

# Laws and Theorems of Boolean Algebra

1a.  $X \cdot 0 = 0$

1b.  $X + 1 = 1$

Annulment Law

2a.  $X \cdot 1 = X$

2b.  $X + 0 = X$

Identity Law

3a.  $X \cdot X = X$

3b.  $X + X = X$

Idempotent Law

4a.  $X \cdot \bar{X} = 0$

4b.  $X + \bar{X} = 1$

Complement Law

5.  $\overline{\overline{X}} = X$

Double Negation Law

6a.  $X \cdot Y = Y \cdot X$

6b.  $X + Y = Y + X$

Commutative Law

7a.  $X(YZ) = (XY)Z = (XZ)Y = XYZ$

Associative Law

7b.  $X + (Y + Z) = (X + Y) + Z = (X + Z) + Y = X + Y + Z$

Associative Law

8a.  $X \cdot (Y + Z) = XY + XZ$

8b.  $X + YZ = (X + Y) \cdot (X + Z)$

Distributive Law

9a.  $\overline{X \cdot Y} = \bar{X} + \bar{Y}$

9b.  $\overline{X + Y} = \bar{X} \cdot \bar{Y}$

de Morgan's Theorem

10a.  $X \cdot (X + Y) = X$

10b.  $X + X \cdot Y = X$

Absorption Law

11a.  $(X + Y) \cdot (X + \bar{Y}) = X$

11b.  $XY + X\bar{Y} = X$

Redundancy Law

12a.  $(X + \bar{Y}) \cdot Y = XY$

12b.  $X\bar{Y} + Y = X + Y$

Redundancy Law

13a.  $(X + Y) \cdot (\bar{X} + Z) \cdot (Y + Z) = (X + Y) \cdot (\bar{X} + Z)$

Consensus Law

13b.  $XY + \bar{X}Z + YZ = XY + \bar{X}Z$

Consensus Law

14a.  $X \oplus Y = (X + \bar{Y}) \cdot (\bar{X} + Y)$

14b.  $X \oplus Y = \bar{X}Y + X\bar{Y}$

XOR Gate

15a.  $X \odot Y = (X + Y) \cdot (\bar{X} \cdot \bar{Y})$

15b.  $X \odot Y = \bar{X}\bar{Y} + XY$

XNOR Gate

15c.  $X \odot Y = (X + Y) \cdot (\bar{X} + \bar{Y})$

XNOR Gate

# Gates

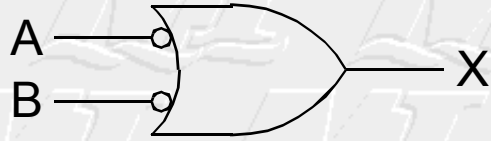
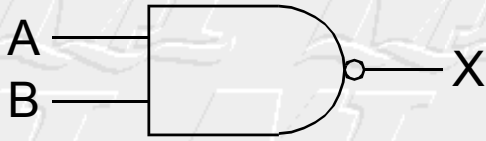
## Standard

## DeMorgan's

NAND

$$X = \overline{A \cdot B}$$

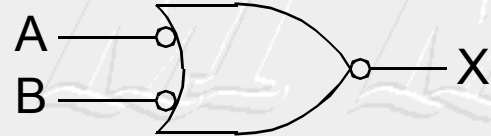
$$X = \overline{\overline{A} + \overline{B}}$$



AND

$$X = A \cdot B$$

$$X = \overline{\overline{A} + \overline{B}}$$



NOR

$$X = \overline{A + B}$$

$$X = \overline{\overline{A} \cdot \overline{B}}$$



OR

$$X = A + B$$

$$X = \overline{\overline{A} \cdot \overline{B}}$$

