RL Bridge bidding Inventor (on-going work)

An attempt to learn and use bidding systems.

As an example we used the continuation after 1 Spade (5+,12-21 h.c.p) – 1 NoTrump (0-2 spades, 8-11).

The idea is to have a policy to recommend an action (bid) given a situation (hand and the previous bidding).

By using DDS as recommended bids for a number of relevant hands we can train a policy-network with Reinforcement Learning. Here we used table-based Q-learning incl Eligibility traces, Q(lambda), for respective hand (spades, hearts, diamonds and h.c.p) and bidding history as state. As actions we allow pass and the nearest 11 bids for each rond, maximum 4 bids + pass.

It seems to be a delicate balance between exploration (try new bids with probability epsilon) and exploatation (select bids known to be good) via parameter epsilon – usually one start with a larger value like 0.5 (select randomly 50%) down to 0.02 (select randomly only 2%; 98% best).

Moved from programming language Python to Julia for a speed improvement of ca 100x. Currently not using any GPU but trivial parallel processing on multiple-cores; run with different parameters and select best results. Memory requirements with 10 processes is about 27 GB RAM and this run took about 3 hours on a 6-core machine (5 years old Intel on Linux).

Some experimental bidding results (Intro is 1 - 1 NT. Only 1N = N orth passes). The topscore value is used with the difference presented and parScore in brackets. Rewards is average lost par-bid topscore count. (Imp is slower to learn because of coarser reward numbers). (Some earlier runs lost -180). The always-pass policy here results in a loss of about -258 points/deal. 2 "best" runs are shown.

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a)
2 2 3 3N n AKQ985.K.AJ4.Q64 6133(19) s J3.QT8.KQ832.975 2353(8) 300 [100]
2 2 3 4 n AJT632.K.Q.Q9762 6115(12) s Q7.A63.98543.KT4 2353(9) 50 [-100]
2 2 4 6 n AKJT2.A.AJ9643.Q 5161(19) s Q.KQ987643.8.KJ6 1813(11) 0 [980]
2 2 3 n KT983.K.KQJ8.A95 5143(16) s J.QT862.7642.KQJ 1543(9) 0 [130]
1N n AKQ95.T.K3.AJ875 5125(17) s J4.AJ852.985.K94 2533(9) -710 [920]
1N n KJ873.J8.AKQ54.2 5251(14) s 62.KQT95.J73.QT7 2533(8) -50 [140]
2 2 2N4 n Q9865.A53.AQ62.Q 5341(14) s K7.QJ8.754.K9832 2335(9) -210 [110]
1N n QJ9542.QJ4.QJ.A5 6322(13) s T7.972.AK75.J986 2344(8) 20 [100]
1N n AJ972.AQT6.QT8.9 5431(13) s K5.K92.K43.QT854 2335(11) -250 [430]
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n AKQ53.AJ4.KT.J64 5323(18) s 64.Q9832.AQ4.952 2533(8) 0 [420]
2 2 2N4
1N n AJT984.K5.Q87.AJ 6232(15) s .A6.AJ63.T986543 0247(9) -250 [400]
1N n AJ954.QJT.T95.A2 5332(12) s 87.K864.2.KQT854 2416(8) -10 [100]
             n KT8763..AKJT3.J2 6052(12) s A2.AT8.Q8762.T85 2353(10) -150 [100]
2 2 3 3N n AQ532.965.AKJ83. 5350(14) s K.QJ73.Q9762.732 1453(8) -430 [130]
1N n AKQJ6.74.Q76.T73 5233(12) s 97.KJ63.K4.A8654 2425(11) -20 [140]
             n K8642.AT654.AJ7. 5530(12) s AT.J32.K532.JT84 2344(9) 0 [420]
2 2 3 4
             n AK0975.A4.A865.4 6241(17) s JT.0965.K732.052 2443(8) 0 [420]
1N n KJ9632.AO.QJ9.95 6232(13) s A8.964.864.AJ843 2335(9) -280 [430]
1N n AKT82.Q8.K76.983 5233(12) s J9.K632.AJT9.652 2443(9) -150 [100]
2 2 3
          n AQ632.2.AK963.K2 5152(16) s K.J9543.QJT8.Q65 1543(9) -250 [400]
1N n AK632.K09.K43.A9 5332(19) s Q5.AJ632.J5.K652 2524(11) -770 [980]
1N n AK0874.A64.5.T87 6313(13) s 2.053.K9862.K094 1354(10) -20 [140]
1N n Q9843.K4.A83.AK7 5233(16) s A5.QJ982.Q75.J32 2533(10) 0 [120]
Lr0.001 reward=-209.04
b)
1N n AQJ652.K.985.Q32 6133(12) s 83.AT8643.KQ.865 2623(9) -50 [-100]
1N n AKQ87.J65.K4.JT6 5323(14) s 2.9.AQJ832.K7542 1165(10) -150 [100]
1N n Q9762.KQ.A6.J984 5224(12) s J4.9764.J972.AK3 2443(9) -150 [100]
1N n KJ743.AQT4.8.K73 5413(13) s T6.K653.AQJT75.4 2461(10) -470 [420]
1N n QJ984.K.AJ42.A98 5143(15) s 3.Q62.K98763.KT3 1363(8) -180 [130]
            n KJ532..AJ3.K9875 5035(12) s 7.AT9764.75.AQ42 1624(10) -600 [400]
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      n AKJT986.KJ97.2.3 7411(12) s .QT652.KJ3.QT942 0535(8) 320 [100]
1N n AJT54.K62.J84.K3 5332(12) s 8.OT8.A92.OT7652 1336(8) 0 [90]
1N n KQJ62.KJ3.543.Q6 5332(12) s T9.T92.Q82.AK942 2335(9) -250 [400]
1N n AKQ32.J7.QJ94.32 5242(13) s 75.AT.T653.KQT54 2245(9) 90 [-140]
2 2 3 4N n AOJ986.K072..762 6403(12) s K2.J.OT87642.KJ5 2173(10) -290 [140]
1N n AT743.T542.A.AJ9 5413(13) s K9.76.K72.KT6432 2236(9) -280 [400]
             n AKQ83.KT.Q8.AK54 5224(21) s JT.J96.AKT75.T62 2353(9) -510 [990]
1N n AQT84.K75.QJ63.T 5341(12) s J.AT9632.KT98.83 1642(8) -190 [140]
         n AKQJ62.KQ9.KJ54. 6340(19) s .AJ875.Q82.KJ532 0535(11) -500 [980]
2 2 3 3N n KQJ62.J9.AQ832.8 5251(13) s A3.62.K975.A7532 2245(11) -570 [420]
1N n AQ983.T54.KT9.AJ 5332(14) s 7.A732.AQJ.T9762 1435(11) 0 [120]
1N n AKJT63.82.K6.JT2 6223(12) s 42.K97.AJT87.075 2353(10) -160 [110]
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n AQT32.AK92.AQT.J 5431(20) s 6.T5.K984.KQT654 1246(8) 0 [920]
2 2N3 3N n AQ932.Q54.AJ986. 5350(13) s 7.AK97.3.KJ98763 1417(11) 0 [400]
              n AKJ632.5.T7.AJ74 6124(13) s 74.J62.AKQ543.T9 2362(10) -500 [980]
1N n AKQJ6.Q84.AT8.K6 5332(19) s 8.AK732.K762.T85 1543(10) -750 [990]
1N n AQ763.KJ4.Q862.T 5341(12) s 52.A953.AJ3.Q532 2434(11) 0 [120]
Lr0.001 reward=-212.19
Some preliminar bidding systems (only first two bids are shown, two more is done but not shown here)
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0265	2	2	2	2	2	3NT	3NT	2NT	3	4	Р	4NT	3	3	3	4	5	5	4	Р
0346	2	2	2	2	2	3	3NT	3	3	4	Р	3NT	4	4	3	Р	4	5	Р	4
0355	2	2	2	2	2	2	Р	3	3	4	3	4	3	5	3	3NT	4	4	5	4
0364	2	2	2	2	3NT	3	2NT	2NT	3	3	4	3	3	4	4NT	3NT	4	3NT	4	4
0436	2	2	2	2	2	3	3NT	3	3	4	3	3NT	3NT	3	4	4NT	5	4	Р	Р
0445	2	2	2	2	2NT	3	3NT	2NT	3	Р	4	3	3	3	3NT	3NT	Р	4	5NT	4NT
0454	2	2	2	2	3	2	3	3	3	4	3	Р	4	4	4	5	4	Р	4NT	5
0463	2	2	2	2	2	4	3	3NT	3	4	3	3	4	Р	4	4NT	4	4	Р	5
0526	2	2	2	2	4	4	3	3	Р	4	3NT	4	3	3	3	3	4NT	5	4	Р
0535	2	2	2	2	3NT	3NT	3	4	4	3	3	3	3NT	4	3	4NT	4	5	Р	Р
0544	2	2	2	2	3NT	3NT	3	4	3	4	3NT	5	3	4	Р	3	3NT	4NT	4	4NT
0553	2	2	2	2	2	2	2NT	3	3	3	4	4	4	3	3	4	4NT	Р	4NT	4
0562	2	2	2	4	4	3	2NT	3	4	3	4	3NT	3NT	4	3	3NT	3NT	4NT	4NT	4
0616	3	2NT	3NT	2	4	4	2NT	4	4	4	4	4	3	3NT	3NT	Р	5	Р	4	5
0625	2	2	2	2	3	2	3	3	3NT	3NT	4	4	4	4	5	4	4	5	5	5
0634	2	2	2	2	2NT	4	Р	3	3	3NT	3	3	4	3	Р	Р	4	4	Р	4
0643	2	2	2	2	3NT	2	3	4	Р	3	4	3NT	3NT	4	4	5	4NT		Р	4
0652	2	2	2	2	4	3	4	3	3NT	3	4	3	3	3	4	3		3NT	4	4NT
0661	3NT	3	3NT	3	2	2	3	3	3	3NT	4	4		4NT	4	4	4NT		5	Р
1066	3	2NT	4	4	2NT	2NT	3NT	3	4	3	4	3NT	4	4	4	4	3NT		4	4
1156	2	2	2	2	2	2	3	2NT		3	3	4	3NT		4	3NT	3NT		4	4
1165	4	3	2	2	4	2NT	4	3NT		3	Р	3	3NT		3NT		Р	3NT	5	4
1246	2	2	2	2	2	2	4	3NT		4	3	3	4	3	4NT		3NT		4	4
1255	2	2	2	2	2	2	Р	Р	3	4	Р	3	3NT	3	4	3	3NT		4	4
1264	2	2	2	2	2	3	3	3	3	Р	3	3	3		3NT	4NT	4	4	4	4
1336	2	2	2	2	2	2	3	3	3	3	3	3	4	Р	3	4	3NT		4	Р
1345	2	2	2	2	2	2	3	4	3	3NT	Р	3NT	4	3	4	4		4NT	4	5
1354	2	2	2	2	2	2	2NT	2NT	3NT	3	3	Р	Р	Р	5	3NT	3NT	4	Р	5

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1426	2	2	2	2	2	3NT	3	2NT	4	3	3	3	4	P	4	4	5	3NT	Р	4
1435	2	2	2	2	2	2NT	P	2NT	3	3NT	3	3	P	P	P	5	3NT	4	4NT	4
1444	2	2	2	2	2	3	4	3	3	3	3	3	4	Р	Р	4	3NT	5	4	4
1453	2	2	2	2	2	2	4	2NT	Р	3	3	5	4	4	Р	3	4	4	5	4
1462	2	2	2	2	2	2	3	2NT	3	3	4	Р	Р	3	4	Р	3NT	4	4NT	4
1516	2	2	2	2	3	3	2NT	3	4	3	3	3NT	3	3NT	3	3NT	5	5	4	5
1525	2	2	2	2	2	2	2NT	2NT	4	3	3	3	3	4	4	3	5	3NT	4	5
1534	2	2	2	2	2	2	3	3	3	3NT	3NT	4	3	4	4	4	5	3NT	5	4
1543	2	2	2	2	2	2	3	Р	3NT	3NT	4	3	4	3	4	3	3NT	4	4	5
1552	2	2	2	2	3NT	3	3	2NT	3NT	3	3NT	3NT	3	3	4	Р	Р	5	4	Р
1561	2	2	2	2	4	3NT	4	2NT	3	3NT	3	3	3	4	3NT	3	4	4	4	4
1606	2	2	2	4	Р	4	3	3	4	4NT	Р	4	3	4	3	5	5	5	5	4
1615	2	2	2	2	3	3	2NT	3	4	3NT	3NT	3	4NT	4	4	4	4	Р	Р	4
1624	2	2	2	2	3	2	3	4	3NT	3	3	4	3NT	4	3	4	4	4	Р	4
1633	2	2	2	2	3	3NT	4	4	4NT	3	3	3	3	4	3NT	4	4	4	5	4
1642	2	2	2	2	3	2	Р	3	Р	Р	3	3NT	4	3	3	Р	3NT	4	4	5
1651	2	2	2	2	3	3	4	2NT	4	3	4	4	3	5	4	4	4	3NT	4	4
1660	2	2	2	2	3	3	4	4	3	3	4NT	4	3	4	3	4	4	4NT	4	4
2056	2	4	2	4	2	2	2NT	3	3	3NT	4	3NT	4	4	3	P	4	4	4	5
2065	2	3	2	2	2NT	4	2NT	3	3	3	4	3	3	3	3	5	P	4	4	P
2146	2	2	2	2	2	2NT	3	4	4	3	3	5	3	3	3	4	5	P	4NT	4
2155	2	2	2	2	2	2NT	3	4	3	P	3	3	3	4	4	3	P	5	4	4
2164	2	2	2	2	2	2	P	3	3	3	4NT	3	3	3	3	3	P	5	4NT	4
2236	2	2	2	2	2	2	P	3	3	P	3	3	P	4	3	3NT	4	P	4	4NT
2245	2	2	2	2	2	2	P	P	P	3	4	3	3	3	3NT	3	3NT	4	4	5
2254	2	2	2	2	2	2	3	3	3	3	3	4NT	3	3	4	3NT	4	4	P	P
2263	2	2	2	2	2	2	P	2NT	3	3	3	3	3	3NT	4	4	3NT	4	P	4
2326	2	2	2	2	2	2	4	P	3	3	P	4	4	4	4NT	P	3NT	P	4NT	4
2335	2	2	2	2	2	2	2NT	2NT	4	3	3	3	3	3	P	P	3NT	3NT	P	- 4NT
2344	2	2	2	2	2	2	3	2NT	3	3	3	4	P	3	3NT	3	3NT	5	4	4
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b)
*** Try 1 Lr=0.001 R=-212.19lambda=0.5eps=0.5 - 0.02 --- North 1st rebid ---
           14
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5530 2 2 2 2 2 2 2 6016 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	5251 5260 5305 5314 5323 5332 5341 5404 5413 5422 5431 5503 5512 5521 5530 6043 6043 6052 6061 6106 6115 6124 6151 6160 6214 6223	2 2 P P P 2 2 P P P 2 2 P P	3 2 3 P P P 2 2 P P 2 2 2 P 2 2 2 2 2 2	2 2 2 P P P 2 2 P P P 3 2 2 2 2 3 2 2 2 2	3 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	2 3 2 2 2 2 3 3 3 2 2 2 2 2 2 2 2 2 2 2
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7321 3
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7402 3
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7420 2
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7501 2
7510 3
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7600 2
--- South's Responses ---
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h.c.p:8-9 10+ 8-9 10+ 8-9 10+
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0634
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0652
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0661	ONT	ONT	2	2	2	4	4	2	2	2	ONT	г	4	2	2	4 N I T	4	4 N I T	4	4
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2533	2	2	3	2	2	2	3	ZNT	4	3	4	4	4	3	4	3	5	3NT		4
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2632	2	2	2	2	2	2	3	3	3	4	2	3	4	4	4	4	4	4	4	5
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