

2.4

$$D[i, j] = \min \begin{cases} D[i-1, j] + \text{del-cost}(\text{source}[i]) \\ D[i, j-1] + \text{ins-cost}(\text{target}[j]) \\ D[i-1, j-1] + \begin{cases} 1, & \text{if } \text{source}[i] \neq \text{target}[j] \\ 0, & \text{if } \text{source}[i] = \text{target}[j] \end{cases} \end{cases}$$

Source →

Target ↓

	#	O	E	A	L
#	0				
L	1	(2, 2, 1) ①	(3, 2, 2) ②	(4, 3, 3) ③	(5, 4, 3) 3
E	2	(2, 3, 2) ②	(3, 3, 1) ①	(4, 2, 3) ②	(4, 3, 4) ③
O	3	(3, 4, 2) ②	(2, 3, 3) ②	(3, 2, 2) ②	(4, 3, 3) ③
A	4	(3, 5, 4) ③	(3, 4, 3) ③	(3, 4, 2) ②	(4, 7, 3) ①

Edit distance of LE O A to O E A L
is 3

- ↳ insertion cost = 1
- ↳ deletion cost = 1
- ↳ Substitution cost = 1
- ↳ i = rows
- ↳ j = columns

2.5

$$D[i, j] = \min \begin{cases} D[i-1, j] + \text{del-cost}(\text{source}[i]) \\ D[i, j-1] + \text{ins-cost}(\text{target}[j]) \\ D[i-1, j-1] + \begin{cases} 2, & \text{if } \text{source}[i] \neq \text{target}[j] \\ 0, & \text{if } \text{source}[i] = \text{target}[j] \end{cases} \end{cases}$$

target
→

#	#	B	R	I	E	F
#	0					
D	1	(2, 2, 2)	3, 2, 3	4, 4, 4	5, 5, 5	6, 6, 6
R	2	3, 3, 3	4, 4, 2	5, 3, 3	6, 4, 6	7, 5, 7
I	3	4, 4, 4	3, 5, 5	4, 4, 2	3, 5, 6	6, 4, 6
V	4	5, 5, 5	4, 6, 6	3, 5, 5	4, 4, 4	5, 5, 5
E	5	6, 6, 6	5, 7, 7	4, 6, 4	5, 5, 3	6, 7, 6

From DRIVE to BRIEF is 4

#	#	D	I	V	E	R	S
#	0						
D	1	2, 2, 0	3, 1, 3	4, 2, 4	5, 3, 5	6, 4, 6	7, 5, 7
R	2	1, 3, 3	2, 2, 2	3, 3, 3	4, 4, 4	5, 5, 3	6, 4, 6
I	3	2, 4, 4	3, 3, 1	4, 2, 4	5, 3, 5	4, 4, 6	5, 5, 5
V	4	3, 5, 5	2, 4, 4	3, 3, 1	4, 2, 4	5, 3, 5	6, 4, 6
E	5	4, 6, 6	3, 5, 5	2, 4, 4	3, 3, 1	4, 2, 4	5, 3, 5

From DRIVE to DIVERS is 3
thus DRIVE is closer to DIVERS.

DRIVE
BRIEF

2.5 is drive closer to brief or to divers

#	D	R	I	V	E	
#	0	1	2	3	4	5
D	1	(2,2,2)	(3,3,3)	(4,4,4)	(5,5,5)	(6,6,6)
R	2	(3,3,3)	(4,4,4)	(5,5,5)	(6,6,6)	(7,7,7)
I	3	(4,4,4)	(5,5,5)	(6,6,6)	(7,7,7)	(8,8,8)
E	4	(5,5,5)	(6,6,6)	(7,7,7)	(8,8,8)	(9,9,9)
F	5	(6,6,6)	(7,7,7)	(8,8,8)	(9,9,9)	(10,10,10)

Note:

- cost are:
- insertion = 1
- deletion = 1
- Substitution = 2
- Same equations as before
- not writing all cell work cause testing two grids (may do at end of min 10 cell)

Edit Distance: 4

#	D	R	I	V	E	
#	0	1	2	3	4	5
D	1	(2,2,0)	(3,1,2)	(4,2,4)	(5,3,4)	(6,4,6)
I	2	(1,3,3)	(2,0,2)	(3,3,1)	(4,2,4)	(5,2,5)
V	3	(2,4,4)	(3,2,3)	(0,4,4)	(3,3,1)	(4,2,4)
E	4	(3,5,5)	(4,4,4)	(3,5,5)	(2,4,4)	(3,3,1)
R	5	(4,6,6)	(5,5,3)	(4,4,6)	(3,5,5)	(2,4,4)
S	6	(5,7,7)	(4,6,6)	(5,5,5)	(4,6,6)	(3,4,5)

DRIVE
DIVERS

DRIVE is closer to DIVERS

Edit Distance: 3