

$$\sum_{\{(i,p):aa_{k,p}=1,dd_{i,p}=1\}} y_{i,p} \leq x_k r_k \quad \forall k \in K \quad (28)$$

$$\{y, z\} \in \mathbb{R}^+$$

The objective (24) minimizes the expected shortage over all scenarios. Constraint (25) enforces the budget. Constraint (27) ensures assigned demand plus shortage add up to point-to-point demand. Constraint (28) enforces capacity along each arc.

#### PS4-2b

Calculate EV.

Run a Python script in a Python shell to solve the problem. The associated deterministic model and scenario data can be found in the folder "PS4/4-2b". The optimal value is 6.1 and the optimal solution is as follows.

$x_{rp}$	
$x(1)$	7.07143
$x(2)$	0
$x(3)$	5.07143
$x(4)$	0
$x(5)$	2.92857
$x(6)$	4.92857
$x(7)$	0

#### PS4-2c

We cannot calculate  $WS$  exactly because it would involve solving  $4.1 * 10^7$  variables. Instead, form a sample mean estimate of  $WS$  based on a sample size of 100. State the point estimate and the associated approximate 95% confidence interval.

Run a Python script to solve the problem. The associated files can be found in the folder "PS4/4-2c". Using 50 samples, a point estimate of  $WS = 6.0$  and 95% CI = [5.11 6.89].

#### PS4-2d

Use the capacity expansion decision from part (b),  $x_{ev}$ , to form a sample mean estimate of  $EEV$  with a sample size of 100. State the point estimate and the associated approximate 95% confidence interval.

Run a Python script to solve the problem. The associated files can be found in the folder "PS4/4-2d". In the deterministic model, a constraint is added fixing the first stage variable  $x$  to  $x_{ws}$ . Using 50 samples, a point of  $EEV = 8.3$  and 95% CI = [7.29 9.31].

#### PS4-2e

Based on your calculations in part (c), form a capacity expansion decision,  $x_{ws}$ . Form a point estimate and approximate 95% confidence interval for  $EWS = cx_{ws} + Eh(x_{ws}, \xi)$ . Again, use a sample size of 100.

Run a Python script to solve the problem. The associated files can be found in the folder "PS4/4-2e". In the deterministic model, a constraint is added fixing the first stage variable  $x$  to  $x_{ws}$  (which is from PS3-c). Using 50 samples, a point of estimate of  $EWS = 7.3$  and 95% CI = [6.49 8.11].

#### PS4-2f

Solve this problem using the Monte Carlo sampling-based approach for assessing solution quality with common random number streams for upper and lower bound estimation. Solve one initial approximating problem in order to generate the candidate solution  $\hat{x}$ . Use  $n_g = 20$  replications. Choose the sample size,  $n$ , so that you obtain what you regard as "reasonable" results. State your recommended capacity-expansion decision and a confidence interval for the quality of the proposed solution.

Run a `computeconf` script to solve the problem, which implements the Mak/Morton/Wood multiple replication procedure to calculate the approximate gap of the stochastic solution. The associated files can be found in the folder "PS4/4-2f". To run, use the following command in the appropriate folder.

```
computeconf-m models -i scenariodata -scenario-tree-downsample-  
fraction=0.2 -solver=gurobi -solve-ef>PartFresults.txt
```

Run a Python script to solve the problem. The associated files can be found in the folder "PS4/4-2e". In the deterministic model, a constraint is added fixing the first stage variable  $x$  to  $x_w$  (which is from PS3-c). Using 50 samples, a point estimate of EWS = 7.3 and 95% CI = [6.49 8.11].

#### PS4-2f

Solve this problem using the Monte Carlo sampling-based approach for assessing solution quality with common random number streams for upper and lower bound estimation. Solve one initial approximating problem in order to generate the candidate solution  $\hat{x}$ . Use  $n_s = 20$  replications. Choose the sample size,  $n$ , so that you obtain what you regard as "reasonable" results. State your recommended capacity-expansion decision and a confidence interval for the quality of the proposed solution.

Run a computeconf script to solve the problem, which implements the Mak/Morton/Wood multiple replication procedure to calculate the approximate gap of the stochastic solution. The associated files can be found in the folder "PS4/4-2f". To run, use the following command in the appropriate folder.

```
computeconf -m models -i scenariodata --scenario-tree-downsample-
fraction=0.2 --solver=gurobi --solve-ef>PartResults.txt
```

$$\sum_{(i,p):m_{i,p}=1, (d_{i,p}=1)} y_{i,p} \leq x_k \quad \forall k \in K \quad (28)$$

$$\{y, z\} \in \mathbb{R}^+$$

The objective (24) minimizes the expected shortage over all scenarios. Constraint (25) enforces the budget. Constraint (27) ensures assigned demand plus shortage add up to point-to-point demand. Constraint (28) enforces capacity along each arc.

#### PS4-2b

Calculate EV.

Run a Python script in a Python shell to solve the problem. The associated deterministic model and scenario data can be found in the folder "PS4/4-2b". The optimal value is 6.1 and the optimal solution is as follows.

	$x_w$
$x(1)$	7.07143
$x(2)$	0
$x(3)$	5.07143
$x(4)$	0
$x(5)$	2.92857
$x(6)$	4.92857
$x(7)$	0

#### PS4-2c

We cannot calculate WS exactly because it would involve solving  $4.1 \cdot 10^7$  variables. Instead, form a sample mean estimate of WS based on a sample size of 100. State the point estimate and the associated approximate 95% confidence interval.

Run a Python script to solve the problem. The associated files can be found in the folder "PS4/4-2c". Using 50 samples, a point estimate of WS = 6.0 and 95% CI = [5.11 6.89].

#### PS4-2d

Use the capacity expansion decision from part (b),  $x_w$ , to form a sample mean estimate of EEV with a sample size of 100. State the point estimate and the associated approximate 95% confidence interval.

Run a Python script to solve the problem. The associated files can be found in the folder "PS4/4-2d". In the deterministic model, a constraint is added fixing the first stage variable  $x$  to  $x_w$ . Using 50 samples, a point estimate of EEV = 8.3 and 95% CI = [7.29 9.31].

#### PS4-2e

Based on your calculations in part (c), form a capacity expansion decision,  $x_w$ . Form a point estimate and approximate 95% confidence interval for EWS =  $\alpha x_w + E[h(x_w, \xi)]$ . Again, use a sample size of 100.

Work was done by Nikola Juskovica from REBC01

```

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\qqquad \qqquad $\displaystyle \sum_{\{(i,p):aa_{k,p}=1,dd_{i,p}=1\}} y_{i,p} \leq x_k r_k$ \hfill $
{\fontfamily{lmss}\selectfont
\text{(28)}
}
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\qqquad \qqquad $\{y,z\} \in {\rm I\!R}^+$

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\begin{flushleft}
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The objective (24) minimizes the expected shortage over all scenarios. Constraint (25) enforces th

Constraint (28) enforces capacity along each arc.
}
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{\color{gray}\textbf{PS4-2b}}

{\fontfamily{lmss}\selectfont
Calculate EV.
}
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Run a Python script in a Python shell to solve the problem. The associated deterministic model and

as follows.
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\multicolumn{2}{|c|}{$x_{rp}$} \\ \hline
$x(1)$ & 7.07143 \\ \hline
$x(2)$ & 0 \\ \hline
$x(3)$ & 5.07143 \\ \hline
$x(4)$ & 0 \\ \hline
$x(5)$ & 2.92857 \\ \hline
$x(6)$ & 4.92857 \\ \hline
$x(7)$ & 0 \\ \hline
\end{tabular}
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{\color{gray}\textbf{PS4-2c}}

```

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We cannot calculate  $WS$  exactly because it would involve solving  $4.1 \times 10^7$  variables. Instead, f

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Run a Python script to solve the problem. The associated files can be found in the folder "PS4/4-2

Using 50 samples, a point estimate of  $WS = 6.0$  and 95\% CI = [5.11 6.89].

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{\color{gray}\textbf{PS4-2d}}

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Use the capacity expansion decision from part (b),  $x_{ev}$ , to form a sample mean estimate of  $EE$

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Run a Python script to solve the problem. The associated files can be found in the folder "PS4/4-2

the deterministic model, a constraint is added fixing the first stage variable  $x$  to  $x_{ws}$ . Us

point of  $EEV = 8.3$  and 95\% CI = [7.29 9.31].

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{\color{gray}\textbf{PS4-2e}}

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Based on your calculations in part (c), form a capacity expansion decision,  $x_{ws}$ . Form a point

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Run a Python script to solve the problem. The associated files can be found in the folder "PS4/4-2

Using 50 samples, a point of estimate of  $EWS = 7.3$  and 95\% CI = [6.49 8.11].

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Solve this problem using the Monte Carlo sampling-based approach for assessing solution quality w

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Run a computeconf script to solve the problem, which implements the Mak/Morton/Wood multiple repli

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\textit{computeconf-m models -i scenariodata --scenario-tree-downsample-}

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\textit{fraction=0.2 --solver=gurobi --solve-ef>PartFresults.txt}  
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