

# Entry and Exit 1

## PhD Industrial Organization

Nicholas Vreugdenhil

# Motivation

- So far, we have studied models where the **market structure is fixed**.
  - Market structure: number of firms, types of products, firm size etc
  - Example of what we have implicitly assumed so far: demand estimation took characteristics of products as fixed, supply side: profit maximization given product characteristics

# Motivation

- Now, we will take a step back and start to think about **endogenous market structure**.
  - Fundamental IO question: why exactly does market structure vary across industries?
  - Clear implications for policy:
  - Example 1: Effects of a merger
  - Example 2: Increasing costs due to environmental regulation
  - Example 3: Bailout of the truck manufacturing industry

# Motivation

- We will start by looking at some simple models of firm entry and exit.
- Theoretical model as a starting point:
- **Stage 1:** Potential entrants decide whether to enter
- **Stage 2:** Firms compete given entry
- Later on in the course we will study dynamic games which contain strategic interactions between firms, investment, entry, and exit, over time.

# Motivation

- **Today:** we will look at some earlier work attempting to estimate entry models.
- As we will see, although these paper are creative, influential, and important, they often require some strong assumptions in order to take the model to data.
- Next time we will see a new strand of literature that resolves a key assumption of these papers.
  - Key assumption: uniqueness of equilibrium

# Plan

1. Bresnahan and Reiss (1991)
2. Mazzeo (2002)
3. Seim (2006)

# Plan

1. **Bresnahan and Reiss (1991)**
2. Mazzeo (2002)
3. Seim (2006)

## Bresnahan and Reiss (1991): Research Questions

- 1. How do profits change with the number of firms?
- 2. How many firms need to enter before an oligopoly market becomes competitive?



## Bresnahan and Reiss (1991): Data

- Isolated markets  $M$  (202 markets)
  - Isolated since it is easier to define a 'market' and 'entry into a market'. I.e. these markets are independent in terms of demand, competition, etc.
  - Pre-internet, they got this data through the phonebook and also by driving (or maybe getting their RA to drive) around small towns in Western USA (!)
- Look at retail/professional services e.g. doctors, dentists, plumbers
- For each market  $m$ : observe active firms  $n_m$ , market size  $s_m$ , and some exogenous market characteristics that may affect demand/costs  $x_m$

## Bresnahan and Reiss (1991): Model

- Homogeneous firms.  $N$  potential entrants.
- Equilibrium number of firms  $n_m$  satisfies:

$$\Pi_m(n_m) \geq 0$$

$$\Pi_m(n_m + 1) < 0$$

- That is, each firm is playing a best response to the other firms: all active firms stay in the market, all inactive firms stay out.

## Bresnahan and Reiss (1991): Model

- Parameterize profit as follows:

$$\Pi_m(n_m) = V_m(n) - F_m(n)$$

- Where  $V_m(n)$  is variable profit:

$$V_m(n) = s_m v_m(n) = s_m (x_m^D \beta - \alpha(n))$$

- $s_m$ : market size
- $v_m(n)$ : variable profit per-capita
- $x_m^D$ : vector of market characteristics that may affect demand (e.g. per-capita income)
- $\beta$ : parameter vector
- $\alpha(n)$ : parameter that captures degree of competition (strictly increasing in  $n$ ).

## Bresnahan and Reiss (1991): Model

- Here,  $F_m(n)$  is fixed cost:

$$F_m(n) = x_m^C \gamma + \delta(n) + \epsilon_m$$

- $x_m^C$ : vector of observable market characteristics that could affect fixed costs (e.g. rental price)
- $\epsilon_m$ : unobservable (to the econometrician) market characteristic
- $\delta(1), \dots, \delta(N)$ : parameters (note: a bit odd that fixed cost depends on  $n$ )

## Bresnahan and Reiss (1991): Model

- Since  $\alpha(n)$  and  $\delta(n)$  increase with  $n$ , can show that profit decreases with  $n$ .
- Can also show that the model has a unique equilibrium  $n_m$  (given exogenous variables) due to strictly decreasing  $\Pi_m(n)$ .

## Bresnahan and Reiss (1991): Estimation

- Assume that unobserved component of entry costs  $\epsilon_m$  is independent of market shares and market characteristics, and is distributed  $N(0, \sigma)$ .
  - Also, normalize scale  $\sigma = 1$ .
- Rearrange equilibrium number of firms condition (i.e.  $\Pi_m(n_m) \geq 0$  and  $\Pi_m(n_m + 1) < 0$ ) in terms of thresholds for  $\epsilon_m$ :

$$T_m(n+1) < \epsilon_m \leq T_m(n)$$

- Where:

$$T_m(n) = s_m x_m^D \beta - x_m^C \gamma - \alpha(n) s_m - \delta(n)$$

## Bresnahan and Reiss (1991): Estimation

- Estimate model using an ordered probit:

$$Pr(n_m = n | s_m, x_m) = \Phi(T_m(n)) - \Phi(T_m(n+1))$$

- Can estimate with maximum likelihood.

## Bresnahan and Reiss (1991): Results

- Get market size entry thresholds.

$$S(n) = \frac{x_m^C \gamma + \delta(n)}{x_m^D \beta - \alpha(n)}$$

- Note that these don't depend in the normalization  $\sigma = 1$ .
- These are the minimum market size to sustain  $n$  firms in the market.
- Compute entry threshold ratios e.g.  $S_2/S_1 = \frac{S(2)}{S(1)}$ 
  - E.g. as number of firms increases by 1, does market double (ratio = 1) or need to more than double (ratio > 1)?



**Table 1**  
**Per Firm Entry Thresholds from**  
**Bresnahan and Reiss (1991b), Table 5**

Profession	$S_2/S_1$	$S_3/S_2$	$S_4/S_3$	$S_5/S_4$
Doctors	1.98	1.10	1.00	0.95
Dentists	1.78	0.79	0.97	0.94
Druggists	1.99	1.58	1.14	0.98
Plumbers	1.06	1.00	1.02	0.96
Tire Dealers	1.81	1.28	1.04	1.03

## Bresnahan and Reiss (1991): Main Findings

- Monopoly to duopoly (for most of the industries studied) requires more than double the market size
  - Their data do not allow them to say why.
  - One explanation: barriers to entry change with  $N$  (cost story).
  - Another explanation: markups change with  $N$  (e.g. consistent with a Cournot model).
- When number of firms  $> 4$ : double market size implies double the number of firms.  
(Consistent with 'contestable market hypothesis': if barriers to entry are low then market behaves in a competitive way.)

# Plan

1. Bresnahan and Reiss (1991)
2. **Mazzeo (2002)**
3. Seim (2006)

# Mazzeo (2002)

- **Question:**
- What drives the product-type decisions of firms in oligopoly markets?
- **Approach**
- Similar assumptions in the model to Bresnahan and Reiss (1991)
  - Complete information
  - No dynamics, no spatial differentiation
- Endogenizes **firm product choice**
- Data from the motel industry (use local markets along US highway exits)



## Mazzeo (2002): Model

- Different types of hotels (H: high-quality, E: economy hotel)
- Hotels choose their type and also whether to enter
- Profit of an active hotel of type  $T \in \{E, H\}$  is:

$$\pi_T(n_E, n_H) = sV_T(x, n_E, n_H) - EC_T(x) - \epsilon_T$$

- Here,  $n_E$  and  $n_H$  represent the number of active hotels of low and high quality in the market.
- $V_T$ : variable profit (per-capita)
- $EC_T(x) + \epsilon_T$ : entry cost for type  $T$  hotels (where  $\epsilon_T$  is unobservable to the researcher).

## Mazzeo (2002): Model

- Paper uses alternative two solution concepts:
  - 1. Stackelberg
    - Specifically, employs the **equilibrium selection rule** that firms enter sequentially with high-quality firms moving first
  - 2. A 'two-stage game': firms choose whether to enter and their type
    - We will now talk more about this alternative

## Mazzeo (2002): Model

- In the **first-stage** the total number of active hotels  $n = n_E + n_H$  is determined similarly to the Bresnahan-Reiss model.
- That is, hotels continue to enter the market so long as there is some configuration  $(n_E, n_H)$  where both low-quality and high-quality hotels make positive profits.

$$\Pi(n) = \max_{n_E, n_H: n_E + n_H = n} \min[\pi_E(n_E, n_H), \pi_H(n_E, n_H)]$$

- Then, the equilibrium number of hotels in the first-stage is  $n^*$  where  $\Pi(n^*) \geq 0$  and  $\Pi(n^* + 1) < 0$
- If  $\pi_E$  and  $\pi_H$  are strictly decreasing in the number of active firms then  $\Pi(n)$  is also strictly decreasing  $\rightarrow n^*$  is **unique**.

## Mazzeo (2002): Model

- In the **second-stage** active hotels simultaneously choose their type or quality level.
- Here, equilibrium is a pair  $(n_E^*, n_H^*)$  such that every firm chooses the type that maximizes its profit given the choices of the other firms.
  - So, low-quality firms are not better off switching to high-quality etc...

$$\pi_E(n_E^*, n_H^*) \geq \pi_H(n_E^* - 1, n_H^* + 1)$$

$$\pi_H(n_E^*, n_H^*) \geq \pi_E(n_E^* + 1, n_H^* - 1)$$

- Mazzeo shows that the equilibrium pair given in the above equations is also unique.



## Mazzeo (2002): Estimation

- Using the equilibrium conditions, possible to obtain a closed-form expression for the region of unobservables  $(\epsilon_E, \epsilon_H)$  that generate a particular value of  $(n_E^*, n_H^*)$ .
- Let  $R_E(n_E, n_H; s, x)$  be the region associated with  $n_E, n_H$  and  $F$  be the CDF of the unobservable variables. Then:

$$Pr(n_E^* = n_E, n_H^* = n_H | s, x) = \int 1\{(\epsilon_E, \epsilon_H) \in R_E(n_E, n_H; s, x)\} dF(\epsilon_E, \epsilon_H)$$

- Can the process similarly to Bresnahan and Reiss (1991): parameterize the payoff function and estimate using observed number of firms in each market using maximum likelihood.

## Mazzeo (2002): Results (not time to go into these in detail)

- Overall, finds evidence that firms have strong incentives to offer different products to their competitors.
- Specifically, “the negative effect that a competitor has on firm payoffs is up to twice as large if that competitor is the same product type” .

# Plan

1. Bresnahan and Reiss (1991)
2. Mazzeo (2002)
3. **Seim (2006)**

- **Question:** How important is spatial differentiation in explaining market power?
- Example: think of two grocery stores located in a city.
  - Differences in demand between locations
  - Positioning compared to competitors
  - Other factors like rent
- Importantly: relaxes the 'isolated market' assumption.
- Application: video-rental industry

FIGURE 1

IMPACT ON PROFITS OF COMPETITORS' LOCATIONS: ILLUSTRATION

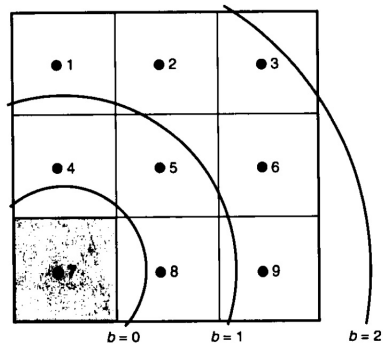


Figure: New firm locates in position 7.

## Seim 2006: Very Brief Overview

- $N$  potential entrants choose whether to enter a market. If enter they choose their location.
- Challenges:
  - Computation complexity (many choices and configurations of firms)
  - Multiple equilibria
- Key assumption: rivals have (some) private information about profitability. Hence, when each firm enters, they do not know for sure where their rivals will enter.
- Then, the choice to enter is made on the expected value of profits taken over the probability that other firms will enter other locations.
- She shows in the paper this makes it easier to compute an equilibrium. Uniqueness is tricky (she has some simulations for simple cases).