                   start++;
                                                                                   15
12
               } else {
                                                                                               }
                                                                                   16
13
                    dp[i][j] = 1 + min({dp[i - 1][j],}
                                                                                          }
                                                            // deletion
                                                                                   17
14
                                                           // insertion
                                        dp[i][j - 1],
                                                                                   18
                                                                                          cout << cant;</pre>
15
                                         dp[i - 1][j - 1]}); // replacement
                                                                                          return 0;
                                                                                   19
16
```

```
20 |}
                                  Count Bits
                             4.3
  |void update_bits_and_sum(long mask, vec<int> &bits_used, long long &sum)
       for (long j = mask; j > 0; j &= j - 1) {
2
           int bit = __builtin_ctzll(j); // lowest bit ON (0-index)
3
           if (bits_used[bit] == 0) {
4
               sum += (1LL << bit);</pre>
5
6
           bits_used[bit]++;
7
8
  |}
9
                                    Queries
```

### ·

## 5.1 Fenwick Tree (BIT)

```
1 #include <bits/stdc++.h>
   #define ll long long
   #define MOD 100000007
   using namespace std;
   const int MAXN = 200000;
   11 BIT[MAXN + 1]; // Array para el BIT
   ll arr[MAXN + 1]; // Array original
   void update(int idx, ll delta, int n) {
10
       while (idx \le n) {
11
           BIT[idx] += delta;
12
           idx += idx & -idx;
13
14
   }
15
16
   11 query(int idx) {
17
       11 sum = 0;
18
       while (idx > 0) {
19
           sum += BIT[idx];
20
           idx -= idx & -idx;
21
       }
22
       return sum;
23
24 | }
```

```
25
   11 rangeQuery(int L, int R) { return query(R) - query(L - 1); }
27
   int main() {
28
       int n, q;
29
       cin >> n >> q;
30
       for (int i = 1; i <= n; i++) {
31
            cin >> arr[i];
32
            update(i, arr[i], n); // init
33
       }
34
35
       while (q--) {
36
            ios::sync_with_stdio(0);
37
            cin.tie(0);
            11 type, a, b;
            cin >> type >> a >> b;
            if (type == 1) {
41
                ll delta = b - arr[a];
                arr[a] = b:
43
                update(a, delta, n);
           } else {
45
                cout << rangeQuery(a, b) << "\n";</pre>
47
       }
48
49
       return 0;
50
51 }
```

#### 5.2 Segment Tree

```
struct SegTree {
       int n;
2
       vec<int> A, st, lazy;
3
       int l(int p) { return p << 1; }</pre>
4
       int r(int p) { return (p << 1) + 1; }
       int conquer(int a, int b) {
6
           if (a == -1) return b;
           if (b == -1) return a;
8
           return a + b;
9
10
       void build(int p, int L, int R) {
11
           if (L == R)
12
                st[p] = A[L];
13
```

```
else {
14
                                                                                         int query(int i, int j) { return query(1, 0, n - 1, i, j); }
               int m = L + (R - L) / 2;
15
                                                                                 <sub>57</sub> |};
               build(l(p), L, m);
16
               build(r(p), m + 1, R);
17
                                                                                                          5.3 Index Compression
               st[p] = conquer(st[l(p)], st[r(p)]);
18
19
                                                                                  1 template <class T>
       }
20
                                                                                    struct Index { // If only 1 use Don't need to copy T type
       void propagate(int p, int L, int R) {
^{21}
                                                                                         vec<T> d;
           if (lazy[p] != -1) {
^{22}
                                                                                         int sz;
                                                                                  4
               st[p] = lazv[p];
23
                                                                                         Index(vec<T> &a) : d(ALL(a)) {
                                                                                  5
               if (L != R) {
24
                                                                                                                               // Sort
                                                                                             sort(ALL(d));
                   lazy[l(p)] = lazy[r(p)] = lazy[p];
25
                                                                                             d.erase(unique(ALL(d)), end(d)); // Erase continuous duplicates
                                                                                  7
               }
26
                                                                                             sz = SZ(d);
                                                                                  8
               lazy[p] = -1;
27
                                                                                         }
                                                                                  9
           }
28
                                                                                         int of(T e) { return lower_bound(ALL(d), e) - begin(d); } // get
                                                                                 10
       }
29
                                                                                             index
       int query(int p, int L, int R, int i, int j) {
30
                                                                                         T at(int i) { return d[i]; } // get value of index
                                                                                 11
           if (i > j || L > j || R < i) return 0;
31
                                                                                 12 };
           propagate(p, L, R);
32
           if (L >= i && R <= j) return st[p];
33
                                                                                                                       Math
           int m = L + (R - L) / 2;
34
           return conquer(query(l(p), L, m, i, j), query(r(p), m + 1, R, i,
35
                                                                                                                  6.1 Sieve
                j));
       }
36
                                                                                    void solve(int n) {
       void update(int p, int L, int R, int i, int j, int v) {
37
                                                                                         for (int x = 2; x \le n; x++) {
           if (i > j || L > j || R < i) return;
38
                                                                                             if (sieve[x]) continue:
                                                                                  3
           propagate(p, L, R);
39
                                                                                             for (int u = 2 * x; u \le n; u += x) {
           if (L >= i && R <= j) {
40
                                                                                                 sieve[u] = 1:
                                                                                  5
               lazy[p] = v;
41
                                                                                             }
                                                                                  6
               propagate(p, L, R);
42
                                                                                  7
           } else {
43
                                                                                  8 }
               int m = L + (R - L) / 2;
44
               update(l(p), L, m, i, j, v);
45
                                                                                                                  6.2 LCM
               update(r(p), m + 1, R, i, j, v);
46
               st[p] = conquer(st[l(p)], st[r(p)]);
47
                                                                                  int lcm(int a, int b) { return (a * b) / __gcd(a, b); }
           }
48
       }
                                                                                                         6.3 Binomial Coefficient
49
       SegTree(int sz) : n(sz), st(4 * n), lazy(4 * n, -1) {}
50
       SegTree(const vec<int> &init) : SegTree((int)init.size()) {
                                                                                  using ll = long long;
51
           A = init;
                                                                                  const int MAXN = 1e6 + 5;
52
           build(1, 0, n - 1);
                                                                                    const 11 \text{ MOD} = 1e9 + 7;
53
                                                                                    11 factorial[MAXN];
54
       void update(int i, int j, int val) { update(1, 0, n - 1, i, j, val);
55
```

```
6 | void build_factorials() {
       factorial[0] = 1;
       for (int i = 1; i < MAXN; i++) {
           factorial[i] = factorial[i - 1] * i % MOD;
9
       }
10
11
   ll binomial_coefficient(int n, int k) {
12
       if (k < 0 \mid | k > n) return 0;
13
       ll denom = factorial[k] * factorial[n - k] % MOD;
14
       return factorial[n] * exp(denom, MOD - 2) % MOD;
15
16 }
```

#### 6.4 Closest Pairs

```
using ld = long double;
   vec<pair<ld, ld>> closestPair(vector<pair<ld, ld>> coord, int n) {
       sort(ALL(coord));
3
       set<pair<ld, ld>> s;
4
       ld squaredDistance = LLONG_MAX;
       vec<pair<ld, ld>> ans;
       int j = 0;
7
       for (int i = 0; i < n; ++i) {
           ld D = ceil(sqrt(squaredDistance));
9
           while (coord[i].first - coord[i].first >= D) {
10
               s.erase({coord[j].second, coord[j].first});
11
               j += 1;
12
           }
13
14
           auto start = s.lower_bound({coord[i].second - D, coord[i].first
15
               });
           auto end = s.upper_bound({coord[i].second + D, coord[i].first});
16
17
           for (auto it = start; it != end; ++it) {
18
               ld dx = coord[i].first - it->second;
19
               ld dy = coord[i].second - it->first;
20
               ld preDist = min(squaredDistance, dx * dx + dy * dy);
21
               if (preDist < squaredDistance) {</pre>
^{22}
                   pair<ld, ld> one = {it->second, it->first};
23
                   pair<ld, ld> two = {coord[i].first, coord[i].second};
24
                    ans = {one, two};
25
                    squaredDistance = preDist;
26
               }
27
           }
28
```

```
29
           // Insert the point as {y-coordinate, x-coordinate}
30
           s.insert({coord[i].second, coord[i].first});
31
32
       return ans;
33
34 }
                              6.5 Distance
double dist(double x1, double y1, double x2, double y2) {
       return sqrt((x1 - x2) * (x1 - x2) + (y1 - y2) * (y1 - y2));
3 | }
                              6.6 Catalan
   const int MOD = ....const int MAX = ....int catalan[MAX];
   void init() {
       catalan[0] = catalan[1] = 1;
       for (int i = 2; i <= n; i++) {
4
           catalan[i] = 0;
5
           for (int j = 0; j < i; j++) {
               catalan[i] += (catalan[j] * catalan[i - j - 1]) % MOD;
               if (catalan[i] >= MOD) {
                   catalan[i] -= MOD;
10
11
       }
12
13 }
                     6.7 Binary Exponentiation
1 | ll power(ll a, ll b, ll m) {
       a %= m;
       ll res = 1:
3
       while (b > 0) {
4
           if (b & 1) res = res * a % m:
5
           a = a * a % m;
6
           b >>= 1;
7
       }
8
       return res;
9
10 }
```