

Exam #2 Information:

- The exam is on Friday, February 28
- The exam will cover chapter 7.2-7.6, 8.1-8.4
- You are allowed a one side sheet of paper with whatever you are wanting (I will be collecting these)

Overview of the sections:

7.2: Integration by parts

- important formula: $\int u dv = uv - \int v du$

- we can use LIATE to help us pick our u and the rest is dv

• for example: $\int x e^x dx$ has LIATE

$\uparrow u = x$ $\uparrow dv = e^x dx$

- After we pick u and dv , find du by taking derivative and find v by integrating dv

- Then plug into formula and proceed from there

- Note: there are some instances where you take 2 by parts i.e. apply by parts 2+ times!

7.3: Trigonometric Integrals

- you will HEAVILY need to utilize identities in this section

- we consider the cases

1. $\int \sin^n x dx$ or $\int \cos^n x dx$

- when $n = \text{odd}$, use $\sin^2 x + \cos^2 x = 1$

- when $n = \text{even}$, use half angle formulas

2. $\int \sin^m x \cos^n x dx$

- if m or n is odd, factor out a term to make even n and use $\sin^2 x + \cos^2 x = 1$ — i.e. reduce to type 1

- for m and n even, use half angle formula

3. $\int \sin mx \cos nx dx$, $\int \sin mx \sin nx dx$, $\int \cos mx \cos nx dx$

- these are nice! they use an easy simplification

$$\sin mx \cos nx = \frac{1}{2} [\sin((m+n)x) + \sin((m-n)x)]$$

$$\sin mx \sin nx = \frac{1}{2} [\cos((m+n)x) - \cos((m-n)x)]$$

$$\cos mx \sin nx = \frac{1}{2} [\cos((m+n)x) + \cos((m-n)x)]$$

4. $\int \tan^n x dx$, $\int \cot^n x dx$

- for \tan , use $\tan^2 x = \sec^2 x - 1$

- for \cot , use $\cot^2 x = \csc^2 x - 1$

5. $\int \tan^m x \sec^n x dx$, $\int \cot^m x \csc^n x dx$

- for n even, pull out $\sec^2 x$ and use $\sec^2 x = \tan^2 x + 1$. same for $\csc x$

- for m odd, pull out $\sec x \tan x$. similar for other case.

7.4: Rationalizing substitutions

- when we have $\sqrt{a^2 - x^2}$ we make the sub $x = a \sin t$

- when we have $\sqrt{a^2 + x^2}$ we make the sub $x = a \tan t$

- when we have $\sqrt{x^2 - a^2}$ we make the sub $x = a \sec t$

• once applying the sub, plug it in for all x and then don't forget to differentiate the sub — your integral should be in terms of t !

• at the end, resolve the sub for x

7.5: Partial Fractions

- for the form: $\frac{D}{(x+a)(x+b)}$ we write $\frac{A}{x+a} + \frac{B}{x+b} = \frac{A(x+b) + B(x+a)}{(x+a)(x+b)} = D$ where D is whatever is in our numerator — ignore denominator and solve for A & B by comparing the order.

- for the form: $\frac{D}{(x-1)^2}$ we write $\frac{A}{x-1} + \frac{B}{(x-1)^2} = \frac{A(x-1) + B}{(x-1)^2} = D$

- for the form: $\frac{D}{x(x^2+1)}$ we write $\frac{A}{x} + \frac{Bx+C}{x^2+1} = \frac{A(x^2+1) + x(Bx+C)}{x(x^2+1)} = D$

8.1 L'Hopitals for $\frac{0}{0}$

- check if we are in $\frac{0}{0}$ form

if so, apply L'H
by taking derivative
of top and bottom
SEPARATELY

if not, proceed as
in calc 1 by
taking limit

check if you are in $\frac{0}{0}$

8.2 L'Hopitals for $\frac{\infty}{\infty}$ and other forms

- Apply chart but for $\frac{\infty}{\infty}$ instead of $\frac{0}{0}$

- For $0 \cdot \infty$, write: $f(x)g(x) = \frac{f(x)}{1/g(x)}$ or $\frac{g(x)}{1/f(x)}$ then do the limit either normally or using L'H
↑ check $0/0$ or ∞/∞

- For $\infty - \infty$, make common denominators

- For $0^\infty, 1^\infty, \infty^0$, use natural log! $\lim f(x)^{g(x)} = L$ then $\lim g(x) \ln f(x) = \ln L$ then use above results

8.3 Improper Integrals