

$$r_{\text{max,scalar}} \in \mathcal{O}\left(q_{\text{s}}^2\right)$$

$$\begin{aligned} r_{\text{max,scalar}} &= r_{\text{max,vector}} \\ \Leftrightarrow q_{\text{s,min,from bound}}^2 &= q^{t^2/2+\mathcal{O}(t)} \\ \Leftrightarrow q_{\text{s,min,from bound}} &= q^{t^2/4+\mathcal{O}(t)} \\ \Rightarrow g_{\text{lower bound}} &= q_{\text{s,min,from bound}} - q_v = q^{t^2/4+\mathcal{O}(t)} \end{aligned}$$

$$(\epsilon = 1, \ell = 1) - \mathcal{N}_{h=3,r,s=4}$$

$$q^{t^2/4+\mathcal{O}(t)}$$

$$(\epsilon = 1, \ell = 1) - N_{h,r,s}$$

$$q^{\frac{\alpha-h+1}{(\alpha-1)(\alpha-h+2)(h-2)}t^2+\mathcal{O}(t)}$$

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