The Rohwer data

February 22, 2011

The data:

```
group SES SAT PPVT Raven
                            n
                               s ns na ss
           49
                         8
                                  6 12 16
       Lo
                 48
                            1
                               2
    1
    1
       Lo
           47
                 76
                       13
                            5 14 14 30 27
    1
       Lo
           11
                 40
                       13
                            0 10 21 16 16
    1
       Lo
                 52
                         9
                            0
                               2 5 17
                            2
                               7 11 26 17
       Lo
                 63
    1
           69
                        15
    1
       Lo
           35
                 82
                       14
                            2 15 21 34 25
                       21
    1
       Lo
            6
                 71
                            0
                              1 20 23 18
    1
       Lo
            8
                 68
                        8
                            0
                               0 10 19 14
       Lo
           49
                 74
                            0
                               0
                                  7 16 13
    1
                       11
            8
                              2 21 26 25
    1
       Lo
                 70
                       15
                            3
                            8 16 15 35 24
    1
       Lo
           47
                 70
                       15
                            5 4 7 15 14
    1
       Lo
            6
                 61
                       11
    1
       Lo
           14
                 54
                       12
                            1 12 13 27 21
    1
       Lo
           30
                 55
                       13
                            2 1 12 20 17
                 54
                            3 12 20 26 22
       Lo
             4
                       10
       Lo
           24
                 40
                       14
                            0
                               2
                                  5 14
    1
                            7 12 21 35 27
    1
           19
                 66
                       13
           45
                            0
                               6
                                  6 14 16
    1
       Lo
                 54
                       10
    1
       Lo
           22
                 64
                       14 12
                               8 19 27 26
    1
       Lo
           16
                 47
                       16
                            3
                               9 15 18 10
    1
       Lo
           32
                 48
                       16
                            0
                               7
                                  9 14 18
       Lo
           37
                 52
                       14
                            4
                               6 20 26 26
    1
       Lo
           47
                 74
                       19
                            4
                               9 14 23 23
    1
    1
       Lo
            5
                 57
                       12
                            0
                               2
                                  4 11
            6
                       10
                            0
                               1 16 15 17
    1
       Lo
                 57
       Lo
           60
                 80
                            3
                              8 18 28 21
    1
    1
       Lo
           58
                 78
                       13
                            1 18 19 34 23
                            2 11
                                  9 23 11
    1
       Lo
            6
                 70
                       16
       Lo
           16
                       14
                            0 10
                                  7 12 8
    1
                 47
    1
       Lo
           45
                 94
                       19
                            8 10 28 32 32
    1
       Lo
            9
                 63
                       11
                            2 12 5 25 14
       Lo
                 76
                       16
                           7 11 18 29 21
           69
```

```
2 5 10 23 24
  Lo
       35
             59
                   11
1
   Lo
       19
             55
                    8
                       0
                          1 14 19 12
   Lo
       58
             74
                   14
                           0 10 18 18
                           4 23 31 26
1
   Lo
       58
             71
                   17
                       6
1
   Lo
       79
             54
                   14
                       0
                           6
                              6 15 14
2
   Ηi
       24
             68
                   15
                       0 10
                             8 21 22
2
   Ηi
        8
             82
                       7
                           3 21 28 21
                   11
2
                       7
             82
                           9 17 31 30
   Ηi
       88
                   13
2
   Ηi
       82
             91
                   18
                       6 11 16 27 25
2
   Ηi
       90
                   13 20 7 21 28 16
             82
2
   Ηi
       77
            100
                   15
                       4 11 18 32 29
2
            100
                       6
                          7 17 26 23
   Ηi
       58
                   13
2
   Ηi
       14
             96
                   12
                       5
                          2 11 22 23
2
                       3 5 14 24 20
   Ηi
        1
             63
                   10
2
                   18 16 12 16 27 30
   Ηi
       98
             91
2
   Ηi
                   10
                       5 3 17 25 24
        8
             87
2
                       2 11 10 26 22
   Ηi
       88
            105
                   21
2
   Ηi
                          4 14 25 19
        4
             87
                   14
                       1
2
   Ηi
       14
             76
                   16 11
                           5 18 27 22
2
                             3 16 11
   Ηi
       38
             66
                   14
                       0
                           0
2
   Ηi
        4
             74
                   15
                       5
                          8 11 12 15
2
   Ηi
       64
             68
                   13
                       1
                           6 10 28 23
2
   Ηi
             98
                   16
                           9 12 30 18
       88
                       1
2
   Ηi
       14
             63
                   15
                       0 13 13 19 16
2
                       4 6 14 27 19
   Ηi
       99
                   16
             94
2
   Ηi
       50
             82
                   18
                       4
                          5 16 21 24
2
   Ηi
       36
                   15
                           6 15 23 28
             89
                       1
2
   Hi
       88
             80
                   19
                       5
                           8 14 25 24
2
   Ηi
       14
             61
                   11
                       4
                           5 11 16 22
2
   Ηi
       24
                   20
                       5
                           7 17 26 15
            102
2
                          4 8 16 14
   Ηi
       24
             71
                   12
                       0
2
   Ηi
       24
            102
                   16
                       4 17 21 27 31
2
   Hi
       50
             96
                       5 8 20 28 26
                   13
2
  Ηi
        8
             55
                   16
                       4
                          7 19 20 13
2
   Ηi
             96
                          7 10 23 19
       98
                   18
                       4
2
   Ηi
       98
             74
                   15
                       2
                          6 14 25 17
2
   Ηi
       50
             78
                   19
                       5 10 18 27 26
```

The SAS code and output:

```
data rohwer;
   infile "Rohwer.dat" firstobs=2;
   input group SES $ SAT PPVT Raven n s ns na ss;
   if SES='Lo';
proc print;
```

```
model SAT PPVT Raven = n s ns na ss;
    mtest;
    n: mtest n;
    s: mtest s;
    ns: mtest ns;
    na: mtest na;
    ss: mtest ss;
proc reg;
    model SAT PPVT Raven = ns na;
    mtest;
    ns2: mtest ns;
    na2: mtest na;
proc reg;
    model SAT PPVT Raven = na;
    na3: mtest;
run;
                                 PPVT
Obs
       group
                 SES
                         SAT
                                          Raven
                                                     n
                                                            s
                                                                  ns
                                                                        na
                                                                               SS
                           49
                                  48
                                             8
                                                            2
  1
         1
                 Lo
                                                     1
                                                                   6
                                                                        12
                                                                               16
  2
                           47
                                  76
                                             13
                                                     5
                                                                               27
          1
                 Lo
                                                           14
                                                                  14
                                                                        30
  3
                                  40
                                            13
                                                     0
                                                           10
                                                                  21
                                                                        16
                                                                               16
         1
                 Lo
                           11
  4
         1
                 Lo
                           9
                                  52
                                             9
                                                     0
                                                            2
                                                                  5
                                                                        17
                                                                                8
  5
                           69
                                  63
                                            15
                                                     2
                                                            7
                                                                        26
                                                                               17
         1
                 Lo
                                                                  11
  6
         1
                 Lo
                           35
                                  82
                                            14
                                                     2
                                                           15
                                                                  21
                                                                        34
                                                                               25
  7
                           6
                                  71
                                            21
                                                     0
                                                                  20
                                                                        23
                                                                               18
         1
                 Lo
                                                            1
  8
         1
                 Lo
                           8
                                  68
                                             8
                                                     0
                                                            0
                                                                  10
                                                                        19
                                                                               14
  9
                           49
                                  74
                                            11
                                                     0
                                                            0
                                                                  7
                                                                        16
                                                                               13
         1
                 Lo
 10
         1
                 Lo
                           8
                                  70
                                            15
                                                     3
                                                            2
                                                                  21
                                                                        26
                                                                               25
                           47
                                  70
                                                                               24
                                            15
                                                           16
                                                                  15
                                                                        35
 11
         1
                 Lo
                                                     8
 12
         1
                 Lo
                           6
                                  61
                                            11
                                                     5
                                                            4
                                                                  7
                                                                        15
                                                                               14
                                                           12
                                                                        27
 13
         1
                           14
                                  54
                                            12
                                                     1
                                                                  13
                                                                               21
                 Lo
                           30
                                  55
                                            13
                                                     2
                                                                        20
 14
         1
                 Lo
                                                            1
                                                                  12
                                                                               17
 15
                 Lo
                           4
                                  54
                                            10
                                                     3
                                                           12
                                                                  20
                                                                        26
                                                                               22
         1
 16
                           24
                                  40
                                            14
                                                     0
                                                            2
                                                                  5
                                                                        14
                                                                                8
         1
                 Lo
 17
          1
                 Lo
                           19
                                  66
                                            13
                                                     7
                                                           12
                                                                  21
                                                                        35
                                                                               27
                                            10
 18
         1
                 Lo
                           45
                                  54
                                                     0
                                                            6
                                                                   6
                                                                        14
                                                                               16
 19
                           22
                                                            8
                                                                  19
                                                                        27
                                                                               26
```

proc reg;

Lo

Lo

Lo

22	1	Lo	37	52	14	4	6	20	26	26
23	1	Lo	47	74	19	4	9	14	23	23
24	1	Lo	5	57	12	0	2	4	11	8
25	1	Lo	6	57	10	0	1	16	15	17
26	1	Lo	60	80	11	3	8	18	28	21
27	1	Lo	58	78	13	1	18	19	34	23
28	1	Lo	6	70	16	2	11	9	23	11
29	1	Lo	16	47	14	0	10	7	12	8
30	1	Lo	45	94	19	8	10	28	32	32
31	1	Lo	9	63	11	2	12	5	25	14
32	1	Lo	69	76	16	7	11	18	29	21
33	1	Lo	35	59	11	2	5	10	23	24
34	1	Lo	19	55	8	0	1	14	19	12
35	1	Lo	58	74	14	1	0	10	18	18
36	1	Lo	58	71	17	6	4	23	31	26
37	1	Lo	79	54	14	0	6	6	15	14

The REG Procedure Model: MODEL1

Dependent Variable: SAT

Number of Observations Read 37

Number of Observations Used 37

Analysis of Variance

Source Model Error Corrected Total	DF 5 31 36	Sum of Squares 3653.77324 13930 17583	Mean Square 730.75465 449.33949	F Value 1.63	Pr > F 0.1824
Root MSE Dependent Mean Coeff Var	21.19763 31.27027 67.78844	R-Square Adj R-Sq	0.2078 0.0800		

Parameter Estimates

		raramouci	HB 01 ma 0CB		
		Parameter	Standard		
Variable	DF	Estimate	Error	t Value	Pr > t
Intercept	1	4.15106	13.79834	0.30	0.7655
n	1	-0.60887	1.67108	-0.36	0.7181
S	1	-0.05016	0.94151	-0.05	0.9579
ns	1	-1.73240	0.91046	-1.90	0.0664
na	1	0.49456	1.03690	0.48	0.6367
SS	1	2.24772	1.10096	2.04	0.0498

The REG Procedure Model: MODEL1

Dependent Variable: PPVT

Number of Observations Read 37 Number of Observations Used 37

Analysis of Variance

			Sum of	Mean		
Source		DF	Squares	Square	F Value	Pr > F
Model		5	2883.67590	576.73518	6.47	0.0003
Error		31	2764.75653	89.18569		
Corrected	Total	36	5648.43243			
Root MSE		9.44382	R-Square	0.5105		
Dependent	Mean	62.64865	Adj R-Sq	0.4316		
Coeff Var		15.07426				
		Paramet	er Estimates			
		Parameter	Standard			
Variable	DF	Estimate	Error	t Value	Pr > t	
Intercept	1	33.00577	6.14734	5.37	<.0001	
n	1	-0.08057	0.74449	-0.11	0.9145	
S	1	-0.72105	0.41945	-1.72	0.0956	
ns	1	-0.29830	0.40562	-0.74	0.4676	

0.46195

0.49049

3.18

0.66

0.0033

0.5138

The REG Procedure Model: MODEL1

na

SS

Dependent Variable: Raven
Number of Observations Read 37
Number of Observations Used 37

1.47042

0.32396

1

Analysis of Variance

		Sum of	Mean		
Source	DF	Squares	${ t Square}$	F Value	Pr > F
Model	5	76.52860	15.30572	1.77	0.1486
Error	31	268.28221	8.65426		
Corrected Total	36	344.81081			
Root MSE	2.94181	R-Square	0.2219		
Dependent Mean	13.24324	Adj R-Sq	0.0965		
Coeff Var	22.21369				

Parameter Estimates

		Parameter	Standard		
Variable	DF	Estimate	Error	t Value	Pr > t
Intercept	1	11.17338	1.91494	5.83	<.0001

n	1	0.21100	0.23191	0.91	0.3699
S	1	0.06457	0.13066	0.49	0.6247
ns	1	0.21358	0.12635	1.69	0.1010
na	1	-0.03732	0.14390	-0.26	0.7971
ss	1	-0.05214	0.15279	-0.34	0.7352

The REG Procedure
Model: MODEL1

Multivariate Test 1

Multivariate Statistics and F Approximations

	S=3	M=0.5	N=1	3.5			
Statistic		Value	F Val	ue Nur	n DF	Den DF	Pr > F
Wilks' Lambda	0.343	316907	2.	54	15	80.458	0.0039
Pillai's Trace	0.825	528864	2.	35	15	93	0.0066
Hotelling-Lawley Trace	1.448	375712	2.	72	15	49.769	0.0042
Roy's Greatest Root	1.055	511542	6.	54	5	31	0.0003

NOTE: F Statistic for Roy's Greatest Root is an upper bound.

The REG Procedure Model: MODEL1

Multivariate Test: n

Multivariate Statistics and Exact F Statistics
S=1 M=0.5 N=13.5

D 1 11 0.0	11 10.0			
Value	F Value	Num DF	Den DF	Pr > F
0.96164244	0.39	3	29	0.7642
0.03835756	0.39	3	29	0.7642
0.03988755	0.39	3	29	0.7642
0.03988755	0.39	3	29	0.7642
	Value 0.96164244 0.03835756 0.03988755	Value F Value 0.96164244 0.39 0.03835756 0.39 0.03988755 0.39	Value F Value Num DF 0.96164244 0.39 3 0.03835756 0.39 3 0.03988755 0.39 3	Value F Value Num DF Den DF 0.96164244 0.39 3 29 0.03835756 0.39 3 29 0.03988755 0.39 3 29

The REG Procedure Model: MODEL1

Multivariate Test: s

Multivariate Statistics and Exact F Statistics

	S=1	M=0.5	N=13.5			
Statistic		Value	F Value	Num DF	Den DF	Pr > F
Wilks' Lambda	0.88	8820667	1.22	3	29	0.3213
Pillai's Trace	0.11	179333	1.22	3	29	0.3213
Hotelling-Lawley Trace	0.12	2586410	1.22	3	29	0.3213
Roy's Greatest Root	0.12	2586410	1.22	3	29	0.3213

The REG Procedure Model: MODEL1

Multivariate Test: ns

Multivariate Statistics and Exact F Statistics

S=1 M=0.5 N=13.5

Statistic Value F Value Num DF Den DF Pr > F

Wilks' Lambda	0.77477885	2.81	3	29	0.0570
Pillai's Trace	0.22522115	2.81	3	29	0.0570
Hotelling-Lawley Trace	0.29069088	2.81	3	29	0.0570
Roy's Greatest Root	0.29069088	2.81	3	29	0.0570

The REG Procedure Model: MODEL1

Multivariate Test: na

Multivariate Statistics and Exact F Statistics

	S=1 $M=0.5$	N=13.5			
Statistic	Value	F Value	Num DF	Den DF	Pr > F
Wilks' Lambda	0.73254211	3.53	3	29	0.0271
Pillai's Trace	0.26745789	3.53	3	29	0.0271
Hotelling-Lawley Trace	0.36510923	3.53	3	29	0.0271
Roy's Greatest Root	0.36510923	3.53	3	29	0.0271

The REG Procedure Model: MODEL1

Multivariate Test: ss

Multivariate Statistics and Exact F Statistics

	S=1 M	=0.5 N=13.5			
Statistic	Val	ue F Value	Num DF	Den DF	Pr > F
Wilks' Lambda	0.861037	67 1.56	3	29	0.2203
Pillai's Trace	0.138962	33 1.56	3	29	0.2203
Hotelling-Lawley Trace	0.161389	37 1.56	3	29	0.2203
Roy's Greatest Root	0.161389	37 1.56	3	29	0.2203

The REG Procedure Model: MODEL1

Dependent Variable: SAT

Number of Observations Read 37 Number of Observations Used

Analysis of Variance

		Sum of	Mean		
Source	DF	Squares	${ t Square}$	F Value	Pr > F
Model	2	1705.56004	852.78002	1.83	0.1765
Error	34	15878	466.99227		
Corrected Total	36	17583			
Root MSE	21.61000	R-Square	0.0970		
Dependent Mean	31.27027	Adj R-Sq	0.0439		
Coeff Var	69.10719				

Parameter Estimates Parameter Standard

Variable	DF	Estimate	Error	t Value	Pr > t	
Intercept	1	12.96360	11.68856	1.11	0.2752	
ns	1	-0.83824	0.80914	-1.04	0.3075	
na	1	1.32322	0.70976	1.86	0.0709	
The REG Pr						
Model: MOD						
Dependent			0.7			
Number of			37			
Number of	Ubservati	ions Used	37			
		An	alysis of Varia	ance		
			Sum of	Mean		
Source		DF	Squares	Square	F Value	Pr > F
Model		2	2552.00497	1276.00248	14.01	<.0001
Error		34	3096.42746	91.07140		
Corrected	Total	36	5648.43243			
Root MSE		9.54313	R-Square	0.4518		
Dependent	Mean	62.64865	Adj R-Sq	0.4196		
Coeff Var		15.23278				
		ъ.				
			er Estimates			
** * 1 7	DE	Parameter	Standard		D > 1.1	
Variable	DF	Estimate	Error	t Value	Pr > t	
Intercept	1 1	36.62049	5.16175	7.09 -0.12	<.0001 0.9084	
ns	1	-0.04141 1.18805	0.35732	-0.12 3.79		
na	1	1.10005	0.31344	3.19	0.0006	
The REG Pr	ocedure					
Model: MOD						
Dependent		: Raven				
Number of			37			
Number of			37			
		An	alysis of Varia	ance		
			Sum of	Mean		
Source		DF	Squares	${ t Square}$	F Value	Pr > F
Model		2	66.86503	33.43252	4.09	0.0256
Error		34	277.94578	8.17488		
Corrected	Total	36	344.81081			

2.85917

13.24324 21.58968

Root MSE

Dependent Mean Coeff Var R-Square

Adj R-Sq

0.1939

0.1465

Parameter Estimates

		Parameter	Standard		
Variable	DF	Estimate	Error	t Value	Pr > t
Intercept	1	10.10329	1.54649	6.53	<.0001
ns	1	0.19540	0.10706	1.83	0.0768
na	1	0.02256	0.09391	0.24	0.8116

The REG Procedure
Model: MODEL1

Multivariate Test 1

Multivariate Statistics and F Approximations

	S=2 $M=0$	N=15			
Statistic	Value	F Value	Num DF	Den DF	Pr > F
Wilks' Lambda	0.46333120	5.00	6	64	0.0003
Pillai's Trace	0.59915258	4.70	6	66	0.0005
Hotelling-Lawley Trace	1.02342563	5.38	6	40.936	0.0004
Roy's Greatest Root	0.86807261	9.55	3	33	0.0001

NOTE: F Statistic for Roy's Greatest Root is an upper bound. NOTE: F Statistic for Wilks' Lambda is exact.

The REG Procedure Model: MODEL1

Multivariate Test: ns2

Multivariate Statistics and Exact F Statistics

	S=1 $M=0$.	5 N=15			
Statistic	Value	F Value	Num DF	Den DF	Pr > F
Wilks' Lambda	0.86310909	1.69	3	32	0.1884
Pillai's Trace	0.13689091	1.69	3	32	0.1884
Hotelling-Lawley Trace	0.15860209	1.69	3	32	0.1884
Roy's Greatest Root	0.15860209	1.69	3	32	0.1884

The REG Procedure Model: MODEL1

Multivariate Test: na2

Multivariate Statistics and Exact F Statistics

	S=1 $M=0$.	5 N=15			
Statistic	Value	F Value	Num DF	Den DF	Pr > F
Wilks' Lambda	0.68623559	4.88	3	32	0.0066
Pillai's Trace	0.31376441	4.88	3	32	0.0066
Hotelling-Lawley Trace	0.45722550	4.88	3	32	0.0066
Roy's Greatest Root	0.45722550	4.88	3	32	0.0066

The REG Procedure Model: MODEL1

Dependent Variable: SAT

Number of Observations Read 37

Analv	212	\circ t	٧a:	rıa	nce

			Sum of	Mean		
Source		DF	Squares	Square	F Value	Pr > F
Model		1	1204.38021	1204.38021	2.57	0.1176
Error		35	16379	467.96906		
Corrected T	otal	36	17583			
Root MSE		21.63259	R-Square	0.0685		
Dependent M Coeff Var	lean	31.27027 69.17942	Adj R-Sq	0.0419		

Parameter Estimates

		Parameter	Standard		
Variable	DF	Estimate	Error	t Value	Pr > t
Intercept	1	13.40010	11.69318	1.15	0.2596
na	1	0.79855	0.49777	1.60	0.1176

The REG Procedure Model: MODEL1

Dependent Variable: PPVT

Number of Observations Read 37

Number of Observations Used 37

Analysis of Variance

		Sum of	Mean		
Source	DF	${ t Squares}$	${ t Square}$	F Value	Pr > F
Model	1	2550.78211	2550.78211	28.82	<.0001
Error	35	3097.65032	88.50429		
Corrected Total	36	5648.43243			
Root MSE	9.40767	R-Square	0.4516		
Dependent Mean	62.64865	Adj R-Sq	0.4359		
Coeff Var	15.01656				

Parameter Estimates

		Parameter	Standard		
Variable	DF	Estimate	Error	t Value	Pr > t
Intercept	1	36.64205	5.08518	7.21	<.0001
na	1	1.16213	0.21647	5.37	<.0001

The REG Procedure Model: MODEL1

Dependent Variable: Raven

Number of Observations Read 37

Number of Observations Used

37

vsis		

		Sum of	Mean		
Source	DF	Squares	${ t Square}$	F Value	Pr > F
Model	1	39.63250	39.63250	4.55	0.0401
Error	35	305.17831	8.71938		
Corrected Total	36	344.81081			
Root MSE	2.95286	R-Square	0.1149		
Dependent Mean	13.24324	Adj R-Sq	0.0897		
Coeff Var	22.29710				

Parameter Estimates

		Parameter	Standard		
Variable	DF	Estimate	Error	t Value	Pr > t
Intercept	1	10.00155	1.59612	6.27	<.0001
na	1	0.14486	0.06795	2.13	0.0401

The REG Procedure Model: MODEL1

Multivariate Test: na3

Multivariate Statistics and Exact F Statistics

	S=1	M=0.5		N=15.5					
Statistic		Value	F	Value	Num	DF	Den	DF	Pr > F
Wilks' Lambda	0.536	881650		9.49		3		33	0.0001
Pillai's Trace	0.463	318350		9.49		3		33	0.0001
Hotelling-Lawley Trace	0.862	283396		9.49		3		33	0.0001
Roy's Greatest Root	0.862	283396		9.49		3		33	0.0001