Neural Networks II: Deep Learning

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(Slides credit to David Rosenberg, He He, et al.)

NYU

Nov 26, 2024

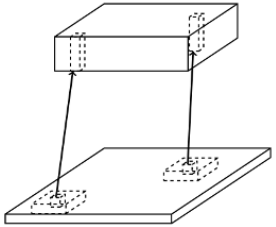
Slides

Logistics

- Homework 4 Due: Dec 3.
- Last lecture: Dec 10 Project presentation.
- Presentation order: Your assigned Group ID.
- Each group has a max of 4 minutes (hard stop) + 1 min Q&A.
- OH this week: Wednesday 1-2pm.

Local connection patterns

- The typical image input layer has 3 channels R G B for color or 1 channel for grayscale.
- The hidden layers may have C channels, at each spatial location (i, j).



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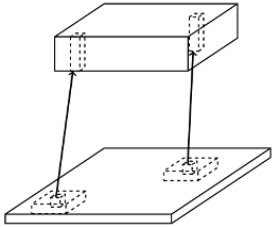
- k is the "kernel" size - do not confuse with the other kernel we learned.
- $z_{i,j,c} = \sum_{i' \in [i\pm k], j' \in [j\pm k], c'} x_{i'j'c'} w_{i,j,i'-i,j'-j,c',c}$



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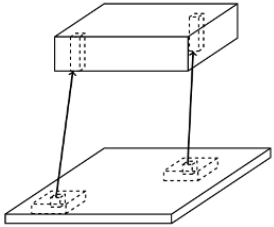
- The spatial awareness (receptive field) of the neighborhood grows bigger as we go deeper.



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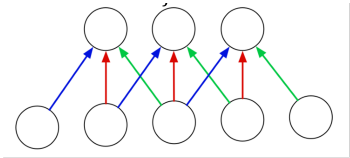
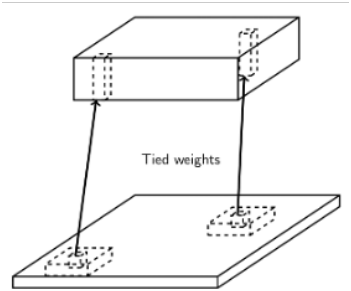
- Local information is the same regardless of the position of an element.
- Solution: We can tie the weights at different locations.





2D convolution

- Using the same weight connections for each activation spatial location works like the "filtering operation" or "convolution"
- The neighborhood window is the filter window.
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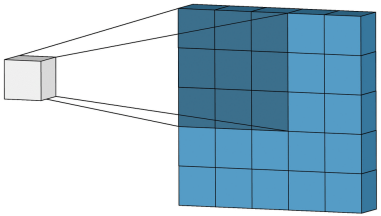

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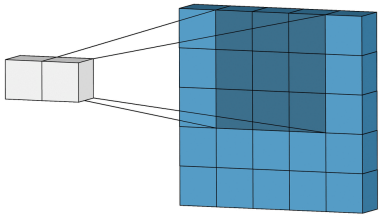

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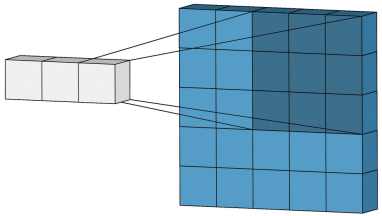

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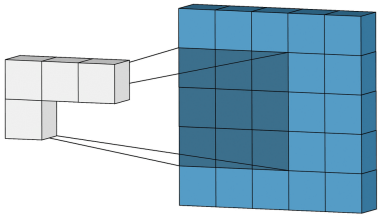

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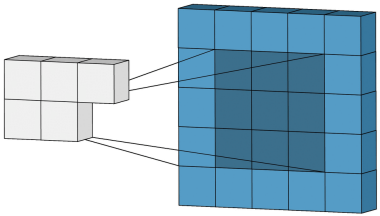

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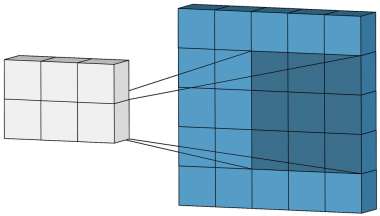

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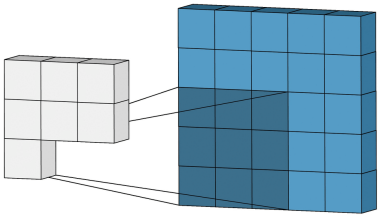

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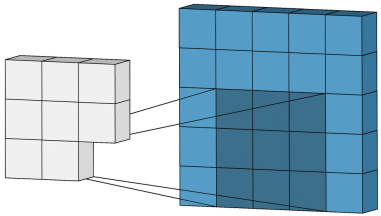

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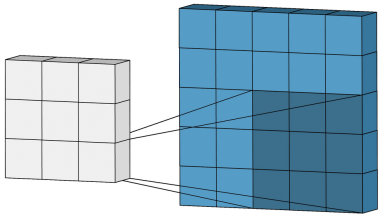
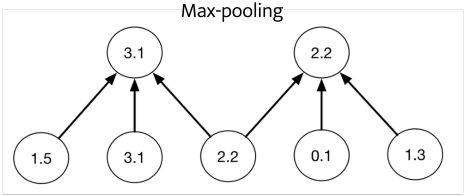


Pooling

- Need to summarize global information more efficiently.
- Pooling reduces image / activation dimensions.
- Max-pooling or average-pooling



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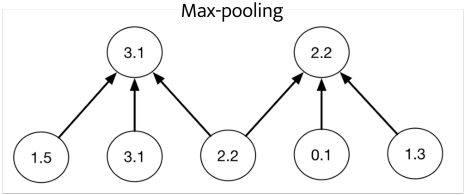

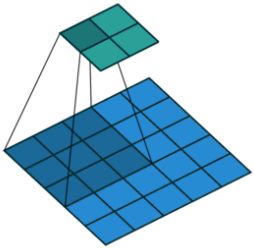

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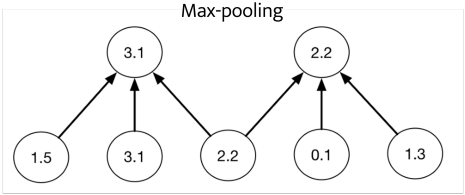

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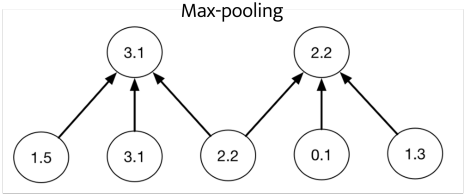

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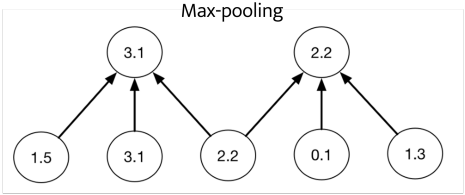
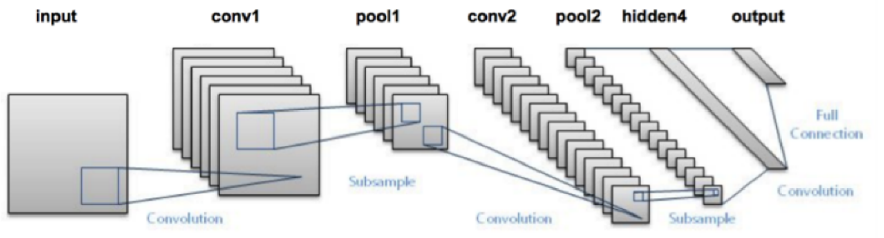


Assembling together: LeNet



- Used by USPS to read post code in the 90s.

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- During the years:
  - Neural networks were difficult to work
  - People focused on feature engineering
  - Then apply SVM or random forest (e.g. AdaBoost face detector)
  - What has changed?

Gradient learning conditioning

Optimization challenges

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- Loss often stalls or blows up.
- Why?
  - Backpropagation: multiplying the Jacobian $\frac{\partial y}{\partial x}$ by each layer.
  - If the maximum singular value of each layer of Jacobian is less than 1: then the gradient will converge to 0 with more layers.
  - If the greater than 1: then the gradient will explode with more layers.
  - The bottom (input) layer may get 0 or infinite gradients.

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- Consider the distribution of whole dataset in the activation space.
  - Intuition: upon initialization, the variance of the activations should stay the same across every layer.

Kaiming Initialization

- Suppose each neuron and weight connection are sampling from a random distribution.

[1] He et al. Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet. ICCV, 2015.

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- Putting altogether, $x_{l+1} = \frac{1}{2} n_l Var[w_l] Var[x_l]$.
- To make the variance constant, we need $\frac{1}{2} n_l Var[w_l] = 1$, $Std[w_l] = \sqrt{2/n_l}$[1].

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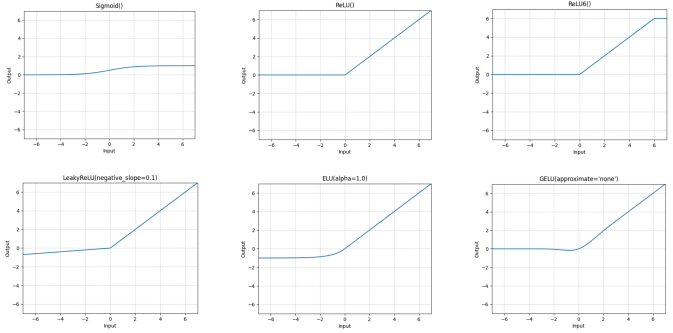
Activation functions

- ReLU was proposed in 2009-2010[2][3], and was successfully used in AlexNet in 2012[4].
- Address the vanishing gradient issue in activations, comparing to sigmoid or tanh.



[2] Jarrett et al. What is the Best Multi-Stage Architecture for Object Recognition? ICCV, 2009.

[3] Nair & Hinton/ Rectified Linear Units Improve Restricted Boltzmann Machines. ICML, 2010.

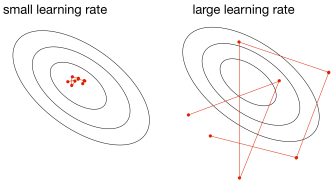
[4] Krizhevsky et al. ImageNet Classification with Deep Convolutional Neural Networks. NIPS, 2012.

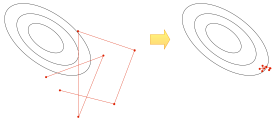
SGD Learning Rate

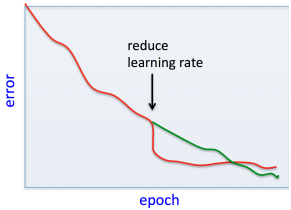
- In stochastic training, the learning rate also influences the fluctuations due to the stochasticity of the gradients.
- Typical strategy:
  - Use a large learning rate early in training so you can get close to the optimum.
  - Gradually decay the learning rate to reduce the fluctuations.

Learning Rate Decay

- We also need to be aware about the impact of learning rate due to the stochasticity.







RMSprop and Adam

- Recall: SGD takes large steps in directions of high curvature and small steps in directions of low curvature.
- RMSprop is a variant of SGD which rescales each coordinate of the gradient to have norm 1 on average. It does this by keeping an exponential moving average s_j of the squared gradients.

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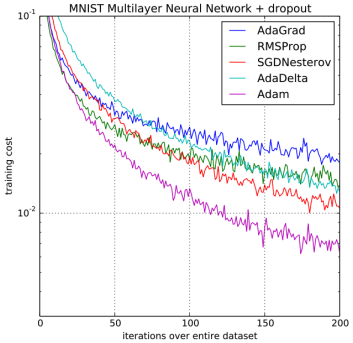
- RMSprop is a variant of SGD which rescales each coordinate of the gradient to have norm 1 on average. It does this by keeping an exponential moving average s_j of the squared gradients.
- The following update is applied to each coordinate j independently:

$$s_j \leftarrow (1-\gamma)s_j + \gamma[\frac{\partial L}{\partial \theta_j}]^2$$

$$\theta_j \leftarrow \theta_j - \frac{\alpha}{\sqrt{s_j + \epsilon}} \frac{\partial L}{\partial \theta_j}$$

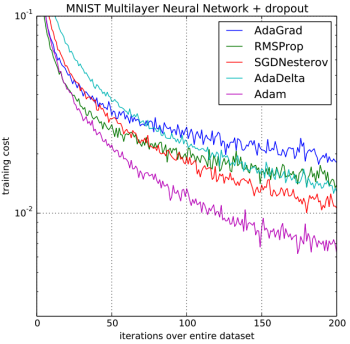
Adam optimizer

- Adam = RMSprop + momentum = Adaptive Momentum estimation
- Smoother estimate of the average gradient and gradient norm.



Adam optimizer

- Adam = RMSprop + momentum = Adaptive Momentum estimation
- Smoother estimate of the average gradient and gradient norm.
- m_t: exponential moving average of gradient.
- v_t: exponential moving average of gradient squared.
- $\hat{m}_t$, $\hat{v}_t$: Bias correction.
- $\theta_t \leftarrow \theta_{t-1} - \alpha \hat{m}_t / (\sqrt{\hat{v}_t} + \epsilon)$
- The "default" optimizer for modern networks.



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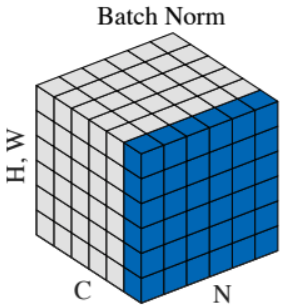
- Weight initialization is tricky, and there is no guarantee that the distribution of activations will stay the same over the learning process.
- What if the weights keep grow bigger and activation may explode?
- We can "normalize" the activations.
- The idea is to control the activation within a normal range: zero-mean, uni-variance.

Batch Normalization (BN)

- In CNNs, neurons across different spatial locations are also samples of the same feature channel.



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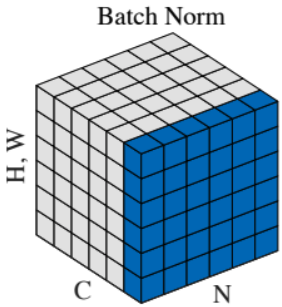

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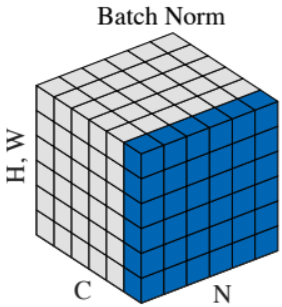

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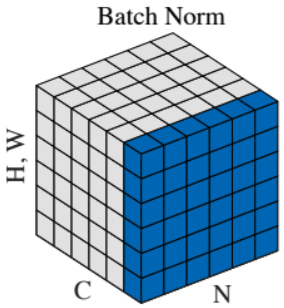
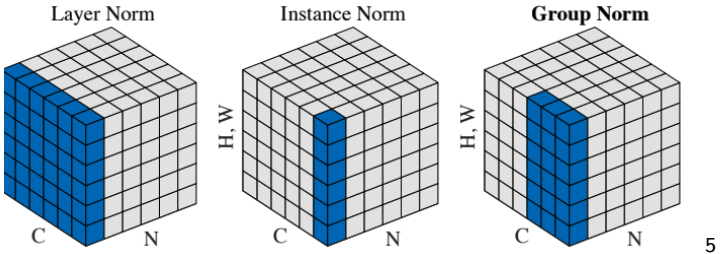


BN Alternatives

- Need a considerable batch size to estimate mean and variance correctly.
- Training is different from testing.
- Alternatives consider the C channel dimension instead of N batch dimension.

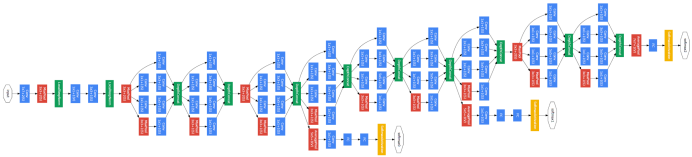


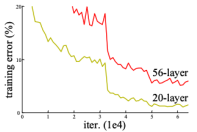
[5]

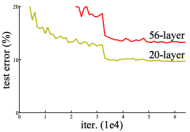
[5] Wu and He. Group normalization. ECCV 2018.

Going Deeper

- The progress of normalization allowed us to train even deeper networks.
- The networks are no longer too sensitive with initialization.
- But the best networks were still around 20 layers and deeper results in worse performance.

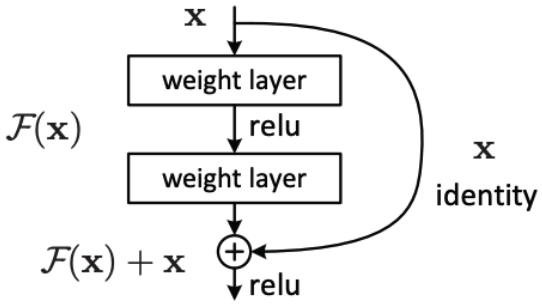






Residual Networks (ResNet)

- Recall in gradient boosting, we are iteratively adding a function to the model to expand the capacity.
- Residual connection: Skip connection to prevent gradient vanishing.[6]



[6] He et al. Deep Residual Learning for Image Recognition. CVPR 2016.

ResNet Success

- Now able to train over 100 layers.
- One of the most important network design choices in the past decade.
- Prevalent in almost all network architectures, including Transformers.

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ResNet Success

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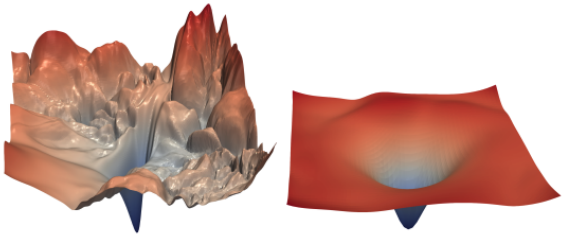
- One of the most important network design choices in the past decade.
- Prevalent in almost all network architectures, including Transformers.
- Loss landscape view: Skip connections makes loss smoother -> easier to optimize [7].

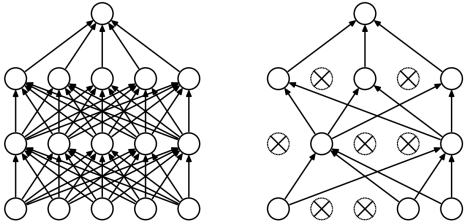


(a) without skip connections (b) with skip connections

[7] Li et al. Visualizing the Loss Landscape of Neural Nets. NIPS 2018.

Dropout[8]

- Want to reduce overfitting in neural networks.
- Stochastically turning off neurons in propagation.



(a) Standard Neural Net (b) After applying dropout.

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Dropout[8]

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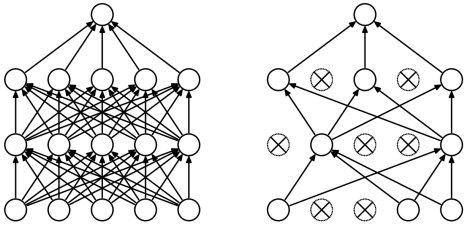
- Training to preserve redundancy.
- Test time: multiplying activations with probability. Model ensembling effect.



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GELU[9]

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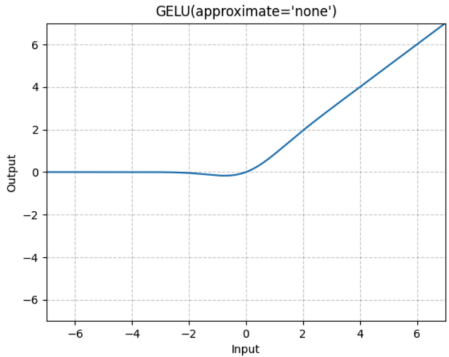

[9] Hendrycks & Gimpel. Gaussian Error Linear Unit (GELU). CoRR abs/1606.08415, 2016.

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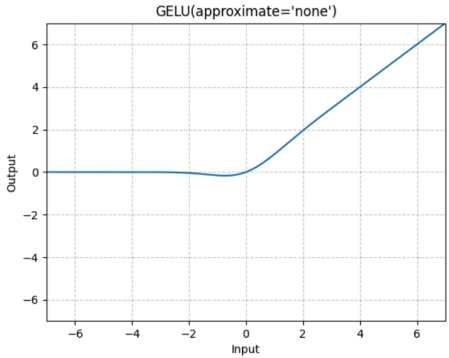

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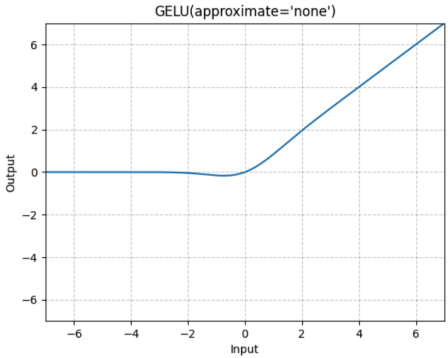

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Data augmentation

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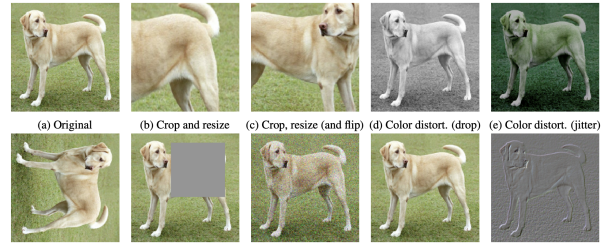
- Create more data points for free



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[10] Chen et al. A Simple Framework for Contrastive Learning of Visual Representations. ICML 2020.

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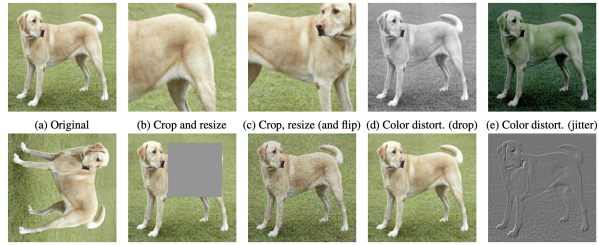

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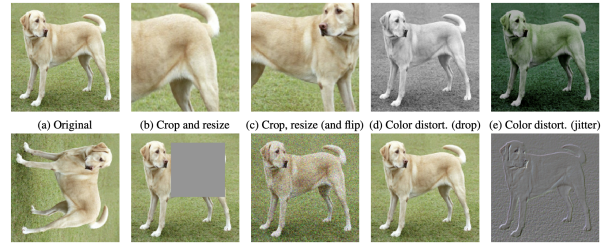

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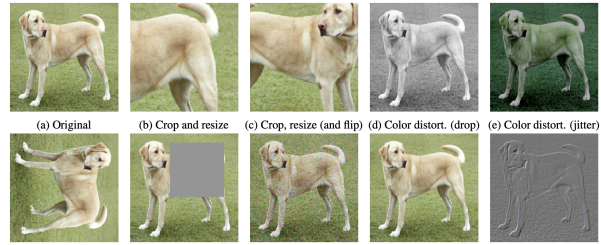

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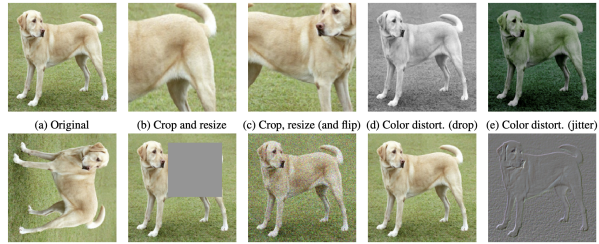

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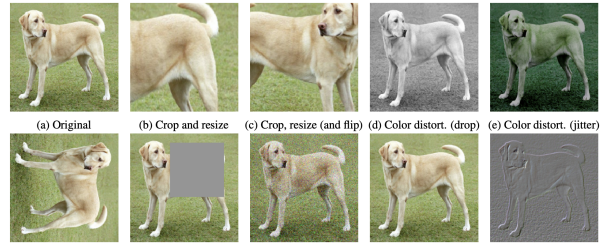
  - Etc.

Image credit[10]



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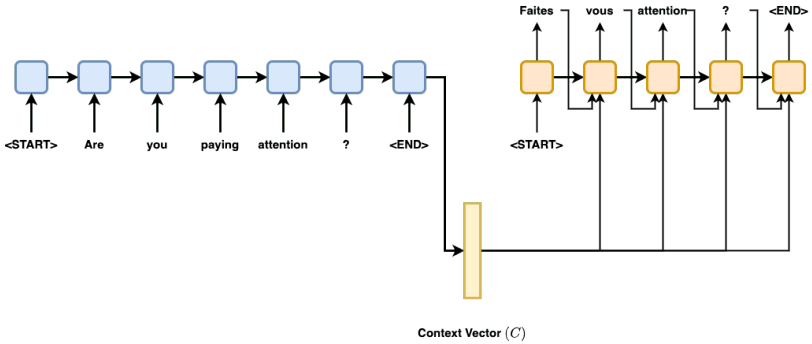
Language and sequential signals

What about natural language

- Neural networks are great for dealing with naturalistic and unstructured signals.



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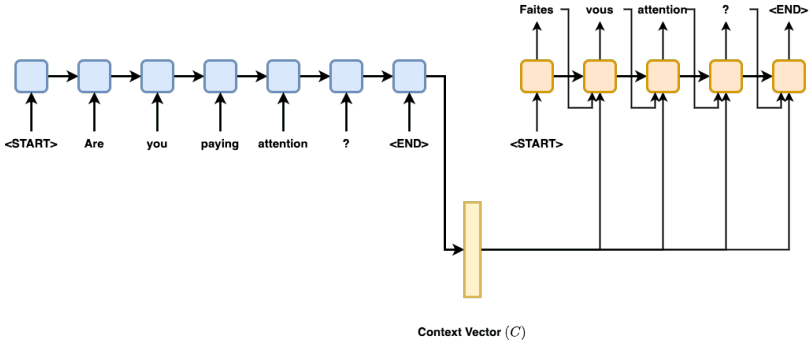
- Past lectures: Feature functions in structured models, but still primitive.



What about natural language

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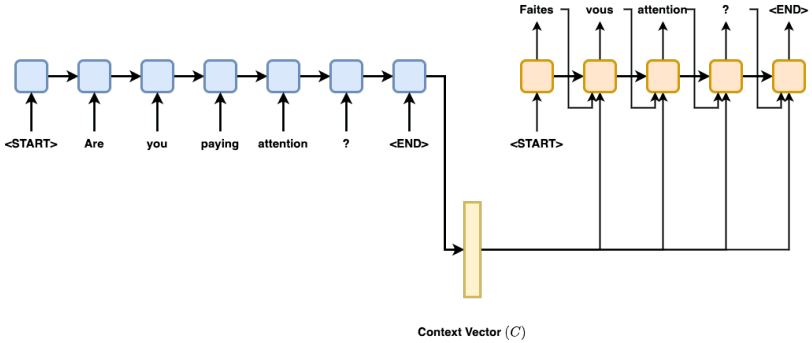
- Past lectures: Feature functions in structured models, but still primitive.
- Design neural networks to accomodate sequential signals such as language.



Word embeddings

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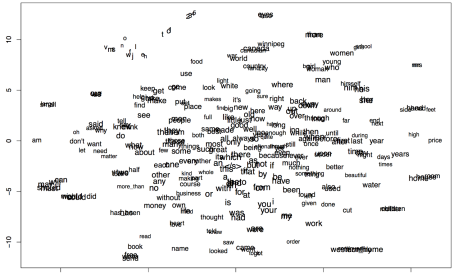

[11]

[11] https://aelang.github.io/word-embeddings.html

Word embeddings

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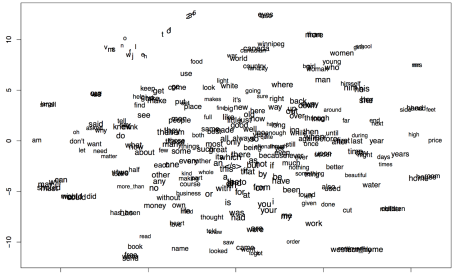

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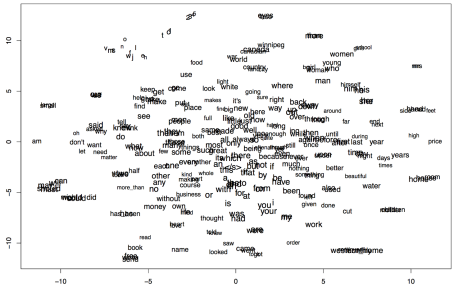

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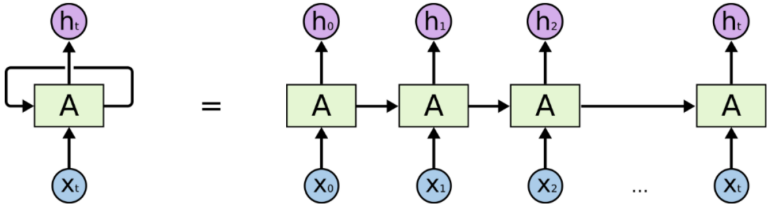
Convolutional vs. recurrent networks

- Recall in images we used the convolution operation.
- We can also use the idea of convolution for temporal signals.



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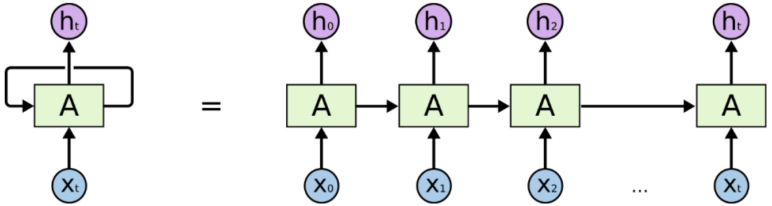
- Two inputs: x_t is the current input, and h_t is the historical hidden state.



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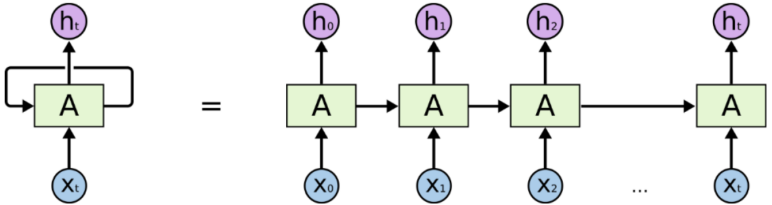
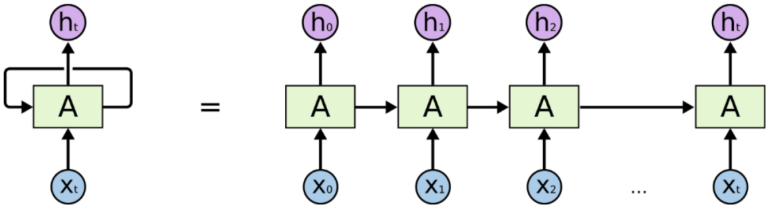
- We can unroll the computation graph into a direct acyclic graph (DAG).



Recurrent neural networks (RNNs)

- A simple RNN can be made similar to a standard NN with one hidden layer.



12

[12] Image credit: Chris Olah https://colah.github.io/posts/2015-08-Understanding-LSTMs/

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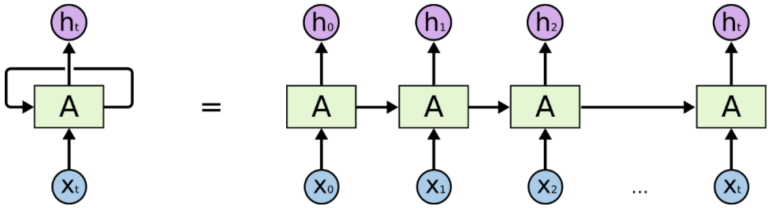

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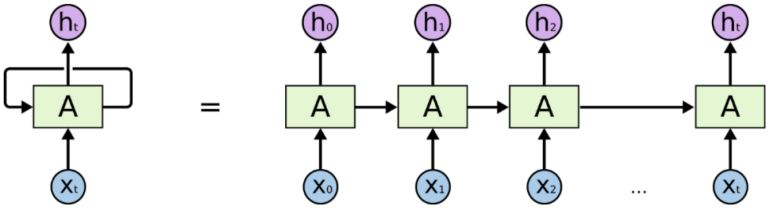

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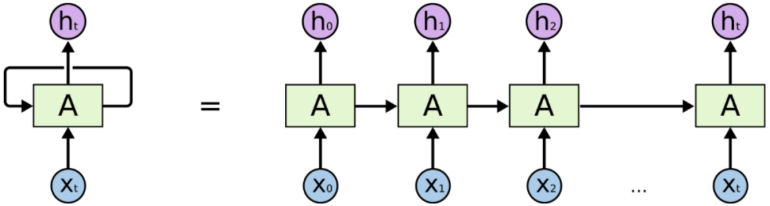
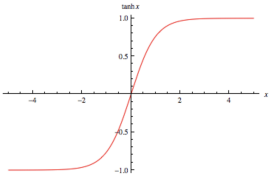
Gradient vanishing

- Every iteration, we multiply the hidden state h_{t-1} from the previous iteration with the same W. Recall the definition of Jacobian.





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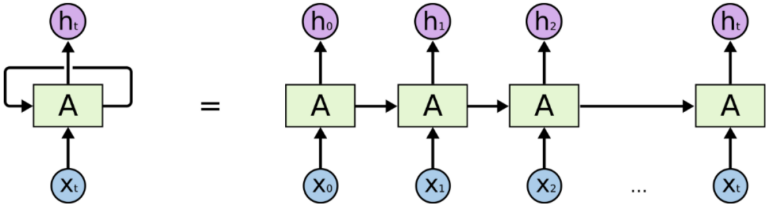

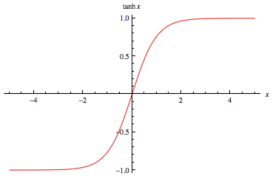

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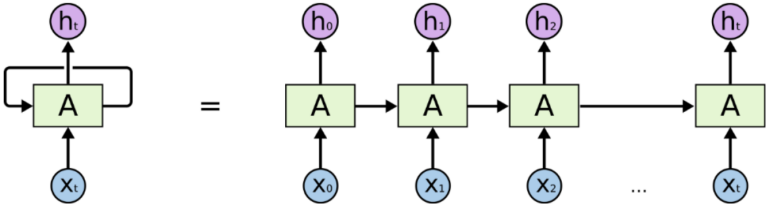
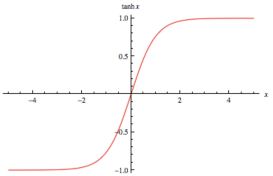
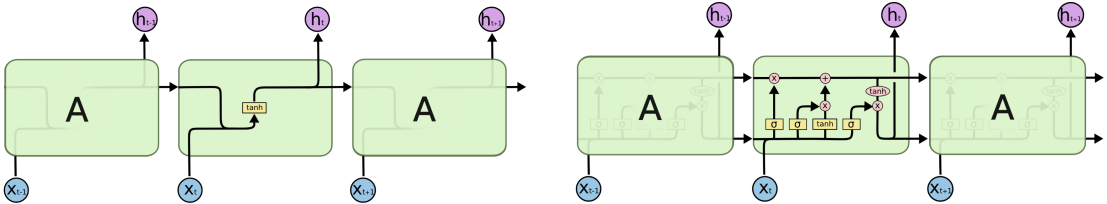
- If the largest singular value of W is less than one then back-propagation will be attenuated.
- Similarly, we apply tanh activation every iteration – further reducing gradient flow.





Gating functions in LSTM

- Long short-term memory is a network that addresses the gradient vanishing problem by introducing gating functions.
- Gating functions provide "shortcuts", like ResNet.



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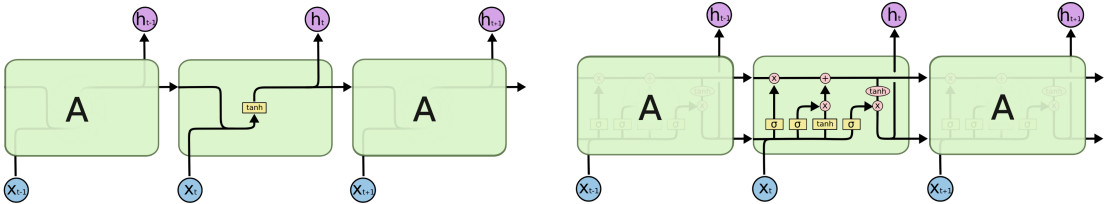

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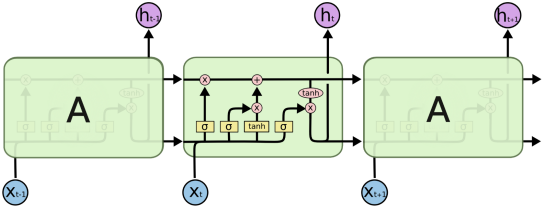

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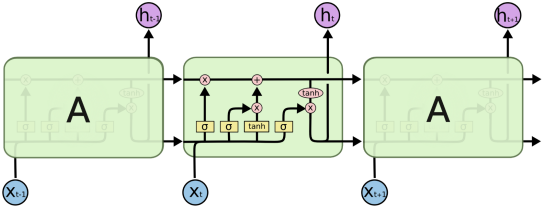

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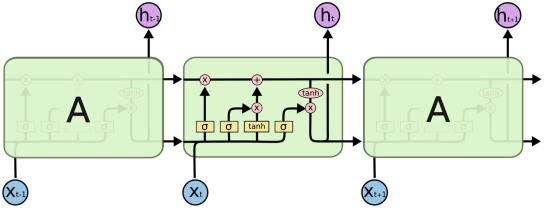

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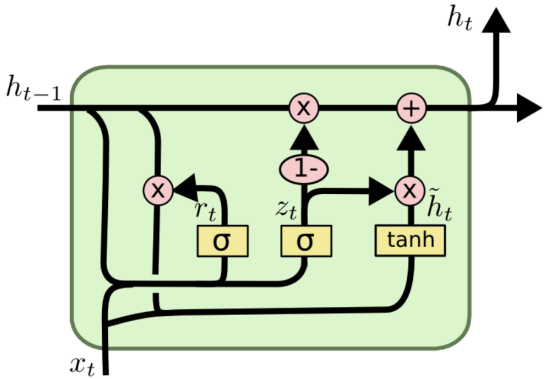

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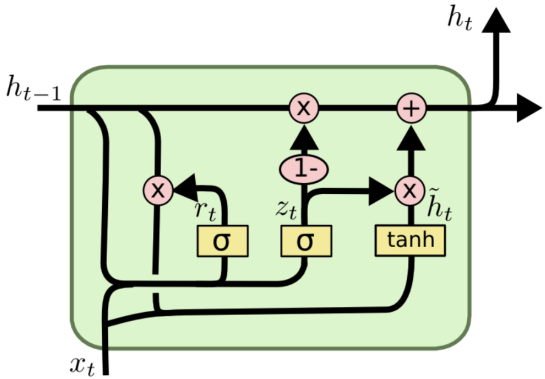

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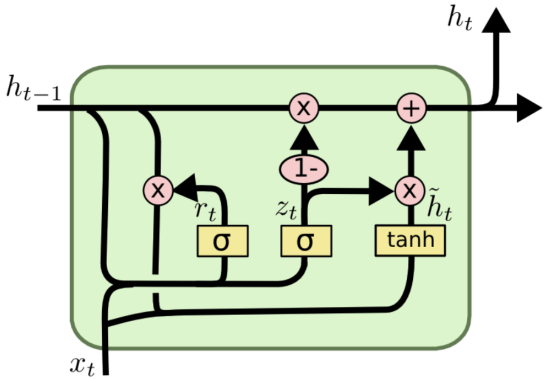

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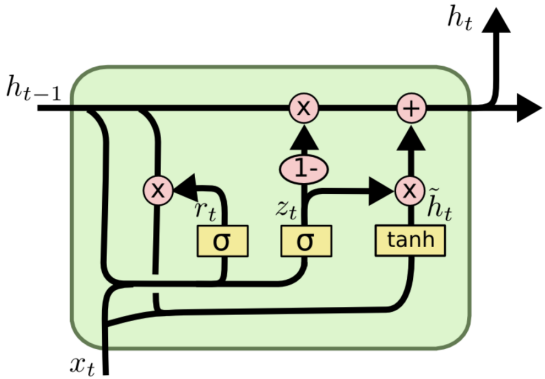

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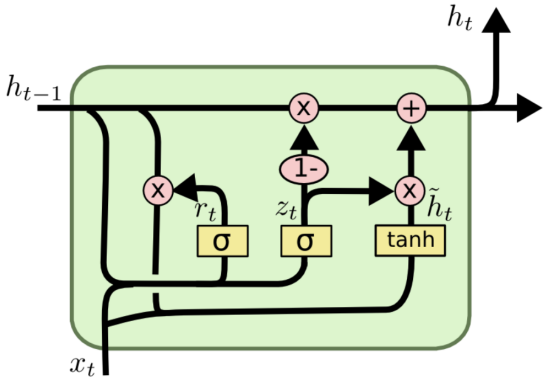

Attention Mechanisms

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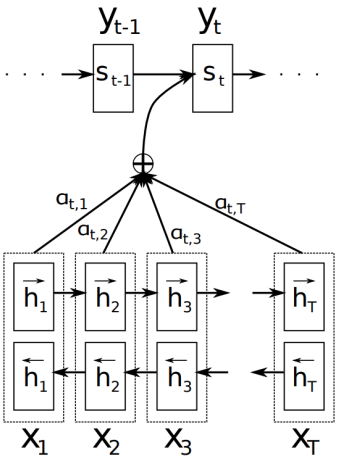

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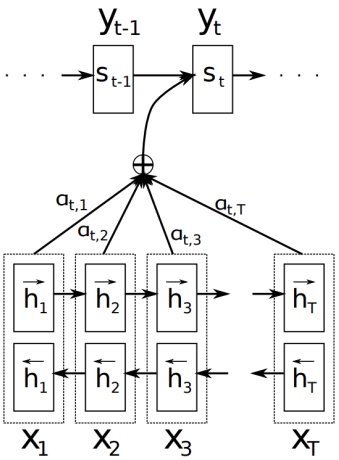

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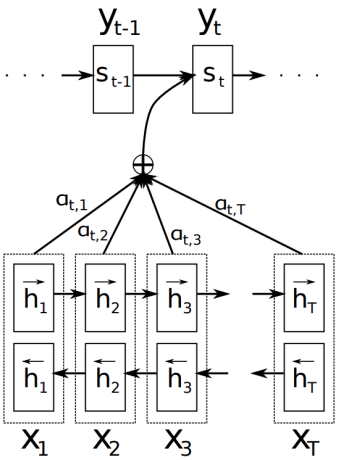

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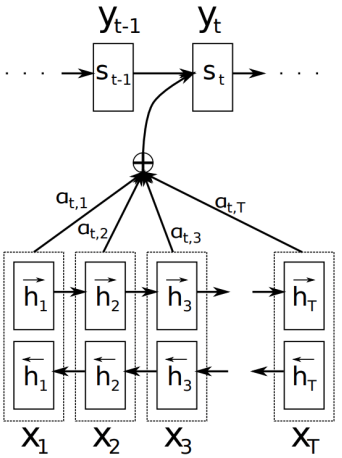

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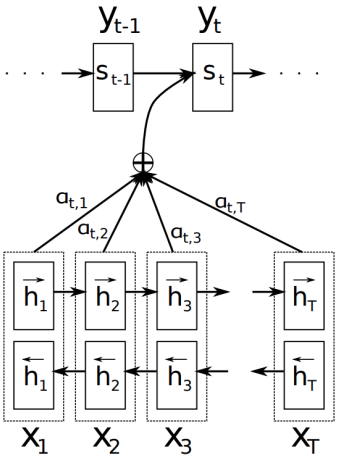

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Transformers ("Attention is All You Need")

- The previous architecture is very complicated.
  - 1 RNN for encoding the tokens.
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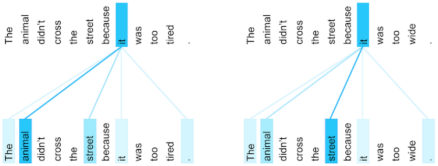

13

[13] Image credit: Google Research Blog

Transformers ("Attention is All You Need")

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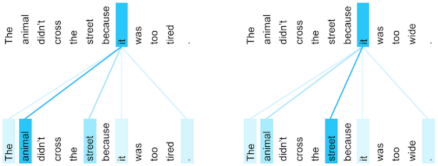
- RNNs have the ability to incorporate past information, so does attention.



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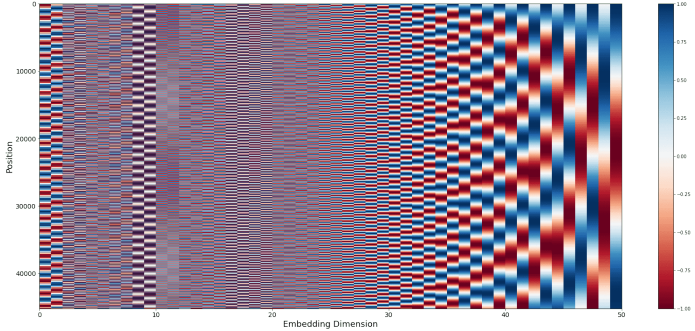
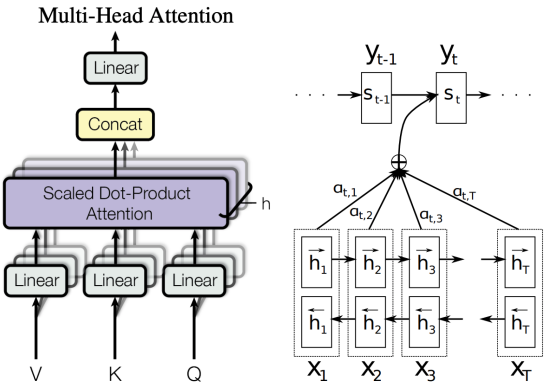


Multi-headed attention

- Map tokens into query, key, and value.



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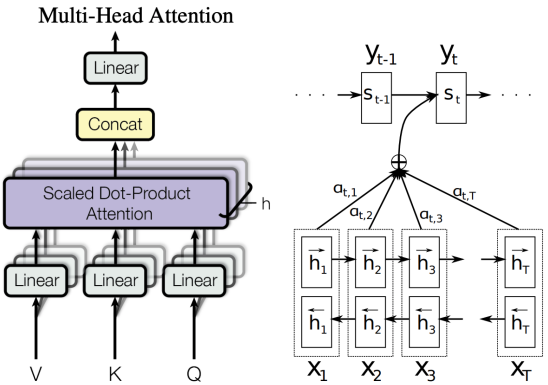

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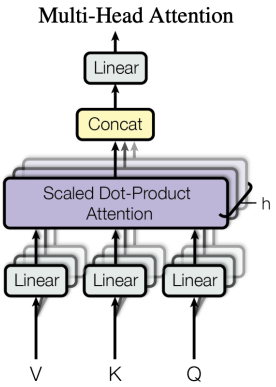

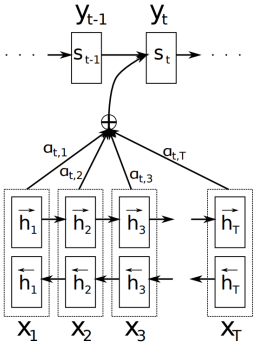

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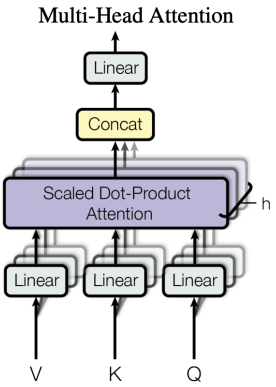

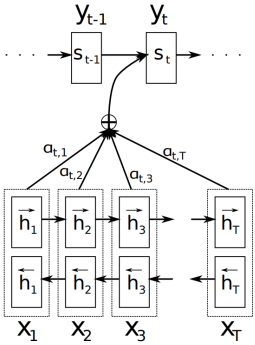

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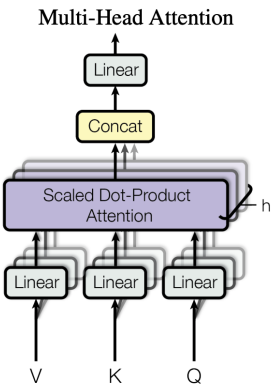

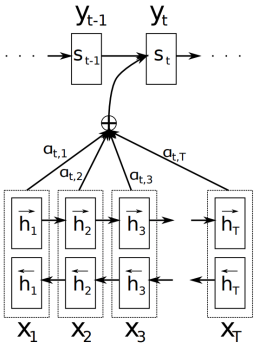

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- Architecture Motifs: MLP, CNN, RNN, Transformers, etc.
- Why deep learning works? Data, optimization, compute.
- Still many open questions: Interpretability, fairness, uncertainty, data efficiency, energy efficiency, theory, etc.

Interpretability in Deep Neural Networks

ML Interpretability

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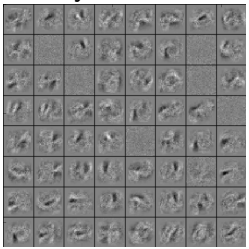
- Neural networks: ?

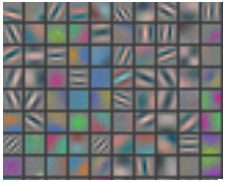
Feature Visualization

- Recall: we can understand what first-layer features are doing by visualizing the weight matrices.

Fully connected



Convolutional



Zeiler and Fergus, Visualizing and understanding convolutional networks, ECCV 2014.

- The better the input matches these weights, the more the feature activates.
- Higher-level weight matrices are hard to interpret.
  - Obvious generalization: visualize higher-level features by seeing what inputs activate them.

Feature Visualization

- One way to formalize: pick the images in the training set which activate a unit most strongly.
- Here's the visualization for layer 1:

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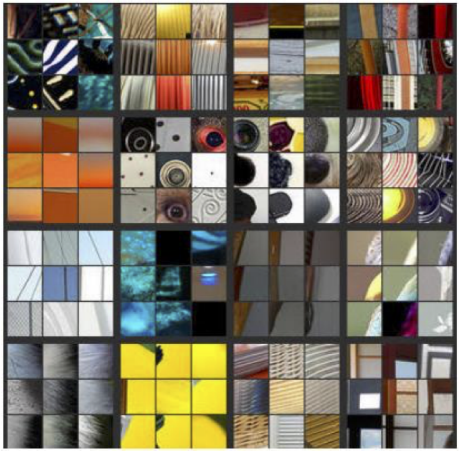
Feature Visualization

- Layer 3:



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Feature Visualization

- Layer 4:

Feature Visualization

- Layer 5:

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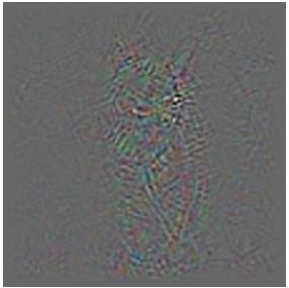
  - We may read too much into the results, e.g. a unit may detect red, and the images that maximize its activation will all be stop signs.
- Can use input gradients to diagnose what the unit is responding to.

Feature Visualization

- Input gradients can be hard to interpret.
- Take a good object recognition conv net (Alex Net) and compute the gradient of $\log p(y = \text{“cat”}|\mathrm{x})$:

Original image

Gradient for “cat”

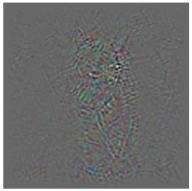


Feature Visualization

- Guided backprop is a total hack to prevent this cancellation.
- Do the backward pass as normal, but apply the ReLU nonlinearity to all the activation error signals.

$$y = \mathrm{ReLU}(z) \qquad \bar{z} = \begin{cases} \bar{y} & \text{if } z > 0 \text{ and } \bar{y} > 0 \\ 0 & \text{otherwise} \end{cases}$$

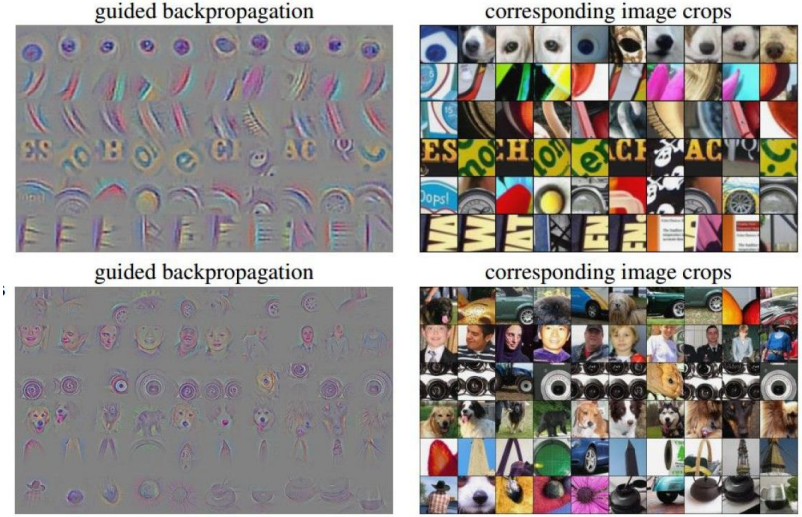
- We want to visualize what excites given unit, not what suppresses it.



Backprop

Guided Backprop

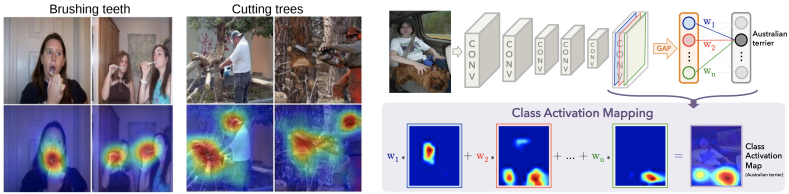
Guided Backprop



Springerberg et al, Striving for Simplicity: The All Convolutional Net (ICLR 2015 workshops)

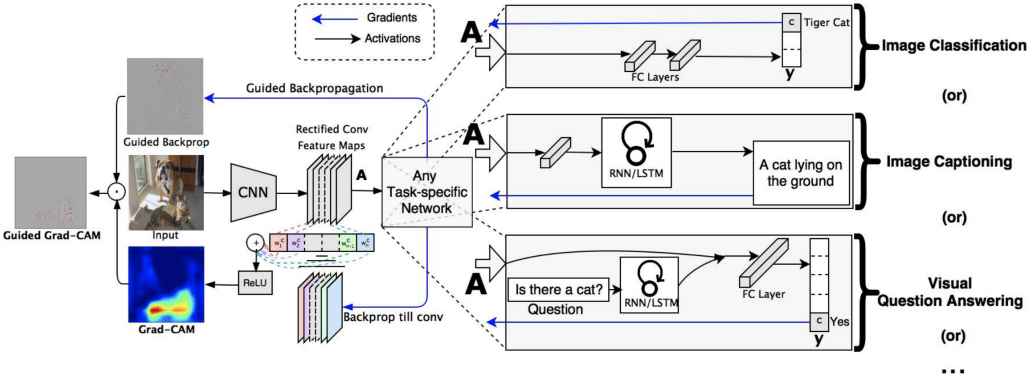
Class activation map (CAM)

- Classification networks typically use global avg pooling before the final layer.
- This pooling layer can already contain semantic information.
- We can visualize a heat map



Zhou et al. Learning deep features for discriminative localization. CVPR 2016.

GradCAM

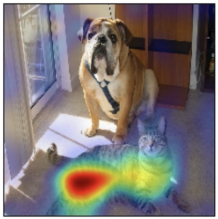


Selvaraju et al. Grad-CAM: Visual explanations from deep networks via gradient-based localization. ICCV 2017.

GradCAM

(a) Original Image

(b) Guided Backprop 'Cat'



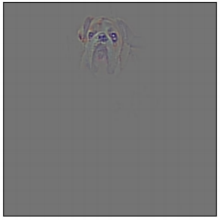
(c) Grad-CAM 'Cat'

(d)Guided Grad-CAM 'Cat'

(g) Original Image

(h) Guided Backprop 'Dog'

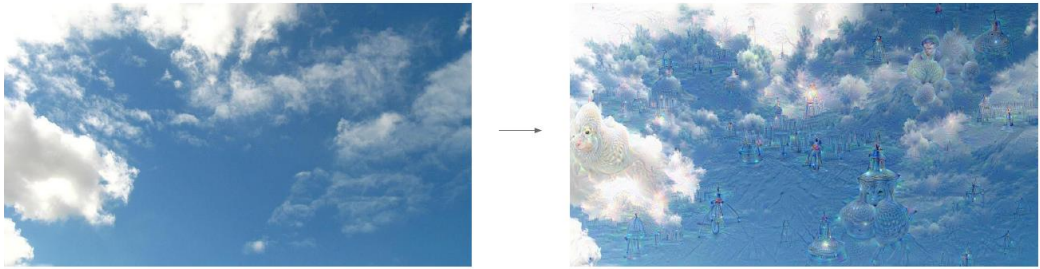
(i) Grad-CAM 'Dog'



(j)Guided Grad-CAM 'Dog'

DeepDream[14]

- Start with an image, and run a conv net on it.
- Change the image such that units which were already highly activated get activated even more strongly. "Rich get richer."



[14] Google Research Blog

DeepDream


"Admiral Dog!"


"The Pig-Snail"


"The Camel-Bird"

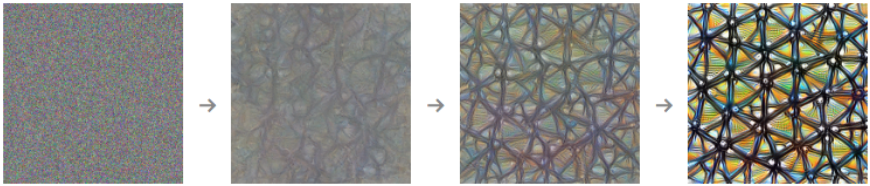

"The Dog-Fish"

DeepDream

Gradient Ascent on Images

- Doing gradient ascent on an image to maximize the activation of a given neuron.

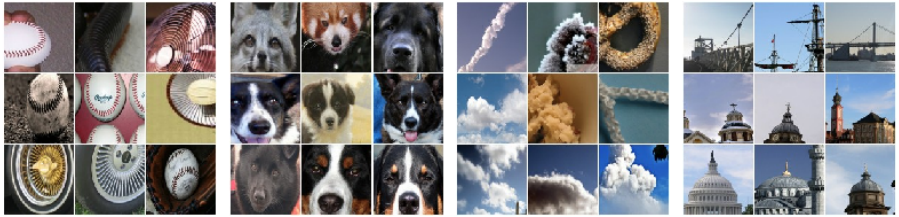
Starting from random noise, we optimize an image to activate a particular neuron (layer mixed4a, unit 11).



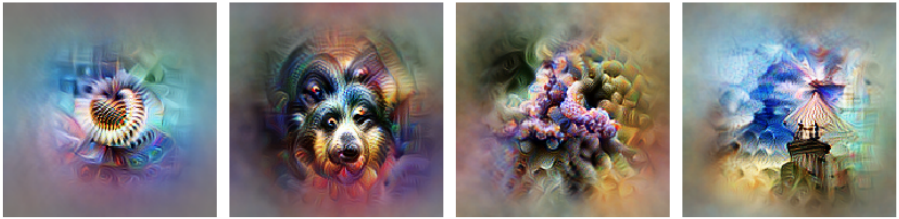
https://distill.pub/2017/feature-visualization/

Gradient Ascent on Images

Dataset Examples show us what neurons respond to in practice



Optimization isolates the causes of behavior from mere correlations. A neuron may not be detecting what you initially thought.



Baseball—or stripes?
mixed4a, Unit 6

Animal faces—or snouts?
mixed4a, Unit 240

Clouds—or fluffiness?
mixed4a, Unit 453

Buildings—or sky?
mixed4a, Unit 492

https://distill.pub/2017/feature-visualization/

Gradient Ascent on Images

- Higher layers in the network often learn higher-level, more interpretable representations

Edges (layer conv2d0) **Textures** (layer mixed3a) **Patterns** (layer mixed4a)

https://distill.pub/2017/feature-visualization/

Gradient Ascent on Images

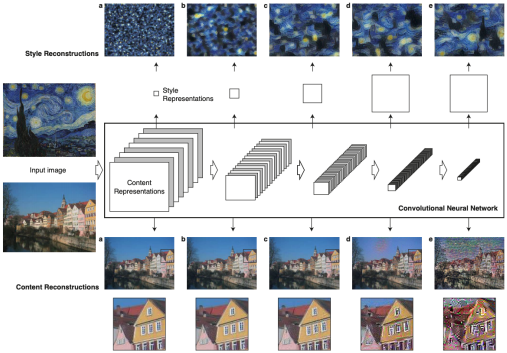
- Higher layers in the network often learn higher-level, more interpretable representations

Parts (layers mixed4b & mixed4c) **Objects** (layers mixed4d & mixed4e)

https://distill.pub/2017/feature-visualization/

Artistic style transfer

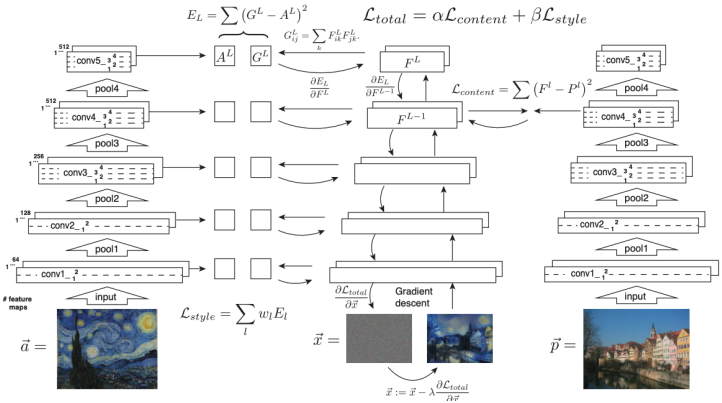
- Activations store content information
- Activation correlation stores style/texture information: $G^l_{ij} = \sum_k F^l_{ik} F^l_{jk}$



Gatys et al., Image style transfer using convolutional neural networks, CVPR 2016.

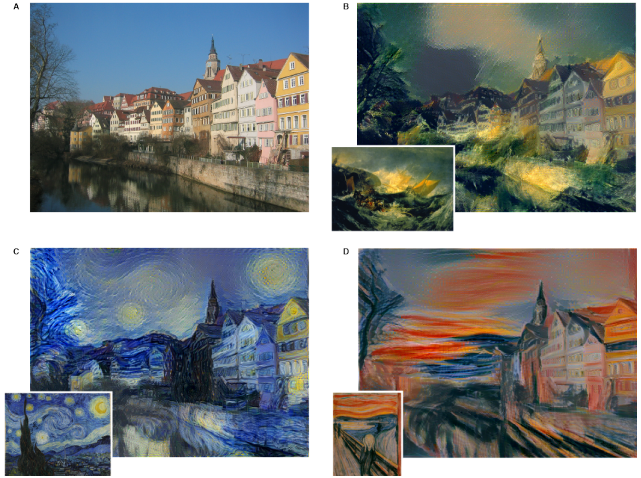
Artistic style transfer

- Optimizing both content & style from random noise



Gatys et al., Image style transfer using convolutional neural networks, CVPR 2016.

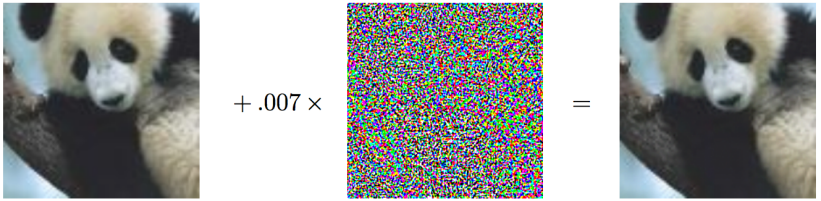
Artistic style transfer



Gatys et al., Image style transfer using convolutional neural networks, CVPR 2016.

Adversarial Examples

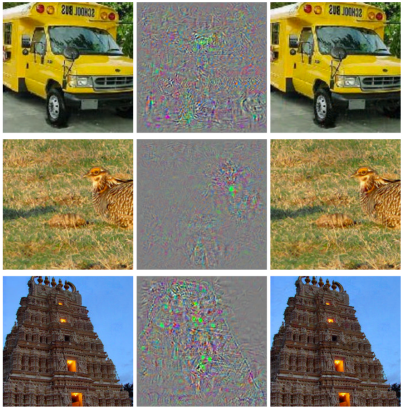
- One of the most surprising findings about neural nets has been the existence of adversarial inputs, i.e. inputs optimized to fool an algorithm.

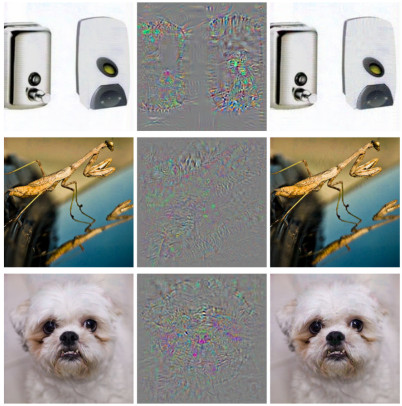


Goodfellow et al., Explaining and harnessing adversarial examples, ICLR 2015.

Adversarial Examples

- The following adversarial examples are misclassified as ostriches. ($10\times$ perturbation visualized in middle.)





Szegedy et al., Intriguing properties of neural networks, ICLR 2014.

Adversarial Examples

- You can print out an adversarial image and take a picture of it, and it still works!

(a) Printout (b) Photo of printout (c) Cropped image

Kurakin et al., Adversarial examples in the physical world, ICLR workshop 2017.

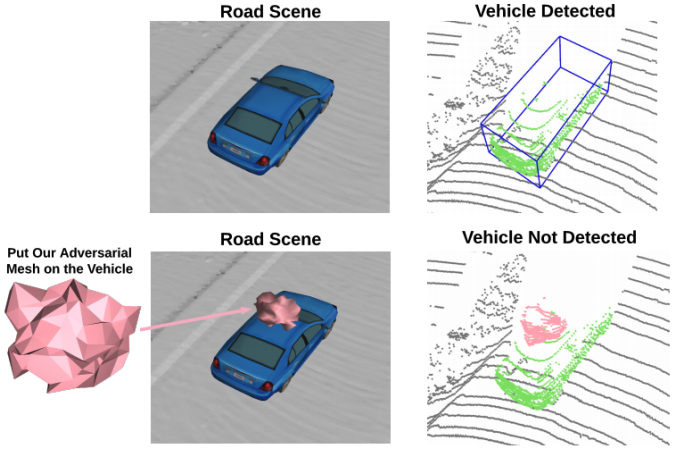
Adversarial Examples

- An adversarial example in the physical world (network thinks it's a gun, from a variety of viewing angles!)

Athalye et al., Synthesizing robust adversarial examples, ICML 2018.

Adversarial Examples

- An adversarial mesh object that can hide cars from LiDAR detector



Tu et al., Physically realizable adversarial examples for LiDAR object detection, CVPR 2020.

Adversarial Defense

- How to defend from adversarial perturbation is still an active research area.

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Adversarial Defense

- How to defend from adversarial perturbation is still an active research area.
- Blackbox vs. whitebox attacks.
- One common approach is to train with millions of adversarial examples.
- Needs to train much longer, and also suffers a drop in accuracy.
- Data augmentation and label smoothing also help.

Summary

- Interpretability - ways to open up the black box of neural networks

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- Knowing what each neuron does is like studying a "brain" with perfect observation and measurement.
- Still very open research area.
- Adversarial examples are safety vulnerabilities of deep neural networks.
- Need more data and innovations in more robust learning objectives.