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Code: 20SC01T

I/II Semester Diploma Examination, Nov/Dec 2024

## ENGINEERING MATHEMATICS

TIME: 3 HOURS

MAX MARKS: 100

- Note: i) Answer any 5 questions from SECTION-A, each question carries 4 marks.
- ii) Answer any 10 questions from SECTION-B, each question carries 5 marks.
- iii) Answer any 5 questions from SECTION-C, each question carries 6 marks.

### SECTION – A

1. If  $A = \begin{bmatrix} 4 & 5 \\ 1 & 2 \end{bmatrix}$  and  $B = \begin{bmatrix} 0 & 6 \\ 1 & 3 \end{bmatrix}$ , find the matrix  $A + 2B$ .
2. If  $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ , find  $A - A^T$ .
3. If the matrix  $A = \begin{pmatrix} x & 1 \\ 3 & 4 \end{pmatrix}$  is singular then find 'x'.
4. Find the slope of the line whose angle of inclination is  $45^\circ$  with the positive x-axis.
5. Find the slope of the straight line passing through the points (2, 6) and (4, 9).

6. Convert  $150^\circ$  into radian and  $\frac{3\pi}{2}$  into degree.
7. If  $y = x^2 + 3 \sin x + e^x + 1$  then find  $\frac{dy}{dx}$
8. Find the slope of the tangent to the curve  $y = x^3 + 1$  at  $(1, 2)$
9. Integrate  $x^2 + \frac{1}{x} + e^x + 2$  with respect to  $x$ .
10. Evaluate  $\int_1^2 x \, dx$

### SECTION – B

11. Verify whether  $AB = BA$  for the matrices  $A = \begin{bmatrix} 3 & 7 \\ 4 & 0 \end{bmatrix}$  and  $B = \begin{bmatrix} 1 & 2 \\ 7 & 3 \end{bmatrix}$ .
12. Find adjoint of the matrix  $A = \begin{bmatrix} 4 & 2 \\ 3 & 1 \end{bmatrix}$ .
13. Find characteristic equation of the matrix  $A = \begin{bmatrix} 3 & 2 \\ 4 & 5 \end{bmatrix}$ .
14. Find equation of the straight line passing through the point  $(3, 2)$  and having slope 5.
15. Find the equation of the straight line passing through the points  $(4, 2)$  and  $(6, 4)$ .
16. Find the equation of straight line having  $x$ -intercept 2 and  $y$ -intercept 3 units respectively

17. Show that the two lines  $2x + y - 4 = 0$  and  $6x + 3y + 10 = 0$  are parallel.
18. Find the slope, x-intercept and y-intercept of the line  $6x + 5y + 10 = 0$
19. Find the value of  $\sin 150^\circ + \cos 120^\circ$ .
20. Simplify:  
 $\sin(90^\circ + \theta) + \cos(180^\circ - \theta) + \tan(270^\circ - \theta) + \cot(360^\circ - \theta)$
21. Write the formula of  $\sin(A + B)$  and hence find the value of  $\sin 75^\circ$
22. Prove that  $\sin 2A = 2\sin A \cos A$  using compound angle formula.
23. If  $y = x^2 + 3x + 7$ , then find  $\frac{d^2y}{dx^2}$
24. If  $y = x \sin x$ , then find  $\frac{dy}{dx}$
25. If  $y = \frac{1+x}{1-x}$ , find  $\frac{dy}{dx}$
26. Evaluate  $\int (x^2(1+x))dx$ .
27. Evaluate  $\int_0^1 (x^2 + 1) dx$ .
28. Evaluate  $\int x e^x dx$ .

## SECTION – C

29. Solve the equations  $3x + 2y = 8$  and  $4x + 5y = 6$  by applying Cramer's rule.
30. Identify the singular and non-singular matrices in the following matrices.  
 $A = \begin{bmatrix} 1 & 7 \\ 0 & 3 \end{bmatrix}$   $B = \begin{bmatrix} 3 & 1 \\ 9 & 3 \end{bmatrix}$   $C = \begin{bmatrix} 7 & 2 \\ 1 & 3 \end{bmatrix}$ .
31. Find the equation of a line passing through the point (1, 3) and parallel to the line  $5x + 2y + 10 = 0$ .
32. Prove that  $\sin 3A = 3 \sin A - 4 \sin^3 A$
33. Write the compound angle formula for  $\tan(A + B)$  and hence prove that  $\tan\left(\frac{\pi}{4} + A\right) = \frac{1 + \tan A}{1 - \tan A}$
34. Write product rule and hence find the derivative of  $y = x^2 e^x \sin x$
35. If  $y$  is the distance travelled in meters by a particle in time  $x$  sec is given  $x^3 + 5x^2 + 3x - 12$ . Find the velocity and acceleration when  $x = 1$  sec.
36. Find equation of tangent to the curve  $y = x^2 + x$  at the point (1,2).
37. Find the area under the curve  $y = 2x + 1$  with  $x$ -axis and ordinates  $x = 0$  &  $x = 2$
38. Find the volume of solid generated by revolving the curve  $y^2 = 3x^2 - 1$  about the axis between  $x = 1$  and  $x = 3$ .

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**GOVERNMENT OF KARNATAKA**  
**DEPARTMENT OF COLLEGIATE AND TECHNICAL EDUCATION**  
**I/II SEMESTER DIPLOMA EXAMINATIONS, NOV-DEC-2024**  
**Sub: Engineering Mathematics** **Code: 20SC01T**

**SCHEME AND MODEL ANSWER**

Q.NO	SCHEME	MARK	Q.NO	SCHEME	MARK
	<b>SECTION-A</b>		20	Applying allied angle concept for each function Calculation and Solution	1+1+1+1 1
1	Finding 2B Writing matrix, $A+2B$ Applying concept of addition of matrices Calculation and answer	1 1 1 1	21	Writing formula Writing given angle in compound angle Substituting in formula Writing standard angle value Calculation and Solution	1 1 1 1 1
2	Finding transpose of A Writing matrix, $A-A^T$ Applying concept of addition of matrices Calculation and answer	1 1 1 1	22	Writing formula Substituting $A=B$ Substituting in formula Simplification Arriving at result	1 1 1 1 1
3	Writing $\det(A)=0$ Applying determinant definition Simplification Solution for x	1 1 1 1	23	Finding first derivative Finding second derivative	3 2
4	Writing given data Slope Formula Substitution Slope value	1 1 1 1	24	Identifying the rule Applying the product rule Writing the derivative of each	1 2 1+1
5	Writing given data Slope Formula Substitution Slope value	1 1 1 1	25	Identifying the rule Applying the quotient rule Writing the derivative of each	1 2 1+1
6	Multiplying by conversion factor for each Conversion value for each	1+1 1+1	26	Multiplying the term Integral of each Adding constant of integration	2 1+1 1
7	Derivative of each term	1+1+1+1	27	Integral of each term Applying limits Calculation and simplification Integral value	1+1 1 1 1

8	Finding derivative Substituting points Slope value	2 1 1	28	Identifying the rule Applying integration by part rule Simplification and solution	1 2 2
9	Integral of each term	1+1+1+1		<b>SECTION-C</b>	
10	Integral of each term Applying limits Calculation and solution	1+1 1 1	29	Finding $\Delta$ Finding $\Delta_1$ and $\Delta_2$ Finding x and y	2 2 2
	<b>SECTION-B</b>		30	Finding determinant of each matrix. Conclusion for each matrix	1+1+1 1+1+1
11	Finding AB Finding BA Conclusion	2 2 1	31	Finding slope given of line Parallel condition Determining slope of parallel line Equation of line in one point form Substitution Simplification and solution	1 1 1 1 1 1
12	Co-factor of each element Writing Adjoint	1+1+1+1 1	32	Writing $3A=2A+A$ Formula for $\sin(A+B)$ Substituting in formula Substituting $\sin 2A$ Substituting $\cos 2A$ Simplification and proving	1 1 1 1 1 1
13	Characteristic definition Applying definition for A Applying determinant definition Calculation Solution	1 1 1 1 1	33	Formula for $\tan(A+B)$ Substituting in the formula on LHS Substituting in the formula on RHS Writing value of $\tan 45^\circ$ Proving LHS=RHS	2 1 1 1 1
14	Slope Formula Slope value Equation of straight line in one point form Substitution Calculation and Solution	1 1 1 1 1	34	For each term in applying product rule Each derivative	1+1+1 1+1+1
15	Slope Formula Slope value Suitable equation of straight line in standard form Substitution	1 1 1 1	35	Finding first derivative Substituting $x=1$ in first derivative Finding velocity Finding second derivative	1 1 1 1

	Calculation and Solution	1 1			Substituting x=1 in second derivative Finding velocity	1 1
16	Equation of straight line in intercept form Substitution Calculation and Solution	2 1 2		36	Finding first derivative Substituting x=1 in first derivative Slope of tangent value Equation of tangent in standard form Substituting Simplification and solution	1 1 1 1 1 1
17	Finding slope of each line Conclusion	2+2 1		37	Area formula Substituting in formula Each integral Applying limit Calculation and solution	1 1 1+1 1 1
18	Writing value of a, b, c Finding slope Finding x-intercept Finding y-intercept	1 2 1 1		38	Volume formula Substituting in formula Each integral Applying limit Calculation and solution	1 1 1+1 1 1
19	Writing each angle in allied angle form Finding value of each Simplification and Solution	1+1 1+1 1				

### MODEL ANSWER

Q. NO	SECTION-A
1	<p>Given <math>A = \begin{bmatrix} 4 &amp; 5 \\ 1 &amp; 2 \end{bmatrix}</math> and <math>B = \begin{bmatrix} 0 &amp; 6 \\ 1 &amp; 3 \end{bmatrix}</math></p> <p><math>2B = \begin{bmatrix} 0 &amp; 12 \\ 2 &amp; 6 \end{bmatrix}</math></p> <p><math>A + 2B = \begin{bmatrix} 4 &amp; 5 \\ 1 &amp; 2 \end{bmatrix} + \begin{bmatrix} 0 &amp; 12 \\ 2 &amp; 6 \end{bmatrix} = \begin{bmatrix} 4+0 &amp; 5+12 \\ 1+2 &amp; 2+6 \end{bmatrix} = \begin{bmatrix} 4 &amp; 17 \\ 3 &amp; 8 \end{bmatrix}</math></p>
2	<p>Given <math>A = \begin{bmatrix} 1 &amp; 2 \\ 3 &amp; 4 \end{bmatrix}</math></p> <p><math>A^T = \begin{bmatrix} 1 &amp; 3 \\ 2 &amp; 4 \end{bmatrix}</math></p> <p><math>A - A^T = \begin{bmatrix} 1 &amp; 2 \\ 3 &amp; 4 \end{bmatrix} - \begin{bmatrix} 1 &amp; 3 \\ 2 &amp; 4 \end{bmatrix} = \begin{bmatrix} 1-1 &amp; 2-3 \\ 3-2 &amp; 4-4 \end{bmatrix} = \begin{bmatrix} 0 &amp; -1 \\ 1 &amp; 0 \end{bmatrix}</math></p>
3	<p>Given <math>A = \begin{pmatrix} x &amp; 1 \\ 3 &amp; 4 \end{pmatrix}</math> is singular</p> <p>If A is singular then <math>\det(A)=0</math></p> <p><math>\begin{vmatrix} x &amp; 1 \\ 3 &amp; 4 \end{vmatrix} = 0 \Rightarrow 4x-3=0 \Rightarrow x=\frac{3}{4}</math></p>
4	<p>Given <math>\theta=45^\circ</math></p> <p>Slope <math>m=\tan \theta \Rightarrow m=\tan 45^\circ=1</math></p>

5	<p>Let <math>(x_1, y_1) = (2, 6)</math> and <math>B = (x_2, y_2) = (4, 9)</math></p> <p>Slope <math>m = \frac{y_2 - y_1}{x_2 - x_1} \Rightarrow m = \frac{9 - 6}{4 - 2} = \frac{3}{2}</math></p>
6	<p><math>x \text{ degree} = \frac{\pi}{180} \times x \text{ radians}</math></p> <p><math>150^\circ = \frac{\pi}{180} \times 150 \text{ radians}</math></p> <p><math>150^\circ = \frac{5\pi}{6} \text{ radians}</math></p> <p><math>x \text{ radians} = \frac{180^\circ}{\pi} \times x \text{ degree}</math></p> <p><math>\frac{3\pi}{2} \text{ radians} = \frac{180^\circ}{\pi} \times \frac{3\pi}{2} \text{ degree}</math></p> <p><math>\frac{3\pi}{2} \text{ radians} = 270 \text{ degree}</math></p>
7	<p>Given <math>y = x^2 + 3 \sin x + e^x + 1</math></p> <p><math>\frac{dy}{dx} = 2x + 3 \cos x + e^x + 0</math></p>
8	<p>Given <math>y = x^3 + 1</math></p> <p><math>\frac{dy}{dx} = 3x^2 + 0</math></p> <p>Slope of tangent at <math>(1, 2)</math> is <math>m = \frac{dy}{dx}</math> at <math>(1, 2)</math></p> <p><math>m = 3(1)^2 = 3</math></p>
9	<p><math>\int \left( x^2 + \frac{1}{x} + e^x + 2 \right) dx = \frac{x^3}{3} + \log x + e^x + 2x + c</math></p>
10	<p><math>\int_1^2 x \, dx = \left[ \frac{x^2}{2} \right]_1^2 = \left[ \frac{2^2}{2} - \frac{1^2}{2} \right] = \frac{3}{2}</math></p>
<b>SECTION-B</b>	
11	<p>Given <math>A = \begin{bmatrix} 3 &amp; 7 \\ 4 &amp; 0 \end{bmatrix}</math> and <math>B = \begin{bmatrix} 1 &amp; 2 \\ 7 &amp; 3 \end{bmatrix}</math></p> <p><math>AB = \begin{bmatrix} 3 &amp; 7 \\ 4 &amp; 0 \end{bmatrix} \begin{bmatrix} 1 &amp; 2 \\ 7 &amp; 3 \end{bmatrix} = \begin{bmatrix} 3 \times 1 + 7 \times 7 &amp; 3 \times 2 + 7 \times 3 \\ 4 \times 1 + 0 \times 7 &amp; 4 \times 2 + 0 \times 3 \end{bmatrix} = \begin{bmatrix} 52 &amp; 27 \\ 4 &amp; 8 \end{bmatrix}</math></p> <p><math>BA = \begin{bmatrix} 1 &amp; 2 \\ 7 &amp; 3 \end{bmatrix} \begin{bmatrix} 3 &amp; 7 \\ 4 &amp; 0 \end{bmatrix} = \begin{bmatrix} 1 \times 3 + 2 \times 4 &amp; 1 \times 7 + 2 \times 0 \\ 7 \times 3 + 3 \times 4 &amp; 7 \times 7 + 3 \times 0 \end{bmatrix} = \begin{bmatrix} 11 &amp; 7 \\ 33 &amp; 49 \end{bmatrix}</math></p> <p>We observe that <math>AB \neq BA</math></p>
12	<p>Given <math>A = \begin{bmatrix} 4 &amp; 2 \\ 3 &amp; 1 \end{bmatrix}</math></p> <p>Cofactor of 4 = +1</p> <p>Cofactor of 2 = -3</p> <p>Cofactor of 3 = -2</p> <p>Cofactor of 1 = +4</p> <p>Adjoint of <math>A = \text{adj} A = \begin{bmatrix} 1 &amp; -2 \\ -3 &amp; 4 \end{bmatrix}</math></p>
13	<p>Given <math>A = \begin{bmatrix} 3 &amp; 2 \\ 4 &amp; 5 \end{bmatrix}</math></p> <p>C.E is given by <math> A - \lambda I  = 0</math></p> <p><math>\left  \begin{bmatrix} 3 &amp; 2 \\ 4 &amp; 5 \end{bmatrix} - \lambda \begin{bmatrix} 1 &amp; 0 \\ 0 &amp; 1 \end{bmatrix} \right  = 0</math></p> <p><math>\begin{vmatrix} 3 - \lambda &amp; 2 \\ 4 &amp; 5 - \lambda \end{vmatrix} = 0</math></p> <p><math>(3 - \lambda)(5 - \lambda) - 4 \times 2 = 0</math></p>



	$\lambda^2 - 8\lambda + 7 = 0$
14	<p>Given <math>m=5</math> and <math>(x_1, y_1) = (3, 2)</math>  Equation of straight line is  <math>y - y_1 = m(x - x_1)</math>  <math>y - 2 = 5(x - 3)</math>  <math>-5x + y + 13 = 0</math> or <math>5x - y - 13 = 0</math> is the required equation of line.</p>
15	<p>Given: <math>(x_1, y_1) = (4, 2)</math> and <math>(x_2, y_2) = (6, 4)</math>  Slope <math>m = \left(\frac{y_2 - y_1}{x_2 - x_1}\right) = \frac{4 - 2}{6 - 4} = 1</math>  Equation of straight line is  <math>y - y_1 = \left(\frac{y_2 - y_1}{x_2 - x_1}\right)(x - x_1)</math>  <math>y - 2 = 1(x - 4)</math>  <math>-x + y - 2 + 4 = 0</math>  <math>-x + y + 2 = 0</math> or <math>x - y - 2 = 0</math> is the required equation of the line.</p>
16	<p>Given that: <math>a = 2</math> and <math>b = 3</math>  Equation of a straight line is <math>\frac{x}{a} + \frac{y}{b} = 1</math>  <math>\Rightarrow \frac{x}{2} + \frac{y}{3} = 1</math>  <math>\Rightarrow \frac{3x + 2y}{6} = 1 \Rightarrow 3x + 2y - 6 = 0</math></p>
17	<p>Given lines <math>l_1: 2x + y - 4 = 0</math> and <math>l_2: 6x + 3y + 10 = 0</math>  Let the slope of <math>l_1</math> be <math>m_1 = -\frac{a}{b} = -\frac{2}{1} = -2</math>  Slope of <math>l_2</math> be <math>m_2 = -\frac{a}{b} = -\frac{6}{3} = -2</math>  We observe that <math>m_1 = m_2</math>, hence given two lines are parallel.</p>
18	<p>Given <math>6x + 5y + 10 = 0</math>  <math>a=6, b=5, c=10</math>  Slope <math>= -\frac{a}{b} = -\frac{6}{5}</math>  x-intercept <math>= -\frac{10}{6} = -\frac{5}{3}</math>  y-intercept <math>= -\frac{10}{5} = -2</math></p>
19	<p><math>\sin 150^\circ = \sin(180^\circ - 30^\circ) = +\sin 30^\circ = +\frac{1}{2}</math>  <math>\cos 120^\circ = \cos(180^\circ - 60^\circ) = -\cos 60^\circ = -\frac{1}{2}</math>  Hence <math>\sin 150^\circ + \cos 120^\circ = \frac{1}{2} - \frac{1}{2} = 0</math></p>
20	<p><math>\sin(90^\circ + \theta) + \cos(180^\circ - \theta) + \tan(270^\circ - \theta) + \cot(360^\circ - \theta)</math>  <math>= (+\cos\theta) + (-\cos\theta) + (+\cot\theta) + (-\cot\theta) = 0</math></p>
21	<p>We know that <math>\sin(A + B) = \sin A \cos B + \cos A \sin B \rightarrow (1)</math>  <math>\sin 75^\circ = \sin(45^\circ + 30^\circ)</math>  Substitute <math>A = 45^\circ, B = 30^\circ</math> in equation (1), then we get  <math>= \sin 45^\circ \cos 30^\circ + \cos 45^\circ \sin 30^\circ</math></p>

	$\sin 75^\circ = \frac{1}{\sqrt{2}} \times \frac{\sqrt{3}}{2} + \frac{1}{\sqrt{2}} \times \frac{1}{2} = \frac{\sqrt{3} + 1}{2\sqrt{2}}$
22	<p>We know that <math>\sin(A + B) = \sin A \cos B + \cos A \sin B \rightarrow (1)</math>  Put <math>B=A</math> in (1) then (1) becomes,  <math>\sin(A + A) = \sin A \cos A + \cos A \sin A</math>  <math>\sin 2A = \sin A \cos A + \sin A \cos A</math>  <math>\sin 2A = 2 \sin A \cos A</math>. Hence proved.</p>
23	<p>Given <math>y = x^2 + 3x + 7</math>  <math>\frac{dy}{dx} = 2x + 3(1) + 0</math>  <math>\frac{dy}{dx} = 2x + 3</math>  <math>\frac{d^2y}{dx^2} = 2(1) + 0 = 2</math></p>
24	<p>Given <math>y = x \sin x</math>  Apply product rule  <math>\frac{dy}{dx} = x \frac{d(\sin x)}{dx} + \sin x \frac{d(x)}{dx} = x(\cos x) + \sin x(1) = x \cos x + \sin x</math></p>
25	<p>Given <math>y = \frac{1+x}{1-x}</math>  Apply quotient rule  <math display="block">\frac{dy}{dx} = \frac{(1-x) \frac{d}{dx}(1+x) - (1+x) \frac{d}{dx}(1-x)}{(1-x)^2}</math> <math display="block">= \frac{(1-x)(0+1) - (1+x)(0-1)}{(1-x)^2}</math> <math display="block">= \frac{(1-x)(1) + (1+x)(1)}{(1-x)^2}</math> <math display="block">= \frac{2}{(1-x)^2}</math></p>
26	$\int (x^2(1+x)) dx = \int (x^2 + x^3) dx = \int (x^2) dx + \int (x^3) dx = \frac{x^3}{3} + \frac{x^4}{4} + c$
27	$\int_0^1 (x^2 + 1) dx = \left[ \frac{x^3}{3} + x \right]_0^1 = \left[ \frac{1^3}{3} + 1 \right] - \left[ \frac{0^3}{3} + 0 \right] = \frac{4}{3}$
28	<p>Let <math>I = \int x e^x dx</math>  Here <math>x</math> is Algebraic function and <math>e^x</math> is Exponential function.  According to the ILATE rule of choosing the first function,  <math>u = I \text{ fn} = x</math> and <math>v = II \text{ fn} = e^x</math>  <math>\int (I \text{ fn} \times II \text{ fn}) dx = I \text{ fn} \int (II \text{ fn}) dx - \int \left( \frac{d}{dx} (I \text{ fn}) \right) (II \text{ fn}) dx</math>  <math display="block">I = \int x e^x dx</math> <math display="block">= x \int e^x dx - \int \left( \frac{d}{dx} (x) \right) e^x dx</math> <math display="block">= x e^x - \int e^x \times 1 dx</math> <math display="block">= x e^x - \int e^x dx</math> <math display="block">= x e^x - e^x + c</math></p>
29	<p>Given <math>3x + 2y = 8</math>  <math>4x + 5y = 6</math>  let <math>\Delta = \begin{vmatrix} 3 &amp; 2 \\ 4 &amp; 5 \end{vmatrix} = 15 - 8 = 7</math></p>

	$\Delta_1 = \begin{vmatrix} 8 & 2 \\ 6 & 5 \end{vmatrix} = 40 - 12 = 28$ $\Delta_2 = \begin{vmatrix} 3 & 8 \\ 4 & 6 \end{vmatrix} = 18 - 32 = -14$ $\therefore x = \frac{\Delta_1}{\Delta} = \frac{28}{7} = 4 \text{ and } y = \frac{\Delta_2}{\Delta} = \frac{-14}{7} = -2$
30	<p>Given <math>A = \begin{bmatrix} 1 &amp; 7 \\ 0 &amp; 3 \end{bmatrix}</math> then <math> A  = \begin{vmatrix} 1 &amp; 7 \\ 0 &amp; 3 \end{vmatrix} = 1 \times 3 - 7 \times 0 = 3</math>  <math> A  \neq 0</math> Hence A is non-singular.</p> <p>Given <math>B = \begin{bmatrix} 3 &amp; 1 \\ 9 &amp; 3 \end{bmatrix}</math> then <math> B  = \begin{vmatrix} 3 &amp; 1 \\ 9 &amp; 3 \end{vmatrix} = 3 \times 3 - 1 \times 9 = 0</math>  <math> B  = 0</math> Hence B is singular.</p> <p>Given <math>C = \begin{bmatrix} 7 &amp; 2 \\ 1 &amp; 3 \end{bmatrix}</math> then <math> C  = \begin{vmatrix} 7 &amp; 2 \\ 1 &amp; 3 \end{vmatrix} = 7 \times 3 - 2 \times 1 = 19</math>  <math> C  \neq 0</math> Hence C is non-singular.</p>
31	<p>slope of given line <math>5x + 2y + 10 = 0</math></p> $m_1 = -\frac{a}{b} = -\frac{5}{2}$ <p>As the required line is parallel to given line</p> $m_1 = m_2 = -\frac{5}{2} = m$ <p>Equation of the required line passing through (1,3) is</p> $y - y_1 = m(x - x_1)$ $y - 3 = -\frac{5}{2}(x - 1)$ $5x + 2y - 11 = 0$
32	$\sin 3A = \sin(2A + A)$ $\sin 3A = \sin 2A \cos A + \cos 2A \sin A$ $\sin 3A = (2 \sin A \cos A) \cos A + (1 - 2 \sin^2 A) \sin A$ $\sin 3A = 2 \sin A \cos^2 A + \sin A - 2 \sin^3 A$ $\sin 3A = 2 \sin A (1 - \sin^2 A) + \sin A - 2 \sin^3 A$ $\sin 3A = 2 \sin A - 2 \sin^3 A + \sin A - 2 \sin^3 A$ $\sin 3A = 3 \sin A - 4 \sin^3 A$
33	$\tan(A + B) = \left( \frac{\tan A + \tan B}{1 - \tan A \tan B} \right)$ <p>Put <math>A = \frac{\pi}{4}</math> <math>B = A</math> in the above</p> <p>We get,</p> $\tan\left(\frac{\pi}{4} + A\right) = \left( \frac{\tan \frac{\pi}{4} + \tan A}{1 - \tan \frac{\pi}{4} \tan A} \right)$ $\tan\left(\frac{\pi}{4} + A\right) = \left( \frac{1 + \tan A}{1 - 1 \cdot \tan A} \right) \quad (\text{as } \tan \frac{\pi}{4} = 1)$ <p>Hence <math>\tan\left(\frac{\pi}{4} + A\right) = \left( \frac{1 + \tan A}{1 - \tan A} \right)</math></p>
34	<p>Given <math>y = x^2 e^x \sin x</math></p> $\frac{dy}{dx} = x^2 e^x \frac{d}{dx}(\sin x) + e^x \sin x \frac{d}{dx}(x^2) + x^2 \sin x \frac{d}{dx}(e^x)$ $\frac{dy}{dx} = x^2 e^x (\cos x) + e^x \sin x (2x) + x^2 \sin x (e^x)$

35	<p>Given <math>y = x^3 + 5x^2 + 3x - 12</math></p> $\frac{dy}{dx} = 3x^2 + 5(2x) + 3(1) - 0$ $\frac{dy}{dx} = 3x^2 + 10x + 3$ $\frac{d^2y}{dx^2} = 3(2x) + 10(1) + 0$ $\frac{d^2y}{dx^2} = 6x + 10$ <p>Velocity at <math>x=1</math> is <math>\frac{dy}{dx}</math> at <math>x=1</math>,</p> <p>Velocity <math>= 3(1)^2 + 10(1) + 3 = 16</math> m/s</p> <p>Acceleration at <math>x=1</math> is <math>\frac{d^2y}{dx^2}</math> at <math>x = 1</math></p> <p>Acceleration <math>= 6(1) + 10 = 16</math> m/s<sup>2</sup></p>
36	<p>Given <math>y = x^2 + x</math></p> $\frac{dy}{dx} = 2x + 1$ <p>Slope of tangent at (1,2) is <math>m = \frac{dy}{dx}</math> at (1,2)</p> $m = 2(1) + 1 = 3$ <p>Equation of tangent to the curve at the point (1,2)</p> $y - y_1 = m(x - x_1)$ $y - 2 = 3(x - 1)$ $-3x + y + 1 = 0 \text{ or } 3x - y - 1 = 0$
37	<p>We know that the area bounded by the curve <math>y=f(x)</math> between <math>x=a</math> and <math>x=b</math> about the <math>x</math>-axis is</p> $A = \int_a^b y \, dx = \int_0^2 (2x + 1) \, dx = \left[ 2 \frac{x^2}{2} + x \right]_0^2 = [x^2 + x]_0^2 = (2^2 + 2) - (0^2 + 0)$ $\therefore A = 6 \text{ square units}$
38	<p>We know that, the volume of the solid formed by revolving the curve <math>y=f(x)</math> and the <math>x</math>-axis between <math>x=a</math> and <math>x=b</math> about the <math>x</math>-axis is</p> $V = \pi \int_a^b y^2 \, dx = \pi \int_1^3 (3x^2 - 1) \, dx = \pi \left[ 3 \frac{x^3}{3} - x \right]_1^3 = \pi [x^3 - x]_1^3$ $= \pi [(3^3 - 3) - (1^3 - 1)] = 24\pi \text{ cubic unit}$

Certified that the scheme of valuation and model answers prepared by me for the code 20SC01T are according to the revised syllabus and are correct.

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