2, 2x, 3x, ... , 199x

Each will be reduced to one of sine numbers

1,0131 ..., 199. There are 199 numbers in both dists, so we only need to show that no two numbers in the first set map onto the same number in the second list. If kx = jx (mod 199), by the cancellation property k = j (mod 199) Sinie 18 k, j < 199, K=j. Hence no Low numbers in the first list are reduced to the same number in the second. Q.E.D.