

## Matched pairs

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Some data:

subject	druga	drugb
1	2.0	3.5
2	3.6	5.7
3	2.6	2.9
4	2.6	2.4
5	7.3	9.9
6	3.4	3.3
7	14.9	16.7
8	6.6	6.0
9	2.3	3.8
10	2.0	4.0

## Matched pairs 1/2

- Data are comparison of 2 drugs for effectiveness at reducing pain.
  - ▶ 12 subjects (cases) were arthritis sufferers
  - ▶ Response is #hours of pain relief from each drug.
- In reading example, each child tried only one reading method.
- But here, each subject tried out both drugs, giving us two measurements.
- Possible because, if you wait long enough, one drug has no influence over effect of other.

## Matched pairs 2/2

- Advantage: focused comparison of drugs. Compare one drug with another on same person, removes a lot of variability due to differences between people.
- Matched pairs, requires different analysis.
- Design: randomly choose 6 of 12 subjects to get drug A first, other 6 get drug B first.

# Packages

```
library(tidyverse)  
library(smmr) # for a sign test later
```

# Reading the data

Values aligned in columns:

```
my_url <-  
  "http://ritsokiguess.site/datafiles/analgesic.txt"  
pain <- read_table(my_url)  
pain %>% slice(1:6) # display first six rows
```

```
# A tibble: 6 x 3  
  subject druga drugb  
    <dbl> <dbl> <dbl>  
1         1     2   3.5  
2         2   3.6   5.7  
3         3   2.6   2.9  
4         4   2.6   2.4  
5         5   7.3   9.9  
6         6   3.4   3.3
```

## Paired $t$ -test

```
with(pain, t.test(druga, drugb, paired = TRUE))
```

### Paired t-test

data: druga and drugb

$t = -2.1677$ ,  $df = 11$ ,  $p\text{-value} = 0.05299$

alternative hypothesis: true mean difference is not equal to 0

95 percent confidence interval:

-4.29941513 0.03274847

sample estimates:

mean difference

-2.133333

- P-value is 0.053.
- Not quite evidence of difference between drugs.

## t-testing the differences

- Likewise, you can calculate the differences yourself and then do a 1-sample t-test on them.

```
pain %>% mutate(diff = druga - drugb) -> pain
pain %>% slice(1:5)
```

```
# A tibble: 5 x 4
  subject druga drugb   diff
  <dbl> <dbl> <dbl> <dbl>
1       1     2     3.5 -1.5
2       2     3.6     5.7 -2.1
3       3     2.6     2.9 -0.300
4       4     2.6     2.4  0.200
5       5     7.3     9.9 -2.6
```



## t-test on the differences

- then throw them into `t.test`, testing that the mean is zero, with same result as before:

```
with(pain, t.test(diff, mu = 0))
```

### One Sample t-test

```
data:  diff
t = -2.1677, df = 11, p-value = 0.05299
alternative hypothesis: true mean is not equal to 0
95 percent confidence interval:
 -4.29941513  0.03274847
sample estimates:
mean of x
-2.133333
```

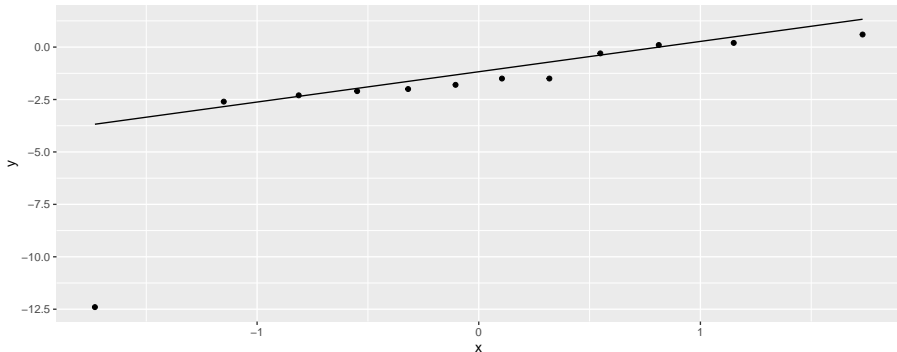
- Same P-value (0.053) and conclusion.

# Assessing normality

- 1-sample and 2-sample t-tests assume (each) group normally distributed.
- Matched pairs analyses assume (theoretically) that differences normally distributed.
- How to assess normality? A normal quantile plot.

## The normal quantile plot (of differences)

```
ggplot(pain,aes(sample=diff))+stat_qq()+stat_qq_line()
```



- Points should follow the straight line. Bottom left one way off, so normality questionable here: outlier.

## What to do instead?

- Matched pairs *t*-test based on one sample of differences
- the differences not normal (enough)
- so do *sign test* on differences, null median 0:

```
sign_test(pain, diff, 0)
```

```
$above_below
```

```
below above
```

```
9      3
```

```
$p_values
```

```
alternative    p_value
```

```
1         lower 0.07299805
```

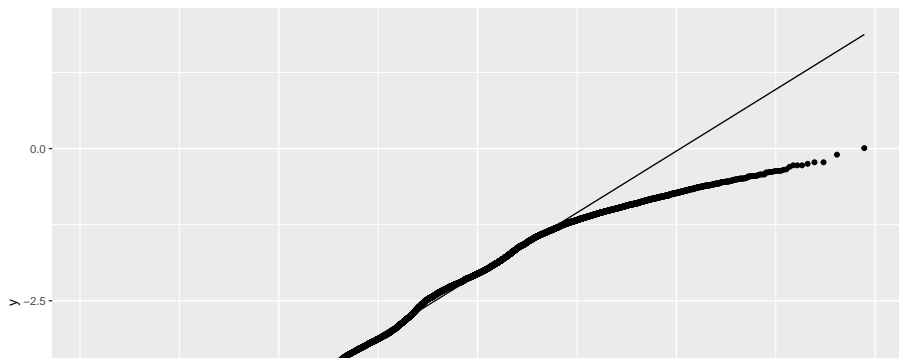
```
2         upper 0.98071289
```

```
3    two-sided 0.14599609
```

## Did we need to worry about that outlier?

Bootstrap sampling distribution of sample mean differences:

```
tibble(sim = 1:10000) %>%  
  rowwise() %>%  
  mutate(my_sample = list(sample(pain$diff, replace = TRUE)))  
  mutate(my_mean = mean(my_sample)) %>%  
  ggplot(aes(sample = my_mean)) + stat_qq() + stat_qq_line()
```



## Comments

- no evidence of any difference between drugs (P-value 0.1460)
- in  $t$ -test, the low outlier difference pulled mean difference downward and made it look more negative than it should have been
- therefore, there really isn't any difference between the drugs.