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Booklet of Code and Output for STAD29/STA 1007 Midterm Exam

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Note that Figures 33, 34 and 35 are at the end of this booklet, because they are printed in colour.

```
library(tidyverse)
## -- Attaching packages -----
tidyverse 1.2.1 --
## v qqplot2 3.1.1
                         v purrr 0.3.2
                         v dplyr 0.8.0.1
## v tibble 2.1.1
## v tidyr 0.8.3.9000 v stringr 1.4.0
## v readr 1.3.1
                        v forcats 0.3.0
## Warning: package 'ggplot2' was built under R version 3.5.3
## Warning: package 'tibble' was built under R version 3.5.3
## Warning: package 'tidyr' was built under R version 3.5.3
## Warning: package 'readr' was built under R version 3.5.2
## Warning: package 'purrr' was built under R version 3.5.3
## Warning: package 'dplyr' was built under R version 3.5.2
## Warning: package 'stringr' was built under R version 3.5.2
## Warning: package 'forcats' was built under R version 3.5.1
## -- Conflicts -----
tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                  masks stats::lag()
library(broom)
## Warning: package 'broom' was built under R version 3.5.2
library(MASS)
##
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##
      select
library(survival)
library(survminer)
## Warning: package 'survminer' was built under R version 3.5.1
## Loading required package: ggpubr
## Warning: package 'ggpubr' was built under R version 3.5.1
## Loading required package: magrittr
## Warning: package 'magrittr' was built under R version 3.5.1
##
## Attaching package: 'magrittr'
## The following object is masked from 'package:purrr':
##
##
      set\_names
## The following object is masked from 'package:tidyr':
##
##
      extract
```

```
reasoning=read.csv("reasoning.csv",header=T)
reasoning
##
     row piano singing computer none
## 1
      1
           2
                1
                         0 5
## 2
       2
            5
                  -1
                           1
                               -1
     3 7 0
4 -2 1
5 2 -4
6 7 0
7 4 0
## 3
                                7
## 4
                          -3
                              0
                          -2
## 5
                                4
     6
                           4
## 6
                                0
    7
                          -1 2
## 7
          4
                  0
## 8
           1
      8
                  1
                           2
                               1
## 9
      9
            0
                   0
                           4
                               -6
## 10 10
                                0
```

Figure 2: Reasoning data

```
reasoning %>%
  gather(lesson, changescore, piano: none) -> reasoning2
```

Figure 3: Processing, part 1

```
reasoning2 %>%
  group_by(lesson) %>%
  summarize(count=n(),m=mean(changescore))
```

Figure 4: Processing, part 2

```
reasoning2 %>%
ggplot(aes(x=lesson,y=changescore))+geom_boxplot()
```

Figure 5: Processing, part 3

```
mercury=read.csv("mercury.csv",header=T)
str(mercury)

## 'data.frame': 38 obs. of 4 variables:
## $ mercury : int 1330 250 450 160 720 810 710 510 1000 150 ...
## $ alkalinity: num 2.5 19.6 5.2 71.4 26.4 4.8 6.6 16.5 7.1 83.7 ...
## $ calcium : num 2.9 4.5 2.8 55.2 9.2 4.6 2.7 13.8 5.2 66.5 ...
## $ pH : num 4.6 7.3 5.4 8.1 5.8 6.4 5.4 7.2 5.8 8.2 ...
```

Figure 6: Fish mercury data (structure)

```
mercury %>%
  gather(xname,x,alkalinity:pH) %>%
  ggplot(aes(x=x,y=mercury))+geom_point()+geom_smooth()+
   facet_wrap(~xname,scales="free",ncol=2)

## `geom_smooth()` using method = 'loess' and formula 'y ~ x'
```

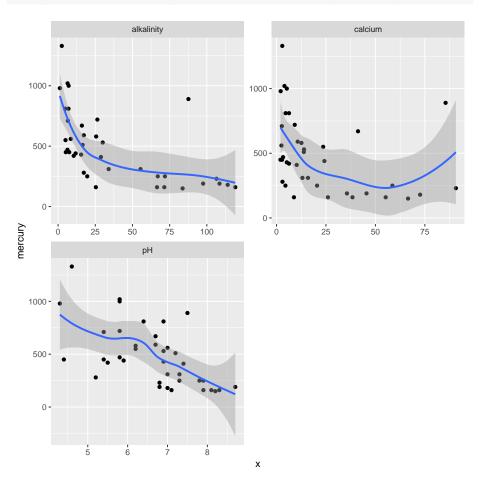


Figure 7: Scatter plots for fish mercury data

```
mercury.1=lm(mercury~alkalinity+calcium+pH,data=mercury)
summary(mercury.1)
##
## Call:
## lm(formula = mercury ~ alkalinity + calcium + pH, data = mercury)
##
## Residuals:
   Min 1Q Median
                             3Q
## -371.46 -140.30 -3.97 106.31 551.98
##
## Coefficients:
            Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1221.451 279.406 4.372 0.00011 ***
                       2.014 -2.324 0.02622 *
## alkalinity -4.681
## calcium
               3.495
                         2.594 1.347 0.18685
## pH
              -96.058
                        46.504 -2.066 0.04656 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 226.4 on 34 degrees of freedom
## Multiple R-squared: 0.4571, Adjusted R-squared: 0.4092
## F-statistic: 9.544 on 3 and 34 DF, p-value: 0.0001024
```

Figure 8: Regression 1 for fish mercury data

```
mercury.2=lm(log(mercury)~log(alkalinity)+log(calcium)+pH,data=mercury)
summary(mercury.2)
##
## Call:
## lm(formula = log(mercury) ~ log(alkalinity) + log(calcium) +
     pH, data = mercury)
##
## Residuals:
##
     Min
               1Q
                  Median
                               3Q
                                      Max
## -0.75244 -0.30191 -0.00783 0.23852 1.22932
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 7.55983 0.48981 15.434 < 2e-16 ***
0.10315 1.425 0.163185
## log(calcium) 0.14702
                -0.07998
                         0.10248 -0.780 0.440527
## pH
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.4099 on 34 degrees of freedom
## Multiple R-squared: 0.6069, Adjusted R-squared: 0.5723
## F-statistic: 17.5 on 3 and 34 DF, p-value: 4.808e-07
```

Figure 9: Regression 2 for fish mercury data

```
mercury.3=update(mercury.2,.~.-log(calcium)-pH)
```

Figure 10: Regression 3 for fish mercury data

```
summary(mercury)
##
      mercury
                    alkalinity
                                      calcium
                                                         рН
##
   Min. : 150.0
                   Min. : 1.20
                                   Min. : 2.000
                                                  Min.
                                                         :4.300
## 1st Qu.: 250.0
                   1st Qu.: 7.20
                                  1st Qu.: 4.525
                                                   1st Qu.:5.800
## Median : 445.0
                   Median : 18.45
                                   Median :11.650
                                                   Median :6.850
## Mean : 488.4
                   Mean : 37.15
                                   Mean :22.361
                                                   Mean :6.634
##
   3rd Qu.: 650.0
                   3rd Qu.: 66.88
                                   3rd Qu.:33.200
                                                   3rd Qu.:7.300
  Max. :1330.0
                   Max. :119.10
                                   Max. :90.700
                                                          :8.700
                                                   Max.
new=data.frame(alkalinity=c(7,67))
new
##
    alkalinity
## 1
             7
## 2
            67
p=predict(mercury.3,new,interval="c")
cbind(new,p)
##
    alkalinity
                 fit
                          lwr
                                    upr
## 1
            7 6.435714 6.252683 6.618745
## 2
            67 5.536953 5.345056 5.728849
```

Figure 11: Prediction for fish mercury data

```
leukemia=read.csv("leukemia.csv", header=T)
leukemia
##
            wbc live
      ag
## 1
            75
       +
                   1
## 2
       +
            260
                   1
## 3
       +
           1000
                   1
## 4
            700
                   1
          3500
## 5
                   0
       + 10000
## 6
                   0
## 7
            300
                   1
## 8
            900
                   0
## 9
           1900
                   0
## 10
           3100
                   0
## 11
           7900
                   0
## 12
       +
            230
                   1
  13
       +
##
            600
                   0
##
  14
       +
           1700
                   0
## 15
       +
            940
                   1
## 16
       +
           5200
                   0
## 17
       + 10000
                   0
## 18
            400
                   0
## 19
            530
                   0
## 20
           2700
                   0
## 21
           2600
                   0
## 22
       - 10000
                   0
## 23
      +
            430
                   1
## 24
       +
          1050
                   1
       +
## 25
            540
                   0
## 26
      +
           3200
                   0
## 27
       + 10000
                   1
## 28
            440
                   1
## 29
            150
                   0
## 30
      -
                   0
          1000
## 31
           2800
                   0
## 32
          2100
                   0
## 33 - 10000
                   0
```

Figure 12: Leukemia data

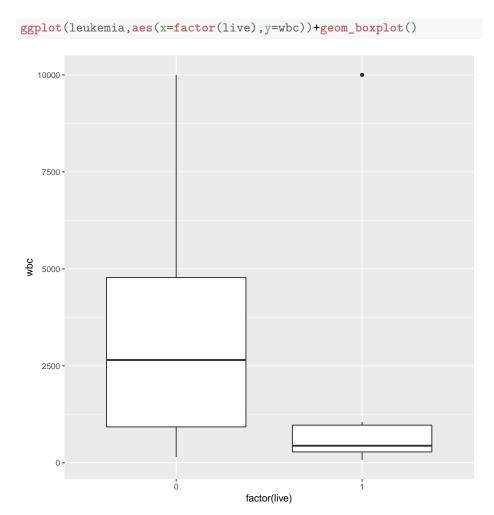


Figure 13: Boxplot of white blood cell count vs. survival $\,$

```
leukemia.1=glm(live~log(wbc)+ag,family="binomial",data=leukemia)
summary(leukemia.1)
##
## Call:
## glm(formula = live ~ log(wbc) + ag, family = "binomial", data = leukemia)
## Deviance Residuals:
##
      Min
           1Q Median
                            3Q
                                       Max
## -1.6599 -0.6568 -0.2803 0.5286
                                     2.1258
##
## Coefficients:
##
   Estimate Std. Error z value Pr(>|z|)
## (Intercept) 5.5433 3.0224 1.834 0.0666.
## log(wbc) -1.1088 0.4609 -2.405 0.0162 *
                        1.0907 2.310 0.0209 *
## ag+
               2.5196
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 42.010 on 32 degrees of freedom
##
## Residual deviance: 26.833 on 30 degrees of freedom
## AIC: 32.833
## Number of Fisher Scoring iterations: 5
```

Figure 14: Logistic regression for leukemia data

Figure 15: Predictions

```
painrelief0=read.table("drugcomp.txt",header=T)
lev=levels(painrelief0$rating)
lev
## [1] "fair"
                 "good"
                            "poor"
                                       "verygood"
painrelief0 %>%
 mutate(rating=ordered(rating,lev[c(3,1,2,4)])) -> painrelief
painrelief
##
      drug
           rating frequency
## 1
      c15
           poor
## 2
      c15
              fair
                          18
## 3
                         20
      c15
              good
      c15 verygood
## 4
                          5
## 5
      c60
           poor
                          30
## 6
      c60
              fair
                          25
## 7
      c60
             good
                          30
## 8
                          8
      c60 verygood
## 9 z100
             poor
                         10
## 10 z100
                          4
              fair
## 11 z100
              good
                          13
## 12 z100 verygood
                          34
painrelief$rating
## [1] poor
               fair
                         good
                                  verygood poor
                                                   fair
                                                            good
## [8] verygood poor
                         fair
                                  good
                                           verygood
## Levels: poor < fair < good < verygood
```

Figure 16: Pain relief data

```
painrelief.1=polr(rating~drug, weight=frequency, data=painrelief)
drop1(painrelief.1,test="Chisq")
## Single term deletions
##
## Model:
## rating ~ drug
## Df AIC LRT Pr(>Chi)
## <none> 557.96
## drug 2 595.87 41.91 7.93e-10 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
new=data.frame(drug=levels(painrelief$drug))
p=predict(painrelief.1,new,type="probs")
cbind(new,p)
##
                                   good verygood
   drug
              poor
                         fair
## 1 c15 0.32446172 0.25034061 0.2972508 0.1279469
## 2 c60 0.34244375 0.25200600 0.2863636 0.1191867
## 3 z100 0.06486819 0.09848111 0.3327126 0.5039381
```

Figure 17: Model-fitting and predictions for pain relief data

```
clematis=read.csv("muenchow.csv",header=T)
str(clematis)
  'data.frame': 96 obs. of 3 variables:
   $ gender : Factor w/ 2 levels "female", "male": 2 2 2 2 2 2 2 2 2 2 ...
             : int 1 1 2 2 4 4 5 5 6 6 ...
   $ wait
   $ observed: Factor w/ 2 levels "no","yes": 2 2 2 2 2 2 2 2 2 2 ...
clematis %>% sample_n(20)
##
      gender wait observed
## 1
               7
        male
                       yes
## 2
     female
               15
                       yes
## 3
               68
        male
                       yes
## 4
     female
               7
                       yes
## 5 female
               29
                       yes
## 6 female
               23
                       yes
## 7 female
               30
                       yes
## 8 female
               18
                       yes
## 9
        male
               19
                       yes
## 10
       male
               1
                       yes
## 11
       male
               61
                       yes
## 12 female
               35
                       yes
               29
## 13 female
                       yes
## 14 female
               39
                       yes
## 15 female
               19
                       yes
## 16 female
               28
                       yes
## 17 female
               90
                       no
## 18 female
               75
                       no
## 19 female
               2
                       yes
## 20
        male
               83
                       yes
```

Figure 18: Clematis data (structure and a few randomly-chosen rows)

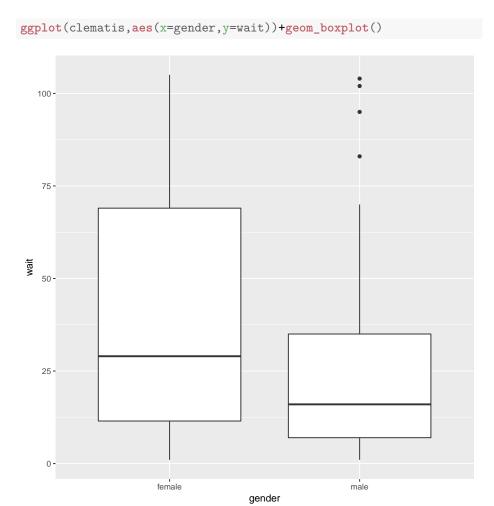


Figure 19: Boxplots of waiting times

```
y=with(clematis,Surv(wait,observed=="yes"))
У
##
    [1]
                1
                     2
                           2
                                4
                                           5
                                                 5
                                                      6
                                                           6
                                                                 6
                                                                                  8
                                      4
## [15]
          8
                8
                     9
                           9
                                9
                                     11
                                          11
                                                14
                                                     14
                                                           14
                                                                16
                                                                      16
                                                                           17
                                                                                 17
## [29]
         18
               19
                    19
                          19
                               27
                                     27
                                          30
                                                31
                                                     35
                                                           36
                                                                40
                                                                      43
                                                                                 61
  [43]
         68
               69
                    70
                          83
                               95
                                    102+ 104+
                                                      2
                                                           4
                                                                 4
                                                                      5
                                                                                  7
##
                                                1
                                                                            6
          7
                                9
   [57]
               8
                     8
                           8
                                     14
                                          15
                                                18
                                                     18
                                                           19
                                                                23
                                                                      23
                                                                           26
                                                                                 28
                                                           43
##
  [71]
         29
               29
                    29
                          30
                               32
                                     35
                                          35
                                                37
                                                     39
                                                                56
                                                                      57
                                                                                 67
## [85]
                          78
                                                     96+ 100+ 102+ 105+
         71
               75
                    75+
                               81
                                     90+
                                          94+
                                                96
```

Figure 20: Construction of response variable

```
clematis.1=coxph(y~gender,data=clematis)
summary(clematis.1)
## Call:
## coxph(formula = y ~ gender, data = clematis)
##
##
   n= 96, number of events= 87
##
##
               coef exp(coef) se(coef)
                                          z Pr(>|z|)
## gendermale 0.5069    1.6602    0.2170    2.336    0.0195 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
             exp(coef) exp(-coef) lower .95 upper .95
##
## gendermale
              1.66
                          0.6023
                                    1.085
##
## Concordance= 0.571 (se = 0.029)
## Likelihood ratio test= 5.47 on 1 df,
                                         p=0.02
## Wald test = 5.46 on 1 df,
                                         p=0.02
## Score (logrank) test = 5.57 on 1 df,
                                         p=0.02
```

Figure 21: Cox model 1

```
clematis.0=coxph(y~1,data=clematis)
anova(clematis.0,clematis.1)

## Analysis of Deviance Table
## Cox model: response is y
## Model 1: ~ 1
## Model 2: ~ gender
## loglik Chisq Df P(>|Chi|)
## 1 -331.66
## 2 -328.93 5.4726 1 0.01932 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Figure 22: Cox model 2 and comparison

```
essay=read.csv("essay.csv",header=T)
essay
##
     ability method score
## 1
        none bluebook 23
## 2
        none bluebook 32
## 3
       none bluebook 25
                      29
## 4
        some bluebook
## 5
       some bluebook 30
## 6
        some bluebook 34
## 7
        lots bluebook
                      31
## 8
        lots bluebook
                       36
## 9
        lots bluebook
                       33
## 10
        none computer
                        32
## 11
        none computer
                        26
## 12
        none computer
                        26
## 13
                        34
        some computer
## 14
        some computer
                        41
## 15
        some computer
                        35
## 16
        lots computer
                        23
## 17
        lots computer
                        26
        lots computer
## 18
                         32
```

Figure 23: Essay marks data

```
essay %>% mutate(ability.ord=ordered(ability,c("none","some","lots"))) %>%
 group_by(ability.ord,method) %>%
  summarize(mean.score=mean(score)) -> essay.means
essay.means
## # A tibble: 6 x 3
## # Groups: ability.ord [3]
    ability.ord method mean.score
    <ord>
             <fct>
                          <dbl>
                             26.7
## 1 none
              bluebook
              computer
## 2 none
## 3 some
              bluebook
                              31
## 4 some
              computer
                              36.7
              bluebook
## 5 lots
                              33.3
## 6 lots
              computer
                              27
```

Figure 24: Essay marks means

Figure 25: Essay marks analysis 1

```
essay.2=aov(score~ability*method,data=essay)
summary(essay.2)
                Df Sum Sq Mean Sq F value Pr(>F)
##
## ability
                 2 127.44
                           63.72 4.606 0.0328 *
## method
                 1 0.22
                            0.22
                                 0.016 0.9012
## ability:method 2 110.78 55.39 4.004 0.0465 *
## Residuals 12 166.00
                          13.83
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Figure 26: Essay marks analysis 2

```
essay %>% filter(method=="computer") %>%
 aov(score~ability,data=.) -> essay.3
summary(essay.3)
##
              Df Sum Sq Mean Sq F value Pr(>F)
## ability
               2 169.56
                          84.78 5.373 0.046 *
## Residuals
               6 94.67
                          15.78
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
TukeyHSD(essay.3,conf.level=0.90)
    Tukey multiple comparisons of means
##
       90% family-wise confidence level
##
##
## Fit: aov(formula = score ~ ability, data = .)
##
## $ability
##
                 diff
                            lwr
                                     upr
                                             p adj
## none-lots 1.000000 -7.1604402 9.16044 0.9493774
## some-lots 9.666667 1.5062264 17.82711 0.0557235
## some-none 8.666667 0.5062264 16.82711 0.0820210
```

Figure 27: Essay marks analysis 3

```
essay %>% filter(method=="bluebook") %>%
 aov(score~ability,data=.) -> essay.4
summary(essay.4)
##
              Df Sum Sq Mean Sq F value Pr(>F)
## ability
               2 68.67
                          34.33
                                  2.888 0.132
## Residuals
               6 71.33
                          11.89
TukeyHSD(essay.4,conf.level=0.90)
##
    Tukey multiple comparisons of means
##
      90% family-wise confidence level
##
## Fit: aov(formula = score ~ ability, data = .)
##
## $ability
##
                 diff
                             lwr
                                        upr
                                               p adj
## none-lots -6.666667 -13.750385 0.417052 0.1207974
## some-lots -2.333333 -9.417052 4.750385 0.7004165
## some-none 4.333333 -2.750385 11.417052 0.3395194
```

Figure 28: Essay marks analysis 4

```
pottery=read.table("pottery.txt",header=T)
pottery
##
        Al
             Fe
                       Ca
                                       Site
                  Mg
                           Na
     14.4 7.00 4.30 0.15 0.51
                                 Llanederyn
     13.8 7.08 3.43 0.12 0.17
                                 Llanederyn
## 3
      14.6 7.09 3.88 0.13 0.20
                                 Llanederyn
## 4
     11.5 6.37 5.64 0.16 0.14
                                 Llanederyn
      13.8 7.06 5.34 0.20 0.20
                                 Llanederyn
## 6
     10.9 6.26 3.47 0.17 0.22
                                 Llanederyn
      10.1 4.26 4.26 0.20 0.18
                                 Llanederyn
## 8
     11.6 5.78 5.91 0.18 0.16
                                 Llanederyn
                                 Llanederyn
## 9 11.1 5.49 4.52 0.29 0.30
## 10 13.4 6.92 7.23 0.28 0.20
                                 Llanederyn
## 11 12.4 6.13 5.69 0.22 0.54
                                 Llanederyn
## 12 13.1 6.64 5.51 0.31 0.24
                                 Llanederyn
## 13 12.7 6.69 4.45 0.20 0.22
                                 Llanederyn
## 14 12.5 6.44 3.94 0.22 0.23
                                 Llanederyn
## 15 11.8 5.44 3.94 0.30 0.04
                                   Caldicot
## 16 11.6 5.39 3.77 0.29 0.06
                                   Caldicot
## 17 18.3 1.28 0.67 0.03 0.03 IslandThorns
## 18 15.8 2.39 0.63 0.01 0.04 IslandThorns
## 19 18.0 1.50 0.67 0.01 0.06 IslandThorns
## 20 18.0 1.88 0.68 0.01 0.04 IslandThorns
## 21 20.8 1.51 0.72 0.07 0.10 IslandThorns
## 22 17.7 1.12 0.56 0.06 0.06
                                AshleyRails
                                AshleyRails
## 23 18.3 1.14 0.67 0.06 0.05
## 24 16.7 0.92 0.53 0.01 0.05
                                AshleyRails
## 25 14.8 2.74 0.67 0.03 0.05
                                AshleyRails
## 26 19.1 1.64 0.60 0.10 0.03
                                AshleyRails
```

Figure 29: Pottery data

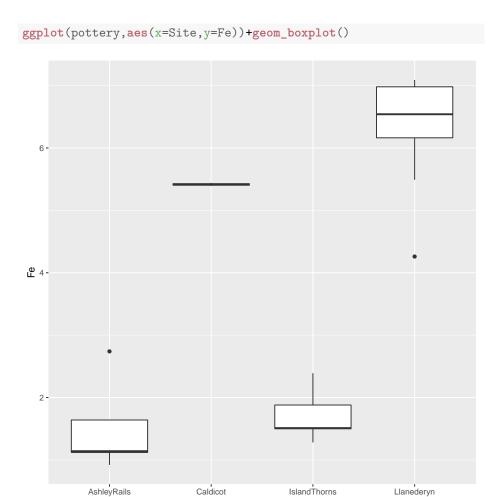


Figure 30: Boxplots of pottery data

Site

```
levels(pottery$Site)

## [1] "AshleyRails" "Caldicot" "IslandThorns" "Llanederyn"

c.a=c(1,0,-1,0)
c.b=c(-1/2,1/2,-1/2,1/2)
c.c=c(0,1,0,-1)
m=cbind(c.a,c.b,c.c)
contrasts(pottery$Site)=m
```

Figure 31: Computations for pottery data

```
pottery.1=lm(Fe~Site,data=pottery)
summary(pottery.1)
##
## Call:
## lm(formula = Fe ~ Site, data = pottery)
##
## Residuals:
## Min
               1Q Median
                                 3Q
                                        Max
## -2.11214 -0.33954 0.01143 0.49036 1.22800
##
## Coefficients:
   Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3.7528 0.1738 21.587 2.68e-16 ***
## Sitec.a -0.1000
                         0.2231 -0.448 0.6584
              4.2816
                      0.3477 12.314 2.42e-11 ***
## Sitec.b
## Sitec.c
             -0.4786
                        0.2667 -1.795 0.0865 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.7055 on 22 degrees of freedom
## Multiple R-squared: 0.9246, Adjusted R-squared: 0.9143
## F-statistic: 89.88 on 3 and 22 DF, p-value: 1.679e-12
```

Figure 32: Analysis for pottery data



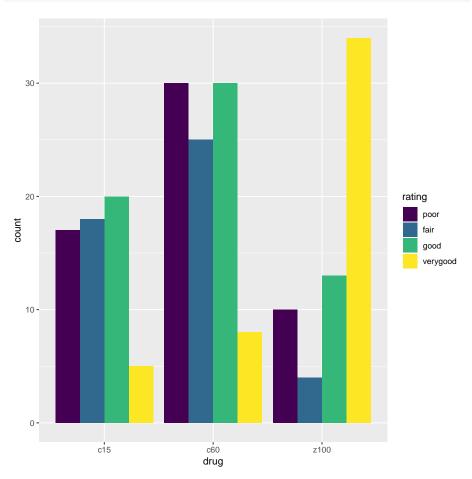


Figure 33: Grouped bar chart of pain relief data

```
genders=with(clematis,levels(gender))
new=data.frame(gender=genders)
p=survfit(clematis.1,new)
new

## gender
## 1 female
## 2 male

ggsurvplot(p)

## Error in .get_data(fit, data = data, complain = FALSE):
The `data` argument should be provided either to ggsurvfit or survfit.
```

Figure 34: Predictions and survival plot

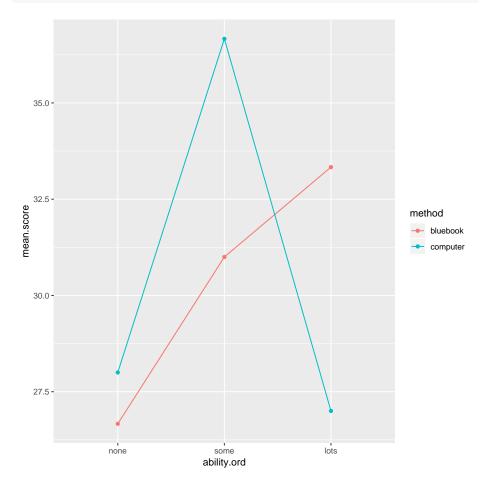


Figure 35: Essay marks plot