

# Schedulability test for a jobset using Deadline Monotonic algorithm

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## INTRODUCTION

For the Real-Time Operating System (ROS01) course taught at Rotterdam University of Applied Science the authors have to prove they understand the theory of RTOS scheduling and can analyse a jobset for a real time system. After the analysis of the jobset the authors should conclude if the jobset is schedulable according to the Deadline Monotonic algorithm.

The schedulability tests assume that the jobset will be executed on a uniprocessor system where tasks are preemptable. It also assumes that there is no context-switching time. It also assumes that the execution of the scheduler does not require the processor, that is, the scheduler runs on another specialized processor.

The system has 4 different kind of shared resources  $k$ . Every shared resource  $k$  has a maximum hold time it may be claimed  $C_k$ . These 4 different shared resources with their respective maximum hold time are given in Table 1.

$k$	$C_k$
1	8
2	20
3	10
4	40

Table 1. Characteristics of the available shared resources.

This document uses task characteristics letters compatible with the letters defined by Cheng in Task  $T_i$  has a maximum computation time  $c_i$ , a deadline  $d_i$  and a period  $p_i$ . The characteristics of the various real-time tasks in this system can be seen in Table 2.

$i$	$p_i$	$d_i$	$c_i$	Uses shared resource
1	400	360	90	R2, R3, R1
2	600	580	50	R4
3	800	400	30	R1
4	700	420	40	R2
5	200	170	100	R4, R3

Table 2. Characteristics of the different tasks

The goal of this document is to prove whether the given real-time tasks in Table 2 are Deadline Monotonic schedulable taking into account the shared resources in Table 1. What now follows is the outline for the rest of this document. Section 1 uses a couple of simple schedulability tests not taking the shared resources into account.

## 1 SIMPLE SCHEDULABILITY TESTS

For the reader who is not familiar with the term schedulability test, a schedulability test is used to validate that a given application can satisfy its specified deadlines when scheduled according to a specific scheduling algorithm<sup>4</sup>. For the reader who is not familiar with the term schedulable utilization, the schedulable utilization is the maximum utilization allowed for a set of tasks that will guarantee a feasible scheduling for the jobset<sup>4</sup>. Now we can represent the first schedulability test. Given a set of  $n$  independent, preemptable and period tasks on a uniprocessor, let  $U$  be the total utilization of this task set. A necessary and sufficient condition for feasible scheduling of this jobset is Equation 1

$$U = \sum_{i=1}^n \frac{c_i}{p_i} \leq 1 \quad \text{Equation 1.}$$

Using Equation 1 we can use the task characteristics from Table 2 and calculate the utilization. If the calculated utilization is greater than 1 we can conclude that the CPU should do more calculations in a time unit than possible and this jobset is not schedulable. Equation 2 contains the elaboration.

$$U = \sum_{i=1}^5 \frac{c_i}{p_i} = \frac{90}{400} + \frac{50}{600} + \frac{30}{900} + \frac{40}{700} + \frac{100}{200} \approx 0.90 \Rightarrow 0.90 \leq 1 \quad \text{Equation 2.}$$

Since the CPU utilization is less than 1 we can conclude that the jobset may be schedulable. We can use the schedulability test in Equation 3 to test if the jobset can be guaranteed scheduled. If this test fails it does not mean that the jobset is not schedulable. Given a set of  $n$  independent, preemptable and period tasks on a uniprocessor, let  $U$  be the total utilization of this jobset. A sufficient condition for feasible scheduling of this jobset is Equation 3.

$$U = \sum_{i=1}^n \frac{c_i}{p_i} \leq n(2^{\frac{1}{n}} - 1) \quad \text{Equation 3.}$$

However, the condition in Equation 3 may result in under-utilization of the CPU<sup>4</sup>. Imagine  $n \rightarrow \infty$  then the utilization is  $\ln(2)$  or  $\approx 0.693$ . Using Equation 3 with the jobset defined in Table 2 results in an elaboration seen in Equation 4. 0.90 is not less than or equal to  $5(2^{\frac{1}{5}} - 1)$  which is approximately 0.74. This means that this test can not ensure that the jobset is schedulable, but it might still be possible.

$$U = \sum_{i=1}^5 \frac{c_i}{p_i} = \frac{90}{400} + \frac{50}{600} + \frac{30}{900} + \frac{40}{700} + \frac{100}{200} \approx 0.90 \text{ which should be } \leq 5(2^{\frac{1}{5}} - 1) \quad \text{Equation 4.}$$

## 2 SCHEDULABILITY TEST WITHOUT TAKING SHARED RESOURCES INTO ACCOUNT

This section will present the reader a schedulability test which can guarantee whether the jobset is Deadline Monotonic schedulable or not. It does not take the shared resources into account. The reader may wonder why we dedicate a section about proving whether the jobset is Deadline Monotonic schedulable without taking the shared resources into account. If this section proves that the jobset is not Deadline Monotonic schedulable without taking the shared resources into account then the jobset will not be Deadline Monotonic schedulable taking the shared resources into account. The prove whether the jobset is Deadline Monotonic which will be presented in the next section and is an extension on the schedulability test presented in this section.

Suppose we have three tasks  $T_1$ ,  $T_2$  and  $T_3$ . Task  $T_1$  has the smallest deadline followed by  $T_2$ , and then  $T_3$ . It is intuitive to see that in order to schedule  $T_1$  its computation time must be less than or equal to its period. Therefore the following necessary and sufficient condition must hold in Equation 5.

$$c_1 \leq p_1 \quad \text{Equation 5.}$$

For  $T_2$  to be feasible scheduled we need to find enough available time in the period  $[0, p_2]$  that is not used by  $T_1$ . Imagine  $T_2$  is finished executing at time  $t$  then the total number of iterations of  $T_1$  is

$$\left\lceil \frac{t}{p_1} \right\rceil \quad \text{Equation 6.}$$

To ensure that  $T_2$  can complete execution at time  $t$  we must ensure that every iteration of  $T_1$  in  $[0, t]$  must be completed and there should still be enough time for  $T_2$  to execute. The available time for  $T_2$  is

$$t = \left\lceil \frac{t}{p_1} \right\rceil c_1 + c_2 \quad \text{Equation 7.}$$

And similar for  $T_3$  to be feasible scheduled there must be enough time available after scheduling  $T_1$  and  $T_2$

$$t = \left\lceil \frac{t}{p_1} \right\rceil c_1 + \left\lceil \frac{t}{p_2} \right\rceil c_2 + c_3 \quad \text{Equation 8.}$$

The only thing we need to consider is how to determine if such  $t$  exists such that the jobset can be feasible scheduled. There are an infinite number of datapoints in the time interval if no discrete time is assumed. However, the value of the ceiling  $\left\lceil \frac{t}{p_1} \right\rceil$  only changes at multiples of  $p_1$  with an increase of  $c_1$ . Thus we only need to show that a  $k$  exists such that

$$kp_1 \geq kc_1 + c_2 \text{ and } kp_1 \leq kp_2 \quad \text{Equation 9.}$$

Therefore, we need to check that

$$t \geq \left\lceil \frac{t}{p_1} \right\rceil c_1 + c_2 \quad \text{Equation 10.}$$

We will use the equations just derived on the jobset of Table 3. This is the same jobset we introduced in Table ??, but is now arranged in order of priority.  $T_1$  has now the highest priority because its deadline is the shortest compared to the other tasks followed by  $T_2$  and so on.

$i$	$p_i$	$d_i$	$c_i$	Uses shared resource
1	200	170	100	R4, R3
2	400	360	90	R2, R3, R1
3	800	400	30	R1
4	700	420	40	R2
5	600	580	50	R4

**Table 3.** Characteristics of the different tasks rearranged in order of priority

Let

$$w_i(t) = \sum_{k=1}^i C_k \left\lceil \frac{t}{p_k} \right\rceil, 0 < t \leq p_i. \quad \text{Equation 11.}$$

The following inequality

$$w_i(t) \leq t \quad \text{Equation 12.}$$

holds for any time instant  $t$  chosen as follows:

$$t = kp_j, j = 1, \dots, i, k = 1 \dots \left\lfloor \frac{p_i}{p_j} \right\rfloor \quad \text{Equation 13.}$$

For  $T_1$ ,  $i = 1, j = 1, \dots, i = 1$ , so

$$k = 1, \dots, \left\lfloor \frac{p_i}{p_j} \right\rfloor = 1, \dots, \left\lfloor \frac{200}{200} \right\rfloor = 1 \quad \text{Equation 14.}$$

Thus,  $t = kp_j = 1(200) = 200$ . Task  $T_1$  is DM schedulable if  $c_1 \leq 170$ . Since  $c_1 = 100 \leq 200$ ,  $T_1$  is DM schedulable.

For  $T_2$ ,  $i = 2, j = 1, \dots, i = 1, 2$ , so

$$k = 1, \dots, \left\lfloor \frac{p_i}{p_j} \right\rfloor = 1, \dots, \left\lfloor \frac{400}{200} \right\rfloor = 1, 2 \quad \text{Equation 15.}$$

Thus,  $t = 1p_1 = 1(200) = 200$  or  $t = 1p_2 = 1(400) = 400$  or  $t = 2p_1 = 2(200) = 400$ . Task  $T_2$  is DM schedulable if  $c_1 + c_2 \leq 200$  or  $2c_1 + c_2 \leq 400$ . Since  $c_1 = 100, c_2 = 90, 2(100) + 90 \leq 400$ , thus  $T_2$  is DM schedulable together with  $T_1$ .

For  $T_3$ ,  $i = 3, j = 1, \dots, i = 1, 2, 3$ , so

$$k = 1, \dots, \left\lfloor \frac{p_i}{p_j} \right\rfloor = 1, \dots, \left\lfloor \frac{800}{200} \right\rfloor = 1, 2, 3, 4 \quad \text{Equation 16.}$$

Thus,  $t = 1p_1 = 1(200) = 200$  or  $t = 1d_2 = 1(400) = 400$  or  $t = 2d_1 = 2(200) = 400$  or  $t = 1d_3 = 1(800) = 800$  or  $t = 3d_1 = 3(200) = 600$  or  $t = 4d_1 = 4(200) = 800$ . Task  $T_3$  is DM schedulable if  $c_1 + c_2 + c_3 \leq 200$  or  $2c_1 + c_2 + c_3 \leq 400$  or  $4c_1 + 2c_2 + c_3 \leq 800$  or  $3c_1 + 2c_2 + c_3 \leq 600$ . Since  $c_1 = 100, c_2 = 90, c_3 = 30, 2(100) + 90 + 30 \leq 400$ , thus  $T_3$  is DM schedulable together with  $T_1$  and  $T_2$ .

For  $T_4$ ,  $i = 4, j = 1, \dots, i = 1, 2, 3, 4$ , so

$$k = 1, \dots, \left\lfloor \frac{p_i}{p_j} \right\rfloor = 1, \dots, \left\lfloor \frac{700}{200} \right\rfloor = 1, 2, 3 \quad \text{Equation 17.}$$

Thus,  $t = 1p_1 = 1(200) = 200$  or  $t = 1d_2 = 1(400) = 400$  or  $t = 2d_1 = 2(200) = 400$  or  $t = 1d_3 = 1(800) = 800$  or  $t = 3d_1 = 3(200) = 600$  or  $t = 1d_4 = 1(700) = 700$ . Task  $T_4$  is DM schedulable if  $c_1 + c_2 + c_3 + c_4 \leq 200$  or  $2c_1 + c_2 + c_3 + c_4 \leq 400$  or  $4c_1 + 2c_2 + c_3 + c_4 \leq 800$  or  $3c_1 + 2c_2 + c_3 + c_4 \leq 600$  or  $4c_1 + 2c_2 + c_3 + c_4 \leq 700$ . Since  $c_1 = 100, c_2 = 90, c_3 = 30, c_4 = 40, 4(100) + 2(180) + 30 + 40 \leq 700$ , thus  $T_4$  is DM schedulable together with  $T_1$  and  $T_2$  and  $T_3$ .

For  $T_5$ ,  $i = 5, j = 1, \dots, i = 1, 2, 3, 4, 5$ , so

$$k = 1, \dots, \left\lfloor \frac{p_i}{p_j} \right\rfloor = 1, \dots, \left\lfloor \frac{600}{200} \right\rfloor = 1, 2, 3 \quad \text{Equation 18.}$$

Thus,  $t = 1p_1 = 1(200) = 200$  or  $t = 1d_2 = 1(400) = 400$  or  $t = 2d_1 = 2(200) = 400$  or  $t = 1d_3 = 1(800) = 800$  or  $t = 3d_1 = 3(200) = 600$  or  $t = 1d_4 = 1(700) = 700$  or  $t = 1d_5 = 1(600) = 600$ . Task  $T_5$  is DM schedulable if  $c_1 + c_2 + c_3 + c_4 + c_5 \leq 200$  or  $2c_1 + c_2 + c_3 + c_4 + c_5 \leq 400$  or  $4c_1 + 2c_2 + c_3 + 2c_4 + 2c_5 \leq 800$  or  $3c_1 + 2c_2 + c_3 + c_4 + c_5 \leq 600$  or  $4c_1 + 2c_2 + c_3 + c_4 + 2c_5 \leq 700$ . Since  $c_1 = 100, c_2 = 90, c_3 = 30, c_4 = 40, c_5 = 50$ ,  $4(100) + 2(90) + 30 + 2(40) + 2(50) \leq 800$ , thus  $T_5$  is DM schedulable together with  $T_1$  and  $T_2$  and  $T_3$  and  $T_4$ .

The above calculations show that the jobset is DM schedulable. However, there is a snag. This is true if  $d_i = p_i$  holds. Table 3 shows that all tasks have a deadline less than their period. The calculations above did not take the deadline less than the period into account.

### 3 SCHEDULABILITY TEST WHERE $D_I \neq P_I$ AND WHICH DOES NOT TAKE SHARED RESOURCES INTO ACCOUNT

A response time analysis can tell the response time for an individual task. Comparing the response time for an individual task to its deadline (Table 3) gives the definitive answer whether the jobset is DM schedulable without taking the shared resources into account. If the test in this section shows that the jobset is not DM schedulable then the jobset is not DM schedulable taking the shared resources into account. Let

$$R_i = C_i + \sum_{j \in hp(i)} \left\lceil \frac{R_i}{T_j} \right\rceil C_j. \quad \text{Equation 19.}$$

The equation above deserves some explanation. The response time for the highest priority task is  $R = C$ . The response time for any other task that has not the highest priority is  $R_i = C_i + I_i$  where  $I$  is the interference from caused by all the higher priority tasks. The interference can be calculated using  $\left\lceil \frac{R_i}{T_j} \right\rceil C_j$ .

$$R_1 = C_1 = 100.$$

For  $T_2$ ,  $i = 2, j = 1 \dots (i - 1) = 1$ , so

$$R_2 = 90 + \left( \left\lceil \frac{90}{200} \right\rceil * 100 \right) = 90 + (1 * 100) = 190 \quad \text{Equation 20.}$$

$$R_2 = 90 + \left( \left\lceil \frac{190}{200} \right\rceil * 100 \right) = 90 + (1 * 100) = 190 \quad \text{Equation 21.}$$

Thus  $R_2 = 190$ .

For  $T_3$ ,  $i = 3, j = 1 \dots (i - 1) = 1, 2$ , so

$$R_3 = 30 + \left( \left\lceil \frac{190}{400} \right\rceil * 90 + \left\lceil \frac{190}{200} \right\rceil * 100 \right) = 30 + (1 * 90) + (1 * 100) = 220 \quad \text{Equation 22.}$$

$$R_3 = 30 + \left( \left\lceil \frac{220}{400} \right\rceil * 90 + \left\lceil \frac{220}{200} \right\rceil * 100 \right) = 30 + (1 * 90) + (2 * 100) = 320 \quad \text{Equation 23.}$$

$$R_3 = 30 + \left( \left\lceil \frac{320}{400} \right\rceil * 90 + \left\lceil \frac{320}{200} \right\rceil * 100 \right) = 30 + (1 * 90) + (2 * 100) = 320 \quad \text{Equation 24.}$$

Thus  $R_3 = 320$

For  $T_4$ ,  $i = 4, j = 1 \dots (i - 1) = 1, 2, 3$ , so

$$\begin{aligned} R_4 &= 40 + \left( \left\lceil \frac{320}{800} \right\rceil * 30 + \left\lceil \frac{320}{400} \right\rceil * 90 + \left\lceil \frac{320}{200} \right\rceil * 100 \right) = 40 + (1 * 30) + (1 * 90) + (2 * 100) \\ &= 40 + 30 + 90 + 200 = 360 \quad \text{Equation 25.} \end{aligned}$$

$$\begin{aligned} R_4 &= 40 + \left( \left\lceil \frac{360}{800} \right\rceil * 30 + \left\lceil \frac{360}{400} \right\rceil * 90 + \left\lceil \frac{360}{200} \right\rceil * 100 \right) = 40 + (1 * 30) + (1 * 90) + (2 * 100) \\ &= 40 + 30 + 90 + 200 = 360 \quad \text{Equation 26.} \end{aligned}$$

Thus  $R_4 = 360$

For  $T_5$ ,  $i = 5, j = 1 \dots (i - 1) = 1, 2, 3, 4$ , so

$$\begin{aligned} R_5 &= 50 + \left( \left\lceil \frac{360}{700} \right\rceil * 40 + \left\lceil \frac{360}{800} \right\rceil * 30 + \left\lceil \frac{360}{400} \right\rceil * 90 + \left\lceil \frac{360}{200} \right\rceil * 100 \right) = 50 + (1 * 40) + (1 * 30) + (1 * 90) + (2 * 100) \\ &= 50 + 40 + 30 + 90 + 200 = 410 \quad \text{Equation 27.} \end{aligned}$$

$$\begin{aligned} R_5 &= 50 + \left( \left\lceil \frac{410}{700} \right\rceil * 40 + \left\lceil \frac{410}{800} \right\rceil * 30 + \left\lceil \frac{410}{400} \right\rceil * 90 + \left\lceil \frac{410}{200} \right\rceil * 100 \right) = 50 + (1 * 40) + (1 * 30) + (2 * 90) + (3 * 100) \\ &= 50 + 40 + 30 + 180 + 300 = 600 \quad \text{Equation 28.} \end{aligned}$$

$$\begin{aligned} R_5 &= 50 + \left( \left\lceil \frac{600}{700} \right\rceil * 40 + \left\lceil \frac{600}{800} \right\rceil * 30 + \left\lceil \frac{600}{400} \right\rceil * 90 + \left\lceil \frac{600}{200} \right\rceil * 100 \right) = 50 + (1 * 40) + (1 * 30) + (2 * 90) + (3 * 100) \\ &= 50 + 40 + 30 + 180 + 300 = 600 \quad \text{Equation 29.} \end{aligned}$$

Thus  $R_5 = 600$

Now that all response times are known we can verify whether  $R_i \leq d_i$  holds for  $1 \leq i \leq 5$ .

$$R_1 = 100, d_1 = 170, 100 \leq 170 \implies \text{true}$$

$$R_2 = 190, d_2 = 360, 190 \leq 360 \implies \text{true}$$

$$R_3 = 320, d_3 = 400, 320 \leq 400 \implies \text{true}$$

$$R_4 = 360, d_4 = 420, 360 \leq 420 \implies \text{true}$$

$$R_5 = 600, d_5 = 580, 600 \leq 580 \implies \text{false}$$

The jobset is not DM schedulable. If  $d_5 = p_5$  the jobset would be DM schedulable. If the jobset did not include  $T_5$  it would be DM schedulable aswell. However, for the sake of completeness we will do calculations which takes the shared resources into account. If no calculation errors are made the conclusion should be the same as this one.

#### 4 SCHEDULABILITY TEST WHERE $D_I \neq P_I$ AND WHICH DOES TAKE SHARED RESOURCES INTO ACCOUNT

The previous section stated that the response time is  $R_i = C_i + I_i$  where  $I$  is the interference caused by higher priority tasks. A task can wait on a shared resource. It is intuitive to see that the time a task is in the blocked state waiting on this shared resource which is not free should be added to the response time. If  $B$  is the maximum amount of time a task could block on shared resources and  $K$  is the amount of shared resources then let

$$B_i = \sum_{k=1}^K usage(k, i) C_k. \quad \text{Equation 30.}$$

Let  $res(a)$  be a collection of used shared resources of Task  $T_a$ . Let  $P_i$  be the priority of  $T_i$  (where  $P_i = \frac{1}{d_i}$ ).  $usage(k, i)$  is a piecewise function defined as

$$usage(k, i) = \begin{cases} 1 & P_j < P_i \wedge j \neq i, P_h \geq P_i, k \in res(j), k \in res(h) \\ 0 & \text{otherwise} \end{cases}$$

Adding the maximum amount of time a task may block on shared resources leaves the following equation

$$R_i = C_i + B_i + I_i. \quad \text{Equation 31.}$$

Using Equation 30 we can calculate the maximum block time for each task. Table 4 shows for each task which resource may cause a block (using the piecewise  $usage(k, i)$  function) and calculates the total block time by adding the maximum hold time of each resource which the task may block on.

$i$	$P_i$	$k = 1$	$k = 2$	$k = 3$	$k = 4$	$B_i$
1	$\frac{1}{170}$	0	0	1	1	50
2	$\frac{1}{360}$	1	1	0	1	68
3	$\frac{1}{400}$	0	1	0	1	60
4	$\frac{1}{420}$	0	0	0	1	40
5	$\frac{1}{580}$	0	0	0	0	0

**Table 4.** Each task and resource passed to  $usage(i, k)$  piecewise function

$$R_1 = C_1 + B_1 = 100 + 50 = 150.$$

For  $T_2$ ,  $i = 2, j = 1 \dots (i - 1) = 1$ , so

$$R_2 = 90 + 68 + \left( \left\lceil \frac{150}{200} \right\rceil * 100 \right) = 90 + 68 + (1 * 100) = 258 \quad \text{Equation 32.}$$

$$R_2 = 90 + 68 + \left( \left\lceil \frac{258}{200} \right\rceil * 100 \right) = 90 + 68 + (2 * 100) = 358 \quad \text{Equation 33.}$$

$$R_2 = 90 + 68 + \left( \left\lceil \frac{358}{200} \right\rceil * 100 \right) = 90 + 68 + (2 * 100) = 358 \quad \text{Equation 34.}$$

Thus  $R_2 = 358$ .

For  $T_3$ ,  $i = 3, j = 1 \dots (i - 1) = 1, 2$ , so

$$R_3 = 30 + 60 + \left(\left\lceil \frac{358}{400} \right\rceil * 90 + \left\lceil \frac{358}{200} \right\rceil * 100\right) = 30 + 60 + (1 * 90) + (2 * 100) = 380 \quad \text{Equation 35.}$$

$$R_3 = 30 + 60 + \left(\left\lceil \frac{380}{400} \right\rceil * 90 + \left\lceil \frac{380}{200} \right\rceil * 100\right) = 30 + 60 + (1 * 90) + (2 * 100) = 380 \quad \text{Equation 36.}$$

Thus  $R_3 = 380$

For  $T_4$ ,  $i = 4, j = 1 \dots (i - 1) = 1, 2, 3$ , so

$$\begin{aligned} R_4 &= 40 + 40 + \left(\left\lceil \frac{380}{800} \right\rceil * 30 + \left\lceil \frac{380}{400} \right\rceil * 90 + \left\lceil \frac{380}{200} \right\rceil * 100\right) = 40 + 40 + (1 * 30) + (1 * 90) + (2 * 100) \\ &= 40 + 40 + 30 + 90 + 200 = 400 \quad \text{Equation 37.} \end{aligned}$$

$$\begin{aligned} R_4 &= 40 + 40 + \left(\left\lceil \frac{400}{800} \right\rceil * 30 + \left\lceil \frac{400}{400} \right\rceil * 90 + \left\lceil \frac{400}{200} \right\rceil * 100\right) = 40 + 40 + (1 * 30) + (2 * 90) + (2 * 100) \\ &= 40 + 40 + 30 + 180 + 200 = 490 \quad \text{Equation 38.} \end{aligned}$$

Thus  $R_4 = 490$

For  $T_5$ ,  $i = 5, j = 1 \dots (i - 1) = 1, 2, 3, 4$ , so

$$\begin{aligned} R_5 &= 50 + 0 + \left(\left\lceil \frac{490}{700} \right\rceil * 40 + \left\lceil \frac{490}{800} \right\rceil * 30 + \left\lceil \frac{490}{400} \right\rceil * 90 + \left\lceil \frac{490}{200} \right\rceil * 100\right) = 50 + 0 + (1 * 40) + (1 * 30) + (2 * 90) + (3 * 100) \\ &= 50 + 40 + 30 + 180 + 300 = 600 \quad \text{Equation 39.} \end{aligned}$$

Thus  $R_5 = 600$

Now that all response times are known we can verify whether  $R_i \leq d_i$  holds for  $1 \leq i \leq 5$ .

$$R_1 = 150, d_1 = 170, 150 \leq 170 \implies \text{true}$$

$$R_2 = 358, d_2 = 360, 358 \leq 360 \implies \text{true}$$

$$R_3 = 380, d_3 = 400, 380 \leq 400 \implies \text{true}$$

$$R_4 = 490, d_4 = 420, 490 \leq 420 \implies \text{false}$$

$$R_5 = 600, d_5 = 580, 600 \leq 580 \implies \text{false}$$

Without taking the shared resources into account the jobset is DM schedulable if  $T_5$  was not included. Taking the shared resources into account this jobset is only DM schedulable if  $T_5$  and  $T_4$  are not included.

## ACKNOWLEDGEMENTS

“”asd“”

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## **5 SUMMARY**