

# Calculus Review

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# Learning Objectives

1. Find derivatives of continuous functions with one variable
2. Find antiderivatives and integrals of functions with one variable

# Differentiation

# Find the *derivative* of the following function

Example 1.1

$$f(x) = 2$$

Derivative of a constant

$$\frac{d}{dx}c = 0$$

Find the *derivative* of the following function

Example 1.2

$$f(x) = 2x$$

Find the *derivative* of the following function

Example 1.3

$$f(x) = 2x + 2$$

# Find the *derivative* of the following function

Example 1.4

$$f(x) = x^2$$

Derivative of x to a constant

$$\frac{d}{dx}x^n = nx^{n-1}$$

Find the *derivative* of the following function

Example 1.5

$$f(x) = 3\sqrt{x} + \frac{2}{x} + 5$$



# Find the *derivative* of the following function

Example 1.6

$$f(x) = e^x$$

Derivative of exponential  
function

$$\frac{d}{dx}e^x = e^x$$

# Find the *derivative* of the following function

Example 1.7

$$f(x) = \ln(x)$$

Derivative of logarithm

$$\frac{d}{dx} \ln(x) = \frac{1}{x}$$

# Find the *derivative* of the following function

Example 1.8

$$f(x) = x^2 e^x$$

Product Rule

$$\frac{d}{dx} f(x)g(x) = f'(x)g(x) + f(x)g'(x)$$

Find the *derivative* of the following function

Example 1.9

$$f(x) = \frac{x^5}{2x+7}$$

# Find the *derivative* of the following function

Example 1.10

$$f(x) = e^{-2x+7}$$

Quotient Rule

$$\frac{d}{dx} \frac{f(x)}{g(x)} = \frac{g(x)f'(x) - f(x)g'(x)}{(g(x))^2}$$

# Find the *derivative* of the following function

Example 1.11

$$f(x) = \ln(x^2)$$

Chain Rule

$$\frac{d}{dx}f(g(x)) = f'(g(x))g'(x)$$

# Integration

Find the *antiderivative* of the following function

Example 2.1

$$f(x) = 2$$



# Find the *antiderivative* of the following function

Example 2.2

$$f(x) = x$$

Integration of  $x$  to a constant

$$\int x^n dx = \frac{x^{n+1}}{n+1} + c$$

Find the *antiderivative* of the following function

Example 2.3

$$f(x) = \frac{1}{x}$$

Find the *antiderivative* of the following function

Example 2.4

$$f(x) = x^{3/2}$$

Find the *antiderivative* of the following function

Example 2.5

$$f(x) = e^x$$

Find the *antiderivative* of the following function

Example 2.6

$$f(x) = e^{-x}$$

Find the *antiderivative* of the following function

Example 2.7

$$f(x) = e^{-2x}$$

# Solve the following integral

Example 3.1

$$\int_0^1 (2x + x^5) dx$$

# Solve the following integral

Example 3.2

$$\int_2^3 e^{-x} dx$$

U-substitution

$$\int f(g(x))g'(x)dx = \int f(u)du$$



# Solve the following integral

Example 3.3

$$\int_2^3 x e^{x^2} dx$$

# Solve the following integral

## Example 3.4

$$\int_0^{\infty} x e^{-x} dx$$

## Integrating by Parts

$$\int f(x)g'(x)dx = f(x)g(x) -$$

$$\int f'(x)g(x)dx$$

OR

$$\int_a^b u dv = uv \Big|_a^b - \int_a^b v du$$

# Solve the following integral

Example 3.5

$$\int_1^2 x^2 \ln(x) dx$$

# Solve the following integral

Example 3.6

$$\int_1^2 \ln(x) dx$$

# Solve the following integral

Example 3.7

$$\int_1^2 x^2 e^x dx$$

