

Problem Set 1: Solutions

Your Name - Net ID - Section Number

Due Oct 6th, 2023

This homework must be turned in on Brightspace by Oct 6th 2023. It must be your own work, and your own work only – you must not copy anyone’s work, or allow anyone to copy yours. This extends to writing code. **You may consult with others, but when you write up, you must do so alone.**

Your homework submission must be written and submitted using Rmarkdown. No handwritten solutions will be accepted. You should submit:

1. A compiled PDF file named yourNetID_solutions.pdf containing your solutions to the problems.
2. A .Rmd file containing the code and text used to produce your compiled pdf named your-NetID_solutions.Rmd.

Note that math can be typeset in Rmarkdown in the same way as Latex. Please make sure your answers are clearly structured in the Rmarkdown file:

1. Label each question part
2. Do not include written answers as code comments. Write out answers and explanations separately.
3. The code used to obtain the answer for each question part should accompany the written answer. Comment your code!

Question 1. Definitions and Examples (20 points)

Answer the following questions. Be as specific and detailed as possible. Give examples.

1. What is the fundamental problem of causal inference? (5 points)
2. Why are experiments important? (5 points)
3. What does ignorability mean? (5 points)
4. What is SUTVA? (5 points)

Question 2. Bed Nets and Malaria (20 points)

Article: Free Distribution or Cost-Sharing? Evidence from a Randomized Malaria Prevention Experiment by Jessica Cohen and Pascaline Dupas

Some economists have argued that “cost-sharing” makes it more likely that a product will be used (versus giving it away for free). Cohen and Dupas partnered with 20 Kenyan prenatal clinics to distribute subsidized anti-malarial bed nets. For each clinic, they varied the extent of the subsidy: either full (free bed-nets, $D_i = 1$) or partial (90% cheaper bed-nets, $D_i = 0$). They measure (among other things) whether women who received bed nets used them (Y_i).

1. What is $\mathbb{E}[Y_i|D_i = 0]$? (5 points)
2. What is $\mathbb{E}[Y_i(1)]$? (5 points)
3. What is $\mathbb{E}[Y_i(1)|D_i = 0]$? (5 points)
4. Cohen and Dupas randomized treatment at the level of the clinic, but the outcomes of interest are at the individual level. Is there a violation of consistency/SUTVA? Why or why not? Argue your case. (5 points)

Question 3. Application (Coding) (30 points)

The STAR (Student-Teacher Achievement Ratio) Project is a four year *longitudinal study* examining the effect of class size in early grade levels on educational performance and personal development.

This exercise is in part based on¹:

Mosteller, Frederick. 1997. "The Tennessee Study of Class Size in the Early School Grades." *Bulletin of the American Academy of Arts and Sciences* 50(7): 14-25.

A longitudinal study is one in which the same participants are followed over time. This particular study lasted from 1985 to 1989 involved 11,601 students. During the four years of the study, students were randomly assigned to small classes, regular-sized classes, or regular-sized classes with an aid. In all, the experiment cost around \$12 million. Even though the program stopped in 1989 after the first kindergarten class in the program finished third grade, collection of various measurements (e.g., performance on tests in eighth grade, overall high school GPA) continued through the end of participants' high school attendance.

We will analyze just a portion of this data to investigate whether the small class sizes improved performance or not. The data file name is `STAR.csv`, which is a CSV data file. The names and descriptions of variables in this data set are:

Name	Description
<code>race</code>	Student's race (White = 1, Black = 2, Asian = 3, Hispanic = 4, Native American = 5, Others = 6)
<code>classtype</code>	Type of kindergarten class (small = 1, regular = 2, regular with aid = 3)
<code>g4math</code>	Total scaled score for math portion of fourth grade standardized test
<code>g4reading</code>	Total scaled score for reading portion of fourth grade standardized test
<code>yearssmall</code>	Number of years in small classes
<code>hsgrad</code>	High school graduation (did graduate = 1, did not graduate = 0)

Note that there are a fair amount of missing values in this data set. For example, missing values arise because some students left a STAR school before third grade or did not enter a STAR school until first grade.

1. Create a new factor variable called `kinder` in the data frame. This variable should recode `classtype` by changing integer values to their corresponding informative labels (e.g., change 1 to `small` etc.). Similarly, recode the `race` variable into a factor variable with four levels (`white`, `black`, `hispanic`, `others`) by combining Asians and Native Americans as the `others` category. For the `race` variable, overwrite the original variable in the data frame rather than creating a new one. Recall that `na.rm = TRUE` can be added to functions in order to remove missing data. (5 points)

```
library("tidyverse")
```

```
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
## v dplyr      1.1.2      v readr      2.1.4
## v forcats    1.0.0      v stringr    1.5.0
## v ggplot2    3.4.2      v tibble     3.2.1
## v lubridate  1.9.2      v tidyr      1.3.0
## v purrr      1.0.1
```

```
## -- Conflicts ----- tidyverse_conflicts() --
```

```
## x dplyr::filter() masks stats::filter()
```

```
## x dplyr::lag()     masks stats::lag()
```

```
## i Use the conflicted package (<http://conflicted.r-lib.org/>) to force all conflicts to become errors
```

```
STAR <- read.csv("STAR2.csv")
```

¹I have provided you with a sample of their larger dataset. Empirical conclusion drawn from this sample may differ from their article.

2. How does performance on fourth grade reading and math tests for those students assigned to a small class in kindergarten compare with those assigned to a regular-sized class? Do students in the smaller classes perform better? Use means to make this comparison while removing missing values. Give a brief substantive interpretation of the results. To understand the size of the estimated effects, compare them with the standard deviation of the test scores. (10 points)
3. Instead of comparing just average scores of reading and math tests between those students assigned to small classes and those assigned to regular-sized classes, look at the entire range of possible scores. To do so, compare a high score, defined as the 66th percentile, and a low score (the 33rd percentile) for small classes with the corresponding score for regular classes. These are examples of *quantile treatment effects*. Does this analysis add anything to the analysis based on mean in the previous question? (Hint: You will use the `quantile()` function in `r`.) (5 points)
4. We examine whether the STAR program reduced the achievement gaps across different racial groups. Begin by comparing the average reading and math test scores between white and minority students (i.e., Blacks and Hispanics) among those students who were assigned to regular classes with no aid. Conduct the same comparison among those students who were assigned to small classes. Give a brief substantive interpretation of the results of your analysis. (5 points)
5. We consider the long term effects of kindergarten class size. Compare high school graduation rates across students assigned to different class types. Also, examine whether graduation rates differ by the number of years spent in small classes. Finally, as done in the previous question, investigate whether the STAR program has reduced the racial gap between white and minority students' graduation rates. Briefly discuss the results. (5 points)

Question 4. Design Your Experiment (30 points)

Design your own experiment from start to finish. Choose an *interesting* question. Explain why observational data may give you the wrong answer. Detail the potential outcomes and a well-defined treatment. Explain the type of experiment (completely random, cluster-design, block/stratified). Will your design ensure a causal treatment effect? (Remember: Be as specific as possible and give examples.)