$$\Rightarrow \mathrm{g} \geq g_{\text{lower bound}} = q_{\text{s,min,from bound}}(q, t, \alpha, h) - q^t$$