

1. The only polynomial of any degree such that $p(-1) = 1$, $p(0) = 0$ and $p(1) = 1$ is the quadratic polynomial $p(x) = x^2$.
2. Let $p(x) = x^3 + 3x^2 - x + 1$ and let $q \in \mathcal{P}_2$ denote the polynomial interpolation of p at $x_0 = 0$, $x_1 = 1$ and $x_2 = 2$. Then there exists a constant $C \neq 0$ such that error satisfies

$$\forall x \in \mathbb{R}, \quad p(x) - q(x) = C(x - x_0)(x - x_1)(x - x_2)$$

3. Given $x_0 < x_1 < \dots < x_n \in \mathbb{R}$ and $y_0, y_1, \dots, y_n \in \mathbb{R}$, there exist multiple polynomials $p \in \mathcal{P}_{n+1}$ such that $p(x_i) = y_i$ for all $i \in \{0, 1, \dots, n\}$.
4. In interpolation, the choice of interpolating points can have an influence on the accuracy of the interpolation.
5. Suppose that $f: [-1, 1] \rightarrow \mathbb{R}$ is the function which to x associates e^x , and for any $n \in \mathbb{N}$, let $f_n \in \mathcal{P}_n$ denote the polynomial interpolating f at $n + 1$ equidistant points $-1 = x_0 < x_1 < \dots < x_n = 1$. Then

$$\lim_{n \rightarrow \infty} \left(\max_{-1 \leq x \leq 1} |f(x) - f_n(x)| \right) = 0.$$

6. There exists a polynomial p such that

$$\forall n \in \mathbb{N}, \quad p(n) = 2^n.$$

7. In Julia, if A is a matrix, then $A[:, 1:2]$ gives the submatrix containing the first two rows of A .
8. In Julia, if A is a matrix, then $A[1:\text{end}, 2, 1:\text{end}, 2]$ gives the matrix obtained by removing the second column and the second row.
9. In Julia, typing `]` in a REPL (command line) enables to access package mode, from which new packages can be installed.
10. In the following code, p is the interpolating polynomial through the data in x and y .

```
using Plots
x = [0, 1, 2, 3]
y = [1, 2, 1, 2]

function p(x)
    return (y[1]
            + diff(y)[1] * x
            + 1/2 * diff(diff(y))[1] * x * (x-1)
            + 1/6 * diff(diff(diff(y)))[1] * x * (x-1) * (x-2))
end

plot(p, xlims=(0, 5))
scatter!(x, y)
```