In [9]:
```
# My standard magic !  You will see this in almost all my notebooks.

from IPython.core.interactiveshell import InteractiveShell
InteractiveShell.ast_node_interactivity = "all"

# Reload all modules imported with %aimport
%load_ext autoreload
%autoreload 1

%matplotlib inline
```

NumPy

VandePlas Chapter 2 (external/PythonDataScienceHandbook/notebooks/02.00-Introduction-to-NumPy.ipynb), Geron notebook (external/handson-ml/tools_numpy.ipynb)

Python lists

Lists are *heterogeneous*: can contain elements of mixed type

In [1]:
```
l = list( range(0,10) )
print(l)
```

```
[0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
```

In [2]:
```
l[2] = "two"
print(l)
```

```
[0, 1, 'two', 3, 4, 5, 6, 7, 8, 9]
```

Heterogeneity == *slow*

- Python interpreter has to constantly examine types

NumPy ndarray

In [3]:
```
import numpy as np
```

NumPy n-dimensional arrays (`ndarray`) are *homogenous*

- Can be faster because don't waste time examining type of each element
- Can be treated as vectors
- Vector arithmetic via compiled code = *fast*

In [4]:
```
l = list( range(0,10))
l_plus_1 = [ e+1 for e in l]
print(l_plus_1)
```

```
[1, 2, 3, 4, 5, 6, 7, 8, 9, 10]
```

In [5]:
```
l_np = np.array( np.arange(0,10))
print(l_np +1)
```

```
[ 1  2  3  4  5  6  7  8  9 10]
```

Speed comparison

In [6]:
```
list_len = 1000
l = list( range(0, list_len))
%timeit [ e+1 for e in l]
```

```
32.9 µs ± 132 ns per loop (mean ± std. dev. of 7 runs, 10000 loops each)
```

In [7]:
```
l_np = np.array( np.arange(0, list_len) )
%timeit l_np +1
```

```
1.04 µs ± 6.71 ns per loop (mean ± std. dev. of 7 runs, 1000000 loops each)
```

When dealing with large datasets, you need NumPy

Basics of NumPy arrays

VanderPlas (external/PythonDataScienceHandbook/notebooks/02.02-The-Basics-Of-NumPy-Arrays.ipynb)

Vandeplas YouTube: Losing your loops - slides (https://speakerdeck.com/jakevdp/losing-your-loops-fast-numerical-computing-with-numpy-pycon-2015?slide=14)

The most operation on ndarrays is indexing.

- ndarray indices are 0-based (i.e, first row/col is numbered 0, not 1)

In [10]:
```
x = np.arange(0,6)

x

x[2]

M = np.arange(0,6).reshape(2,3)
M

M[1,1]
```

Out[10]:
```
array([0, 1, 2, 3, 4, 5])
```

Out[10]:
```
2
```

Out[10]:
```
array([[0, 1, 2],
       [3, 4, 5]])
```

Out[10]:
```
4
```

Slicing

- Python (not just NumPy) upper bound of index is NOT inclusive

In [11]:
```
print("x: ", x)
print("x tail: ", x[2:])
print("x head: ", x[:2])
```

```
x:  [0 1 2 3 4 5]
x tail:  [2 3 4 5]
x head:  [0 1]
```

Strides

```
x[start:stop:step]
```

In [12]:
```
x[1:5:2]
```

Out[12]:
```
array([1, 3])
```

Reshaping

In [12]:
```
grid = np.arange(1, 10).reshape((3, 3))
print(grid)
```

```
[[1 2 3]
 [4 5 6]
 [7 8 9]]
```

Add dimensions

In [13]:
```
x = np.arange(0,6)
print("x: ", x)
print("x shape: ", x.shape)

print("x re-shaped: ", x.reshape(1,-1))
print("x re-shaped shape: ", x.reshape(1,-1).shape)

print("x w/newaxis: ", x[ np.newaxis,:])
print("x w/newaxis sja[e: ", x[ np.newaxis,:].shape)
```

```
x:  [0 1 2 3 4 5]
x shape:  (6,)
x re-shaped:  [[0 1 2 3 4 5]]
x re-shaped shape:  (1, 6)
x w/newaxis:  [[0 1 2 3 4 5]]
x w/newaxis sja[e:  (1, 6)
```

Concatentation, splitting

In [14]:
```
x = np.array([1, 2, 3])
y = np.array([3, 2, 1])
x
y

np.concatenate([x, y])
```

Out[14]:
```
array([1, 2, 3])
```

Out[14]:
```
array([3, 2, 1])
```

Out[14]:
```
array([1, 2, 3, 3, 2, 1])
```

You can concatenate multi-dimensional ndarrays:

In [15]:
```
M1 = np.array([ [1, 2, 3],
                [4, 5, 6]
              ])

M2 = np.array([ [ 7,  8,  9 ],
                [ 10, 11, 12]
              ])

M1
M2

np.concatenate([ M1, M2 ])
```

Out[15]:
```
array([[1, 2, 3],
       [4, 5, 6]])
```

Out[15]:
```
array([[ 7,  8,  9],
       [10, 11, 12]])
```

Out[15]:
```
array([[ 1,  2,  3],
       [ 4,  5,  6],
       [ 7,  8,  9],
       [10, 11, 12]])
```

You can also specify the dimension on which to concatenate

In [16]:
```
M1
M2

np.concatenate([ M1, M2 ], axis=1)
```

Out[16]:
```
array([[1, 2, 3],
       [4, 5, 6]])
```

Out[16]:
```
array([[ 7,  8,  9],
       [10, 11, 12]])
```

Out[16]:
```
array([[ 1,  2,  3,  7,  8,  9],
       [ 4,  5,  6, 10, 11, 12]])
```

You can also use `vstack` (vertical stack) and `hstack` (horizontal stack)

In [17]:
```
x = np.array([1, 2, 3])
grid = np.array([[9, 8, 7],
                 [6, 5, 4]])

y = np.array( [ [100],
                [200]
              ])
x
grid

print("vstack:")
# vertically stack the arrays
np.vstack([x, grid])

print("hstack:")
y
grid
np.hstack( [y, grid])
```

Out[17]:
```
array([1, 2, 3])
```

Out[17]:
```
array([[9, 8, 7],
       [6, 5, 4]])
```

```
vstack:
```

Out[17]:
```
array([[1, 2, 3],
       [9, 8, 7],
       [6, 5, 4]])
```

```
hstack:
```

Out[17]:
```
array([[100],
       [200]])
```

```
Out[17]:  array([[9, 8, 7],
                 [6, 5, 4]])
```

```
Out[17]:  array([[100,   9,   8,   7],
                 [200,   6,   5,   4]])
```

Ufuncs

Vandeplass (external/PythonDataScienceHandbook/notebooks/02.03-Computation-on-arrays-ufuncs.ipynb#Introducing-UFuncs)

Math

- element-wise operations
- vectorized for speed
- operator overloading
    - +, -, *, /
    - <, ==, >
    - provides natural syntax
        - `l + 1`
        - `np.add(l,1)

In [18]:
```
x = np.array( np.arange(0,10))
print("x: ", x)
print("+1: ", x + 1)
print("+1 verbose: ", np.add(x,1))
print("-1: ", x -1)
```

```
x:  [0 1 2 3 4 5 6 7 8 9]
+1:  [ 1  2  3  4  5  6  7  8  9 10]
+1 verbose:  [ 1  2  3  4  5  6  7  8  9 10]
-1:  [-1  0  1  2  3  4  5  6  7  8]
```

Aggregates

Vanderplass (external/PythonDataScienceHandbook/notebooks/02.03-Computation-on-arrays-ufuncs.ipynb#Aggregates)

- Aggregation: taking a one-dimensional slice of an ndarray and reducing it to a scalar
    - also known as **reduce**

Best illustrated with an example

In [19]:
```
x = np.arange(1, 6)
print("x: ", x)
print("x reduced by add: ",np.add.reduce(x))

# Less verbose synonym
print("x reduced by add, via sum", x.sum())
```

```
x:  [1 2 3 4 5]
x reduced by add:  15
x reduced by add, via sum 15
```

Aggregates on multi-dimensional ndarray: choose your dimension

In [20]:
```
x = np.arange(1,7).reshape(2,3)
print("x: ", x)

print("x reduced on first dimension: ", x.sum(axis=0))

print("x reduced on second dimension: ", x.sum(axis=1))
```

```
x:  [[1 2 3]
 [4 5 6]]
x reduced on first dimension:  [5 7 9]
x reduced on second dimension:  [ 6 15]
```

Cumulative

Closely related to `reduce`: `accumulate`

```
 - running operations, e.g, running sum
```

In [21]:
```
print("x: ", x)
print("x running sum: ", np.add.accumulate(x))  # NOTE: not a method ON x; x is
 a parameter

# Less verbose synonym. n.b., WITHOUT an axis arg,, it will flatten x before sum
ming
print("x running sum via cumsum: ", x.cumsum(axis=0))
```

```
x:  [[1 2 3]
 [4 5 6]]
x running sum:  [[1 2 3]
 [5 7 9]]
x running sum via cumsum:  [[1 2 3]
 [5 7 9]]
```

Broadcasting

Vanderplass (external/PythonDataScienceHandbook/notebooks/02.05-Computation-on-arrays-broadcasting.ipynb)

You hopefully intuitively understand what NumPy does when a binary operator is applied to 2 identically-shaped arguments

In [22]:
```
a = np.array([0, 1, 2])
b = np.array([5, 5, 5])
a + b
```

Out[22]:
```
array([5, 6, 7])
```

But what happens if the two arguments have different shape ? Simplest case: one argument is dimension 0 or 1:

In [23]:
```
print("a: ", a)
print("a + 1: ", a+1)
```

```
a:  [0 1 2]
a + 1:  [1 2 3]
```

Next case: what if one argument is identical to the other EXCEPT is missing a dimension:

In [24]:
```
M = np.arange(1,10).reshape(3,3)

print("a shape (", a.shape, "): ", a)
print("M shape (", M.shape, "):\n", M)
print("a + M shape(", (a+M).shape, "):\n", a + M)
```

```
a shape ( (3,) ):  [0 1 2]
M shape ( (3, 3) ):
 [[1 2 3]
 [4 5 6]
 [7 8 9]]
a + M shape( (3, 3) ):
 [[ 1  3  5]
 [ 4  6  8]
 [ 7  9 11]]
```

NumPy took a one dimensional ndarray `a` and treated it like a 2-d ndarray by repeated it's rows

This is called **broadcasting**

Broadcasting follows some simple rules (quoted from Vanderplass (external/PythonDataScienceHandbook/notebooks/02.05-Computation-on-arrays-broadcasting.ipynb)):