# Amplicon data of two different marker genes from the same samples

#### **GPU** functionality

- CUDA/NVDA GPU was loaded and functions
- Mac ARM/metal GPU device is functional

#### **Bayesian distributions**

- Hamiltonian/MCMC/NUTS functionality working
- SVI (Machine learning) functionality working

#### Next

In [1]: import os

• Current model works for 16s PCs (6) and only 1 18s PC. Predicting a matrix looks straight forward for SVI/Machine learning Bayesian.

```
l<sub>mpor<sup>t</sup> a<sup>ll th</sup>e <sup>d</sup>epen<sup>d</sup>enc<sup>i</sup>es</sub>
```

```
import pandas as pd
import numpy as np
import subprocess

In [2]:
import logging
import os

import torch
import matplotlib.pyplot as plt
import numpy as np
import pandas as pd
import seaborn as sns
from torch.distributions import constraints

import pyro
import pyro.distributions as dist
import pyro.optim as optim
```

# Move to working directory

```
In [6]:
os.chdir("C:/Users/Kimani.Kimbrough/MarineDNA/Data")
```

# 01. This section imports the amplicon data sets as raw counts and calls an R script to model the ASV occurrences as probability distributions.

Import amp<sup>licon data sheets as pandas data f</sup>rames and take a look

```
file1 = "Flyer2018_16S_table_counts.tsv"
file2 = "Flyer2018_18S_table_counts.tsv"
asvs1 = pd.read_csv(file1, index_col=0, sep="\t")
asvs2 = pd.read_csv(file2, index_col=0, sep="\t")
Fun the function in a loop over both amplican data sets and make a list of two data frames
```

# 02. Reduce dimensionality and visualize principal components

```
In [8]:
    from sklearn.decomposition import PCA
    import seaborn as sns
```

#### From untransformed matrices

```
In [9]:
         df 16S = pd.read csv('Flyer2018 16S counts modeled.tsv', index col=0,
         sep="\t")
         df 18S = pd.read csv('Flyer2018 18S counts modeled.tsv', index col=0,
         sep="\t")
In [10]:
         df 16S logodds = pd.read csv('Flyer2018 16S counts modeled logodds.tsv',
         index col=0, sep="\t")
         df 18S logodds = pd.read csv('Flyer2018 18S counts modeled logodds.tsv',
         index col=0, sep="\t")
In [11]:
         df 18S logodds.head(3)
Out[11]:
                             ASV_1
                                      ASV_2
                                               ASV_3
                                                        ASV_4
                                                                 ASV_5
                                                                          ASV_6
                                                                                   ASV_7
         CN18Fc12_8_eDNA -10.756859 -10.593197 -8.643773 -8.788970 -8.055674 -5.545171 -4.441849 -2.56
         CN18Fc19 5 eDNA -9.610935 -10.697727 -9.834517 -1.237623 -8.055740 -5.750287 -5.297517 -3.49
         CN18Fc21 6 eDNA -9.526299 -10.299450 -7.894128 -9.666646 -7.648044 -5.544435 -4.821070 -2.90
        3 rows × 7385 columns
```

### From untransformed matrices

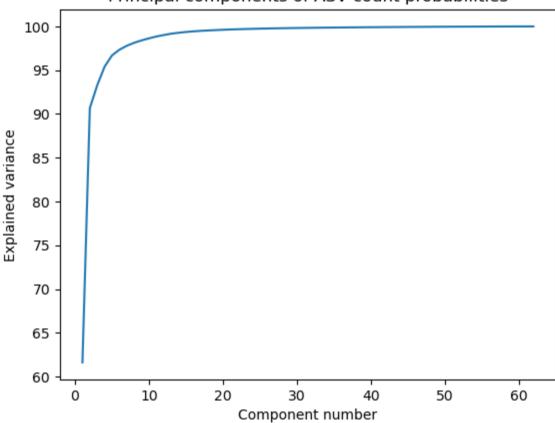
```
In [12]: # Untransformed 16S
    pca = PCA(n_components=62)
    pca.fit_transform(df_16S)
    variance_array_16S = np.cumsum(pca.explained_variance_ratio_ * 100)
    #variance_array_16S

In [13]: # Untransformed 18S
    pca = PCA(n_components=62)
    pca.fit_transform(df_18S)
    variance_array_18S = np.cumsum(pca.explained_variance_ratio_ * 100)
    #variance_array_18S
```

From log\_o<sup>dd</sup>s <sup>t</sup>rans<sup>f</sup>orme<sup>d</sup> ma<sup>t</sup>r<sup>i</sup>ces

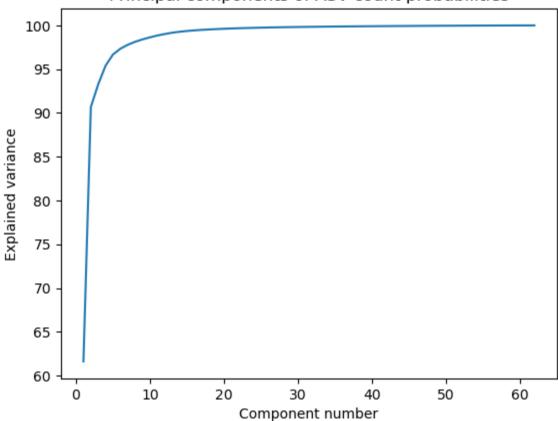
```
In [14]: # Log-odds transformed 16S
           pca = PCA(n_components=62)
           pca.fit transform(df 16S logodds)
           variance_array_16S_logodds = np.cumsum(pca.explained_variance_ratio_ *
           100)
           #variance array 16S logodds
In [15]:
           # Log-odds transformed 18S
           pca = PCA(n_components=62)
           pca.fit transform(df 18S logodds)
           variance array 18S logodds = np.cumsum(pca.explained variance ratio *
           100)
           #variance array 18S Logodds
           <sup>Pl</sup>o<sup>t</sup> componen<sup>t</sup>s vs var<sup>i</sup>ance exp<sup>l</sup>aine<sup>d</sup>
           Base<sup>d</sup> on t<sup>h</sup>e resu<sup>l</sup>ts a<sup>b</sup>ove we w<sup>ill</sup> use t<sup>h</sup>e var<sup>i</sup>ances genera<sup>ted f</sup>rom t<sup>h</sup>e rav
           <sup>(</sup>un<sup>t</sup>rans<sup>f</sup>orme<sup>d)</sup> coun<sup>t</sup> pro<sup>b</sup>a<sup>biliti</sup>es
           Func<sup>ti</sup>on <sup>t</sup>o <sup>f</sup>orma<sup>t</sup> var<sup>i</sup>ance numpy array <sup>f</sup>or sea<sup>b</sup>orn p<sup>l</sup>o
In [16]:
           def format_variance_data_for_plotting(variance_array):
                df = pd.DataFrame(variance_array, columns = ["Explained variance"])
                df = df.reset_index(level=0)
                df['index'] = df['index'] + 1
                df = df.rename(columns = {"index" : "Component number"})
                return(df)
In [17]: # 16S count data
           df variance = format variance data for plotting(variance array 16S)
           sns.lineplot(data=df_variance, x="Component number",
                            y="Explained variance").set(title='Principal components of
           ASV count probabilities')
           [Text(0.5, 1.0, 'Principal components of ASV count probabilities')]
Out[17]:
```

# Principal components of ASV count probabilities



Out[18]: [Text(0.5, 1.0, 'Principal components of ASV count probabilities')]

## Principal components of ASV count probabilities



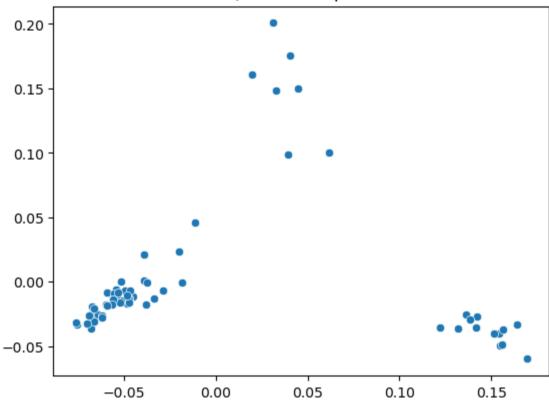
# P'et principal components of raw ASV count probabilities

```
In [19]: pca_16 = PCA(n_components=3)
    pcs_16 = pca.fit_transform(df_16S)

    pc1_values_16 = pcs_16[:,0]
    pc2_values_16 = pcs_16[:,1]
    sns.scatterplot(x=pc1_values_16, y=pc2_values_16).set(title="16S PCA, raw count probabilities")

Out[19]: [Text(0.5, 1.0, '16S PCA, raw count probabilities')]
```

## 16S PCA, raw count probabilities

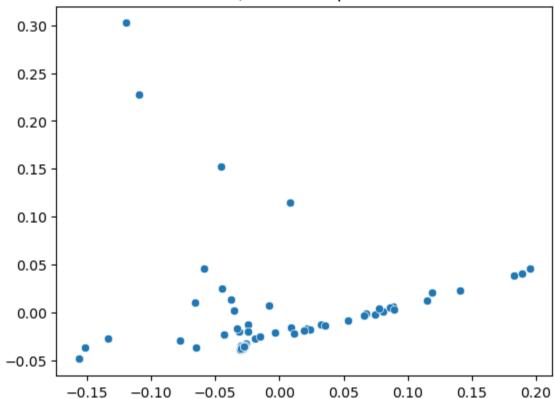


```
In [20]: pca_118 = PCA(n_components=3)
    pcs_18 = pca.fit_transform(df_18S)

pc1_values_18 = pcs_18[:,0]
    pc2_values_18 = pcs_18[:,1]
    sns.scatterplot(x=pc1_values_18, y=pc2_values_18).set(title="18S PCA, raw count probabilities")
```

Out[20]: [Text(0.5, 1.0, '18S PCA, raw count probabilities')]

#### 18S PCA, raw count probabilities



# 03. Test the power of 16S data as a predictor for 18S data

#### Function to extract defined number of PCs with sample labels

```
In [21]:
    def extract_PCs_labeled(df_asvs_modeled, num_pcs):
        pca = PCA(n_components=num_pcs)
        pcs = pca.fit_transform(df_asvs_modeled)
        array = pcs[:, :num_pcs]
        cols = list()
        for i in range(1, num_pcs+1):
            n="PC%s" % i
            cols.append(n)
        df = pd.DataFrame(array, index=df_16S.index, columns = cols)
        return(df)
```

#### Export the first six PCs of the 16S data which explain 97% of the variance

```
In [22]: pcs_16S = extract_PCs_labeled(df_16S, 6)
pcs_16S.to_csv("Flyer2018_16S_PCs.tsv", sep="\t")
```

pcs\_16S

| _    |     | _ |    | - |
|------|-----|---|----|---|
| )11. | † I | • | ') |   |
| Ju   | U   | _ | _  |   |

|                  | PC1       | PC2       | PC3       | PC4       | PC5       | PC6       |
|------------------|-----------|-----------|-----------|-----------|-----------|-----------|
| CN18Fc12_8_eDNA  | -0.020128 | 0.023832  | -0.024139 | 0.038050  | -0.016783 | 0.001938  |
| CN18Fc19_5_eDNA  | -0.075552 | -0.033142 | 0.010200  | -0.011909 | 0.003156  | -0.002386 |
| CN18Fc21_6_eDNA  | -0.048505 | -0.016760 | -0.003077 | 0.003165  | -0.006532 | 0.004679  |
| CN18Fc22_6_eDNA  | -0.066767 | -0.022830 | 0.005425  | -0.001503 | -0.004624 | 0.003922  |
| CN18Fc24_6_eDNA  | -0.059178 | -0.008103 | -0.005169 | 0.006752  | -0.001524 | 0.001449  |
| •••              | •••       | •••       | •••       | •••       |           | •••       |
| CN18SESPkoa_SC42 | 0.131701  | -0.035945 | 0.003022  | -0.002341 | -0.002827 | 0.002591  |
| CN18SESPkoa_SC44 | 0.032810  | 0.148524  | -0.005046 | 0.012712  | -0.028669 | -0.015435 |
| CN18SESPkoa_SC45 | 0.141820  | -0.035358 | 0.004186  | 0.004716  | -0.003955 | 0.000039  |
| CN18SESPkoa_SC47 | 0.136522  | -0.025320 | -0.000650 | 0.013615  | -0.006447 | -0.002134 |
| CN18SESPkoa_SC49 | 0.138331  | -0.028862 | 0.002282  | 0.010463  | -0.006027 | -0.001998 |

62 rows × 6 columns

pre<sup>di</sup>c<sup>ti</sup>ve power

```
In [23]: pcs_18S = extract_PCs_labeled(df_18S, 2)
        pcs_18S.to_csv("Flyer2018_18S_PCs.tsv", sep="\t")
        pcs_18S
```

Out[23]:

|                  | PC1       | PC2       |
|------------------|-----------|-----------|
| CN18Fc12_8_eDNA  | -0.018686 | -0.027522 |
| CN18Fc19_5_eDNA  | -0.133394 | -0.027902 |
| CN18Fc21_6_eDNA  | -0.031460 | -0.019696 |
| CN18Fc22_6_eDNA  | -0.042921 | -0.023416 |
| CN18Fc24_6_eDNA  | -0.151135 | -0.036783 |
| •••              |           |           |
| CN18SESPkoa_SC42 | -0.026949 | -0.034856 |
| CN18SESPkoa_SC44 | -0.029892 | -0.037498 |
| CN18SESPkoa_SC45 | -0.027413 | -0.035936 |
| CN18SESPkoa_SC47 | -0.027500 | -0.036121 |
| CN18SESPkoa_SC49 | -0.027284 | -0.035349 |

62 rows × 2 columns

```
Pass resu<sup>lt</sup>s of 165 and 185 PCAS <sup>to B</sup>ayes<sup>i</sup>an mo<sup>d</sup>eling R <sup>S</sup>cr<sup>i</sup>p<sup>t</sup>
         Pyro Pytorch linear mo<sup>d</sup>el
            fine variables based on PCA results from above; can only pass strings to R
In [24]:
         path to rscript =
         "/Users/nastassia.patin/GitHub/MarineDNA/PC_bayesian_runner_test.R"
         num 18S PCs = "2" # Number of PCs to predict in 18S data
         num_16S_preds = "6" # Number of predictor PCs to use from 16S data; as
         many as account for expected variance of predictor
         num ind = "62" # Number of observances (samples) in 18S data
         Run the function and display summary output
In [25]:
         #bayes summary 16S 18S =
         bayesian modeling of two markergenes(path to rscript,
                                                                            num 18S PCs,
         num_16S_preds,
                                                                            num_ind)
         #bayes_summary_16S_18S
In [26]:
         print(pcs_16S.columns.values)
         ['PC1' 'PC2' 'PC3' 'PC4' 'PC5' 'PC6']
In [27]:
         df1 = pcs_16S[['PC1', 'PC2', 'PC3', 'PC4', 'PC5', 'PC6']]
         df1.columns = ['pc1_values_16', 'pc2_values_16', 'pc3_values_16',
         'pc4_values_16', 'pc5_values_16', 'pc6_values_16']
         df2 = pcs_18S[['PC1']]
         df2.columns = ['pc1_values_18']
         df = pd.merge(df1, df2, left_index=True, right_index=True)
In [29]:
         def model(pc1_values_16, pc2_values_16, pc3_values_16, pc4_values_16,
         pc5 values 16, pc6 values 16, pc1 values 18):
              a = pyro.sample("a", dist.Normal(0., 100000.))
             b_PC1 = pyro.sample("b1", dist.Normal(0., 10000.))
             b PC2 = pyro.sample("b2", dist.Normal(0., 10000.))
```

```
b_PC3 = pyro.sample("b3", dist.Normal(0., 10000.))
b_PC4 = pyro.sample("b4", dist.Normal(0., 10000.))
b_PC5 = pyro.sample("b5", dist.Normal(0., 10000.))
b_PC6 = pyro.sample("b6", dist.Normal(0., 10000.))
sigma = pyro.sample("sigma", dist.Uniform(0., 10000.))

mean = a + b_PC1 * pc1_values_16 + b_PC2 * pc2_values_16 + b_PC3 * pc3_values_16 + b_PC4 * pc4_values_16 + b_PC5 * pc5_values_16 + b_PC6 * pc6_values_16
with pyro.plate("data", len(pc6_values_16)):
    return pyro.sample("obs", dist.Normal(mean, sigma), obs=pc1_values_18)
```

```
In [40]:
        from pyro.infer.autoguide import AutoMultivariateNormal, init to mean
        guide = AutoMultivariateNormal(model, init loc fn=init to mean)
        svi = SVI(model,
                   guide,
                   optim.Adam({"lr": .01}),
                   loss=Trace ELBO())
        pc1 values 16, pc2 values 16, pc3 values 16, pc4 values 16, pc5 values 16,
        pc6_values_16, pc1_values_18 = train[:, 0], train[:, 1], train[:, 2],
        train[:, 3], train[:, 4], train[:, 5], train[:, 6]
        pyro.clear param store()
        for i in range(num iters):
             elbo = svi.step(pc1 values 16, pc2 values 16, pc3 values 16,
        pc4_values_16, pc5_values_16, pc6_values_16, pc1_values_18)
             if i % 500 == 0:
                 logging.info("Elbo loss: {}".format(elbo))
```

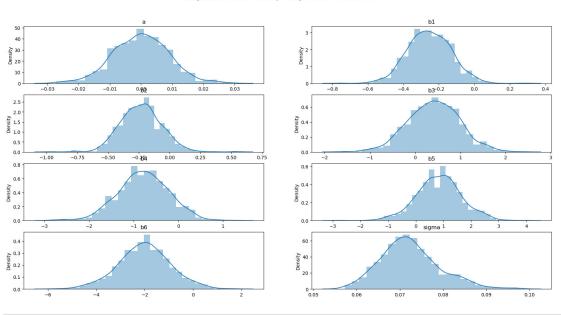
```
Elbo loss: 663.874231338501
        Elbo loss: 337.2063698768616
        Elbo loss: 71.16333341598511
        Elbo loss: 9.3086519241333
        Elbo loss: 9.785514831542969
        Elbo loss: 10.661048889160156
        Elbo loss: 8.096829414367676
        Elbo loss: 11.31319808959961
        Elbo loss: 12.004347801208496
        Elbo loss: 10.443873405456543
In [31]: # Utility function to print latent sites' quantile information.
         def summary(samples):
             site stats = {}
             for site name, values in samples.items():
                 marginal site = pd.DataFrame(values)
                 describe = marginal site.describe(percentiles=[.05, 0.25, 0.5,
         0.75, 0.95]).transpose()
                 site stats[site name] = describe[["mean", "std", "5%", "25%",
         "50%","75%","95%"]]
             return site_stats
In [32]: # Prepare training data
         df4 = df[['pc1_values_16', 'pc2_values_16', 'pc3_values_16',
         'pc4_values_16', 'pc5_values_16', 'pc6_values_16', 'pc1_values_18']]
         df5 = df4[np.isfinite(df.pc1_values_18)]
         train = torch.tensor(df5.values, dtype=torch.float)
In [33]: from pyro.infer import SVI, Trace_ELBO
         svi = SVI(model,
                   guide,
                   optim.Adam({"lr": .05}),
                   loss=Trace ELBO())
         pc1 values 16, pc2 values 16, pc3 values 16, pc4 values 16, pc5 values 16,
         pc6_values_16, pc1_values_18 = train[:, 0], train[:, 1], train[:, 2],
         train[:, 3], train[:, 4], train[:, 5], train[:, 6]
         pyro.clear param store()
         num_iters = 5000 if not smoke_test else 2
```

```
for i in range(num_iters):
             elbo = svi.step(pc1 values 16, pc2 values 16, pc3 values 16,
         pc4_values_16, pc5_values_16, pc6_values_16, pc1_values_18)
             if i % 500 == 0:
                 logging.info("Elbo loss: {}".format(elbo))
        Elbo loss: 670.0780696868896
        Elbo loss: 13.34172248840332
        Elbo loss: 17.20850944519043
        Elbo loss: 9.504776954650879
        Elbo loss: 9.566930770874023
        Elbo loss: 10.968674659729004
        Elbo loss: 11.626540184020996
        Elbo loss: 9.353282928466797
        Elbo loss: 18.191561698913574
        Elbo loss: 13.249004364013672
In [34]:
        # Prepare training data
         train = torch.tensor(df.values, dtype=torch.float)
         #train
In [35]:
        from pyro.infer import Predictive
         num_samples = 1000
         predictive = Predictive(model, guide=guide, num samples=num samples)
         svi_samples = {k: v.reshape(num_samples).detach().cpu().numpy()
                        for k, v in predictive(pc1_values_16, pc2_values_16,
         pc3_values_16, pc4_values_16, pc5_values_16, pc6_values_16,
         pc1_values_18).items()
                        if k != "obs"}
In [36]: from pyro.infer import MCMC, NUTS
         nuts kernel = NUTS(model)
         mcmc = MCMC(nuts_kernel, num_samples=1000, warmup_steps=200)
         mcmc.run(pc1 values 16, pc2 values 16, pc3 values 16, pc4 values 16,
         pc5_values_16, pc6_values_16, pc1_values_18)
```

```
hmc_samples = {k: v.detach().cpu().numpy() for k, v in
        mcmc.get samples().items()}
        Sample: 100% | 1200/1200 [01:21, 14.81it/s, step size=5.97e-01, acc. prob=
        0.903]
In [37]:
        for site, values in summary(hmc samples).items():
            print("Site: {}".format(site))
            print(values, "\n")
        Site: a
                        std
                                 5%
                                         25%
                                                  50%
                                                           75%
                                                                    95%
              mean
        0.005905 0.014473
        Site: b1
                                 5%
                                         25%
                                                  50%
                                                           75%
                                                                    95%
              mean
                        std
        Site: b2
              mean
                       std
                                5%
                                        25%
                                                 50%
                                                          75%
                                                                   95%
        0 -0.231491   0.16589 -0.492472 -0.343375 -0.230323 -0.128819   0.027552
        Site: b3
                        std
                                5%
                                        25%
                                                 50%
                                                          75%
                                                                   95%
        0 0.410288 0.565431 -0.48369 0.025277 0.411468 0.798516 1.316391
        Site: b4
                                 5%
                                       25%
                                                50%
                                                         75%
                                                                  95%
              mean
                       std
        0 -0.780196  0.56178 -1.684114 -1.13819 -0.772413 -0.397522  0.145287
        Site: b5
                                 5%
                                         25%
                                                  50%
                                                           75%
                                                                    95%
              mean
                        std
        0 0.846589 0.802281 -0.473396 0.333958 0.884097 1.346998 2.224882
        Site: b6
                                 5%
                                                  50%
                        std
                                         25%
                                                           75%
                                                                    95%
              mean
        0 -2.010562 1.069957 -3.802254 -2.692759 -1.999521 -1.322854 -0.195606
        Site: sigma
                                 5%
                                         25%
                                                  50%
                                                           75%
                                                                    95%
              mean
                        std
        0 0.072411 0.006784 0.062412 0.067775 0.071762 0.076364 0.084708
In [38]:
        sites = ["a", "b1", "b2", "b3", "b4", "b5", "b6", "sigma"]
        fig, axs = plt.subplots(nrows=4, ncols=2, figsize=(20, 10))
        fig.suptitle("Marginal Posterior density - Regression Coefficients",
        fontsize=16)
        for i, ax in enumerate(axs.reshape(-1)):
```

```
site = sites[i]
#sns.distplot(svi_samples[site], ax=ax, label="SVI (DiagNormal)")
sns.distplot(hmc_samples[site], ax=ax, label="HMC")
ax.set_title(site)
handles, labels = ax.get_legend_handles_labels()
fig.legend(handles, labels, loc='upper right');
```

Marginal Posterior density - Regression Coefficients



```
In [39]:
        predictive = Predictive(model, guide=guide, num_samples=num_samples)
         svi_mvn_samples = {k: v.reshape(num_samples).detach().cpu().numpy()
                            for k, v in predictive(pc1_values_18, pc1_values_16,
        pc2_values_16, pc3_values_16, pc4_values_16, pc5_values_16,
         pc6_values_16).items()
                            if k != "obs"}
        fig, axs = plt.subplots(nrows=2, ncols=2, figsize=(12, 10))
        fig.suptitle("Marginal Posterior density - Regression Coefficients",
        fontsize=16)
        for i, ax in enumerate(axs.reshape(-1)):
             site = sites[i]
             sns.distplot(svi mvn samples[site], ax=ax, label="SVI (Multivariate
        Normal)")
             sns.distplot(hmc_samples[site], ax=ax, label="HMC")
             ax.set_title(site)
        handles, labels = ax.get_legend_handles_labels()
        fig.legend(handles, labels, loc='upper right');
```

## Marginal Posterior density - Regression Coefficients

