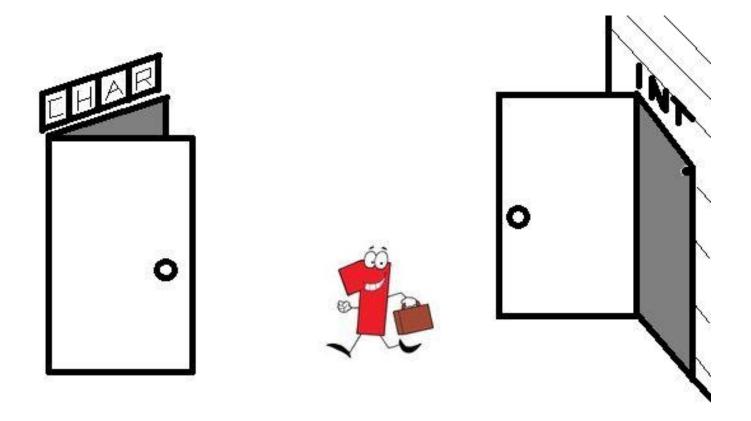


Computer Engineering 1

Motivation





http://www.instructables.com

Agenda



- Type conversion
 - signed ↔ unsigned
 - Extension
 - Truncation

Learning Objectives



At the end of this lesson you will be able

- to explain the casting of integer types in C
- to apply the assembly instructions associated with casting
- to say how a given memory content is interpreted for different integer types in C
- to give the memory content after storing different C integer types



Integer ranges based on word sizes

8-bit	hex	unsigned	signed
	0×00	0	0
	$0 \times 7 F$	127	127
	0x80	128	-128
			• • •
	0xFF	255	-1

16-bit	hex	unsigned	signed
	0x0000	0	0
	• • •	• • •	• • •
	0x7FFF	32 ' 767	32 ' 767
	0x8000	32'768	-32 ' 768
	• • •	• • •	• • •
	0xFFFF	65 ' 535	-1

32-bit	hex	unsigned	signed	
	0x0000 0000	0	0	
	• • •	• • •	• • •	
	0x7FFF'FFFF	2'147'483'647	2'147'483'647	
	0x8000 ' 0000	2'147'483'648	-2'147'483'648	
	• • •	• • •	• • •	
	OxFFFF'FFFF	4'294'967'295	-1	

Integer Casting in C: Type conversion



■ signed ←→ unsigned

Extension

$$int_8_t \rightarrow int16_t \rightarrow int32_t \rightarrow int64_t$$
 signed $uint_8_t \rightarrow uint16_t \rightarrow uint32_t \rightarrow uint64_t$ unsigned

Truncation

int64_t	\rightarrow	int32_t	\rightarrow	int16_t	>	int_8	signed
uint64_t	\rightarrow	uint32_t	\rightarrow	uint16_t	\rightarrow	uint_8	unsigned



■ signed ←→ unsigned

signed
$$-\mathbf{b}_3 \cdot \mathbf{2}^3 + \mathbf{b}_2 \cdot \mathbf{2}^2 + \mathbf{b}_1 \cdot \mathbf{2}^1 + \mathbf{b}_0 \cdot \mathbf{2}^0$$

unsigned $+\mathbf{b}_3 \cdot \mathbf{2}^3 + \mathbf{b}_2 \cdot \mathbf{2}^2 + \mathbf{b}_1 \cdot \mathbf{2}^1 + \mathbf{b}_0 \cdot \mathbf{2}^0$

Casts in red area

- → Small negative numbers turn into large positive numbers
- → Large positive numbers turn into small negative numbers

binary	unsigned	signed 2' compl.
0000	0	0
0001	1	1
0010	2	2
0011	3	3
0100	4	4
0101	5	5
0110	6	6
0111	7	7
1000	8	-8
1001	9	-7
1010	10	-6
1011	11	-5
1100	12	-4
1101	13	-3
1110	14	-2
1111	15	-1



Casting

unsigned

 \rightarrow

signed

signed

 \rightarrow

unsigned

Bit representation stays the same, but interpretation changes

Example 4-Bit

• 1011b -

→ Interpretation as unsigned

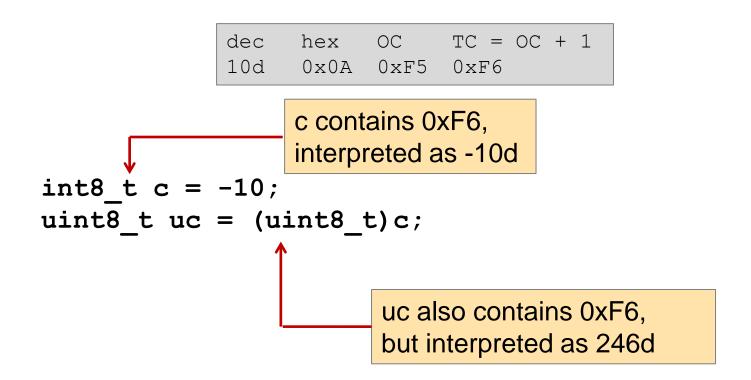
11d

→ Interpretation as signed

-5d

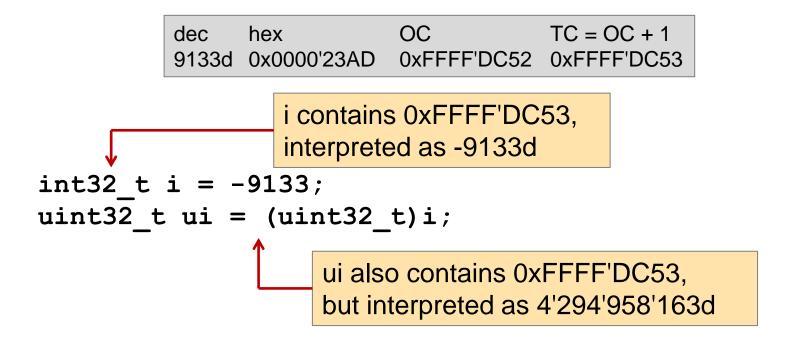


- Example 1: signed 8-bit → unsigned 8-bit
 - Bit representation stays the same, interpretation changes





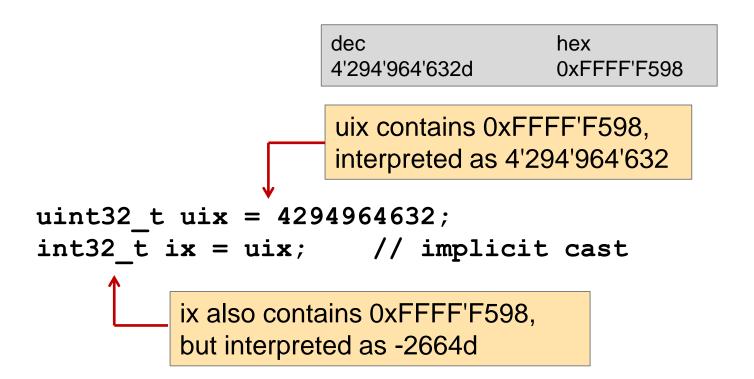
- Example 2: signed 32-bit → unsigned 32-bit
 - Bit representation stays the same, interpretation changes



Explicit cast is not even required
uint32_t ui2 = i; // implicit cast



- Example 3: Cast unsigned 32-bit → signed 32-bit
 - Bit representation stays the same, interpretation changes





- If one of the operands is unsigned, C performs an implicit cast for the signed values to unsigned
 - Example n = 32: signed ∈ [-2'147'483'648, 2'147'483'647]
 - Can lead to strange results (red lines)

Expression	Туре	Evaluation
0 == 0U	unsigned	1
-1 < 0	signed	1
-1 < 0U	unsigned	0
2'147'483'647 > -2'147'483'647 - 1	signed	1
2'147'483'647U > -2'147'483'647 - 1	unsigned	0
2'147'483'647 > (int) 2'147'483'648U	signed	1
-1 > -2	signed	1
(unsigned) -1 > -2	unsigned	1

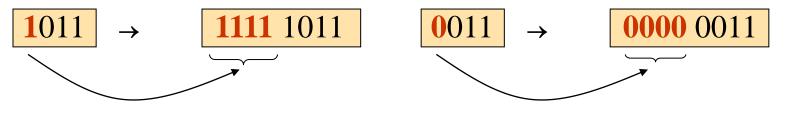
Examples: R. Bryant, D. O'Hallaron

Integer Casting



- Extension: 4 Bit → 8 Bit
 - Unsigned → Zero Extension

Signed → Sign Extension



Integer Casting: Sign Extension



Sign Extension Cortex-M0 (signed values)

- Extend word-length without changing value
- SXTB Extends an 8-bit value to a 32-bit value
- SXTH Extends a 16-bit value to a 32-bit value

Zero Extension Cortex-M0 (unsigned values)

- Extend word-length, fill with zeroes
- UXTB Extends an 8-bit value to a 32-bit value
- UXTH Extends a 16-bit value to a 32-bit value

Examples

```
SXTB R3, R10 ; Extract lowest byte of the value in R10, ; sign extend it and write the result to R3
UXTH R2, R3 ; Extract lower two bytes of the value in R3, ; zero extend it and write the result to R2
```

Integer Casting: Sign Extension



Example Sign Extension

```
int16_t sx = 15213;
int32_t ix = (int32_t)sx;

int16_t sy = -15213;
int32_t iy = (int32_t)sy;
```

```
dec
                           bin
             hex
     15213
                                              00111011 01101101
                  0x3B6D
SX
                           00000000 00000000 00111011 01101101
ix 15213
           0x0000'3B6D
    -15213
                  0xC493
                                             11000100 10010011
sy
iy
    -15213
             0xFFFF'C493
                           11111111 11111111 11000100 10010011
```

signed Integer Types: from small to large

→ Sign bit is copied to the left

Integer Casting: Truncation



- **■** Truncation: Reduce number of digits
 - Cast cuts the left most digits
- Unsigned → modulo Operation

```
uint32_t x = 287962;
uint16_t sx = (uint16_t)x;
uint32_t y = (uint32_t)sx;
```

```
0 \times 0000464DA \rightarrow 287'962
0 \times 64DA \rightarrow 25'818
0 \times 000064DA \rightarrow 25'818
```

■ Signed → possible change of sign!

```
int32_t x = 53191;
int16_t sx = (int16_t) x;
int32_t y = (int32_t) sx;
```

```
0x0000CFC7 → 53'191
0xCFC7 → -12'345
0xFFFFCFC7 → -12'345
```

Conclusion



Integer Casts

Type Conversions

signed – unsigned

Small negative numbers correspond to large positive numbers

Extensions

Add additional bits

signed sign extension copy sign bit to the leftunsigned zero extension fill left bits with zero

Truncations

Cut left most digits

signed possible change of sign

unsigned results in modulo operation