Nathan Wemmer

Code ▼

Chapter 11 - Assignment 9

Section 11.1

Section 11.1.2

Section 11.1.3

Hide

setwd("C:/Users/Nathan/Desktop/school/statistical data management/therbook")
results <- read.table("yields.txt",header=T)
attach(results)
names(results)</pre>

[1] "sand" "clay" "loam"

Hide

results

sand <int></int>	clay <int></int>	loam <int></int>
6	17	13
10	15	16
8	3	9
6	11	12
14	14	15
17	12	16
9	12	17
11	8	13
7	10	18
11	13	14

Hide sapply(list(sand,clay,loam),mean) [1] 9.9 11.5 14.3 Hide (frame <- stack(results))</pre> values ind <int> <fctr> 6 sand 10 sand 8 sand 6 sand 14 sand 17 sand 9 sand 11 sand 7 sand 11 sand 1-10 of 30 rows Previous 1 2 3 Next Hide names(frame) <- c("yield","soil")</pre> attach(frame) head(frame) yield soil <int> <fctr> 1 6 sand 2 10 sand 3 8 sand 4 6 sand

14 sand

17 sand

5

6

```
6 rows
                                                                                             Hide
tapply(yield,soil,var)
              clay
                         loam
12.544444 15.388889 7.122222
                                                                                             Hide
#fligner.test(y~soil)
fligner.test(yield~soil)
    Fligner-Killeen test of homogeneity of variances
data: yield by soil
Fligner-Killeen:med chi-squared = 0.36507, df = 2,
p-value = 0.8332
                                                                                             Hide
plot(yield~soil,col="green")
sum((yield-mean(yield))^2)
[1] 414.7
                                                                                             Hide
sand-mean(sand)
 [1] -3.9 0.1 -1.9 -3.9 4.1 7.1 -0.9 1.1 -2.9 1.1
                                                                                             Hide
clay-mean(clay)
 [1] 5.5 3.5 -8.5 -0.5 2.5 0.5 0.5 -3.5 -1.5 1.5
                                                                                             Hide
loam-mean(loam)
 [1] -1.3 1.7 -5.3 -2.3 0.7 1.7 2.7 -1.3 3.7 -0.3
```

```
sum((sand-mean(sand))^2)
[1] 112.9
                                                                                                 Hide
sum((clay-mean(clay))^2)
[1] 138.5
                                                                                                 Hide
sum((loam-mean(loam))^2)
[1] 64.1
                                                                                                 Hide
sum(sapply(list(sand,clay,loam),function (x) sum((x-mean(x))^2)))
[1] 315.5
                                                                                                 Hide
tapply(yield,soil,var)
               clay
                         loam
     sand
12.544444 15.388889 7.122222
                                                                                                 Hide
mean(tapply(yield,soil,var))
[1] 11.68519
                                                                                                 Hide
qf(.95,2,27)
[1] 3.354131
                                                                                                 Hide
1-pf(4.24,2,27)
[1] 0.02503987
```

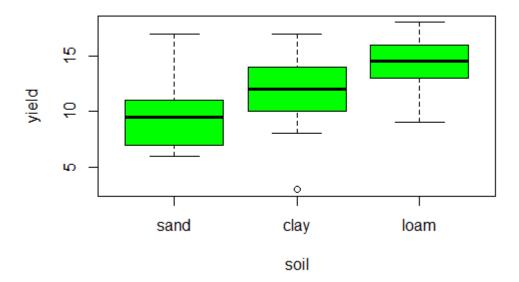
Hide

```
summary(aov(yield~soil))
```

```
Df Sum Sq Mean Sq F value Pr(>F)
soil 2 99.2 49.60 4.245 0.025 *
Residuals 27 315.5 11.69
---
Signif. codes:
0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

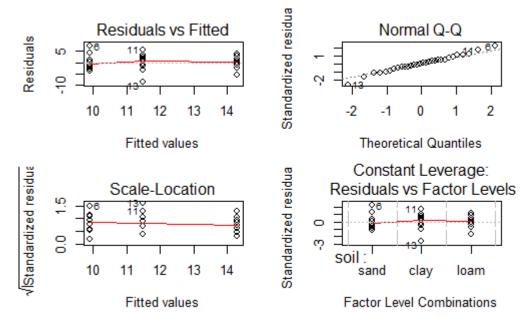
Hide

```
par(mfrow=c(2,2))
```



Hide

plot(aov(yield~soil))



Section 11.1.4

```
Hide

model <- aov(yield~soil)
model.tables(model,se=T)

Tables of effects

soil
soil
sand clay loam
-2.0 -0.4 2.4

Standard errors of effects
soil
1.081
replic. 10
```

model.tables(model, "means", se=T)

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```
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Tables of means
Grand mean
11.9
soil
soil
sand clay loam
9.9 11.5 14.3
Standard errors for differences of means
        soil
       1.529
replic.
          10
                                                                                          Hide
summary.lm(model)
Call:
aov(formula = yield ~ soil)
Residuals:
  Min
         1Q Median
                       3Q
                             Max
  -8.5 -1.8 0.3
                       1.7
                              7.1
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
                      1.081 9.158 9.04e-10 ***
(Intercept)
              9.900
soilclay
              1.600
                       1.529 1.047 0.30456
              4.400
                       1.529 2.878 0.00773 **
soilloam
---
Signif. codes:
0 '***, 0.001 '**, 0.01 '*, 0.05 '., 0.1 ', 1
Residual standard error: 3.418 on 27 degrees of freedom
Multiple R-squared: 0.2392, Adjusted R-squared: 0.1829
F-statistic: 4.245 on 2 and 27 DF, p-value: 0.02495
                                                                                          Hide
qt(0.975,18)
```

[1] 2.100922

Hide

2*(1 - pt(2.88, df = 18))

[1] 0.009966426

Section 11.1.5

Hide

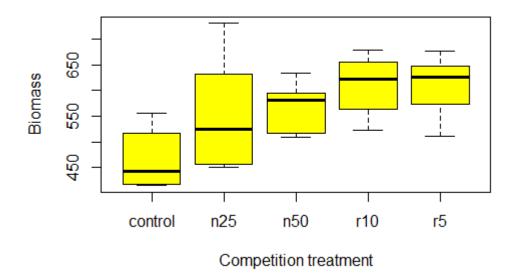
```
setwd("C:/Users/Nathan/Desktop/school/statistical data management/therbook")
comp <- read.table("competition.txt",header=T)

attach(comp)
names(comp)</pre>
```

```
[1] "biomass" "clipping"
```

Hide

```
plot(clipping, biomass, xlab="Competition treatment",
    ylab="Biomass", col="yellow")
```



```
Df Sum Sq Mean Sq F value Pr(>F)
clipping 4 85356 21339 4.302 0.00875 **
Residuals 25 124020 4961
---
Signif. codes:
0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Hide

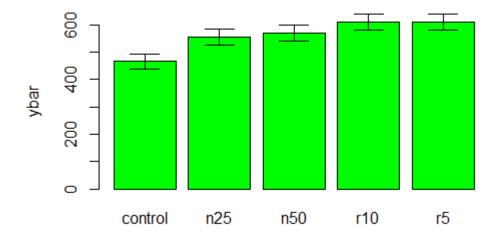
table(clipping)

```
clipping
control n25 n50 r10 r5
6 6 6 6 6
```

Hide

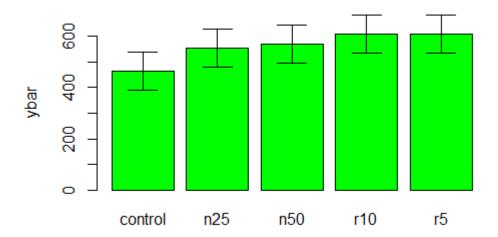
```
se <- rep(28.75,5)

labels <- levels(clipping)
ybar <- tapply(biomass,clipping,mean)
error.bars(ybar,se,labels)</pre>
```



Hide

error.bars(ybar,2.570582*se,labels)

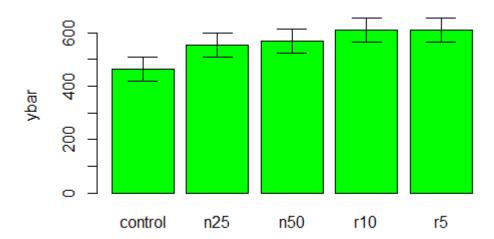


qt(0.975,10)*sqrt(2*4961/6)

[1] 90.60794

Hide

lsd <- qt(0.975,10)*sqrt(2*4961/6)
lsdbars <- rep(lsd,5)/2
error.bars(ybar,lsdbars,labels)</pre>



Section 11.2

```
setwd("C:/Users/Nathan/Desktop/school/statistical data management/therbook")
weights <- read.table("growth.txt",header=T)
attach(weights)</pre>
```

```
The following objects are masked from weights (pos = 3):
    diet, gain, supplement

The following objects are masked from weights (pos = 4):
    diet, gain, supplement

The following objects are masked from weights (pos = 10):
    diet, gain, supplement

The following objects are masked from weights (pos = 11):
    diet, gain, supplement

The following objects are masked from weights (pos = 12):
    diet, gain, supplement
```

```
labs <- c("Barley","Oats","Wheat")
legend(locator(1),labs,fill= c("orange","yellow","cornsilk"))</pre>
```

```
Error in locator(1) : plot.new has not been called yet
```

Section 11.3

```
Hide
```

Hide

```
yields <- read.table("splityield.txt",header=T)
attach(yields)

The following object is masked from frame:
    yield</pre>
```

Hide

names(yields)

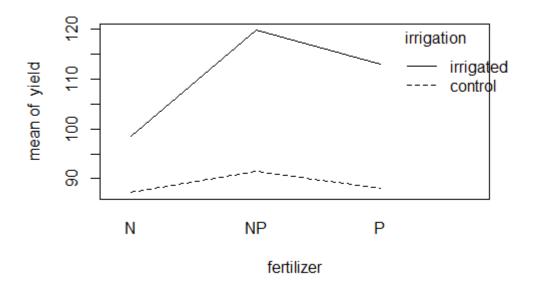
```
[1] "yield"
                 "block"
                              "irrigation" "density"
[5] "fertilizer"
                                                                                             Hide
model <-
  aov(yield~irrigation*density*fertilizer+Error(block/irrigation/density))
summary(model)
Error: block
          Df Sum Sq Mean Sq F value Pr(>F)
Residuals 3 194.4
                     64.81
Error: block:irrigation
           Df Sum Sq Mean Sq F value Pr(>F)
irrigation 1
               8278
                       8278
                             17.59 0.0247 *
Residuals
                1412
                         471
Signif. codes:
0 (***, 0.001 (**, 0.01 (*, 0.05 (., 0.1 ( , 1
Error: block:irrigation:density
                   Df Sum Sq Mean Sq F value Pr(>F)
                        1758
                             879.2 3.784 0.0532 .
density
irrigation:density 2
                       2747 1373.5
                                     5.912 0.0163 *
Residuals
                        2788
                              232.3
Signif. codes:
0 (***, 0.001 (**, 0.01 (*, 0.05 (., 0.1 ( , 1
Error: Within
                              Df Sum Sq Mean Sq F value
fertilizer
                               2 1977.4
                                         988.7 11.449
irrigation:fertilizer
                              2 953.4
                                         476.7
                                                 5.520
density:fertilizer
                              4 304.9
                                          76.2
                                                 0.883
irrigation:density:fertilizer 4 234.7
                                          58.7
                                                 0.680
Residuals
                              36 3108.8
                                          86.4
                                Pr(>F)
                              0.000142 ***
fertilizer
irrigation:fertilizer
                             0.008108 **
density:fertilizer
                              0.484053
irrigation:density:fertilizer 0.610667
Residuals
```

Hide

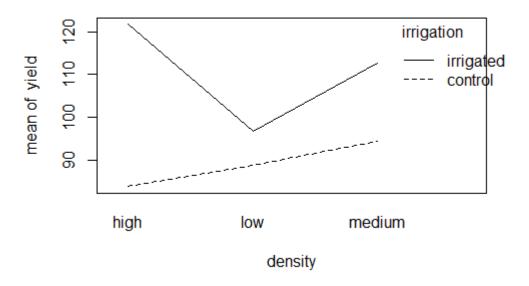
```
interaction.plot(fertilizer,irrigation,yield)
```

0 (***, 0.001 (**, 0.01 (*, 0.05 (., 0.1 (, 1

Signif. codes:



interaction.plot(density,irrigation,yield)



Section 11.4

rats <- read.table("rats.txt",header=T)

attach(rats)
names(rats)

[1] "Glycogen" "Treatment" "Rat" "Liver"</pre>

```
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Hide

Treatment <- factor(Treatment)
Rat <- factor(Rat)
Liver <- factor(Liver)
```

```
Df Sum Sq Mean Sq F value Pr(>F)
Treatment 2 1558 778.8 14.5 3.03e-05 ***
Residuals 33 1773 53.7
---
Signif. codes:
0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Hide

```
(means <- tapply(Glycogen, list(Treatment, Rat), mean))</pre>
```

model <- aov(Glycogen~Treatment)</pre>

summary(model)

```
1 2
1 132.5000 148.5000
2 149.6667 152.3333
3 134.3333 136.0000
```

Hide

```
treat <- gl(3,1,length=6)
model <- aov(as.vector(means)~treat)
summary(model)</pre>
```

```
Df Sum Sq Mean Sq F value Pr(>F)
treat 2 259.6 129.80 2.929 0.197
Residuals 3 132.9 44.31
```

```
model2 <- aov(Glycogen~Treatment+Error(Treatment/Rat/Liver))
summary(model2)</pre>
```

```
Error: Treatment
         Df Sum Sq Mean Sq
Treatment 2 1558
                    778.8
Error: Treatment:Rat
         Df Sum Sq Mean Sq F value Pr(>F)
Residuals 3 797.7
                     265.9
Error: Treatment:Rat:Liver
         Df Sum Sq Mean Sq F value Pr(>F)
               594
Residuals 12
                      49.5
Error: Within
         Df Sum Sq Mean Sq F value Pr(>F)
Residuals 18
               381
                     21.17
```

Hide

```
varcomps <- c(21.17,14.165,36.065)
100*varcomps/sum(varcomps)</pre>
```

[1] 29.64986 19.83894 50.51120

Section 11.5

Hide

```
daphnia <- read.table("Daphnia.txt",header=T)
attach(daphnia)
names(daphnia)</pre>
```

[1] "Growth.rate" "Water" "Detergent" "Daphnia"

```
model1 <- aov(Growth.rate~Water*Detergent*Daphnia)
summary(model1)</pre>
```

```
Df Sum Sq Mean Sq F value
                                                    Pr(>F)
                             1.99
                                    1.985
Water
                         1
                                            2.850 0.097838
Detergent
                         3
                             2.21
                                    0.737
                                           1.059 0.375478
                         2
Daphnia
                           39.18 19.589 28.128 8.23e-09
Water:Detergent
                         3
                            0.17
                                    0.058
                                           0.084 0.968608
Water:Daphnia
                         2 13.73
                                    6.866
                                           9.859 0.000259
Detergent:Daphnia
                         6 20.60
                                    3.433
                                           4.930 0.000532
Water:Detergent:Daphnia 6
                            5.85
                                           1.399 0.234324
                                    0.975
Residuals
                        48 33.43
                                   0.696
Water
Detergent
Daphnia
Water:Detergent
Water:Daphnia
Detergent:Daphnia
Water:Detergent:Daphnia
Residuals
---
Signif. codes:
0 (***, 0.001 (**, 0.01 (*, 0.05 (., 0.1 ( , 1
```

```
model2 <- lm(Growth.rate~Water*Detergent*Daphnia)
summary(model2)</pre>
```

```
Call:
lm(formula = Growth.rate ~ Water * Detergent * Daphnia)
Residuals:
             1Q Median
    Min
                             3Q
                                    Max
-1.4882 -0.5440 0.0239 0.3560 1.5250
Coefficients:
                                         Estimate Std. Error
(Intercept)
                                          2.81126
                                                     0.48181
                                         -0.15808
WaterWear
                                                     0.68138
DetergentBrandB
                                         -0.03536
                                                     0.68138
DetergentBrandC
                                          0.47626
                                                     0.68138
DetergentBrandD
                                         -0.21407
                                                     0.68138
DaphniaClone2
                                          0.49637
                                                     0.68138
DaphniaClone3
                                          2.05526
                                                     0.68138
WaterWear:DetergentBrandB
                                          0.46455
                                                     0.96361
WaterWear: DetergentBrandC
                                         -0.27431
                                                     0.96361
                                          0.21729
WaterWear:DetergentBrandD
                                                     0.96361
WaterWear:DaphniaClone2
                                          1.38081
                                                     0.96361
WaterWear:DaphniaClone3
                                          0.43156
                                                     0.96361
DetergentBrandB:DaphniaClone2
                                          0.91892
                                                     0.96361
DetergentBrandC:DaphniaClone2
                                         -0.16337
                                                     0.96361
DetergentBrandD:DaphniaClone2
                                          1.01209
                                                     0.96361
DetergentBrandB:DaphniaClone3
                                         -0.06490
                                                     0.96361
DetergentBrandC:DaphniaClone3
                                         -0.80789
                                                     0.96361
DetergentBrandD:DaphniaClone3
                                         -1.28669
                                                     0.96361
WaterWear:DetergentBrandB:DaphniaClone2 -1.26380
                                                     1.36275
WaterWear:DetergentBrandC:DaphniaClone2
                                         1.35612
                                                     1.36275
WaterWear:DetergentBrandD:DaphniaClone2
                                         0.77616
                                                     1.36275
WaterWear:DetergentBrandB:DaphniaClone3 -0.87443
                                                     1.36275
WaterWear:DetergentBrandC:DaphniaClone3 -1.03019
                                                     1.36275
WaterWear:DetergentBrandD:DaphniaClone3 -1.55400
                                                     1.36275
                                         t value Pr(>|t|)
                                           5.835 4.48e-07
(Intercept)
WaterWear
                                          -0.232 0.81753
DetergentBrandB
                                          -0.052 0.95883
DetergentBrandC
                                           0.699
                                                 0.48794
DetergentBrandD
                                          -0.314
                                                  0.75475
                                           0.728
                                                  0.46986
DaphniaClone2
DaphniaClone3
                                           3.016
                                                  0.00408
WaterWear:DetergentBrandB
                                           0.482
                                                 0.63193
WaterWear: DetergentBrandC
                                          -0.285
                                                  0.77712
                                           0.225
WaterWear:DetergentBrandD
                                                 0.82255
WaterWear:DaphniaClone2
                                           1.433 0.15835
WaterWear:DaphniaClone3
                                           0.448
                                                 0.65627
DetergentBrandB:DaphniaClone2
                                           0.954 0.34506
DetergentBrandC:DaphniaClone2
                                          -0.170
                                                  0.86609
DetergentBrandD:DaphniaClone2
                                           1.050
                                                  0.29884
DetergentBrandB:DaphniaClone3
                                          -0.067
                                                  0.94658
DetergentBrandC:DaphniaClone3
                                          -0.838 0.40597
DetergentBrandD:DaphniaClone3
                                          -1.335 0.18809
```

```
WaterWear:DetergentBrandB:DaphniaClone2 -0.927
                                                 0.35837
WaterWear:DetergentBrandC:DaphniaClone2
                                          0.995
                                                 0.32466
WaterWear:DetergentBrandD:DaphniaClone2
                                          0.570
                                                 0.57164
WaterWear:DetergentBrandB:DaphniaClone3
                                         -0.642
                                                 0.52414
WaterWear: DetergentBrandC: DaphniaClone3
                                         -0.756
                                                 0.45337
WaterWear:DetergentBrandD:DaphniaClone3
                                         -1.140
                                                 0.25980
                                        ***
(Intercept)
WaterWear
DetergentBrandB
DetergentBrandC
DetergentBrandD
DaphniaClone2
DaphniaClone3
WaterWear:DetergentBrandB
WaterWear:DetergentBrandC
WaterWear: DetergentBrandD
WaterWear:DaphniaClone2
WaterWear:DaphniaClone3
DetergentBrandB:DaphniaClone2
DetergentBrandC:DaphniaClone2
DetergentBrandD:DaphniaClone2
DetergentBrandB:DaphniaClone3
DetergentBrandC:DaphniaClone3
DetergentBrandD:DaphniaClone3
WaterWear:DetergentBrandB:DaphniaClone2
WaterWear:DetergentBrandC:DaphniaClone2
WaterWear:DetergentBrandD:DaphniaClone2
WaterWear:DetergentBrandB:DaphniaClone3
WaterWear:DetergentBrandC:DaphniaClone3
WaterWear:DetergentBrandD:DaphniaClone3
Signif. codes:
0 (***, 0.001 (**, 0.01 (*, 0.05 (., 0.1 ( , 1
Residual standard error: 0.8345 on 48 degrees of freedom
Multiple R-squared: 0.7147,
                                Adjusted R-squared:
F-statistic: 5.227 on 23 and 48 DF, p-value: 7.019e-07
```

Hide

summary.lm(model1)

```
Call:
aov(formula = Growth.rate ~ Water * Detergent * Daphnia)
Residuals:
             1Q Median
                             3Q
    Min
                                    Max
-1.4882 -0.5440 0.0239 0.3560 1.5250
Coefficients:
                                         Estimate Std. Error
(Intercept)
                                          2.81126
                                                     0.48181
WaterWear
                                         -0.15808
                                                     0.68138
DetergentBrandB
                                         -0.03536
                                                     0.68138
DetergentBrandC
                                          0.47626
                                                     0.68138
DetergentBrandD
                                         -0.21407
                                                     0.68138
DaphniaClone2
                                          0.49637
                                                     0.68138
DaphniaClone3
                                          2.05526
                                                     0.68138
WaterWear:DetergentBrandB
                                          0.46455
                                                     0.96361
WaterWear: DetergentBrandC
                                         -0.27431
                                                     0.96361
                                          0.21729
WaterWear:DetergentBrandD
                                                     0.96361
WaterWear:DaphniaClone2
                                          1.38081
                                                     0.96361
WaterWear:DaphniaClone3
                                          0.43156
                                                     0.96361
DetergentBrandB:DaphniaClone2
                                          0.91892
                                                     0.96361
DetergentBrandC:DaphniaClone2
                                         -0.16337
                                                     0.96361
DetergentBrandD:DaphniaClone2
                                          1.01209
                                                     0.96361
DetergentBrandB:DaphniaClone3
                                         -0.06490
                                                     0.96361
DetergentBrandC:DaphniaClone3
                                         -0.80789
                                                     0.96361
DetergentBrandD:DaphniaClone3
                                         -1.28669
                                                     0.96361
WaterWear:DetergentBrandB:DaphniaClone2 -1.26380
                                                     1.36275
WaterWear:DetergentBrandC:DaphniaClone2
                                         1.35612
                                                     1.36275
WaterWear:DetergentBrandD:DaphniaClone2
                                         0.77616
                                                     1.36275
WaterWear:DetergentBrandB:DaphniaClone3 -0.87443
                                                     1.36275
WaterWear:DetergentBrandC:DaphniaClone3 -1.03019
                                                     1.36275
WaterWear:DetergentBrandD:DaphniaClone3 -1.55400
                                                     1.36275
                                         t value Pr(>|t|)
                                           5.835 4.48e-07
(Intercept)
WaterWear
                                          -0.232 0.81753
DetergentBrandB
                                          -0.052
                                                 0.95883
DetergentBrandC
                                           0.699
                                                 0.48794
DetergentBrandD
                                          -0.314
                                                  0.75475
                                           0.728
                                                  0.46986
DaphniaClone2
DaphniaClone3
                                           3.016
                                                  0.00408
WaterWear:DetergentBrandB
                                           0.482
                                                 0.63193
WaterWear: DetergentBrandC
                                          -0.285
                                                  0.77712
                                           0.225
WaterWear:DetergentBrandD
                                                  0.82255
WaterWear:DaphniaClone2
                                           1.433
                                                 0.15835
WaterWear:DaphniaClone3
                                           0.448
                                                 0.65627
DetergentBrandB:DaphniaClone2
                                           0.954
                                                 0.34506
DetergentBrandC:DaphniaClone2
                                          -0.170
                                                  0.86609
DetergentBrandD:DaphniaClone2
                                           1.050
                                                  0.29884
DetergentBrandB:DaphniaClone3
                                          -0.067
                                                  0.94658
DetergentBrandC:DaphniaClone3
                                          -0.838 0.40597
DetergentBrandD:DaphniaClone3
                                          -1.335 0.18809
```

```
WaterWear:DetergentBrandB:DaphniaClone2 -0.927
                                                 0.35837
WaterWear:DetergentBrandC:DaphniaClone2
                                          0.995
                                                 0.32466
WaterWear:DetergentBrandD:DaphniaClone2
                                          0.570
                                                 0.57164
WaterWear:DetergentBrandB:DaphniaClone3
                                         -0.642
                                                 0.52414
WaterWear: DetergentBrandC: DaphniaClone3
                                         -0.756
                                                 0.45337
WaterWear:DetergentBrandD:DaphniaClone3
                                         -1.140
                                                 0.25980
                                        ***
(Intercept)
WaterWear
DetergentBrandB
DetergentBrandC
DetergentBrandD
DaphniaClone2
DaphniaClone3
WaterWear:DetergentBrandB
WaterWear:DetergentBrandC
WaterWear: DetergentBrandD
WaterWear:DaphniaClone2
WaterWear:DaphniaClone3
DetergentBrandB:DaphniaClone2
DetergentBrandC:DaphniaClone2
DetergentBrandD:DaphniaClone2
DetergentBrandB:DaphniaClone3
DetergentBrandC:DaphniaClone3
DetergentBrandD:DaphniaClone3
WaterWear:DetergentBrandB:DaphniaClone2
WaterWear:DetergentBrandC:DaphniaClone2
WaterWear:DetergentBrandD:DaphniaClone2
WaterWear:DetergentBrandB:DaphniaClone3
WaterWear:DetergentBrandC:DaphniaClone3
WaterWear:DetergentBrandD:DaphniaClone3
Signif. codes:
0 (***, 0.001 (**, 0.01 (*, 0.05 (., 0.1 ( , 1
Residual standard error: 0.8345 on 48 degrees of freedom
Multiple R-squared: 0.7147,
                                Adjusted R-squared:
F-statistic: 5.227 on 23 and 48 DF, p-value: 7.019e-07
```

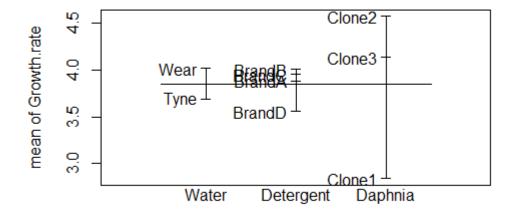
Hide

summary.aov(model2)

```
Df Sum Sq Mean Sq F value
                                                     Pr(>F)
                                     1.985
                              1.99
                                             2.850 0.097838
Water
                         1
Detergent
                          3
                              2.21
                                     0.737
                                             1.059 0.375478
                          2
Daphnia
                            39.18
                                    19.589
                                            28.128 8.23e-09
Water:Detergent
                         3
                             0.17
                                     0.058
                                             0.084 0.968608
Water:Daphnia
                         2
                            13.73
                                     6.866
                                             9.859 0.000259
                            20.60
                                     3.433
                                             4.930 0.000532
Detergent:Daphnia
                         6
                             5.85
Water:Detergent:Daphnia 6
                                     0.975
                                             1.399 0.234324
Residuals
                        48
                            33.43
                                     0.696
Water
Detergent
Daphnia
Water:Detergent
Water:Daphnia
Detergent:Daphnia
Water:Detergent:Daphnia
Residuals
---
Signif. codes:
0 (***, 0.001 (**, 0.01 (*, 0.05 (., 0.1 ( , 1
```

Hide

plot.design(Growth.rate~Water*Detergent*Daphnia)



Factors

Hide

model.tables(model1, "means", se = TRUE)

Tables of means Grand mean 3.851905 Water Water Tyne Wear 3.686 4.018 Detergent Detergent BrandA BrandB BrandC BrandD 3.885 4.010 3.955 3.558 Daphnia Daphnia Clone1 Clone2 Clone3 2.840 4.577 4.139 Water:Detergent Detergent Water BrandA BrandB BrandC BrandD Tyne 3.662 3.911 3.814 3.356 Wear 4.108 4.109 4.095 3.760 Water:Daphnia Daphnia Water Clone1 Clone2 Clone3 Tyne 2.868 3.806 4.383 Wear 2.812 5.348 3.894 Detergent:Daphnia Daphnia Detergent Clone1 Clone2 Clone3 BrandA 2.732 3.919 5.003 BrandB 2.929 4.403 4.698 BrandC 3.071 4.773 4.019 BrandD 2.627 5.214 2.834 Water:Detergent:Daphnia , , Daphnia = Clone1 Detergent Water BrandA BrandB BrandC BrandD Tyne 2.811 2.776 3.288 2.597 Wear 2.653 3.082 2.855 2.656 , , Daphnia = Clone2 Detergent Water BrandA BrandB BrandC BrandD Tyne 3.308 4.191 3.621 4.106

```
Wear 4.530 4.615 5.925 6.322
, , Daphnia = Clone3
      Detergent
Water BrandA BrandB BrandC BrandD
  Tyne 4.867 4.766 4.535 3.366
 Wear 5.140 4.630 3.504 2.303
Standard errors for differences of means
        Water Detergent Daphnia Water:Detergent
                  0.2782 0.2409
        0.1967
                                          0.3934
replic.
            36
                      18
        Water:Daphnia Detergent:Daphnia
               0.3407
                                 0.4818
replic.
                   12
                                      6
        Water:Detergent:Daphnia
                         0.6814
replic.
                              3
```

Section 11.6

TukeyHSD(model)

```
Hide
data <- read.table("Fungi.txt",header=T)</pre>
attach(data)
names(data)
[1] "Habitat"
                   "Fugus.yield"
                                                                                                    Hide
model <- aov(Fugus.yield~Habitat)</pre>
summary(model)
              Df Sum Sq Mean Sq F value Pr(>F)
                           501.8
                                   72.14 <2e-16 ***
Habitat
                   7527
Residuals
            144
                   1002
                             7.0
Signif. codes:
0 (***, 0.001 (**, 0.01 (*, 0.05 (., 0.1 ( , 1
                                                                                                     Hide
```

Tukey multiple comparisons of means 95% family-wise confidence level

Fit: aov(formula = Fugus.yield ~ Habitat)

\$Habitat

\$Habitat			
	diff	lwr	upr
Ash-Alder	3.53292777	-0.5808096	7.6466651
Aspen-Alder	12.78574402	8.6720067	16.8994814
Beech-Alder	12.32365349	8.2099161	16.4373908
Birch-Alder	14.11348150	9.9997441	18.2272189
Cherry-Alder	10.29508769	6.1813503	14.4088250
Chestnut-Alder	12.24107899	8.1273416	16.3548163
Holmoak-Alder	-1.44360558	-5.5573429	2.6701318
Hornbeam-Alder	10.60271044	6.4889731	14.7164478
Lime-Alder	19.19458205	15.0808447	23.3083194
Oak-Alder	20.29457340	16.1808360	24.4083108
Pine-Alder	14.34084715	10.2271098	18.4545845
Rowan-Alder	6.29495226	2.1812149	10.4086896
Spruce-Alder	-2.15119456	-6.2649319	1.9625428
Sycamore-Alder	2.80900108	-1.3047363	6.9227384
Willow-Alder	2.77635167	-1.3373857	6.8900890
			13.3665536
Aspen-Ash	9.25281625	5.1390789	
Beech-Ash	8.79072572	4.6769884	12.9044631
Birch-Ash	10.58055373	6.4668164	14.6942911
Cherry-Ash	6.76215993	2.6484226	10.8758973
Chestnut-Ash	8.70815122	4.5944139	12.8218886
Holmoak-Ash	-4.97653335	-9.0902707	-0.8627960
Hornbeam-Ash	7.06978268	2.9560453	11.1835200
Lime-Ash	15.66165428	11.5479169	19.7753916
Oak-Ash	16.76164563	12.6479083	20.8753830
Pine-Ash	10.80791938	6.6941820	14.9216567
Rowan-Ash	2.76202449	-1.3517129	6.8757618
Spruce-Ash	-5.68412232	-9.7978597	-1.5703850
Sycamore-Ash	-0.72392669	-4.8376640	3.3898107
Willow-Ash	-0.75657610	-4.8703135	3.3571613
Beech-Aspen	-0.46209053	-4.5758279	3.6516468
Birch-Aspen	1.32773748	-2.7859999	5.4414748
Cherry-Aspen	-2.49065633	-6.6043937	1.6230810
Chestnut-Aspen	-0.54466504	-4.6584024	3.5690723
Holmoak-Aspen	-14.22934960	-18.3430870	-10.1156123
Hornbeam-Aspen	-2.18303358	-6.2967709	1.9307038
Lime-Aspen	6.40883803	2.2951007	10.5225754
Oak-Aspen	7.50882938	3.3950920	11.6225667
Pine-Aspen	1.55510312	-2.5586342	5.6688405
Rowan-Aspen	-6.49079177	-10.6045291	-2.3770544
Spruce-Aspen	-14.93693858	-19.0506759	-10.8232012
Sycamore-Aspen	-9.97674295	-14.0904803	-5.8630056
Willow-Aspen	-10.00939235	-14.1231297	-5.8956550
Birch-Beech	1.78982801	-2.3239093	5.9035654
Cherry-Beech	-2.02856580	-6.1423031	2.0851716
Chestnut-Beech	-0.08257450	-4.1963119	4.0311629
Holmoak-Beech	-13.76725907	-17.8809964	-9.6535217

_	1/2010			rtatian v
	Hornbeam-Beech	-1.72094305	-5.8346804	2.3927943
	Lime-Beech	6.87092856	2.7571912	10.9846659
	Oak-Beech	7.97091991	3.8571826	12.0846573
	Pine-Beech	2.01719366	-2.0965437	6.1309310
	Rowan-Beech	-6.02870123	-10.1424386	-1.9149639
	Spruce-Beech	-14.47484805	-18.5885854	-10.3611107
	Sycamore-Beech	-9.51465241	-13.6283898	-5.4009151
	Willow-Beech	-9.54730182	-13.6610392	-5.4335645
	Cherry-Birch	-3.81839381	-7.9321312	0.2953435
	Chestnut-Birch	-1.87240252	-5.9861399	2.2413348
	Holmoak-Birch	-15.55708708	-19.6708244	-11.4433497
	Hornbeam-Birch	-3.51077106	-7.6245084	0.6029663
	Lime-Birch		0.9673632	
	Oak-Birch	6.18109190	2.0673545	10.2948293
	Pine-Birch	0.22736565	-3.8863717	4.3411030
	Rowan-Birch	-7.81852924	-11.9322666	-3.7047919
	Spruce-Birch	-16.26467606	-20.3784134	-12.1509387
	Sycamore-Birch	-11.30448042	-15.4182178	-7.1907431
	Willow-Birch	-11.33712983	-15.4508672	-7.2233925
	Chestnut-Cherry	1.94599129	-2.1677461	6.0597286
	Holmoak-Cherry	-11.73869328	-15.8524306	-7.6249559
	Hornbeam-Cherry	0.30762275	-3.8061146	4.4213601
	Lime-Cherry	8.89949435	4.7857570	13.0132317
	Oak-Cherry	9.99948571		14.1132231
	Pine-Cherry		-0.0679779	
	Rowan-Cherry	-4.00013544	-8.1138728	0.1136019
	Spruce-Cherry	-12.44628225	-16.5600196	-8.3325449
	Sycamore-Cherry	-7.48608662	-11.5998240	-3.3723493
	Willow-Cherry	-7.51873603		-3.4049987
	Holmoak-Chestnut		-17.7984219	-9.5709472
	Hornbeam-Chestnut	-1.63836854	-5.7521059	2.4753688
	Lime-Chestnut	6.95350306	2.8397657	11.0672404
	Oak-Chestnut	8.05349441	3.9397571	12.1672318
	Pine-Chestnut	2.09976816	-2.0139692	6.2135055
	Rowan-Chestnut		-10.0598641	-1.8323894
	Spruce-Chestnut	-14.39227354		-10.2785362
	Sycamore-Chestnut	-9.43207791	-13.5458153	-5.3183406
	Willow-Chestnut	-9.46472732	-13.5784647	-5.3509900
	Hornbeam-Holmoak	12.04631603	7.9325787	16.1600534
	Lime-Holmoak	20.63818763	16.5244503	24.7519250
	Oak-Holmoak	21.73817898	17.6244416	25.8519163
	Pine-Holmoak	15.78445273	11.6707154	19.8981901
	Rowan-Holmoak	7.73855784	3.6248205	11.8522952
	Spruce-Holmoak	-0.70758898	-4.8213263	3.4061484
	Sycamore-Holmoak	4.25260666	0.1388693	8.3663440
	Willow-Holmoak	4.21995725	0.1062199	8.3336946
l	Lime-Hornbeam	8.59187160	4.4781343	12.7056090
l	Oak-Hornbeam	9.69186296	5.5781256	13.8056003
l	Pine-Hornbeam	3.73813670	-0.3756007	7.8518741
l	Rowan-Hornbeam	-4.30775819	-8.4214955	-0.1940208
l	Spruce-Hornbeam	-12.75390500	-16.8676424	-8.6401676
l	Sycamore-Hornbeam	-7.79370937	-11.9074467	-3.6799720
l	Willow-Hornbeam	-7.82635878	-11.9400961	-3.7126214
l	Oak-Lime	1.09999135	-3.0137460	5.2137287
ř				

```
Pine-Lime
                                            -0.7399975
                    -4.85373490 -8.9674723
Rowan-Lime
                  -12.89962979 -17.0133671
                                             -8.7858924
Spruce-Lime
                  -21.34577661 -25.4595140 -17.2320393
                  -16.38558097 -20.4993183 -12.2718436
Sycamore-Lime
Willow-Lime
                  -16.41823038 -20.5319677 -12.3044930
                                            -1.8399889
Pine-Oak
                    -5.95372625 -10.0674636
Rowan-Oak
                  -13.99962114 -18.1133585
                                             -9.8858838
Spruce-Oak
                  -22.44576796 -26.5595053 -18.3320306
Sycamore-Oak
                  -17.48557232 -21.5993097 -13.3718350
Willow-Oak
                  -17.51822173 -21.6319591 -13.4044844
Rowan-Pine
                    -8.04589489 -12.1596322 -3.9321575
Spruce-Pine
                  -16.49204170 -20.6057791 -12.3783043
Sycamore-Pine
                  -11.53184607 -15.6455834
                                             -7.4181087
Willow-Pine
                  -11.56449548 -15.6782328
                                             -7.4507581
Spruce-Rowan
                   -8.44614681 -12.5598842
                                             -4.3324095
Sycamore-Rowan
                    -3.48595118
                                -7.5996885
                                              0.6277862
Willow-Rowan
                   -3.51860059 -7.6323379
                                              0.5951368
Sycamore-Spruce
                    4.96019563
                                              9.0739330
                                  0.8464583
Willow-Spruce
                    4.92754622
                                  0.8138089
                                              9.0412836
Willow-Sycamore
                    -0.03264941
                                 -4.1463868
                                              4.0810879
                       p adj
Ash-Alder
                  0.1844088
Aspen-Alder
                  0.0000000
Beech-Alder
                  0.0000000
Birch-Alder
                  0.0000000
Cherry-Alder
                  0.0000000
Chestnut-Alder
                  0.0000000
Holmoak-Alder
                  0.9975654
Hornbeam-Alder
                  0.0000000
Lime-Alder
                  0.0000000
Oak-Alder
                  0.0000000
Pine-Alder
                  0.0000000
Rowan-Alder
                  0.0000410
Spruce-Alder
                  0.9036592
Sycamore-Alder
                  0.5644643
Willow-Alder
                  0.5848838
Aspen-Ash
                  0.0000000
Beech-Ash
                  0.0000000
Birch-Ash
                  0.0000000
Cherry-Ash
                  0.0000065
Chestnut-Ash
                  0.0000000
Holmoak-Ash
                  0.0042690
Hornbeam-Ash
                  0.0000018
Lime-Ash
                  0.0000000
0ak-Ash
                  0.0000000
Pine-Ash
                  0.0000000
Rowan-Ash
                  0.5938269
Spruce-Ash
                  0.0003946
Sycamore-Ash
                  0.9999996
Willow-Ash
                  0.999993
Beech-Aspen
                  1.0000000
Birch-Aspen
                  0.9990469
Cherry-Aspen
                  0.7546149
Chestnut-Aspen
                  1.0000000
```

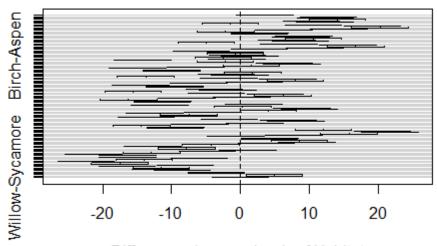
1/2019	
Holmoak-Aspen	0.0000000
Hornbeam-Aspen	0.8929860
Lime-Aspen	0.0000264
0ak-Aspen	0.0000003
Pine-Aspen	0.9946232
Rowan-Aspen	0.0000191
Spruce-Aspen	0.0000000
Sycamore-Aspen	0.0000000
Willow-Aspen	0.0000000
Birch-Beech	0.9787523
Cherry-Beech	0.9381871
Chestnut-Beech	1.0000000
Holmoak-Beech	0.0000000
Hornbeam-Beech	0.9852674
Lime-Beech	0.0000042
Oak-Beech	0.0000000
Pine-Beech	0.9408763
Rowan-Beech	0.0001123
Spruce-Beech	0.0000000
Sycamore-Beech	0.0000000
Willow-Beech	0.0000000
Cherry-Birch	0.1011027
Chestnut-Birch	0.9682125
Holmoak-Birch	0.0000000
Hornbeam-Birch	
	0.1925375
Lime-Birch	0.0030585
Oak-Birch	0.0000633
Pine-Birch	1.0000000
Rowan-Birch	0.0000001
Spruce-Birch	0.0000000
Sycamore-Birch	0.0000000
Willow-Birch	0.0000000
Chestnut-Cherry	0.9558589
Holmoak-Cherry	0.0000000
Hornbeam-Cherry	1.0000000
Lime-Cherry	0.0000000
Oak-Cherry	0.0000000
Pine-Cherry	0.0592074
Rowan-Cherry	0.0661686
Spruce-Cherry	0.0000000
Sycamore-Cherry	0.0000003
Willow-Cherry	0.0000003
Holmoak-Chestnut	0.0000000
Hornbeam-Chestnut	0.9908681
Lime-Chestnut	0.0000030
Oak-Chestnut	0.0000000
Pine-Chestnut	0.9193954
Rowan-Chestnut	0.0001526
Spruce-Chestnut	0.0000000
Sycamore-Chestnut	0.0000000
Willow-Chestnut	0.0000000
Hornbeam-Holmoak	0.0000000
Lime-Holmoak	0.0000000
Oak-Holmoak	0.0000000
Car Hotilloak	3.000000

0.0000000
0.0000001
0.9999997
0.0349691
0.0380910
0.0000000
0.0000000
0.1207078
0.0302058
0.0000000
0.0000001
0.0000001
0.9999007
0.0062590
0.0000000
0.0000000
0.0000000
0.0000000
0.0001484
0.0000000
0.0000000
0.0000000
0.0000000
0.0000000
0.0000000
0.0000000
0.0000000
0.0000000
0.2019434
0.1896363
0.0044944
0.0049788
1.0000000

Hide

plot(TukeyHSD(model))

95% family-wise confidence level



Differences in mean levels of Habitat

Hide

pairwise.t.test(Fugus.yield, Habitat)

Pairwise comparisons using t tests with pooled SD

data: Fugus.yield and Habitat

```
Alder
                Ash
                        Aspen
                                Beech
                                        Birch
                                               Cherry
         0.10011 -
Ash
Aspen
         < 2e-16 6.3e-11 -
Beech
         < 2e-16 5.4e-10 1.00000 -
Birch
         < 2e-16 1.2e-13 1.00000 1.00000 -
Cherry
        4.7e-13 2.9e-06 0.87474 1.00000 0.04943 -
Chestnut < 2e-16 7.8e-10 1.00000 1.00000 1.00000 1.00000
Holmoak 1.00000 0.00181 < 2e-16 < 2e-16 < 2e-16 3.9e-16
Hornbeam 1.1e-13 8.6e-07 1.00000 1.00000 0.10057 1.00000
Lime
         < 2e-16 < 2e-16 1.1e-05 1.9e-06 0.00131 3.3e-10
0ak
         < 2e-16 < 2e-16 1.4e-07 2.0e-08 2.7e-05 1.9e-12
Pine
         < 2e-16 3.9e-14 1.00000 1.00000 1.00000 0.02757
Rowan
        1.8e-05 0.51826 8.5e-06 4.7e-05 3.9e-08 0.03053
        1.00000 0.00016 < 2e-16 < 2e-16 < 2e-16 < 2e-16
Spruce
Sycamore 0.50084 1.00000 2.1e-12 1.9e-11 3.3e-15 1.5e-07
Willow
         0.51826 1.00000 1.9e-12 1.6e-11 2.8e-15 1.4e-07
         Chestnut Holmoak Hornbeam Lime
                                                 Pine
Ash
Aspen
Beech
Birch
Cherry
Chestnut -
Holmoak < 2e-16
Hornbeam 1.00000 < 2e-16 -
Lime
        1.4e-06 < 2e-16 1.3e-09
0ak
        1.5e-08 < 2e-16 8.4e-12 1.00000 -
Pine
        1.00000 < 2e-16 0.05975 0.00253 6.1e-05 -
Rowan
        6.2e-05 5.3e-08 0.01380 < 2e-16 < 2e-16 1.5e-08
         Spruce
Sycamore 2.7e-11 0.01586 4.2e-08 < 2e-16 < 2e-16 1.1e-15
Willow
         2.4e-11 0.01702 3.8e-08 < 2e-16 < 2e-16 9.3e-16
         Rowan
                Spruce Sycamore
Ash
Aspen
Beech
Birch
Cherry
Chestnut -
Holmoak
Hornbeam -
Lime
0ak
Pine
Rowan
Spruce
        2.5e-09 -
Sycamore 0.10218 0.00187 -
Willow
        0.10057 0.00203 1.00000
```

P value adjustment method: holm

Hide

pairwise.t.test(Fugus.yield, Habitat, p.adjust.method="none")

Pairwise comparisons using t tests with pooled ${\sf SD}$

data: Fugus.yield and Habitat

	Alder	Ash	Aspen	Beech	Birch	Cherry
Ash	0.00323	-	-	-	-	-
Aspen	< 2e-16	8.9e-13	_	_	_	_
Beech	< 2e-16	7.8e-12	0.69581	-	-	_
Birch	< 2e-16	1.4e-15	0.26218	0.13135	-	_
Cherry	5.9e-15	5.6e-08	0.03645	0.08761	0.00150	_
Chestnut	< 2e-16	1.1e-11	0.64494	0.94428	0.11461	0.10116
Holmoak	0.22299	4.3e-05	< 2e-16	< 2e-16	< 2e-16	< 2e-16
Hornbeam	1.3e-15	1.6e-08	0.06625	0.14673	0.00342	0.79462
Lime	< 2e-16	< 2e-16	2.3e-07	3.6e-08	3.0e-05	4.7e-12
0ak	< 2e-16	< 2e-16	2.4e-09	3.2e-10	5.6e-07	2.5e-14
Pine	< 2e-16	4.7e-16	0.18945	0.08938	0.84742	0.00079
Rowan	3.6e-07	0.02057	1.7e-07	1.0e-06	6.3e-10	0.00090
Spruce	0.07026	3.6e-06	< 2e-16	< 2e-16	< 2e-16	< 2e-16
Sycamore	0.01855	0.54035	2.8e-14	2.6e-13	< 2e-16	2.7e-09
Willow	0.01993	0.52226	2.4e-14	2.2e-13	< 2e-16	2.3e-09
	Chestnu ⁻	t Holmoal	k Hornbe	am Lime	0ak	Pine
Ash	-	-	-	-	-	-
Aspen	-	-	-	-	-	-
Beech	-	-	-	-	-	-
Birch	-	-	-	-	-	-
Cherry	-	-	-	-	-	-
Chestnut	-	-	-	-	-	-
Holmoak	< 2e-16	-	-	-	-	-
Hornbeam	0.16697	< 2e-1	5 -	-	-	-
Lime	2.5e-08	< 2e-1	5 2.0e-1	1 -	-	-
0ak	2.2e-10	< 2e-1	5 1.1 e-1	3 0.352	50 -	-
Pine	0.07715	< 2e-1	6 0.0018	7 6.5e-0	05 1.3e-	06 -
Rowan	1.4e-06	9.0e-1	0.0003	5 < 2e-:	16 < 2e-	16 2.3e-10
Spruce	< 2e-16	0.5495	2 < 2e-1	5 < 2e-:	16 < 2e-	16 < 2e-16
Sycamore	3.8e-13	0.00043	3 7.1e-10	0 < 2e-:	16 < 2e-	16 < 2e-16
Willow	3.3e-13	0.0004	7 6.1e-10	0 < 2e-:	16 < 2e-	16 < 2e-16
	Rowan	Spruce	Sycamore	e		
Ash	-	-	-			
Aspen	-	-	-			
Beech	-	-	-			
Birch	-	-	-			
Cherry	-	-	-			
Chestnut	-	-	-			
Holmoak	-	-	-			
Hornbeam	-	-	-			
Lime	-	-	-			
0ak	-	-	-			
Pine	-	-	-			
Rowan	-	-	-			
Spruce	3.8e-11	-	-			
Sycamore			-			
Willow	0.00335	5.1e-05	0.97796			

```
P value adjustment method: none
```

Hide

```
install.packages("multcomp")
```

```
WARNING: Rtools is required to build R packages but is not currently installed. Please download
and install the appropriate version of Rtools before proceeding:
https://cran.rstudio.com/bin/windows/Rtools/
Installing package into 怮柂C:/Users/Nathan/Documents/R/win-library/3.6怮拃
(as 恸拖lib恸蚱 is unspecified)
also installing the dependencies 嗷拖zoo嗷蚱,嗷拖mvtnorm嗷蚱,嗷拖TH.data嗷蚱,嗷拖sandwich嗷蚱
trying URL 'https://cran.rstudio.com/bin/windows/contrib/3.6/zoo 1.8-6.zip'
Content type 'application/zip' length 1103803 bytes (1.1 MB)
downloaded 1.1 MB
trying URL 'https://cran.rstudio.com/bin/windows/contrib/3.6/mvtnorm 1.0-11.zip'
Content type 'application/zip' length 271942 bytes (265 KB)
downloaded 265 KB
trying URL 'https://cran.rstudio.com/bin/windows/contrib/3.6/TH.data_1.0-10.zip'
Content type 'application/zip' length 8487682 bytes (8.1 MB)
downloaded 8.1 MB
trying URL 'https://cran.rstudio.com/bin/windows/contrib/3.6/sandwich 2.5-1.zip'
Content type 'application/zip' length 1382340 bytes (1.3 MB)
downloaded 1.3 MB
trying URL 'https://cran.rstudio.com/bin/windows/contrib/3.6/multcomp_1.4-10.zip'
Content type 'application/zip' length 730914 bytes (713 KB)
downloaded 713 KB
```

```
package 'zoo' successfully unpacked and MD5 sums checked
package 'mvtnorm' successfully unpacked and MD5 sums checked
package 'TH.data' successfully unpacked and MD5 sums checked
package 'sandwich' successfully unpacked and MD5 sums checked
package 'multcomp' successfully unpacked and MD5 sums checked

The downloaded binary packages are in
    C:\Users\Nathan\AppData\Local\Temp\RtmpqW2mFi\downloaded_packages
```

Section 11.7

```
data <- read.table("manova.txt",header=T)</pre>
attach(data)
names(data)
[1] "tear"
               "gloss"
                          "opacity" "rate"
                                                "additive"
                                                                                               Hide
Y <- cbind(tear, gloss, opacity)
model <- manova(Y~rate*additive)</pre>
summary(model)
              Df Pillai approx F num Df den Df
                                                  Pr(>F)
               1 0.61814 7.5543
                                       3 14 0.003034 **
rate
               1 0.47697
                                       3
                                             14 0.024745 *
additive
                           4.2556
rate:additive 1 0.22289
                          1.3385
                                             14 0.301782
Residuals
              16
Signif. codes:
0 (***, 0.001 (**, 0.01 (*, 0.05 (., 0.1 ( , 1
                                                                                               Hide
summary.aov(model)
```

```
Response tear :
             Df Sum Sq Mean Sq F value Pr(>F)
rate
              1 1.7405 1.74050 15.7868 0.001092 **
              1 0.7605 0.76050 6.8980 0.018330 *
additive
rate:additive 1 0.0005 0.00050 0.0045 0.947143
Residuals
            16 1.7640 0.11025
---
Signif. codes:
0 (***, 0.001 (**, 0.01 (*, 0.05 (., 0.1 ( , 1
Response gloss:
             Df Sum Sq Mean Sq F value Pr(>F)
              1 1.3005 1.30050 7.9178 0.01248 *
rate
additive
              1 0.6125 0.61250 3.7291 0.07139 .
rate:additive 1 0.5445 0.54450 3.3151 0.08740 .
Residuals
            16 2.6280 0.16425
_ _ _
Signif. codes:
0 (***, 0.001 (**, 0.01 (*, 0.05 (., 0.1 (), 1
Response opacity:
             Df Sum Sq Mean Sq F value Pr(>F)
rate
              1 0.421 0.4205 0.1036 0.7517
additive
              1 4.901 4.9005 1.2077 0.2881
rate:additive 1 3.960 3.9605 0.9760 0.3379
             16 64.924 4.0578
Residuals
```