Repeated Measures ANOVA

Repeated measures by profile analysis

- More than one response measurement for each subject. Might be
- measurements of the same thing at different times
- measurements of different but related things
- Generalization of matched pairs ("matched triples", etc.).
- Variation: each subject does several different treatments at different times (called crossover design).
- Expect measurements on same subject to be correlated, so assumptions of independence will fail.
- Called *repeated measures*. Different approaches, but *profile analysis* uses Manova (set up right way).
- Another approach uses mixed models (random effects).

Packages

```
library(car)
library(tidyverse)
```

Example: histamine in dogs

- 8 dogs take part in experiment.
- Dogs randomized to one of 2 different drugs.
- Response: log of blood concentration of histamine 0, 1, 3 and 5 minutes after taking drug. (Repeated measures.)
- Data in dogs.txt, column-aligned.

Read in data

```
my url <- "http://www.utsc.utoronto.ca/~butler/d29/dogs.txt"
dogs <- read table(my url)</pre>
##
## -- Column specification
## cols(
##
     dog = col_character(),
##
     drug = col_character(),
##
     x = col character(),
##
     lh0 = col double(),
     lh1 = col double(),
##
     lh3 = col_double().
##
     lh5 = col double()
##
## )
```

Setting things up

dogs

dog	drug	X	lh0	lh1	lh3	lh5
A	Morphine	N	-3.22	-1.61	-2.30	-2.53
В	Morphine	Ν	-3.91	-2.81	-3.91	-3.91
C	Morphine	Ν	-2.66	0.34	-0.73	-1.43
D	Morphine	Ν	-1.77	-0.56	-1.05	-1.43
Ε	Trimethaphan	Ν	-3.51	-0.48	-1.17	-1.51
F	Trimethaphan	Ν	-3.51	0.05	-0.31	-0.51
G	Trimethaphan	Ν	-2.66	-0.19	0.07	-0.22
Н	Trimethaphan	Ν	-2.41	1.14	0.72	0.21

```
response <- with(dogs, cbind(lh0, lh1, lh3, lh5))
dogs.1 <- lm(response ~ drug, data = dogs)</pre>
```

The repeated measures MANOVA

Get list of response variable names; we call them times. Save in data frame.

```
times <- colnames(response)
times.df <- data.frame(times=factor(times))
dogs.2 <- Manova(dogs.1,
   idata = times.df,
   idesign = ~times
)
dogs.2</pre>
```

```
##

## Type II Repeated Measures MANOVA Tests: Pillai test statistic

## Df test stat approx F num Df den Df Pr(>F)

## (Intercept) 1 0.76347 19.3664 1 6 0.004565 **

## drug 1 0.34263 3.1272 1 6 0.127406

## times 1 0.94988 25.2690 3 4 0.004631 **

## drug:times 1 0.89476 11.3362 3 4 0.020023 *

## ---

## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Wide and long format

- Interaction significant. Pattern of response over time different for the two drugs.
- Want to investigate interaction.

The wrong shape

But data frame has several observations per line ("wide format"):

```
dogs %>% slice(1:6)
```

dog	drug	X	lh0	lh1	lh3	lh5
A	Morphine	N	-3.22	-1.61	-2.30	-2.53
В	Morphine	Ν	-3.91	-2.81	-3.91	-3.91
C	Morphine	Ν	-2.66	0.34	-0.73	-1.43
D	Morphine	Ν	-1.77	-0.56	-1.05	-1.43
E	Trimethaphan	Ν	-3.51	-0.48	-1.17	-1.51
F	Trimethaphan	Ν	-3.51	0.05	-0.31	-0.51

- Plotting works with data in "long format": one response per line.
- The responses are log-histamine at different times, labelled 1h-something. Call them all 1h and put them in one column, with the time they belong to labelled.

Running pivot_longer, try 1

dog	drug	х	time	lh		
A	Morphine	N	lh0	-3.22		
Α	Morphine	Ν	lh1	-1.61		
Α	Morphine	Ν	lh3	-2.30		
Α	Morphine	Ν	lh5	-2.53		
В	Morphine	Ν	lh0	-3.91		
В	Morphine	Ν	lh1	-2.81		
В	Morphine	Ν	lh3	-3.91		
В	Morphine	Ν	lh5	-3.91		
C	Morphine	Ν	lh0	-2.66		
C	Morphine	Ν	lh1	0.34		
C	Morphine	Ν	lh3	-0.73		
C	Morphine	Ν	lh5	-1.43		
D	Morphine	Ν	lh0	-1.77		
D	Morphine	Ν	lh1	-0.56		
D	Morphine	Ν	lh3	-1.05		
D	Mornhine N Ih5 -1 43 Repeated Measures ANOVA					

Getting the times

Not quite right: for the times, we want just the numbers, not the letters lh every time. Want new variable containing just number in time: parse_number.

dog	drug	×	timex	lh	time
A	Morphine	N	lh0	-3.22	0
Α	Morphine	N	lh1	-1.61	1
Α	Morphine	N	lh3	-2.30	3
Α	Morphine	N	lh5	-2.53	5
В	Morphine	N	lh0	-3.91	0
В	Morphine	N	lh1	-2.81	1
В	Morphine	N	lh3	-3.91	3
В	Morphine	N	lh5	-3.91	5
C	Morphine	N	lh0	-2.66	0
-			**		

Repeated Measures ANOVA

What I did differently

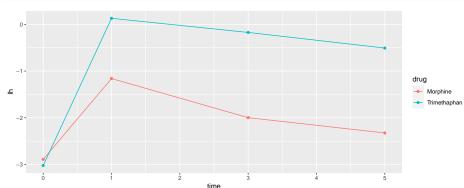
- I realized that pivot_longer was going to produce something like lh1, which I needed to do something further with, so this time I gave it a temporary name timex.
- This enabled me to use the name time for the actual numeric time.
- This works now, so next save into a new data frame dogs.long.

Saving the pipelined results

This says:

- Take data frame dogs, and then:
- Combine the columns 1h0 through 1h5 into one column called 1h, with the column that each 1h value originally came from labelled by timex, and then:
- Pull out numeric values in timex, saving in time and then:
- save the result in a data frame dogs.long.

Interaction plot



Comments

- Plot mean 1h value at each time, joining points on same drug by lines.
- drugs same at time 0
- after that, Trimethaphan higher than Morphine.
- Effect of drug not consistent over time: significant interaction.

Take out time zero

- Lines on interaction plot would then be parallel, and so interaction should no longer be significant.
- Go back to original "wide" dogs data frame.

```
response <- with(dogs, cbind(lh1, lh3, lh5)) # excl time 0
dogs.1 <- lm(response ~ drug, data = dogs)
times <- colnames(response)
times.df <- data.frame(times=factor(times))
dogs.2 <- Manova(dogs.1,
   idata = times.df,
   idesign = ~times
)</pre>
```

Results and comments

dogs.2

```
##
## Type II Repeated Measures MANOVA Tests: Pillai test statistic
## Df test stat approx F num Df den Df Pr(>F)
## (Intercept) 1 0.54582 7.2106 1 6 0.036281 *
## drug 1 0.44551 4.8207 1 6 0.070527 .
## times 1 0.85429 14.6569 2 5 0.008105 **
## drug:times 1 0.43553 1.9289 2 5 0.239390
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

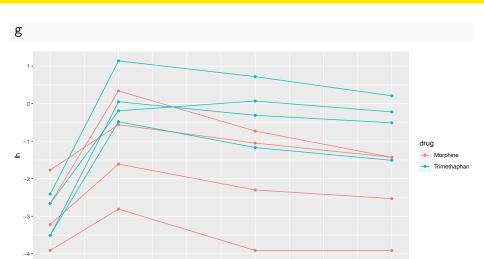
- Correct: interaction no longer significant.
- Significant effect of time.
- Drug effect not quite significant (some variety among dogs within drug).

Is the non-significant drug effect reasonable?

- Plot actual data: 1h against days, labelling observations by drug: "spaghetti plot".
- Uses long data frame (confusing, yes I know):
- Plot (time,lh) points coloured by drug
- and connecting measurements for each dog by lines.
- This time, we want group=dog (want the measurements for each dog joined by lines), but colour=drug:

```
g <- ggplot(dogs.long, aes(
    x = time, y = lh,
    colour = drug, group = dog
)) +
    geom_point() + geom_line()</pre>
```

The spaghetti plot



time

Comments

- For each dog over time, there is a strong increase and gradual decrease in log-histamine. This explains the significant time effect.
- The pattern is more or less the same for each dog, regardless of drug. This explains the non-significant interaction.
- Most of the trimethaphan dogs (blue) have higher log-histamine throughout (time 1 and after), and some of the morphine dogs have lower.
- But two of the morphine dogs have log-histamine profiles like the trimethaphan dogs. This ambiguity is probably why the drug effect is not quite significant.

Mixed models

- Another way to fit repeated measures
- Subjects (on whom repeated measures taken) are random sample of all possible subjects (random effects)
- Times and treatments are the only ones we care about (fixed effects)
- Use package lme4 function lmer (like lm in some ways)
- Uses long-format "tidy" data

Fitting the model

```
library(lme4)
# dogs.long
dogs.2=lmer(lh~drug*time+(1|dog),data=dogs.long)
```

 note specification of random effect: each dog has "random intercept" that moves log-histamine up or down for that dog over all times

What can we drop?

using drop1:

	npar	AIC	LRT	Pr(Chi)
	NA	113.2597	NA	NA
drug:time	1	114.2130	2.953368	0.0856988

Interaction again not significant, but P-value smaller than before

Re-fit without interaction

```
dogs.3=update(dogs.2,.~.-drug:time)
drop1(dogs.3,test="Chisq")
```

	npar	AIC	LRT	Pr(Chi)
	NA	114.2130	NA	NA
drug	1	115.5691	3.356021	0.0669597
time	1	114.9631	2.750099	0.0972484

- This time neither drug nor (surprisingly) time is significant.
- MANOVA and 1mer methods won't agree, but both valid ways to approach problem.

The exercise data

- 30 people took part in an exercise study.
- Each subject was randomly assigned to one of two diets ("low fat" or "non-low fat") and to one of three exercise programs ("at rest", "walking", "running").
- There are $2 \times 3 = 6$ experimental treatments, and thus each one is replicated 30/6 = 5 times.
- Nothing unusual so far.
- However, each subject had their pulse rate measured at three different times (1, 15 and 30 minutes after starting their exercise), so have repeated measures.

Reading the data

)

```
Separated by tabs:
url <- "http://www.utsc.utoronto.ca/~butler/d29/exercise.txt"</pre>
exercise.long <- read_tsv(url)</pre>
##
## -- Column specification ----
## cols(
##
     id = col double(),
##
     diet = col character(),
##
     exertype = col_character(),
##
     pulse = col_double(),
##
     time = col character()
```

The data

exercise.long %>% slice(1:8)

id	diet	exertype	pulse	time
1	nonlowfat	atrest	85	min01
1	nonlowfat	atrest	85	min15
1	nonlowfat	atrest	88	min30
2	nonlowfat	atrest	90	min01
2	nonlowfat	atrest	92	min15
2	nonlowfat	atrest	93	min30
3	nonlowfat	atrest	97	min01
3	nonlowfat	atrest	97	min15

- This is "long format", which is usually what we want.
- But for repeated measures analysis, we want wide format!
- pivot_wider.

Making wide format

 pivot_wider needs: a column that is going to be split, and the column to make the values out of:

id	diet	exertype	min01	min15	min30
6	lowfat	atrest	83	83	84
17	lowfat	walking	103	109	90
23	nonlowfat	running	98	105	99
11	nonlowfat	walking	86	86	84
13	nonlowfat	walking	90	92	93

 Normally pivot_longer min01, min15, min30 into one column called pulse labelled by the number of minutes. But Manova needs it the other way.

Setting up the repeated-measures analysis

Make a response variable consisting of min01, min15, min30:
response <- with(exercise.wide, cbind(min01, min15, min30))</pre>

• Predict that from diet and exertype and interaction using lm:

```
exercise.1 <- lm(response ~ diet * exertype,
  data = exercise.wide
)</pre>
```

• Run this through Manova:

Results

exercise.2

```
##
  Type II Repeated Measures MANOVA Tests: Pillai test statistic
##
                     Df test stat approx F num Df den Df
                          0.99767 10296.7
                                                    24 < 2.2e-16 ***
  (Intercept)
## diet
                          0.37701
                                     14.5
                                                    24 0.0008483 ***
                      2 0.79972 47.9
                                              2
                                                    24 4.166e-09 ***
## exertype
                      2 0.28120 4.7
## diet:exertype
                                                    24 0.0190230 *
## times
                         0.78182 41.2
                                                    23 2.491e-08 ***
                      1 0.25153 3.9
                                                    23 0.0357258 *
## diet:times
                      2 0.83557
                                 8.6
                                              4
                                                    48 2.538e-05 ***
## exertype:times
                      2 0.51750
                                 4.2
                                              4
                                                    48 0.0054586 **
## diet:exertype:times
## ---
## Signif. codes:
                 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

- Three-way interaction significant, so cannot remove anything.
- Pulse rate depends on diet and exercise type *combination*, and *that* is different for each time.

Making some graphs

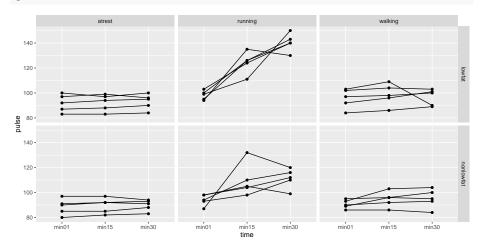
- Three-way interactions are difficult to understand. To make an attempt, look at some graphs.
- Plot time trace of pulse rates for each individual, joined by lines, and make *separate* plots for each diet-exertype combo.
- ggplot again. Using long data frame:

```
g <- ggplot(exercise.long, aes(
  x = time, y = pulse,
  group = id
)) + geom point() + geom line() +
  facet grid(diet ~ exertype)
```

• facet_grid(diet~exertype): do a separate plot for each combination of diet and exercise type, with diets going down the page and exercise types going across. (Graphs are usually landscape, so have the factor exertype with more levels going across.) Repeated Measures ANOVA

The graph(s)

g



Comments on graphs

- For subjects who were at rest, no change in pulse rate over time, for both diet groups.
- For walking subjects, not much change in pulse rates over time.
 Maybe a small increase on average between 1 and 15 minutes.
- For both running groups, an overall increase in pulse rate over time, but the increase is stronger for the lowfat group.
- No consistent effect of diet over all exercise groups.
- No consistent effect of exercise type over both diet groups.
- No consistent effect of time over all diet-exercise type combos.

"Simple effects" of diet for the subjects who ran

- Looks as if there is only any substantial time effect for the runners. For them, does diet have an effect?
- Pull out only the runners from the wide data:

```
exercise.wide %>%
filter(exertype == "running") -> runners.wide
```

 Create response variable and do MANOVA. Some of this looks like before, but I have different data now:

```
response <- with(runners.wide, cbind(min01, min15, min30))
runners.1 <- lm(response ~ diet, data = runners.wide)
times <- colnames(response)
times.df <- data.frame(times=factor(times))
runners.2 <- Manova(runners.1,
   idata = times.df,
   idesign = ~times
)</pre>
```

Results

runners.2

```
##
## Type II Repeated Measures MANOVA Tests: Pillai test statistic
## Df test stat approx F num Df den Df Pr(>F)
## (Intercept) 1 0.99912 9045.3 1 8 1.668e-13 ***
## diet 1 0.84986 45.3 1 8 0.0001482 ***
## times 1 0.92493 43.1 2 7 0.0001159 ***
## diet:times 1 0.68950 7.8 2 7 0.0166807 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

text under

- The diet by time interaction is still significant (at $\alpha=0.05$): the effect of time on pulse rates is different for the two diets.
- At $\alpha = 0.01$, the interaction is not significant, and then we have only two (very) significant main effects of diet and time.

How is the effect of diet different over time?

• Table of means. Only I need long data for this, so make it (in a pipeline):

- ## `summarise()` has grouped output by 'time'. You can override
 - Result of summarize is data frame, so can save it (and do more with it if needed).

Understanding diet-time interaction

• The summary:

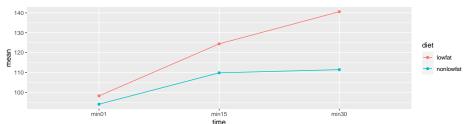
SIIMM

time	diet	mean	sd
min01	lowfat	98.2	3.701351
min01	nonlowfat	94.0	4.527693
min15	lowfat	124.4	8.619745
min15	nonlowfat	109.8	13.122500
min30	lowfat	140.6	7.197222
min30	nonlowfat	111.4	7.924645

- Pulse rates at any given time higher for lowfat (diet effect),
- Pulse rates increase over time of exercise (time effect),
- but the amount by which pulse rate higher for a diet depends on time: diet by time interaction.

Interaction plot

 We went to trouble of finding means by group, so making interaction plot is now mainly easy:



Comment on interaction plot

- The lines are not parallel, so there is interaction between diet and time for the runners.
- The effect of time on pulse rate is different for the two diets, even though all the subjects here were running.