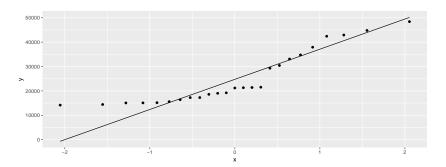


Assumptions

- ► The t procedures we have seen so far come with assumption of normally-distributed data
- but how much does that normality matter?
- Central Limit Theorem says that sampling distribution of sample mean is "approximately normal" if sample size is "large".
- Hence same applies to difference of two sample means.
- ▶ How to use this in practice? Draw a picture and make a call about whether sample size large enough.

Blue Jays attendances

```
ggplot(jays, aes(sample = attendance)) +
stat_qq() + stat_qq_line()
```



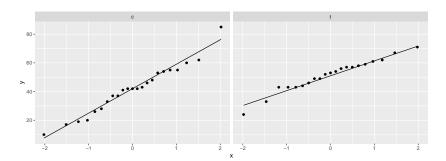
Comments

- Distribution of attendances somewhat skewed to the right (because of the short lower tail and the sort-of curve)
- lacktriangle Sample size n=25 is reasonably large in Central Limit Theorem terms
- \blacktriangleright Use of t may be OK here despite skewed shape.

Learning to read

Make normal quantile plots, one for each sample:

```
ggplot(kids, aes(sample = score)) +
  stat_qq() + stat_qq_line() +
  facet_wrap(~ group)
```



Comments

- with sample sizes over 20 in each group, these are easily normal enough to use a *t*-test.
- the (sampling distribution of the) difference between two sample means tends to have a more normal distribution than either sample mean individually, so that two-sample t tends to be better than you'd guess.

Pain relief

▶ With matched pairs, assumption is of normality of *differences*, so work those out first:

```
pain %>% mutate(diff = druga - drugb) -> pain
pain
```

```
# A tibble: 12 x 4
   subject druga drugb diff
     <dbl> <dbl> <dbl> <dbl> <dbl>
             2 	 3.5 - 1.5
 1
         2 \quad 3.6 \quad 5.7 \quad -2.1
 3
         3 2.6 2.9 -0.300
4
        4 2.6 2.4 0.200
 5
         5 7.3 9.9 -2.6
 6
         6 3.4 3.3 0.100
 7
            14.9 16.7 -1.80
 8
         8
            6.6 6 0.600
            2.3 \quad 3.8 \quad -1.5
```

Normality of differences

```
ggplot(pain,aes(sample=diff)) + stat_qq() + stat_qq_line()
  0.0 -
  -2.5 -
  -5.0 -
  -7.5 -
 -10.0 -
 -12.5 -
                     -1
```

Comments

- ► This is very non-normal (the low outlier)
- \blacktriangleright The sample size of n=12 is not large
- ▶ We should have concerns about our matched pairs *t*-test.

Doing things properly

- ightharpoonup The right way to use a t procedure:
 - draw a graph of our data (one of the standard graphs, or normal quantile plot)
 - use the graph to assess sufficient normality given the sample size
 - for a two-sample test, assess equality of spreads (boxplot easier for this)
 - ▶ if necessary, express our doubts about the t procedure (for now), or do a better test (later).

Looking ahead

- Looking at a normal quantile plot and assessing it with the sample size seems rather arbitrary. Can we do better? (Yes: using the bootstrap, later.)
- ▶ What to do if the *t* procedure is not to be trusted? Use a different test (later):
 - one sample: sign test
 - two samples: Mood's median test
 - matched pairs: sign test on differences.
- ▶ If you have heard about the signed rank or rank sum tests: they come with extra assumptions that are usually not satisfied if normality fails.