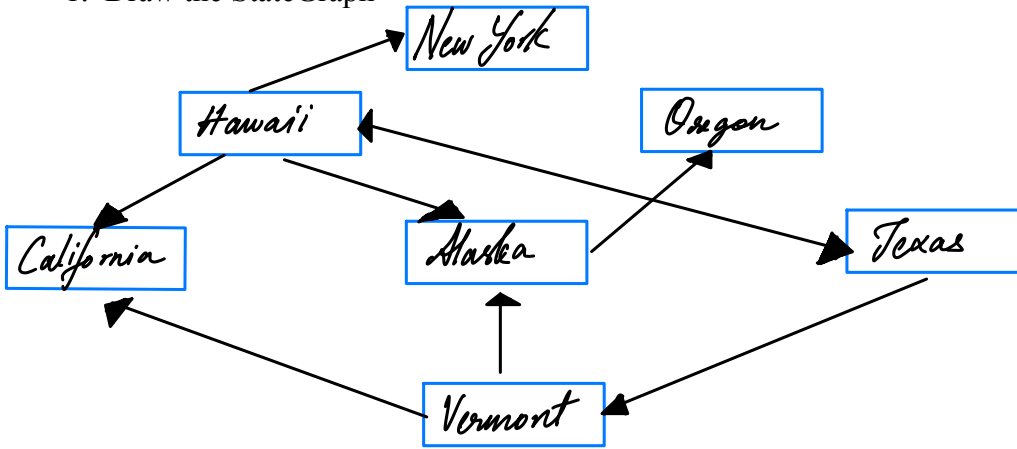


$V(\text{StateGraph}) = \{\text{Oregon, Alaska, Texas, Hawaii, Vermont, New York, California}\}$
 $E(\text{StateGraph}) = \{(\text{Alaska, Oregon}), (\text{Hawaii, Alaska}), (\text{Hawaii, Texas}), (\text{Texas, Hawaii}), (\text{Hawaii, California}), (\text{Hawaii, New York}), (\text{Texas, Vermont}), (\text{Vermont, California}), (\text{Vermont, Alaska})\}$

1. Draw the StateGraph



1. Describe the graph pictured above, using the formal graph notation.

$V(\text{StateGraph}) = \{\text{Oregon, Alaska, Texas, Hawaii, Vermont, New York, California}\}$
 $E(\text{StateGraph}) = \{(\text{Alaska, Oregon}), (\text{Hawaii, Alaska}), (\text{Hawaii, Texas}), (\text{Texas, Hawaii}), (\text{Hawaii, California}), (\text{Hawaii, New York}), (\text{Texas, Vermont}), (\text{Vermont, California}), (\text{Vermont, Alaska})\}$

2. a. Is there a path from Oregon to any other state in the graph?

No

b. Is there a path from Hawaii to every other state in the graph?

Yes

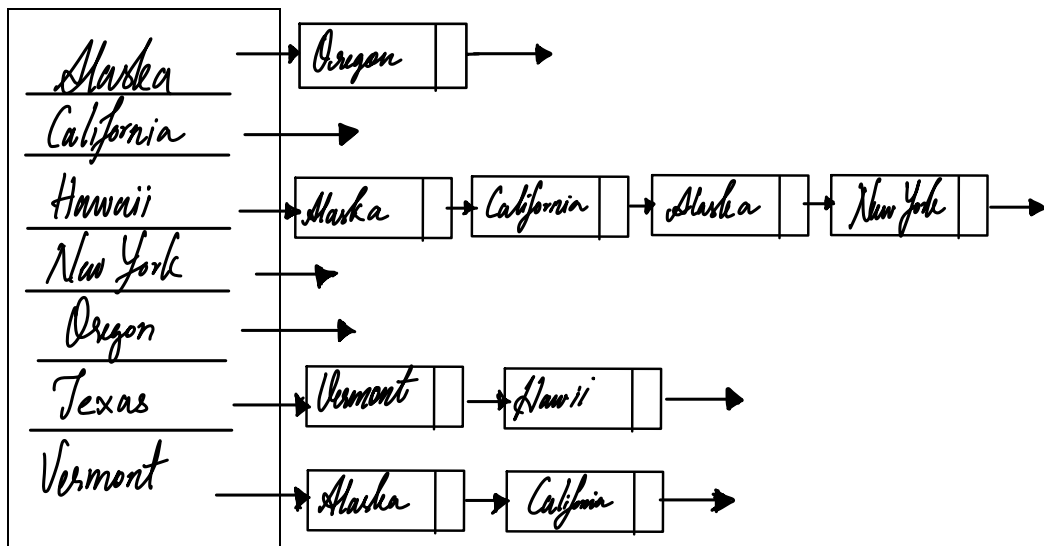
c. From which state(s) in the graph is there a path to Hawaii?

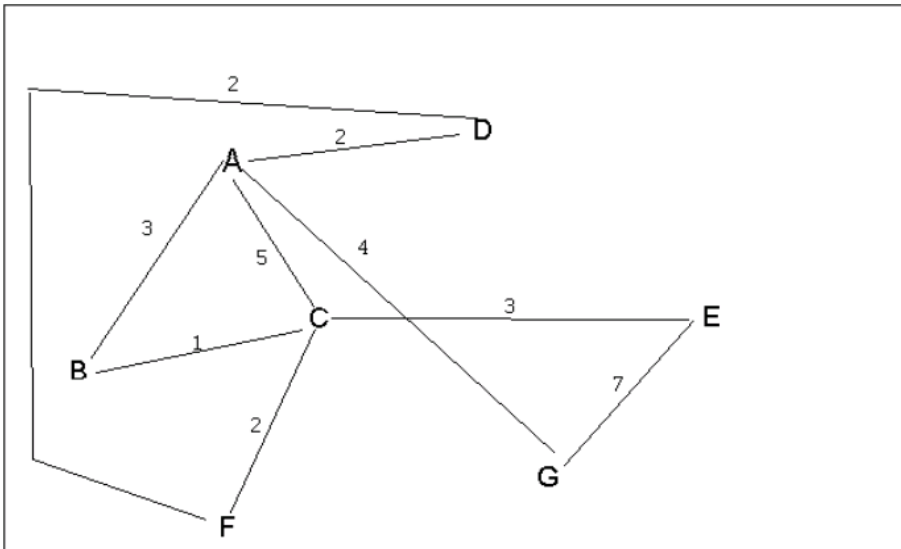
Texas

3. a. Show the adjacency matrix that would describe the edges in the graph.
Store the vertices in alphabetical order

States									
Alaska	0	0	0	0	1	0	0		
California	0	0	0	0	0	0	0		
Hawaii	1	1	0	1	0	1	0		
New York	0	0	0	0	0	0	0		
Oregon	0	0	0	0	0	0	0		
Texas	0	0	1	0	0	0	1		
Vermont	1	1	0	0	0	0	0		

3. b. Show the adjacency lists
that would describe the edges in the graph





4 a. Which of the following lists the graph nodes in depth first order beginning with E?

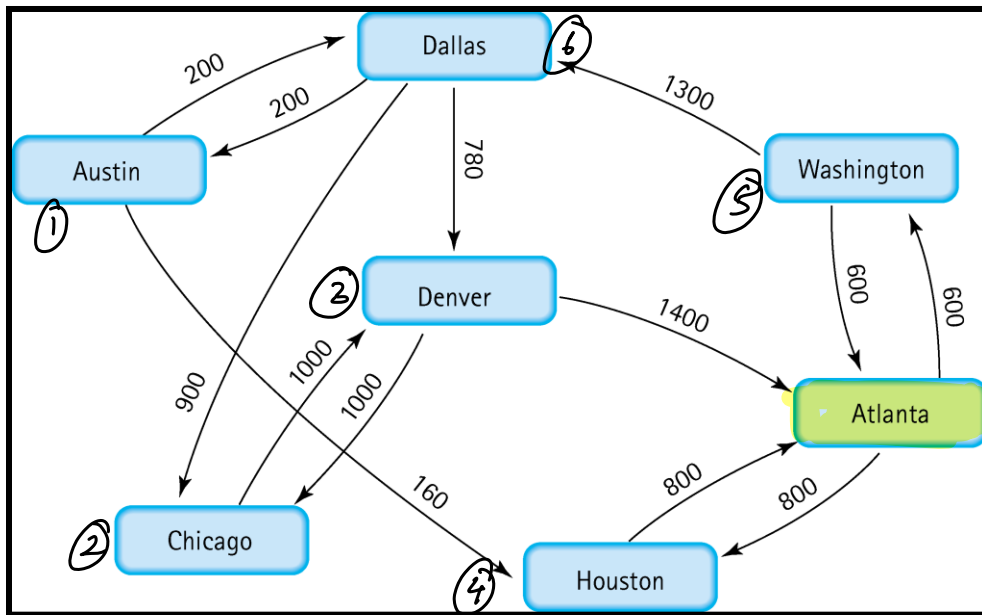
- A) E, G, F, C, D, B, A
- B) G, A, E, C, B, F, D
- C) E, G, A, D, F, C, B
- D) E, C, F, B, A, D, G

option C

4 b. Which of the following lists the graph nodes in breadth first order beginning at F?

- A) F, C, D, A, B, E, G
- B) F, D, C, A, B, C, G
- C) F, C, D, B, G, A, E
- D) a, b, and c are all breadth first traversals

option A



5. Find the shortest distance from **Atlanta** to every other city

① Atlanta - Austin $600 + 1300 + 200 = 2100$

② Atlanta - Chicago $600 + 1300 + 900 = 2800$

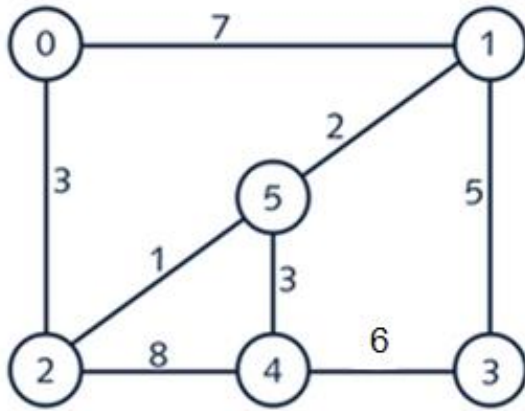
③ Atlanta - Denver $600 + 1300 + 780 = 2680$

④ Atlanta - Houston 800

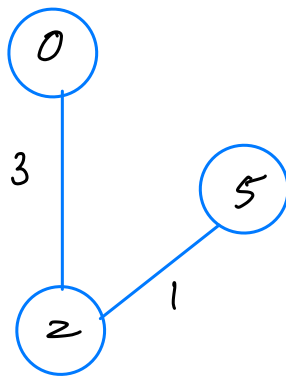
⑤ Atlanta - Washington 600

⑥ Atlanta - Dallas $600 + 1300 = 1900$

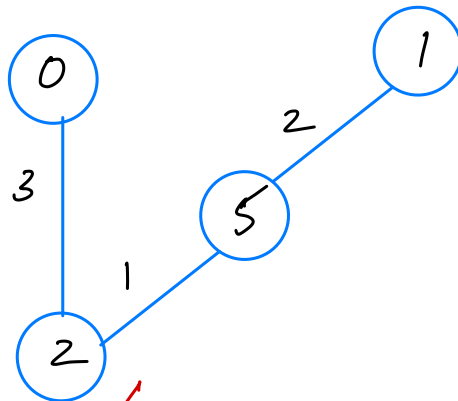
6. Find the **minimal spanning tree** using Prim's algorithm. Use 0 as the source vertex . Show the steps.



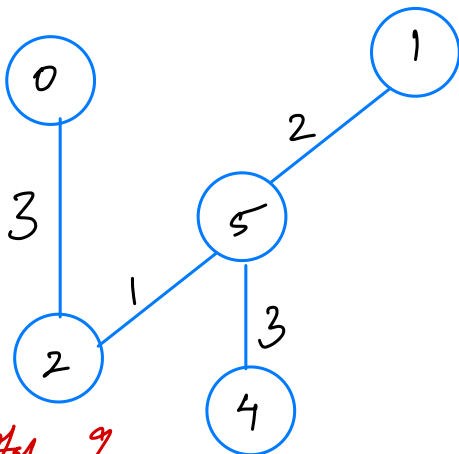
Total path 3



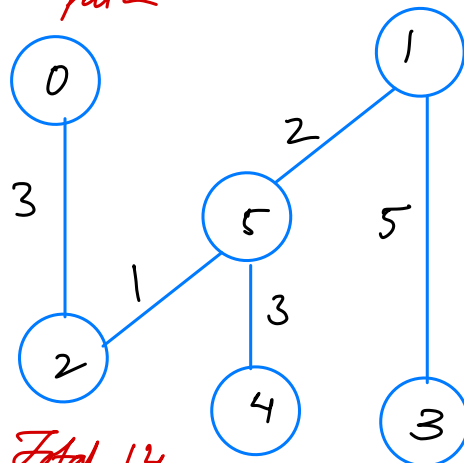
Total path 4



Total path 6

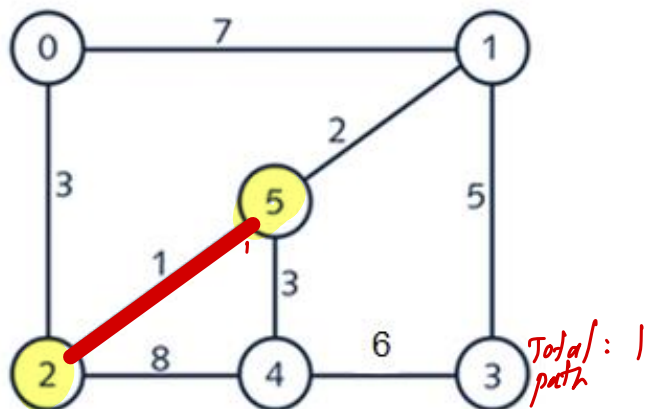


Total path 9

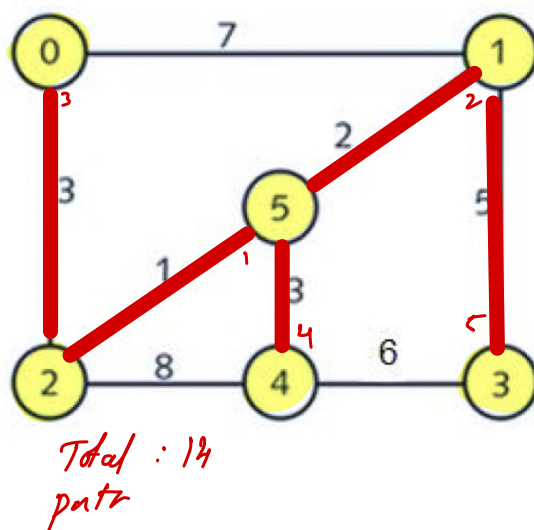
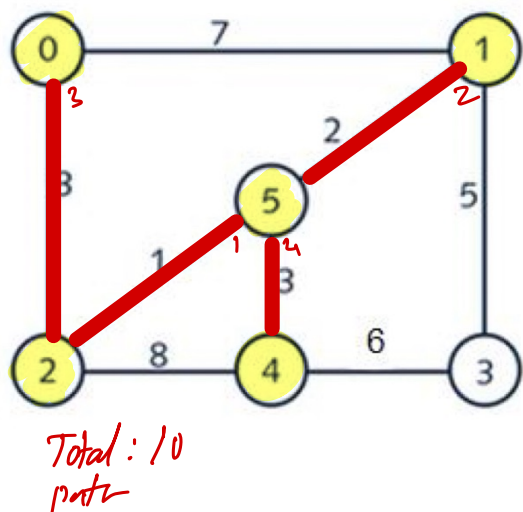
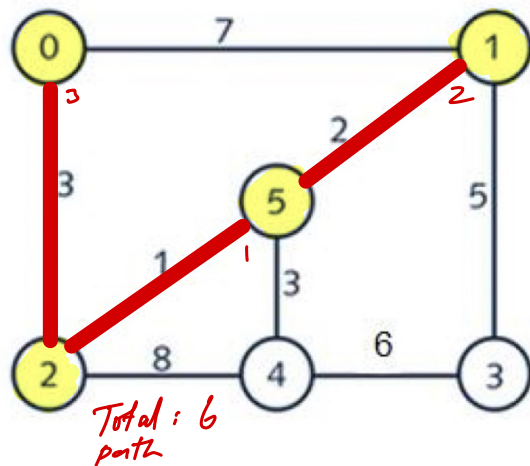
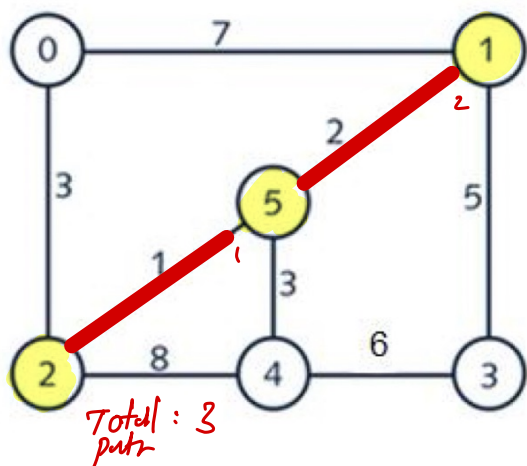


Total path 14

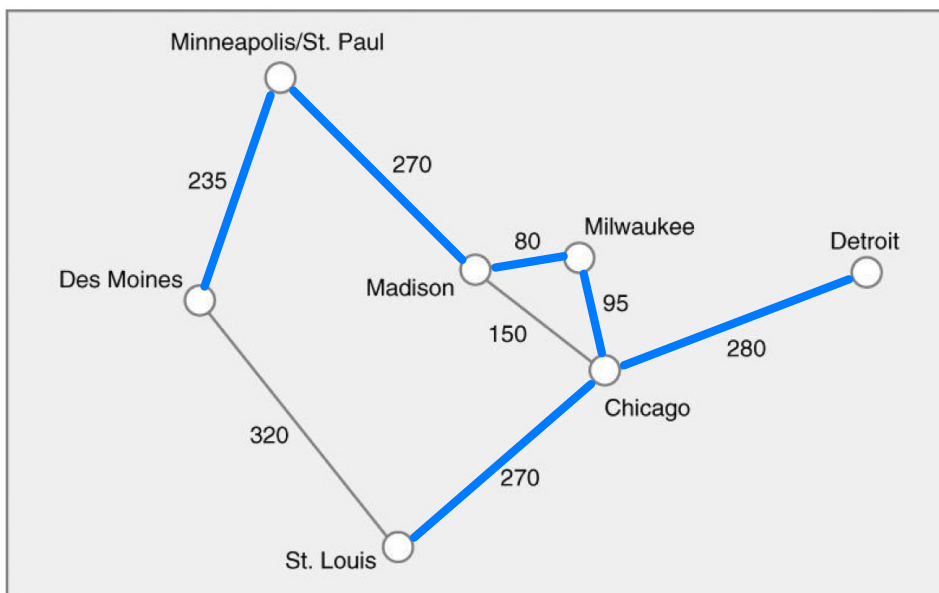
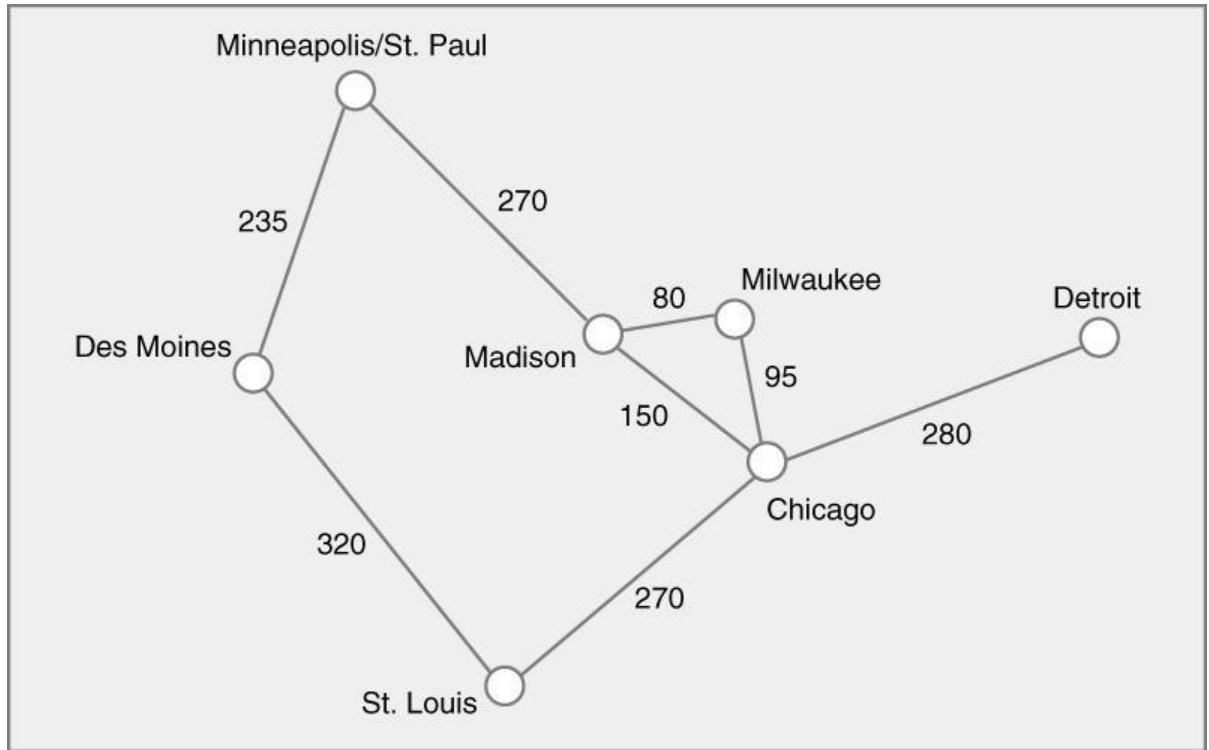
7. Find the **minimal spanning tree** using Kruskal's algorithm. Show the weights in order and the steps.



2-5 : 1
 1-5 : 2
 0-2 : 3
 4-5 : 3
 1-3 : 5
 3-4 : 6
 0-1 : 7
 2-4 : 8



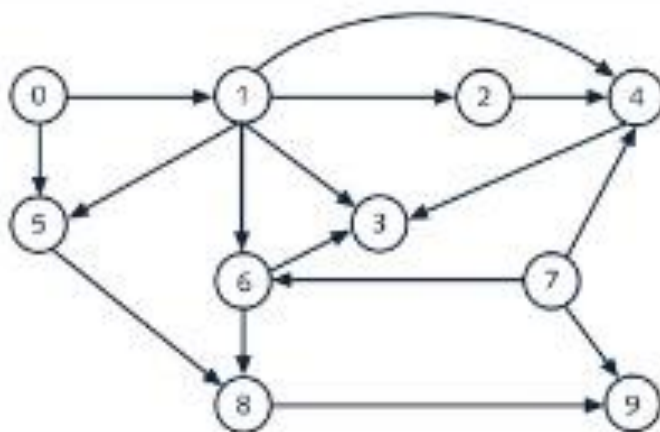
8. Find the minimal spanning tree using the algorithm you prefer. Use Minneapolis/St. Paul as the source vertex



Using Kruskal's

Madison - Milwaukee 80
Milwaukee - Chicago 95
Minneapolis - Des Moines 235
Minneapolis - Madison 270
Chicago - St. Louis 270

steps using arrays predCount, topologicalOrder and a queue



Prod Count
Topological Order
game

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
0	1	1	3	3	2	2	0	2	2

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]

0, 7

Prod Count
Topological Order
qune

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
0	0	1	3	3	1	2	0	2	2

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
0									

7, 1

Pred Count

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
0	0	1	3	2	1	1	0	2	1

Topological Order

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
0	7								

queue

1

Pred Count

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
0	0	0	2	1	0	0	0	2	1

Topological Order

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
0	7	1							

queue

2, 5, 6

Pred Count

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
0	0	0	1	0	0	0	0	0	1

Topological Order

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
0	7	1	2	5	6				

queue

4, 8

Pred Count

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
0	0	0	0	0	0	0	0	0	0

Topological Order

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
0	7	1	2	5	6	4	8		

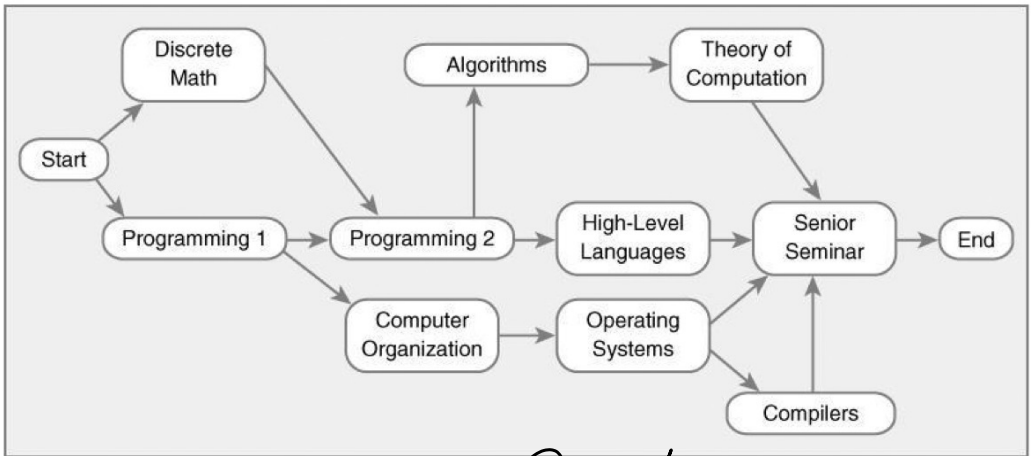
queue

3, 9

Prd Count
Topological Order
queue

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
0	0	0	0	0	0	0	0	0	0
[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
0	7	1	2	5	6	4	8	3	9

10. List the nodes of the graph in a breadth first topological ordering.



- ① Start
- ② Discrete Math
- ③ Programming 1
- ④ Computer Organization
- ⑤ Programming 2
- ⑥ Operating Systems
- ⑦ Algorithms
- ⑧ High level languages
- ⑨ Compilers
- ⑩ Theory of Computation
- ⑪ Senior Seminar
- ⑫ End.