## The men-track-field data

## March 24, 2011

## The data:

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10.39
       20.81
               46.84
                       1.81
                              3.70
                                    14.04
                                            29.36
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                                    16.28
                                            34.71
                                                    161.83
The SAS code and output:
options linesize=70;
data track;
    infile "men_track_field.dat";
    input m100 m200 m400 m800 m1500 m5000 m10000 marathon
        country $;
proc princomp out=PC;
proc print;
    var country Prin1 Prin2;
symbol1 pointlabel=('#country');
proc gplot;
    plot Prin2*Prin1;
run;
The PRINCOMP Procedure
Observations
                       55
```

| Simple Statistics                     |                             |                 |            |         |             |  |  |  |  |
|---------------------------------------|-----------------------------|-----------------|------------|---------|-------------|--|--|--|--|
|                                       | m100                        | m200            |            | 400     | m800        |  |  |  |  |
| Mean                                  | 10.47109091                 | 20.94036364     | 46.43872   | 727     | 1.793272727 |  |  |  |  |
| StD                                   | 0.35142921                  | 0.64464737      | 1.45701    | 757     | 0.063684830 |  |  |  |  |
|                                       |                             | Simple Stat     |            |         |             |  |  |  |  |
|                                       | m1500 m5000 m10000 marathon |                 |            |         |             |  |  |  |  |
| Mean                                  | 3.698181818                 | 13.84581818     |            |         | 136.6240000 |  |  |  |  |
| StD                                   | 0.155909410                 | 0.80116048      | 1.80773162 |         | 9.2270335   |  |  |  |  |
| 01221000                              |                             |                 |            |         |             |  |  |  |  |
| Correlation Matrix                    |                             |                 |            |         |             |  |  |  |  |
|                                       | m100                        | m200            | m400       | m800    | m1500       |  |  |  |  |
| m100                                  | 1.0000                      | 0.9226          | 0.8411     | 0.7560  | 0.7002      |  |  |  |  |
| m200                                  | 0.9226                      | 1.0000          | 0.8507     | 0.8066  | 0.7750      |  |  |  |  |
| m400                                  | 0.8411                      | 0.8507          | 1.0000     | 0.8702  | 0.8353      |  |  |  |  |
| m800                                  | 0.7560                      | 0.8066          | 0.8702     | 1.0000  | 0.9180      |  |  |  |  |
| m1500                                 | 0.7002                      | 0.7750          | 0.8353     | 0.9180  | 1.0000      |  |  |  |  |
| m5000                                 | 0.6195                      | 0.6954          | 0.7786     | 0.8636  | 0.9281      |  |  |  |  |
| m10000                                | 0.6325                      | 0.6965          | 0.7872     | 0.8690  | 0.9347      |  |  |  |  |
| marathon                              | 0.5199                      | 0.5962          | 0.7050     | 0.8065  | 0.8655      |  |  |  |  |
|                                       | Correla                     | tion Matrix     |            |         |             |  |  |  |  |
|                                       | m5000                       | m10000          | marathon   |         |             |  |  |  |  |
| m100                                  | 0.6195                      | 0.6325          | 0.5199     |         |             |  |  |  |  |
| m200                                  | 0.6954                      | 0.6965          | 0.5962     |         |             |  |  |  |  |
| m400                                  | 0.7786                      | 0.7872          | 0.7050     |         |             |  |  |  |  |
| m800                                  | 0.8636                      | 0.8690          | 0.8065     |         |             |  |  |  |  |
| m1500                                 | 0.9281                      | 0.9347          | 0.8655     |         |             |  |  |  |  |
| m5000                                 | 1.0000                      | 0.9746          | 0.9322     |         |             |  |  |  |  |
| m10000                                | 0.9746                      | 1.0000          | 0.9432     |         |             |  |  |  |  |
| marathon                              | 0.9322                      | 0.9432          | 1.0000     |         |             |  |  |  |  |
|                                       |                             |                 |            |         |             |  |  |  |  |
|                                       | _                           | es of the Corre |            |         |             |  |  |  |  |
|                                       | Eigenvalue                  | Difference      | Proportion | Cumulat |             |  |  |  |  |
| 1                                     | 6.62214613                  | 5.74452784      | 0.8278     |         | 3278        |  |  |  |  |
| 2                                     | 0.87761829                  | 0.71829715      | 0.1097     |         | 9375        |  |  |  |  |
| 3                                     | 0.15932114                  | 0.03527176      | 0.0199     |         | 9574        |  |  |  |  |
| 4                                     | 0.12404939                  | 0.04416911      | 0.0155     | 0.9     | 729         |  |  |  |  |
| 5                                     | 0.07988027                  | 0.01191512      | 0.0100     |         | 9829        |  |  |  |  |
| 6                                     | 0.06796515                  | 0.02154562      | 0.0085     | 0.9     | 9914        |  |  |  |  |
| The PRINCOMP Procedure                |                             |                 |            |         |             |  |  |  |  |
| Eigenvalues of the Correlation Matrix |                             |                 |            |         |             |  |  |  |  |
|                                       | Eigenvalue                  | Difference      | Proportion | Cumulat | ive         |  |  |  |  |
| 7                                     | 0.04641953                  | 0.02381943      | 0.0058     |         | 972         |  |  |  |  |
| 8                                     | 0.02260010                  |                 | 0.0028     |         | 0000        |  |  |  |  |
| -                                     |                             |                 | 5.0020     |         |             |  |  |  |  |

|        |          | I        | Eigenvectors |          |          |
|--------|----------|----------|--------------|----------|----------|
|        |          | Prin1    | Prin2        | Prin3    | Prin4    |
| m100   |          | 0.317556 | 0.566878     | 0.332262 | 0.127628 |
| m200   |          | 0.336979 | 0.461626     | 0.360657 | 259116   |
| m400   |          | 0.355645 | 0.248273     | 560467   | 0.652341 |
| m800   |          | 0.368684 | 0.012430     | 532482   | 479999   |
| m1500  |          | 0.372810 | 139797       | 153443   | 404510   |
| m5000  |          | 0.364374 | 312030       | 0.189764 | 0.029588 |
| m10000 |          | 0.366773 | 306860       | 0.181752 | 0.080069 |
| marath |          | 0.341926 | 438963       | 0.263209 | 0.299512 |
| maraun | .011     |          | Eigenvectors | 0.200203 | 0.233312 |
|        |          | Prin5    | Prin6        | Prin7    | Prin8    |
| m100   |          | 0.262555 | 593704       | 0.136241 | 0.105542 |
|        |          |          |              |          |          |
| m200   |          | 153957   | 0.656137     | 112640   | 096054   |
| m400   |          | 218323   | 0.156625     | 002854   | 000127   |
| m800   |          | 0.540053 | 014692       | 238016   | 038165   |
| m1500  |          | 487715   | 157843       | 0.610011 | 0.139291 |
| m5000  |          | 253979   | 141299       | 591299   | 0.546697 |
| m10000 |          | 133176   | 219017       | 176871   | 796795   |
| marath | on       | 0.497928 | 0.315285     | 0.398822 | 0.158164 |
| Obs    | countr   | y Prin1  | Prin2        |          |          |
| 1      | ar       | 0.2619   | -0.34488     |          |          |
| 2      | au       | -2.4464  | -0.21617     |          |          |
| 3      | at       | -0.8076  | 0.48689      |          |          |
| 4      | be       | -2.0413  | 0.26195      |          |          |
| 5      | bm       | 0.7393   | -1.76694     |          |          |
| 6      | bm<br>br | -1.5583  | -0.64115     |          |          |
| 7      | bu       | 1.9719   | 0.25720      |          |          |
| 8      | ca       | -1.7464  | -0.50035     |          |          |
| 9      | cl       | -0.3811  | -0.20141     |          |          |
| 10     | cn       | 0.4090   | 0.35778      |          |          |
| 11     | CO       | -0.3901  | 0.49998      |          |          |
| 12     | ck       | 10.5556  | 1.50877      |          |          |
| 13     |          | 2.2966   | 1.67064      |          |          |
| 14     | cr       | -1.3726  | -0.02878     |          |          |
| 15     | cz<br>dk | -1.3720  | 0.38730      |          |          |
|        |          | 1.7149   | -2.44900     |          |          |
| 16     | dr<br>£: |          |              |          |          |
| 17     | fi<br>£  | -1.6920  | 0.40882      |          |          |
| 18     | fr       | -2.1719  | -0.50289     |          |          |
| 19     | dee      | -2.5901  | -0.31067     |          |          |
| 20     | dew      | -2.5527  | -0.41137     |          |          |
| 21     | uk       | -3.0242  | -0.27891     |          |          |
| 22     | gr       | -0.3796  | -0.60178     |          |          |
| 23     | gu       | 2.6724   | 1.27121      |          |          |

| 24 | hu         | -1.2052 | -0.15153 |
|----|------------|---------|----------|
| 25 | in         | -0.1652 | 0.67647  |
| 26 | id         | 2.7478  | -0.60317 |
| 27 | ir         | -0.8842 | 0.94602  |
| 28 | il         | 0.4346  | 0.67428  |
| 29 | it         | -2.7269 | -0.98986 |
| 30 | jр         | -1.2379 | 0.41357  |
| 31 | ke         | -2.1683 | 0.53371  |
| 32 | kr         | 0.2075  | -0.30153 |
| 33 | krn        | 1.6837  | 1.56473  |
| 34 | lu         | 0.2205  | -0.27934 |
| 35 | my         | 1.7083  | -1.72273 |
| 36 | mt         | 4.2587  | 0.66695  |
| 37 | mx         | -0.6785 | 0.84175  |
| 38 | nl         | -1.5554 | 0.70244  |
| 39 | nz         | -1.5997 | 0.92336  |
| 40 | no         | -0.8115 | 1.05664  |
| 41 | png        | 3.9092  | 0.08554  |
| 42 | ${\tt ph}$ | 2.0704  | -0.18932 |
| 43 | pl         | -2.0006 | -0.46260 |
| 44 | pt         | -0.9164 | 1.30473  |
| 45 | rm         | -1.1965 | 0.53077  |
| 46 | sg         | 3.1221  | -1.78902 |
| 47 | es         | -1.4806 | 0.50665  |
| 48 | se         | -1.6032 | 0.02323  |
| 49 | ch         | -1.6390 | 0.19593  |
| 50 | tw         | 0.9505  | 0.04203  |
| 51 | th         | 2.7618  | -1.66979 |
| 52 | tr         | 0.2661  | 1.38304  |
| 53 | us         | -3.4306 | -1.11019 |
| 54 | ru         | -2.6269 | -0.75696 |
| 55 | WS         | 7.2312  | -1.90208 |

