Maths Bootcamp

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Overleaf

October 11, 2024

Parallel Lines

Definition of Percentage

- A **percentage** is a way of expressing a number as a fraction of 100.
- It is denoted by the symbol
- The formula to calculate a percentage is:

$$\text{Percentage} = \left(\frac{\text{Part}}{\text{Whole}} \right) \times 100$$

- Example: If you score 45 out of 60 on a test, the percentage is:

$$\left(\frac{45}{60} \right) \times 100 = 75\%$$
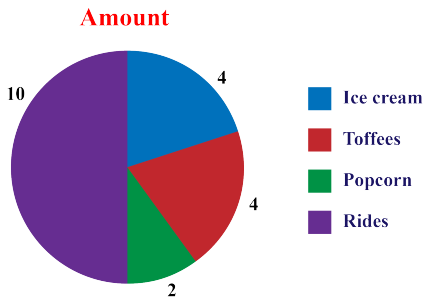
Ratio vs Rate

Figure: ratio

Figure: rate

- Ratio
    - Compares similar quantities
    - Uses colon notation (e.g., 3:2)
    - Example: 5 apples to 3 oranges
- Rate
    - Compares quantities with different units
    - Expresses change between quantities
    - Uses "per unit" (e.g., 5 miles per hour)
    - Example: Cost per pound, heartbeats per minute

Proportional Relationship

Definition

A proportional relationship is a relationship between two quantities where the ratio between them remains constant. If two variables are proportional, it means they can be expressed in the form:

$$y = kx$$

where k is the constant of proportionality and it can be an integer or a fraction or an irrational number.

Proportionality Problem: Mixing Chemicals

Problem

A person mixes $15ml$ of bleach with $3.75L$ of water for sanitizing solution for a daycare. What are the possible combinations

- **A.** 12 mL bleach and 3L water
- **B.** 6 mL bleach and 1.5L water
- **C.** 3 mL leach and 0.75L water
- **D.** 20 mL bleach and 5.5L water

Problem

Is the area of square is propotional to side length ?

Proportionality vs. Linearity

- A **proportional relationship** always passes through the origin $(0, 0)$.
- The general form of a proportional relationship is:

$$y = kx$$

  where k is the constant of proportionality.
- A **linear relationship** can pass through any point, not necessarily the origin.
- The general form of a linear relationship is:

$$y = mx + b$$

  where m is the slope and b is the y-intercept.
- Key Difference:
  - In a proportional relationship, $b = 0$, so the line always passes through $(0, 0)$.
  - In a linear relationship, b can be any value, so the line does not need to pass through the origin.

Variability

Variability

Variability refers to how data points differ from one another within a data set. In real-world data, there is almost always some variation because no two measurements, observations, or events are exactly the same.
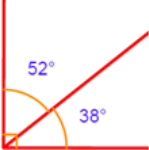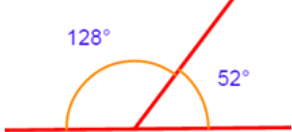
Variability Problems

- How much does my pet weight ?
- What is the average number of cars in a parking lot on Monday mornings ?
- Am i hungry?
- How often am I hungry after lunch ?
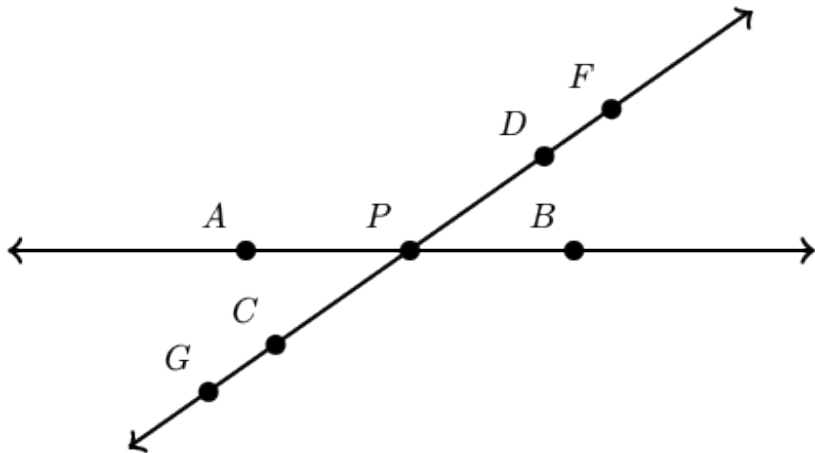- How much time do you spend on facebook every month?

Eucledian Gemotery

Angles

Supplementary and Complementary Angles

Type of Angles	Description	Example
Complementary Angles	Angles that add up to 90°	52° 38°
Supplementary Angles	Angles that add up to 180°	128° 52°

Problem 1

Similarity in Triangles

Proportional Relationship

A relationship between two quantities is proportional if the ratio between those quantities is always equivalent. We will look at side length ratios to find out whether triangles are similar or not

Similarity in All Shapes

The concept of similarity applies to any two shapes that have the same **shape** but may differ in **size**. **Conditions for Similarity**:

- **Corresponding angles must be equal**: The angles in one shape must match the angles in the other.
- **Corresponding sides must be proportional**: The lengths of corresponding sides must have the same ratio (scaling factor).

Examples of Similar Shapes:

- **Quadrilaterals**: Squares, rectangles, rhombuses, and parallelograms can be similar if corresponding angles are equal and side lengths are proportional.
- **Polygons**: Any polygons (pentagons, hexagons, etc.) can be similar if corresponding angles and side lengths meet the conditions.
- **Circles**: All circles are similar because they have the same shape. The ratio of their radii, diameters, or circumferences is the scaling factor.
- **3D Shapes**: Cubes, spheres, pyramids, and other 3D shapes can also be similar if angles and sides are proportional.

Key Point: Similarity applies to all shapes, both in 2D and 3D, as long as the conditions of equal angles and proportional sides are met.

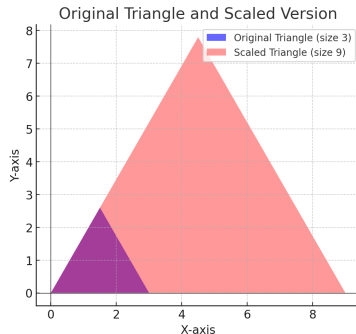# Original Triangle and Scaled Version

Figure: A triangle of size 3 and its scaled version by a factor of 3

Similar Triangles Postulates

- **Angle-Angle (AA) Similarity Postulate:**
  - If two angles of one triangle are congruent to two angles of another triangle, the triangles are similar.
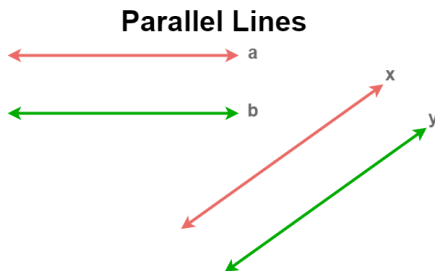- **Side-Angle-Side (SAS) Similarity Postulate:**
  - If one angle of a triangle is congruent to one angle of another triangle, and the sides that include these angles are proportional, then the triangles are similar.
- **Side-Side-Side (SSS) Similarity Postulate:**
  - If the three sides of one triangle are proportional to the three corresponding sides of another triangle, the triangles are similar.

Parallel Lines

- **Definition:** Two or more lines that are always the same distance apart and never meet, no matter how far they are extended.
- They run in the same direction and have the same slope.
- Example: Think of train tracks running side by side—they never cross each other.

Parallel Lines

Transversals