# Logistic Regression

# Logistic regression

- When response variable is measured/counted, regression can work well.
- But what if response is yes/no, lived/died, success/failure?
- Model probability of success.
- Probability must be between 0 and 1; need method that ensures this.
- Logistic regression does this. In R, is a generalized linear model with binomial "family":

```
glm(y ~ x, family="binomial")
```

• Begin with simplest case.

# **Packages**

```
library(MASS, exclude = "select")
library(tidyverse)
library(marginaleffects)
library(broom)
library(nnet)
# library(conflicted)
# conflict_prefer("select", "dplyr")
# conflict_prefer("filter", "dplyr")
# conflict_prefer("rename", "dplyr")
# conflict_prefer("summarize", "dplyr")
```

# The rats, part 1

• Rats given dose of some poison; either live or die:

dose status

- 0 lived
- 1 died
- 2 lived
- 3 lived
- 4 died
- 5 died

#### Read in:

```
my_url <- "http://ritsokiguess.site/datafiles/rat.txt"
rats <- read_delim(my_url, " ")
rats</pre>
```

## This doesn't work

```
status.0 <- glm(status ~ dose, family = "binomial", data = ra</pre>
```

```
Error in eval(family$initialize): y values must be 0 <= y <= :
```

Values of response variable (here status) must be either:

- 1 = "success", 0 = "failure"
- a factor (not text) with two levels.

## Basic logistic regression

• So, make response into a factor first:

```
rats2 <- rats %>% mutate(status = factor(status))
rats2
```

• then fit model:

status.1 <- glm(status ~ dose, family = "binomial", data = rate</pre>

## Output

#### summary(status.1)

```
Call:
glm(formula = status ~ dose, family = "binomial", data = rats:
```

## Coefficients:

```
Estimate Std. Error z value Pr(>|z|)
(Intercept) 1.6841 1.7979 0.937 0.349
dose -0.6736 0.6140 -1.097 0.273
```

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 8.3178 on 5 degrees of freedom Residual deviance: 6.7728 on 4 degrees of freedom

AIC: 10.773

# Interpreting the output

- ullet Like (multiple) regression, get tests of significance of individual x's
- Here not significant (only 6 observations).
- "Slope" for dose is negative, meaning that as dose increases, probability of event modelled (survival) decreases.

# Output part 2: predicted survival probs

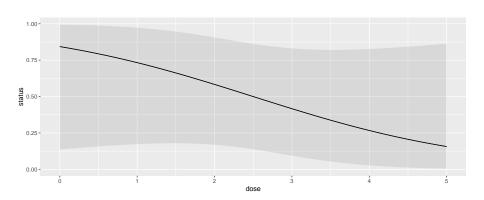
```
cbind(predictions(status.1)) %>%
  select(dose, estimate, conf.low, conf.high)

dose estimate conf.low conf.high
1     0 0.8434490 0.137095792 0.9945564
```

```
2 1 0.7331122 0.173186479 0.9729896
3 2 0.5834187 0.168847561 0.9061463
4 3 0.4165813 0.093853682 0.8311524
5 4 0.2668878 0.027010413 0.8268135
6 5 0.1565510 0.005443589 0.8629042
```

# On a graph

## plot\_predictions(status.1, condition = "dose")



## The rats, more

- More realistic: more rats at each dose (say 10).
- Listing each rat on one line makes a big data file.
- Use format below: dose, number of survivals, number of deaths.

```
dose lived died

0 10 0

1 7 3

2 6 4

3 4 6

4 2 8

5 1 9
```

- 6 lines of data correspond to 60 actual rats.
- Saved in rat2.txt.

#### These data

```
my_url <- "http://ritsokiguess.site/datafiles/rat2.txt"
rat2 <- read_delim(my_url, " ")
rat2</pre>
```

```
# A tibble: 6 x 3
dose lived died
<dbl> <dbl> <dbl> 1
0 10 0
1 7 3
3 2 6 4
4 3 4 6
5 4 2 8
6 5 1
```

## Response matrix:

- Each row contains *multiple* observations.
- Create *two-column* response with cbind:
  - #survivals in first column,
  - ▶ #deaths in second.

```
with(rat2, cbind(lived, died))
```

```
lived died
[1,] 10 0
[2,] 7 3
[3,] 6 4
[4,] 4 6
[5,] 2 8
[6,] 1 9
```

# Fit logistic regression

• constructing the response in the glm:

```
rat2.1 <- glm(cbind(lived, died) ~ dose, family = "binomial",</pre>
```

## Output

Significant effect of dose now:

```
summary(rat2.1)
```

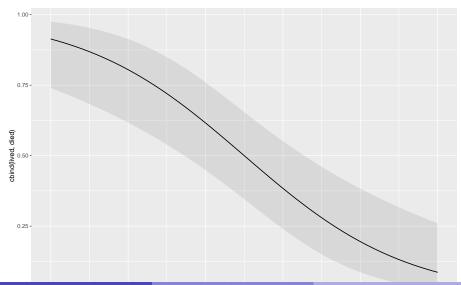
```
Call:
glm(formula = cbind(lived, died) ~ dose, family = "binomial",
   data = rat2
Coefficients:
           Estimate Std. Error z value Pr(>|z|)
(Intercept) 2.3619 0.6719 3.515 0.000439 ***
dose -0.9448 0.2351 -4.018 5.87e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '
(Dispersion parameter for binomial family taken to be 1)
```

# Predicted survival probs

```
new <- datagrid(model = rat2.1, dose = 0:5)
cbind(predictions(rat2.1, newdata = new)) %>%
select(estimate, dose, conf.low, conf.high)
```

# On a picture

plot\_predictions(rat2.1, condition = "dose")



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### Comments

- Significant effect of dose.
- Effect of larger dose is to decrease survival probability ("slope" negative; also see in decreasing predictions.)
- Confidence intervals around prediction narrower (more data).

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# Multiple logistic regression

- ullet With more than one x, works much like multiple regression.
- Example: study of patients with blood poisoning severe enough to warrant surgery. Relate survival to other potential risk factors.
- Variables, 1=present, 0=absent:
  - survival (death from sepsis=1), response
  - shock
  - malnutrition
  - alcoholism
  - age (as numerical variable)
  - bowel infarction
- See what relates to death.

#### Read in data

```
my_url <-
   "http://ritsokiguess.site/datafiles/sepsis.txt"
sepsis <- read_delim(my_url, " ")
sepsis</pre>
```

# A tibble: 106 x 6							
	${\tt death}$	${\tt shock}$	${\tt malnut}$	${\tt alcohol}$	age	bowelinf	
	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	
1	0	0	0	0	56	0	
2	0	0	0	0	80	0	
3	0	0	0	0	61	0	
4	0	0	0	0	26	0	
5	0	0	0	0	53	0	
6	1	0	1	0	87	0	
7	0	0	0	0	21	0	
8	1	0	0	1	69	0	
9	0	0	0	0	57	0	

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# Make sure categoricals really are

```
sepsis %>%
mutate(across(-age, \(x) factor(x))) -> sepsis
```

# The data (some)

#### sepsis

```
A tibble: 106 x 6
   death shock malnut alcohol
                                   age bowelinf
   <fct> <fct> <fct> <fct> <fct>
                                <dbl> <fct>
                                    56 0
                                    80 0
 3 0
                0
                                    61 0
                0
                                    26 0
                                    53 0
                0
                                    87 0
                0
                                    21 0
                                    69 0
                0
                                    57 0
10 0
                                    76 0
 i 96 more rows
```

Logistic Regression

#### Fit model

```
sepsis.1 <- glm(death ~ shock + malnut + alcohol + age +
  bowelinf,
family = "binomial",
data = sepsis
)</pre>
```

## Output part 1

Call:

```
summary(sepsis.1)
```

Signif. codes:

```
glm(formula = death ~ shock + malnut + alcohol + age + boweling
   family = "binomial", data = sepsis)
Coefficients:
         Estimate Std. Error z value Pr(>|z|)
(Intercept) -9.75391 2.54170 -3.838 0.000124 ***
shock1 3.67387 1.16481 3.154 0.001610 **
malnut1 1.21658 0.72822 1.671 0.094798 .
alcohol1 3.35488 0.98210 3.416 0.000635 ***
    age
bowelinf1 2.79759 1.16397 2.403 0.016240 *
```

0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' '

## Removing malnut

```
sepsis.2 <- update(sepsis.1, . ~ . - malnut)
summary(sepsis.2)</pre>
```

```
Call:
```

```
glm(formula = death ~ shock + alcohol + age + bowelinf, family
    data = sepsis)
```

#### Coefficients:

```
Estimate Std. Error z value Pr(>|z|)

(Intercept) -8.89459 2.31689 -3.839 0.000124 ***
shock1 3.70119 1.10353 3.354 0.000797 ***
alcohol1 3.18590 0.91725 3.473 0.000514 ***
age 0.08983 0.02922 3.075 0.002106 **
bowelinf1 2.38647 1.07227 2.226 0.026039 *
---
```

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' :

### Comments

- Most of the original x's helped predict death. Only malnut seemed not to add anything.
- Removed malnut and tried again.
- Everything remaining is significant (though bowelinf actually became less significant).
- All coefficients are *positive*, so having any of the risk factors (or being older) *increases* risk of death.

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## Predictions from model without "malnut"

• A few (rows of original dataframe) chosen "at random":

```
sepsis %>% slice(c(4, 1, 2, 11, 32)) -> new
new
```

```
# A tibble: 5 x 6

death shock malnut alcohol age bowelinf
<fct> <fct> <fct> <fct> <fct> <fct> <fct> <fct> <fct> <dbl> <fct> 

1 0 0 0 0 26 0

2 0 0 0 0 56 0

3 0 0 0 0 80 0

4 1 0 0 1 66 1

5 1 0 0 1 49 0
```

```
cbind(predictions(sepsis.2, newdata = new)) %>%
  select(estimate, conf.low, conf.high, shock:bowelinf)
```

estimate conf.low conf.high shock malnut alcohol age

#### Comments

- Survival chances pretty good if no risk factors, though decreasing with age.
- Having more than one risk factor reduces survival chances dramatically.
- Usually good job of predicting survival; sometimes death predicted to survive.

# Another way to assess effects

of age:

```
new <- datagrid(model = sepsis.2, age = seq(30, 70, 10))
new</pre>
```

```
      shock alcohol bowelinf age rowid

      1
      0
      0
      0
      30
      1

      2
      0
      0
      0
      40
      2

      3
      0
      0
      0
      50
      3

      4
      0
      0
      0
      60
      4

      5
      0
      0
      0
      70
      5
```

# Assessing age effect

```
cbind(predictions(sepsis.2, newdata = new)) %>%
  select(estimate, shock:age)
```

# Assessing shock effect

```
new <- datagrid(shock = c(0, 1), model = sepsis.2)
new</pre>
```

```
      alcohol
      age bowelinf shock rowid

      1
      0 51.28302
      0 0 1

      2
      0 51.28302
      0 1 2
```

```
cbind(predictions(sepsis.2, newdata = new)) %>%
  select(estimate, death:shock)
```

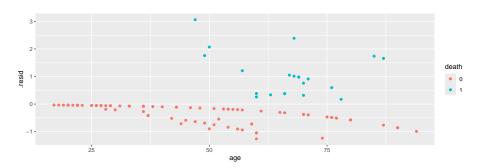
```
estimate death shock
1 0.01354973 0 0
2 0.35742607 0 1
```

# Assessing proportionality of odds for age

- An assumption we made is that log-odds of survival depends linearly on age.
- Hard to get your head around, but basic idea is that survival chances go continuously up (or down) with age, instead of (for example) going up and then down.
- In this case, seems reasonable, but should check:

# Residuals vs. age

```
sepsis.2 %>% augment(sepsis) %>%
ggplot(aes(x = age, y = .resid, colour = death)) +
geom_point()
```



### Comments

- No apparent problems overall.
- Confusing "line" across: no risk factors, survived.

## Probability and odds

For probability p, odds is p/(1-p):

Prob	Odds	Log-odds	Words
0.5	$0.5 \ / \ 0.5 = 1.00$	0.00	even money
0.1	0.1 / 0.9 = 0.11	-2.20	9 to 1
0.4	0.4 / 0.6 = 0.67	-0.41	1.5 to 1
8.0	0.8 / 0.2 = 4.00	1.39	4 to 1 on

- Gamblers use odds: if you win at 9 to 1 odds, get original stake back plus 9 times the stake.
- Probability has to be between 0 and 1
- Odds between 0 and infinity
- Log-odds can be anything: any log-odds corresponds to valid probability.
- Thus, predict *log-odds of probability* from explanatory variable(s), rather than probability itself.

### Odds ratio

- Suppose 90 of 100 men drank wine last week, but only 20 of 100 women.
- Prob of man drinking wine 90/100 = 0.9, woman 20/100 = 0.2.
- Odds of man drinking wine 0.9/0.1 = 9, woman 0.2/0.8 = 0.25.
- Ratio of odds is 9/0.25 = 36.
- Way of quantifying difference between men and women: "odds of drinking wine 36 times larger for males than females".

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# Sepsis data again

• Recall prediction of probability of death from risk factors:

#### sepsis

# A tibble: 106 x 6									
	death	${\tt shock}$	${\tt malnut}$	${\tt alcohol}$	age	bowelinf			
	<fct></fct>	<fct></fct>	<fct></fct>	<fct></fct>	<dbl></dbl>	<fct></fct>			
1	0	0	0	0	56	0			
2	0	0	0	0	80	0			
3	0	0	0	0	61	0			
4	0	0	0	0	26	0			
5	0	0	0	0	53	0			
6	1	0	1	0	87	0			
7	0	0	0	0	21	0			
8	1	0	0	1	69	0			
9	0	0	0	0	57	0			
10	0	0	1	0	76	0			
# i	. 96 mc	re ro	/S						

## Multiplying the odds

Can interpret slopes by taking "exp" of them. We ignore intercept.

```
sepsis.2.tidy %>%
  mutate(exp_coeff=exp(estimate)) %>%
  select(term, exp_coeff)
```

```
# A tibble: 5 x 2
term exp_coeff
<chr> <chr> 1 (Intercept) 0.000137
shock1 40.5
alcohol1 24.2
age 1.09
bowelinf1 10.9
```

## Interpretation

- These say "how much do you *multiply* odds of death by for increase of 1 in corresponding risk factor?" Or, what is odds ratio for that factor being 1 (present) vs. 0 (absent)?
- Eg. being alcoholic vs. not increases odds of death by 24 times
- One year older multiplies odds by about 1.1 times. Over 40 years, about  $1.09^{40}=31$  times.

### Odds ratio and relative risk

- Relative risk is ratio of probabilities.
- Above: 90 of 100 men (0.9) drank wine, 20 of 100 women (0.2).
- Relative risk 0.9/0.2=4.5. (odds ratio was 36).
- When probabilities small, relative risk and odds ratio similar.
- Eg. prob of man having disease 0.02, woman 0.01.
- Relative risk 0.02/0.01 = 2.

### Odds ratio vs. relative risk

Odds for men and for women:

```
(od1 <- 0.02 / 0.98) # men
```

[1] 0.02040816

```
(od2 <- 0.01 / 0.99) # women
```

[1] 0.01010101

Odds ratio

```
od1 / od2
```

[1] 2.020408

• Very close to relative risk of 2.

# More than 2 response categories

- With 2 response categories, model the probability of one, and prob of other is one minus that. So doesn't matter which category you model.
- With more than 2 categories, have to think more carefully about the categories: are they
- ordered: you can put them in a natural order (like low, medium, high)
- nominal: ordering the categories doesn't make sense (like red, green, blue).
- R handles both kinds of response; learn how.

# Ordinal response: the miners

- Model probability of being in given category or lower.
- Example: coal-miners often suffer disease pneumoconiosis. Likelihood of disease believed to be greater among miners who have worked longer.
- Severity of disease measured on categorical scale: none, moderate, severe.

## Miners data

• Data are frequencies:

Exposure	None	Moderate	Severe
5.8	98	0	0
15.0	51	2	1
21.5	34	6	3
27.5	35	5	8
33.5	32	10	9
39.5	23	7	8
46.0	12	6	10
51.5	4	2	5

## Reading the data

Data in aligned columns with more than one space between, so:

```
my_url <- "http://ritsokiguess.site/datafiles/miners-tab.txt"
freqs <- read_table(my_url)</pre>
```

### The data

### freqs

```
# A tibble: 8 x 4
  Exposure None Moderate Severe
     <dbl> <dbl>
                    <dbl> <dbl>
       5.8
              98
                               0
      15
              51
3
      21.5
              34
                        6
                               3
      27.5 35
                               8
5
      33.5 32
                       10
6
              23
                               8
      39.5
      46
              12
                        6
                              10
8
      51.5
               4
                               5
```

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# **Tidying**

```
freqs %>%
  pivot_longer(-Exposure, names_to = "Severity", values_to =
  mutate(Severity = fct_inorder(Severity)) -> miners
```

### Result

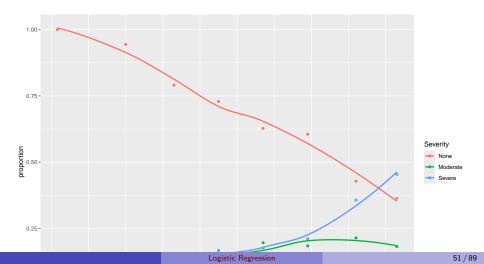
#### miners

```
A tibble: 24 \times 3
   Exposure Severity
                      Freq
      <dbl> <fct>
                     <dbl>
        5.8 None
                         98
        5.8 Moderate
 3
        5.8 Severe
       15
            None
                         51
 5
       15 Moderate
 6
       15 Severe
       21.5 None
                         34
8
       21.5 Moderate
                          6
 9
       21.5 Severe
10
       27.5 None
                         35
# i 14 more rows
```

# Plot proportions against exposure 1/2

```
miners %>%
 group_by(Exposure) %>%
 mutate(proportion = Freq / sum(Freq)) -> prop
prop
 A tibble: 24 x 4
 Groups: Exposure [8]
  Exposure Severity Freq proportion
     <dbl> <fct> <dbl>
                             <dbl>
       5.8 None
                      98
       5.8 Moderate
       5.8 Severe
    15
          None
                     51 0.944
 5
      15 Moderate 2
                            0.0370
 6
      15 Severe
                         0.0185
      21.5 None
                     34
                            0.791
 8
      21.5 Moderate
                            0.140
```

# Plot proportions against exposure 2/2



# Reminder of data setup

#### miners

```
A tibble: 24 \times 3
   Exposure Severity Freq
      <dbl> <fct>
                     <dbl>
        5.8 None
                         98
        5.8 Moderate
 3
        5.8 Severe
       15
           None
                         51
 5
       15 Moderate
       15
            Severe
       21.5 None
                         34
8
       21.5 Moderate
                          6
 9
       21.5 Severe
                          3
10
       27.5 None
                         35
# i 14 more rows
```

# Fitting ordered logistic model

Use function polr from package MASS. Like glm.

```
sev.1 <- polr(Severity ~ Exposure,
  weights = Freq,
  data = miners
)</pre>
```

# Output: not very illuminating

```
sev.1 <- polr(Severity ~ Exposure,
  weights = Freq,
  data = miners,
)</pre>
```

```
summary(sev.1)
```

```
Call:
```

```
polr(formula = Severity ~ Exposure, data = miners, weights = l
```

#### Coefficients:

Value Std. Error t value Exposure 0.0959 0.01194 8.034

#### Intercepts:

Value Std. Error t value None | Moderate 3.9558 0.4097 9.6558

## Does exposure have an effect?

Fit model without Exposure, and compare using anova. Note 1 for model with just intercept:

```
sev.0 <- polr(Severity ~ 1, weights = Freq, data = miners)
anova(sev.0, sev.1)</pre>
```

Likelihood ratio tests of ordinal regression models

```
Response: Severity

Model Resid. df Resid. Dev Test Df LR stat.

1 1 369 505.1621

2 Exposure 368 416.9188 1 vs 2 1 88.24324

Pr(Chi)

1
2 0
```

Exposure definitely has effect on severity of disease.

## Another way

• What (if anything) can we drop from model with exposure?

```
drop1(sev.1, test = "Chisq")
Single term deletions
Model:
Severity ~ Exposure
        Df AIC LRT Pr(>Chi)
<none> 422.92
Exposure 1 509.16 88.243 < 2.2e-16 ***
Signif. codes:
0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Nothing. Exposure definitely has effect.

# Predicted probabilities 1/2

```
freqs %>% select(Exposure) -> new
new
```

```
# A tibble: 8 x 1
  Exposure
     <dbl>
       5.8
      15
3
      21.5
4
      27.5
5
      33.5
6
      39.5
      46
8
      51.5
```

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# Predicted probabilities 2/2

```
cbind(predictions(sev.1, newdata = new)) %>%
  select(group, estimate, Exposure) %>%
  pivot_wider(names_from = group, values_from = estimate)
```

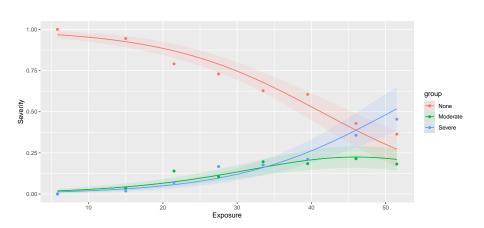
```
# A tibble: 8 x 4
 Exposure None Moderate Severe
    <dbl> <dbl> <dbl> <dbl> <
      5.8 0.968 0.0191 0.0132
2
     15 0.925 0.0433 0.0314
3
     21.5 0.869 0.0739 0.0569
4
     27.5 0.789 0.114 0.0969
5
     33.5 0.678 0.162 0.160
6
     39.5 0.542 0.205 0.253
7
     46 0.388 0.224 0.388
     51.5 0.272
                 0.210 0.517
8
```

# Plot of predicted probabilities

```
plot_predictions(model = sev.1, condition = c("Exposure", "grogeom_point(data = prop, aes(x = Exposure, y = proportion, condition = c("Exposure", "grogeom_point(data = prop, aes(x = Exposure, y = proportion, condition = c("Exposure", "grogeom_point(data = prop, aes(x = Exposure, y = proportion, condition = c("Exposure", "grogeom_point(data = prop, aes(x = Exposure, y = proportion, condition = c("Exposure", "grogeom_point(data = prop, aes(x = Exposure, y = proportion, condition = c("Exposure", "grogeom_point(data = prop, aes(x = Exposure, y = proportion, condition = c("Exposure", "grogeom_point(data = prop, aes(x = Exposure, y = proportion, condition = c("Exposure, y = proportion, y = proportion, y = proportion, condition = c("Exposure, y = proportion, y = prop
```

# The graph

#### ggg



### Comments

- Model appears to match data well enough.
- As exposure goes up, prob of None goes down, Severe goes up (sharply for high exposure).
- So more exposure means worse disease.

## Unordered responses

- With unordered (nominal) responses, can use generalized logit.
- Example: 735 people, record age and sex (male 0, female 1), which of 3 brands of some product preferred.
- Data in mlogit.csv separated by commas (so read\_csv will work):

```
my_url <- "http://ritsokiguess.site/datafiles/mlogit.csv"
brandpref <- read_csv(my_url)</pre>
```

# The data (some)

### brandpref

```
A tibble: 735 x 3
   brand
            sex
                   age
   <dbl> <dbl> <dbl>
                    24
                    26
                    26
                    27
 5
                    27
 6
                    27
                    27
8
                    27
 9
                    27
10
                    27
   725 more rows
```

## Bashing into shape

sex and brand not meaningful as numbers, so turn into factors:

#### brandpref

```
# A tibble: 735 x 3
brand sex age
<fct> <fct> <fct> <dbl>
1 1 male 24
2 1 male 26
3 1 male 26
4 1 female 27
5 1 female 27
```

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## Fitting model

• We use multinom from package nnet. Works like polr.

```
library(nnet)
# levels(brandpref$sex)
brands.1 <- multinom(brand ~ age + sex, data = brandpref)</pre>
# weights: 12 (6 variable)
initial value 807.480032
iter 10 value 702.990572
final value 702.970704
converged
summary(brands.1)
```

#### Call:

multinom(formula = brand ~ age + sex, data = brandpref)

## Can we drop anything?

• Unfortunately drop1 seems not to work:

```
drop1(brands.1, test = "Chisq", trace = 0)
```

trying - age

Error in if (trace) {: argument is not interpretable as logical

 So, fall back on fitting model without what you want to test, and comparing using anova.

# Do age/sex help predict brand? 1/3

Fit models without each of age and sex:

```
brands.2 <- multinom(brand ~ age, data = brandpref)

# weights: 9 (4 variable)
initial value 807.480032
iter 10 value 706.796323
iter 10 value 706.796322
final value 706.796322
converged</pre>
```

```
brands.3 <- multinom(brand ~ sex, data = brandpref)</pre>
```

```
# weights: 9 (4 variable)
initial value 807.480032
final value 791.861266
converged
```

# Do age/sex help predict brand? 2/3

```
anova(brands.2, brands.1)
```

Likelihood ratio tests of Multinomial Models

```
anova(brands.3, brands.1)
```

Likelihood ratio tests of Multinomial Models

```
Response: brand
```

# Do age/sex help predict brand? 3/3

- age definitely significant (second anova)
- sex significant also (first anova), though P-value less dramatic
- Keep both.
- Expect to see a large effect of age, and a smaller one of sex.

## Another way to build model

• Start from model with everything and run step:

```
step(brands.1)
```

```
Start: ATC=1417.94
brand ~ age + sex
trying - age
# weights: 9 (4 variable)
initial value 807.480032
final value 791.861266
converged
trying - sex
# weights: 9 (4 variable)
initial value 807.480032
iter 10 value 706.796323
iter 10 value 706.796322
final value 706.796322
```

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# Making predictions

Find age 5-number summary, and the two sexes:

#### summary(brandpref)

```
brand sex age
1:207 female:466 Min. :24.0
2:307 male :269 1st Qu.:32.0
3:221 Median :32.0
Mean :32.9
3rd Qu.:34.0
Max. :38.0
```

Space the ages out a bit for prediction (see over).

### **Combinations**

```
new <- datagrid(age = seq(24, 40, 4), # cover the entire range
             sex = c("female", "male"), model = brands.1)
new
  age sex rowid
   24 female
2 24 male 2
3 28 female 3
4
  28 male 4
5 32 female 5
6 32 male 6
7 36 female 7
8 36 male
           8
9 40 female
               9
10
   40 male
              10
```

# new <- datagrid(age = seq(24, 40, 4), # cover the entire ran # model = brands.1)

### The predictions

```
cbind(predictions(brands.1, newdata = new)) %>%
  select(group, estimate, age, sex) %>%
  pivot_wider(names_from = group, values_from = estimate)
```

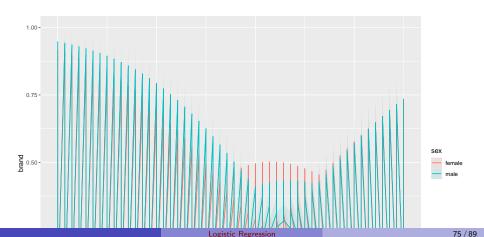
```
# A tibble: 10 \times 5
    age sex
  <dbl> <fct> <dbl> <dbl> <dbl>
                               <dbl>
     24 female 0.915 0.0819 0.00279
 1
     24 male 0.948 0.0502 0.00181
     28 female 0.696 0.271 0.0329
     28 male 0.793 0.183 0.0236
 5
     32 female 0.291 0.495 0.214
 6
     32 male 0.405 0.408 0.187
     36 female 0.0503 0.374 0.576
 8
     36 male 0.0795 0.350 0.571
 9
     40 female 0.00473 0.153 0.842
10
     40 male 0.00759 0.146 0.847
```

#### Comments

- Young males prefer brand 1, but older males prefer brand 3.
- Females similar, but like brand 1 less and brand 2 more.
- A clear brand effect, but the sex effect is less clear.

### Making a plot

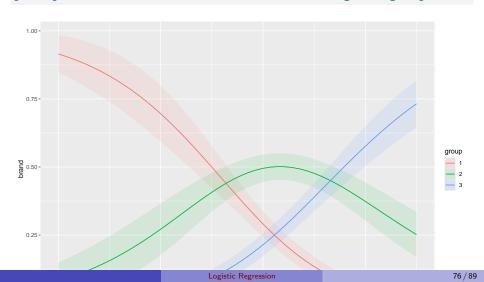
• I thought plot\_predictions doesn't work as we want, but I was (sort of) wrong about that:



## Making it go

• We have to include group in the condition:

```
plot_predictions(brands.1, condition = c("age", "group"))
```



#### Comments

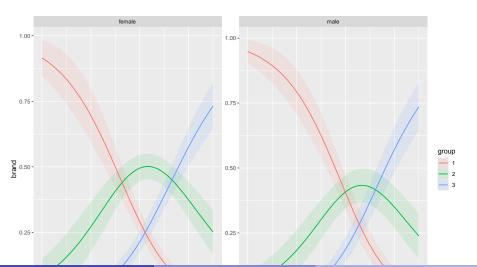
- This picks the most common sex in the data (females).
- See younger females prefer brand 1, older ones preferring brand 3.

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#### For each sex

If we add the other variable to the end, we get facets for sex:

plot\_predictions(brands.1, condition = c("age", "group", "sex")



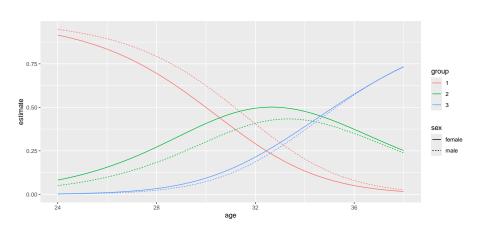
Logistic Regression

### A better graph

- but the male-female difference was significant. How?
- don't actually plot the graph, then plot the right things:

# The graph

g



## Digesting the plot

- Brand vs. age: younger people (of both genders) prefer brand 1, but older people (of both genders) prefer brand 3. (Explains significant age effect.)
- Brand vs. sex: females (solid) like brand 1 less than males (dashed), like brand 2 more (for all ages).
- Not much brand difference between genders (solid and dashed lines of same colours close), but enough to be significant.
- Model didn't include interaction, so modelled effect of gender on brand same for each age, modelled effect of age same for each gender. (See also later.)

#### Alternative data format

Summarize all people of same brand preference, same sex, same age on one line of data file with frequency on end:

#### brandpref

```
A tibble: 735 \times 3
   brand sex
                   age
   <fct> <fct> <dbl>
1 1
         male
                    24
2 1
         male
                    26
                    26
3 1
         male
         female 27
5 1
         female
                 27
6.3
         female
                    27
                    27
         male
8 1
         male
                    27
         female
                    27
9
                    27
10 1
         male
```

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## Getting alternative data format

```
brandpref %>%
  group_by(age, sex, brand) %>%
  summarize(Freq = n()) %>%
  ungroup() -> b
b
```

```
# A tibble: 65 x 4
    age sex brand Freq
  <dbl> <fct> <fct> <int>
     24 male 1
2 26 male 1
3
  27 female 1
   27 female 3
5
  27 male 1
6
     28 female 1
                       6
     28 female 2
8
     28 female 3
```

## Fitting models, almost the same

- Just have to remember weights to incorporate frequencies.
- Otherwise multinom assumes you have just 1 obs on each line!
- Again turn (numerical) sex and brand into factors:

```
b %>%
  mutate(sex = factor(sex)) %>%
  mutate(brand = factor(brand)) -> bf
b.1 <- multinom(brand ~ age + sex, data = bf, weights = Freq)
b.2 <- multinom(brand ~ age, data = bf, weights = Freq)</pre>
```

#### P-value for sex identical

```
anova(b.2, b.1)
```

Likelihood ratio tests of Multinomial Models

```
Response: brand

Model Resid. df Resid. Dev Test Df LR stat.

1 age 126 1413.593

2 age + sex 124 1405.941 1 vs 2 2 7.651236

Pr(Chi)

1
2 0.02180496
```

Same P-value as before, so we haven't changed anything important.

# Trying interaction between age and gender

```
brands.4 <- update(brands.1, . ~ . + age:sex)</pre>
```

```
# weights: 15 (8 variable)
initial value 807.480032
iter 10 value 703.191146
iter 20 value 702.572260
iter 30 value 702.570900
iter 30 value 702.570893
iter 30 value 702.570893
converged
```

```
anova(brands.1, brands.4)
```

Likelihood ratio tests of Multinomial Models

Response: brand

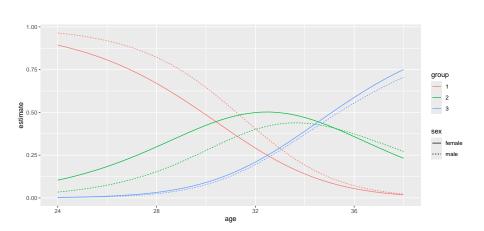
Logistic Regression

'^a+

## Make graph again

# Not much difference in the graph

### g4



# Compare model without interaction

g

