

$$8 - 2 = 6.$$

Floating Point Subtraction (Binary)

1. Align binary points:

- Align binary point of the number with smaller exponent

2. Add significands:

3. Normalize result:

4. Round and renormalize if necessary:

NB. We assumed that significands can be only 4 bits or digits.

precision format.

Problem: Perform binary floating-point subtraction and convert the resulting values to IEEE-754 single. Finally convert them to hexadecimal values.

$$0.5 - 0.4375$$

$$0.5_{10} = 0.1_2$$

$$\begin{aligned} 0.5 \times 2 &= 1.0 \\ &= 1.0 \times 2^{-1} \end{aligned}$$

$$0.5_{10} = 1.0 \times 2^{-1}$$

step 1

$$\begin{aligned} 0.5_{10} &= 1.000 \times 2^{-1} \\ - 0.4375_{10} &= -0.111 \times 2^{-1} \end{aligned}$$

$$0.4375_{10} = 0.0111_2$$

$$0.4375 \times 2 = 0.875$$

$$0.875 \times 2 = 1.75$$

$$0.75 \times 2 = 1.5$$

$$0.5 \times 2 = 1.0$$

$$\begin{aligned} - 0.4375 &= -1.11 \times 2^{-2} \\ &= -0.111 \times 2^{-1} \end{aligned}$$

$$(0.111)_2 \text{ 1's complement} = 1.000$$

$$2's \text{ complement}(0.111) = \begin{array}{r} 1.000 \\ +1 \\ \hline 1.001 \end{array}$$

$$\begin{array}{r} 0.5 = 1.000 \\ -0.4375 = +1.001 \\ \hline \quad \quad \quad \times 0.001 \end{array}$$

$$\text{Result} = \underbrace{0.001}_{} \times 2^{-1} = \underline{1.000 \times 2^{-4}}$$

$$\text{sign} = 0$$

$$\text{exponent} = -4 + 127 = 123_{10} = 01111011_2$$

$$\text{fraction} = 0.001$$

Floating Point Multiplication

- 1. Add exponents:
- 2. Multiply significands:
- 3. Normalize result:
4. Round and renormalize if necessary:
- 5. Determine the sign of result from signs of operands

NB. We assumed that significands can be only 4 digits of the significands and two digits of the exponents.

Floating Point Multiplication (Decimal)

Consider a 4-digit decimal example: $(1.110 \times 10^{10}) \times (9.2 \times 10^{-5})$

Operand 1

e_1

Operand 2

e_2

$$= 10.212 \times 10^5$$

1. Add exponents

$$e_1 = 10$$

$$e_2 = -5$$

$$e = e_1 + e_2 = 10 - 5 = 5$$

2. Multiply significant

$$\begin{array}{r} 1.110 \\ \times 9.2 \\ \hline 10.212 \end{array}$$

$$\text{Result} = 10.212 \times 10^5$$

$$3. \text{ Result} = 10.21 \times 10^5$$

→ \therefore 5, $\text{sign} = (+) \times (+) = +$

$$\boxed{10.21 \times 10^5}$$

Problem: Perform binary floating-point multiplication and convert the resulting values to IEEE-754 single precision format. Finally convert them to hexadecimal values.

$$0.5 * -0.4375$$

$$0.5_{10} = 0.1_2 = \underbrace{1.0}_{e1} \times 2^{-1}$$

$$0.4375_{10} = 0.0111_2 = \underbrace{1.11}_{e2} \times 2^{-2}$$

1. Add exponent)

$$e = e1 + e2 = -1 - 2 = -3$$

$$2. \quad \begin{aligned} 0.5 &= \boxed{1.000} \times 2^{-1} \\ 0.4375 &= \boxed{1.110} \times 2^{-2} \end{aligned}$$

$$\begin{array}{r} 1.000 \\ 1.110 \\ \hline 0.000 \\ 1000 \\ 1000 \\ 1000 \\ \hline 1.110000 \end{array}$$

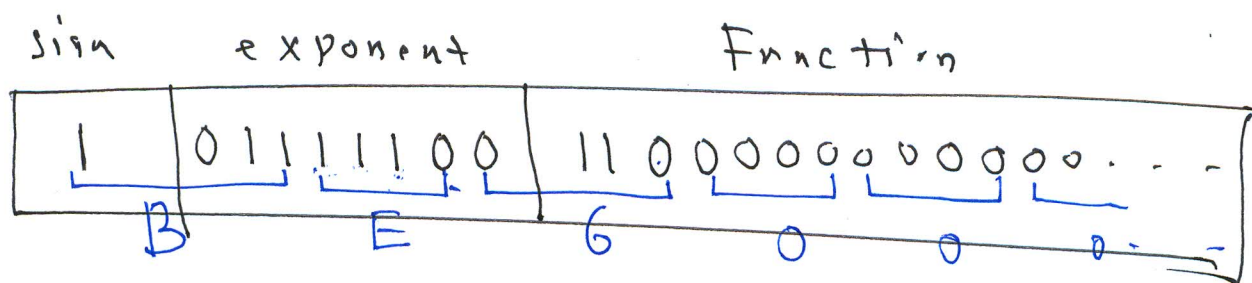
3. Result = 1.11×2^{-3}

5. Sign = $(+) * (-) = -$

$$\text{Sign} = 1$$

$$\text{Exponent} = -3 + 127 = 124_{10} = 01111100_2$$

$$\text{Fraction} = 0.11$$



0XB E600000 ✓

b. Perform the following computation and convert the resulting values in IEEE-754 single precision format.

b

$$-7.25 * 6.5 = ?$$

$$7.25 = 111.01$$

$$= \underline{1.1101} \times 2^2$$

$$6.5 = 110.1$$

$$= \underline{1.101} \times 2^2$$

1. $e_1 = 2 \quad e_2 = 2$

$$e = e_1 + e_2 = \textcircled{4}$$

2. $\underline{1.1101} \times \underline{1.101} = 10.1111001$

$$\text{Result} = 10.1111001 \times 2^4$$

3. Normalize = $\underline{1.01111001} \times 2^{\textcircled{5}}$

5. sign = $(-) * (+) = (-) \text{ve}$

$$\text{sign} = 1$$

$$\text{exponent} = 5 + 127 = 132_{10} = 10000100_2$$

$$\text{fraction} = 0111001$$