

Chapter 12 Homework

$$1. P(x=0) = 0.00001 = \frac{\mu^0}{0!} e^{-\mu}$$

$$= \frac{1}{1} e^{-\mu}$$

$$0.00001 = e^{-\mu}$$

$$\ln(0.00001) = -\mu$$

$$\mu = -\ln(0.00001) = 11.513$$

$$E[X] = \mu = \boxed{11.513}$$

$$2. \text{Pois}(2) \quad P(x \leq 1) = P(x=0) + P(x=1)$$

$$P(x=0) = \frac{2^0}{0!} e^{-2} = \frac{1}{1} e^{-2} = e^{-2}$$

$$P(x=1) = \frac{2^1}{1!} e^{-2} = \frac{2}{1} e^{-2} = 2e^{-2}$$

$$P(x \leq 1) = e^{-2} + 2e^{-2}$$

$$= 3e^{-2}$$

$$= \boxed{0.406}$$

$$3. 11.5 \text{ cars arrive in 20 minutes}$$

$$1) \frac{11.5 \text{ cars}}{20 \text{ min}} \cdot \frac{1 \text{ min}}{60 \text{ sec}} = \frac{23}{40} \cdot \frac{1}{60} = \boxed{\frac{23}{2400} \text{ cars/sec.}}$$

$$2) \frac{23}{2400} \text{ cars/sec} \cdot 20 \text{ sec} = \boxed{\frac{23}{120} \text{ cars}}$$

$$3) \lambda = \frac{23}{2400} \text{ cars/sec.}$$

$$1/\lambda = \frac{2400}{23} \text{ sec/car}$$

$$4) \mu = \lambda t = \frac{23}{2400} \text{ cars/sec} \cdot 10 \text{ sec} = \frac{23}{240} \text{ cars}$$

$$P(x=0) = \frac{\left(\frac{23}{240}\right)^0}{0!} e^{-23/240} = \frac{1}{1} e^{-23/240} = \boxed{\frac{1}{e^{23/240}} = 0.909}$$

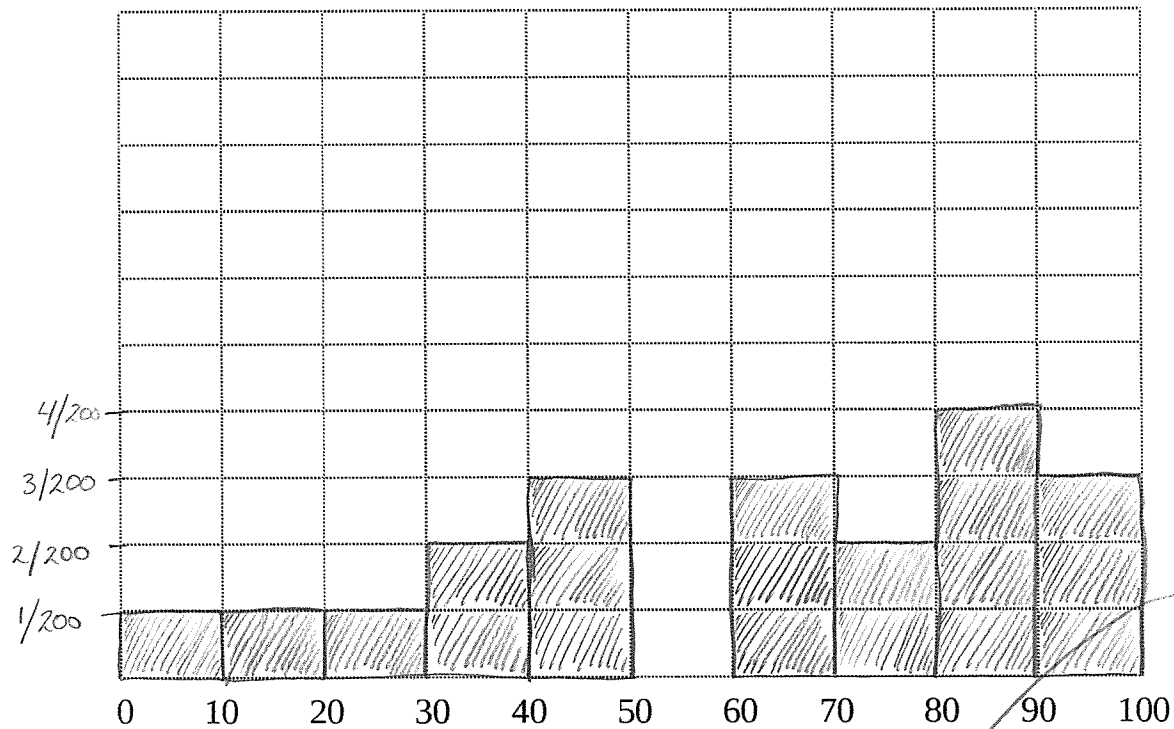
$$5) P(x < 2) = P(x=0) + P(x=1)$$

$$P(x=1) = \frac{\left(\frac{23}{240}\right)^1}{1!} e^{-23/240} = \left(\frac{23}{240}\right) \frac{1}{e^{23/240}} = \frac{23}{240 \cdot e^{23/240}} = 0.087$$

$$P(x < 2) = \frac{1}{e^{23/240}} + \frac{23}{240 \cdot e^{23/240}} = 0.996$$

Question 3.(1) According to the definition in the textbook, draw a histogram for the following numbers in $[0, 100)$, using the given grid (i.e., letting the width of bins be 10). Mark the height of the bins in the histogram according to the textbook definition of histogram.

~~79.3~~, ~~44.2~~, ~~36.4~~, ~~65.2~~, ~~37~~, ~~62.4~~, ~~12.7~~, ~~43.8~~, ~~96.8~~, ~~83.1~~,
~~94.7~~, ~~26.7~~, ~~80.7~~, ~~86.7~~, ~~71.4~~, ~~25~~, ~~87.8~~, ~~65~~, ~~41.7~~, ~~94.3~~



$$\text{height} = \frac{x}{20 \cdot 10} = \frac{x}{200}$$

