

$$\begin{aligned}
\Pr\left[\mathcal{E}_{r_1,r_2,r_3}\right] &= \Pr\left[\text{rk}\left[\begin{array}{c} A^{(r_1)} \\ \hline A^{(r_2)} \\ \hline A^{(r_3)} \\ \hline \end{array}\right] < 2t\right] = \sum_{i=0}^{2t-1} \Pr\left[\text{rk}\left[\begin{array}{c} A^{(r_1)} \\ \hline A^{(r_2)} \\ \hline A^{(r_3)} \\ \hline \end{array}\right] = i\right] \\
&\stackrel{1}{=} \sum_{i=0}^{2t-1} \frac{\text{NM}_{i,3t,3t}}{q^{(3t)\cdot(3t)}} \\
&= \sum_{i=0}^{2t-1} \frac{\prod_{j=0}^{i-1} \frac{(q^{3t}-q^j)^2}{q^i-q^j}}{q^{9t^2}}.
\end{aligned}$$

$$\begin{array}{l}
[n\times m] \\
i \\
\mathbb{F}_q
\end{array}$$

$$\text{NM}_{i,n,m} = \prod_{j=0}^{i-1} \frac{(q^m-q^j)\,(q^n-q^j)}{q^i-q^j}.$$