

## GROUP BLUE MATHS NOTES, EXERCISES AND ASSIGNMENTS

### TOPIC: LONGITUDES AND LATITUDES

#### Instructions

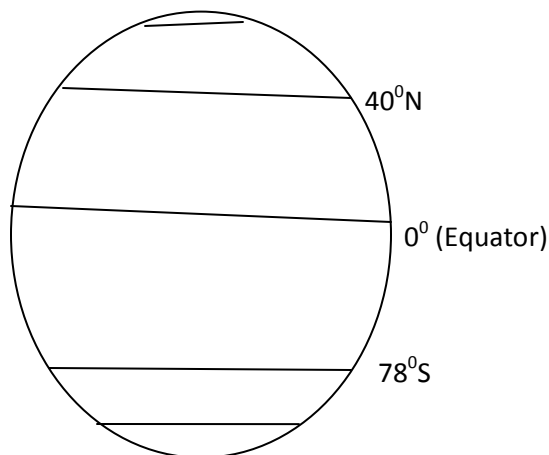
- Read the notes keenly
- Study the examples given carefully
- Sketching the question is very important
- In some worked examples, the working is displayed but the final answer **NOT** given. In such cases provide the answer.
- Attempt all the questions given after each subtopic.

#### LONGITUDES AND LATITUDES

- Longitudes and latitudes are imaginary lines drawn on the earth's surface.
- They are used to locate positions of places on the earth's surface.

#### LATITUDES

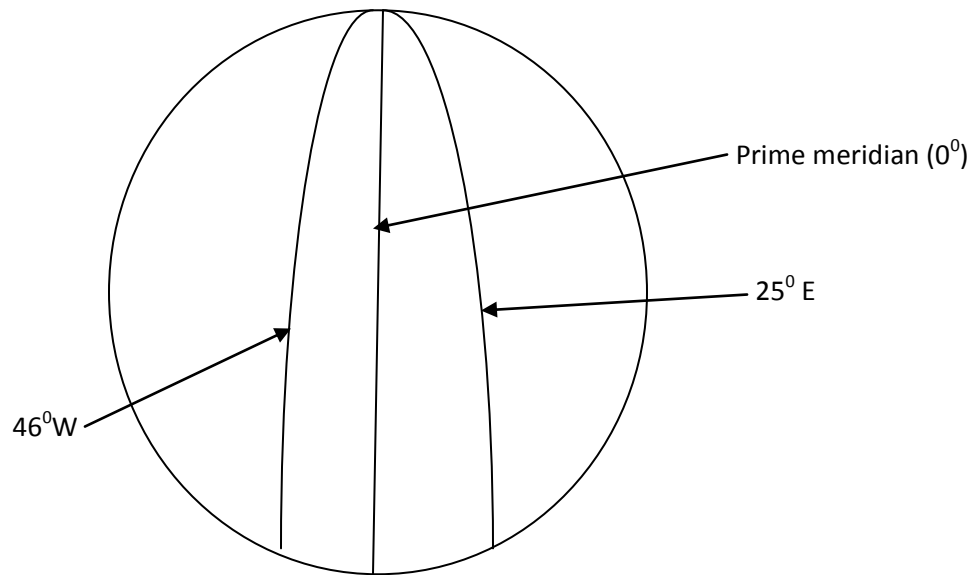
- These are imaginary lines drawn on the earth's surface.
- They run from West to East
- The **main** latitude is the Equator and is assigned  $0^{\circ}$  and is used as the reference latitude.
- All other latitudes are measured North or South of Equator.
- Latitudes run from  $0^{\circ}$  to  $90^{\circ}$  North and from  $0^{\circ}$  to  $90^{\circ}$  South of equator. e.g. the latitude  $31^{\circ}$  south of equator is written as  $31^{\circ}\text{S}$  and the latitude  $45^{\circ}$  north of equator is written as  $45^{\circ}\text{N}$ .



#### LONGITUDES (Meridians)

- These are imaginary lines drawn on the earth's surface.
- They run from North to South
- The **main** longitude is the Prime meridian or Greenwich Meridian and is assigned  $0^{\circ}$  and is used as the reference longitude.
- All other longitudes are measured East or West of Prime meridian.

- Longitudes run from  $0^{\circ}$  to  $180^{\circ}$  East and from  $0^{\circ}$  to  $180^{\circ}$  West of Prime meridian. e.g. the longitude  $71^{\circ}$  East of Prime meridian is written as  $71^{\circ}$ E and the longitude  $105^{\circ}$  West of Prime meridian is written as  $105^{\circ}$ W



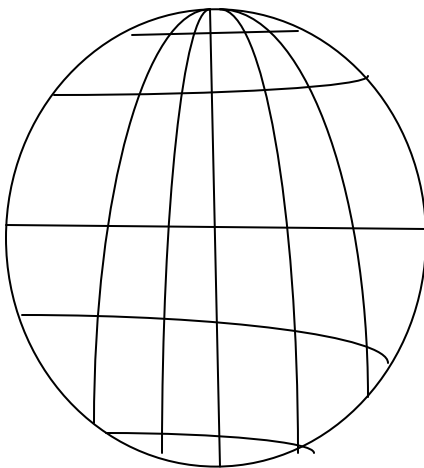
### **POSITION OF A PLACE ON THE EARTH'S SURFACE**

- Any position on the earth's surface is defined by the intersection of its latitude and longitude.
- It is given by the ordered pair of coordinates (latitude, longitude) e.g. a town P is on latitude  $37^{\circ}$ S and longitude  $139^{\circ}$ East, its position is written as P( $37^{\circ}$ S,  $139^{\circ}$ E)

### **WORKED EXAMPLES AND EXERCISE**

1. Use the figure below to give the position of the following points.

a) A   b)B   c) C   d)D   e)E   f) F   g) G   h) H



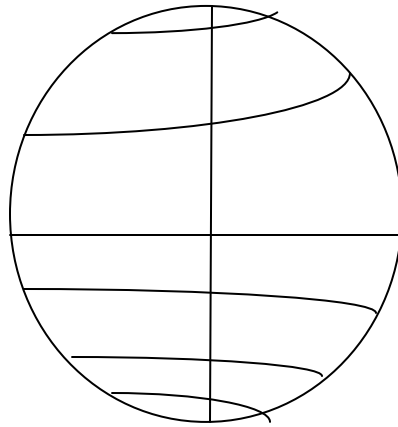
A( $20^{\circ}$ N,  $15^{\circ}$ W)

B( $5^{\circ}$ S,  $10^{\circ}$ E)

C( $0^{\circ}$ ,  $100^{\circ}$ W)

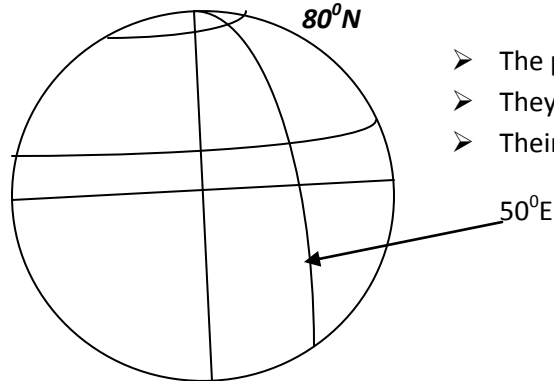
'Do the rest'

2. Using the sketch below of the earth's surface, locate the given points whose positions are given.  
 A( $45^{\circ}\text{N}$ ,  $20^{\circ}\text{W}$ ), B( $36^{\circ}\text{S}$ ,  $82^{\circ}\text{E}$ ), C( $0^{\circ}$ ,  $20^{\circ}\text{W}$ ), D( $45^{\circ}\text{N}$ ,  $82^{\circ}\text{E}$ ), E( $36^{\circ}\text{S}$ ,  $20^{\circ}\text{W}$ ), F( $45^{\circ}\text{N}$ ,  $0^{\circ}$ )



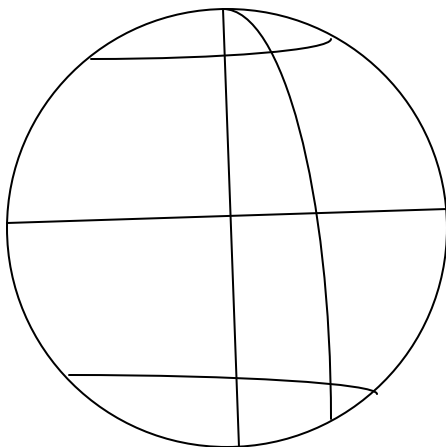
**LATITUDE DIFFERENCE FOR POINTS ON THE SAME LONGITUDE**

**CASE 1**



- The points P and Q lie on the same longitude ( $50^{\circ}\text{E}$ )
- They lie on the same side of equator i.e. North
- Their latitude difference is  $(80^{\circ} - 10^{\circ}) = 70^{\circ}$

**CASE 2**



- The points P and Q lie on the same longitude ( $72^{\circ}\text{E}$ )
- They lie on the opposite side of equator
- Their latitude difference is  $(40^{\circ} + 52^{\circ}) = 92^{\circ}$
- **NB.** If the points lie on the opposite sides of equator , latitude difference is the sum of the angles of the latitudes .

### WORKED EXAMPLES AND EXERCISE

Complete the table below. Points A and B lie on the same longitude.

	Latitude of A	Latitude of B	Latitude difference
a)	43°N	83°N	$83 - 43 = 40^0$
b)	62°S	14°S	$62 - 14 = 48^0$
c)	40°N	36°S	$40 + 36 = 76^0$
d)	13°S	88°S	
e)	60°N	15°N	
f)	53°S	32°N	
g)	25°N	38°S	

### LONGITUDE DIFFERENCE FOR POINTS ON THE SAME LATITUDE

- Longitude difference is calculated the same way as latitude difference i.e. same as the two cases above

Complete the table below. P and Q lie on the same latitude.

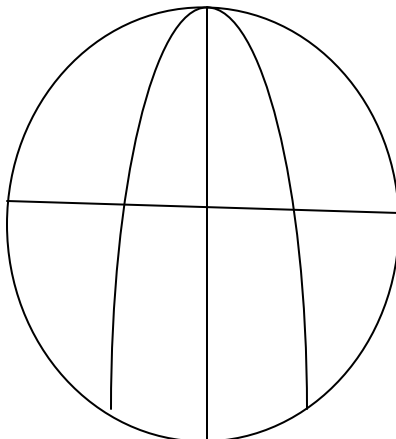
	Longitude of P	Longitude of Q	Longitude difference
a)	42°	150°	$150 - 42 = 108^0$
b)	100°	172°	$172 - 100 = 72^0$
c)	30°	80°	$80 + 30 = 110^0$
d)	136°	20°	
e)	10°	38°	
f)	90°	12°	
g)	14°	83°	

### GREAT AND SMALL CIRCLES

- Longitudes and latitudes can be grouped as great and small circles.

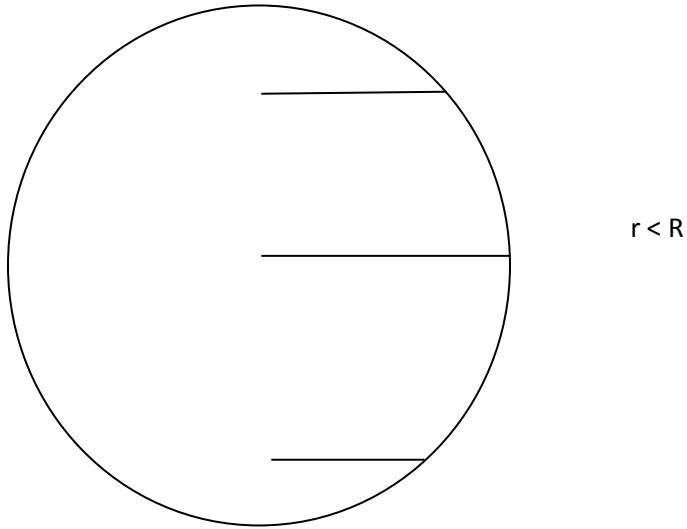
#### GREAT CIRCLE

- A great circle is a circle that has the same radius as that of the earth.
- All longitudes have the same radius as that of the earth.
- Equator has the same radius as that of the earth.
- Therefore all longitudes and equator are great circles.
- N.B. The only latitude which is a great circle is the equator



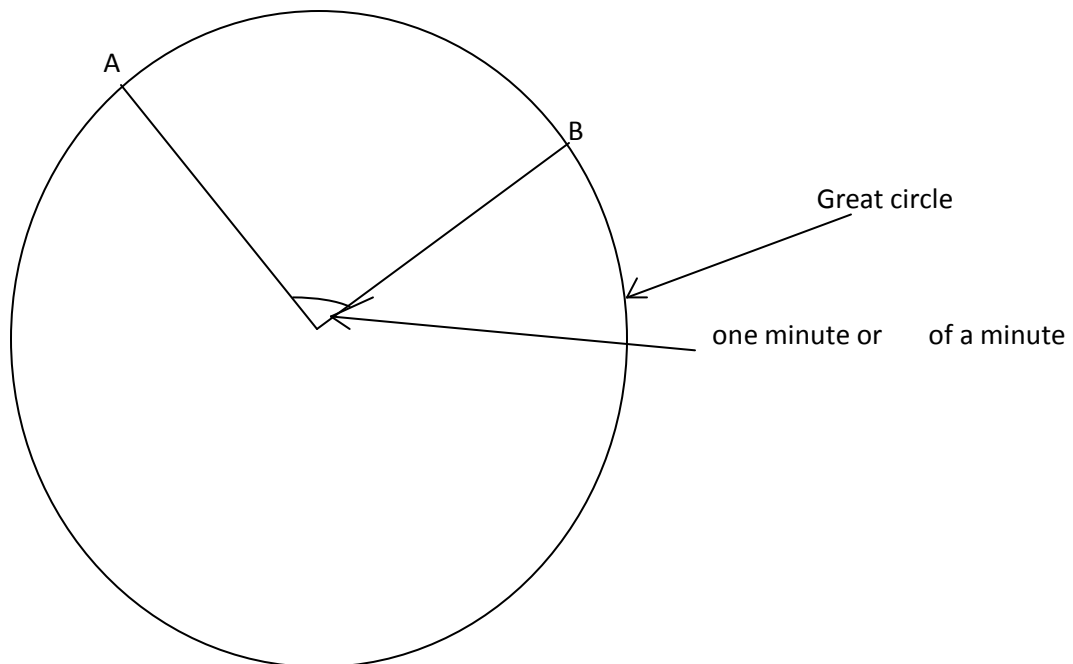
### **SMALL CIRCLES (CIRCLES OF LATITUDES)**

- A small circle or a circle of latitude is a circle whose radius is smaller than that of the earth.
- All latitudes except equator are small circles.



### **NAUTICAL MILE (nm)**

- A nautical mile(nm) is the SI unit for measuring distances covered by ships and aeroplanes.
- Consider the figure below.



- The arc AB subtends an angle of one minute( $1'$ ) at the centre of a great circle.
- The arc length AB is equivalent to 1 nautical mile.
- Hence a nautical mile is the length of an arc of a great circle that subtends an angle of one minute ( $1'$ ) at the centre of the earth.

- **N.B**  $1^{\circ} = 60'$  (60 minutes) , hence  $1^{\circ}$  is subtended by an arc length of 60 nm

$1^{\circ} = 60 \text{ nm}$
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**DISTANCE ALONG A GREAT CIRCLE IN NAUTICAL MILES (nm)**

- To find the distance in nautical miles along a great circle, we use the formula

$L = 60a$  where  $a$  is;

- (i) Latitude difference if the points lie on the same longitude
- (ii) Longitude difference if the points lie on Equator

**WORKED EXAMPLES AND EXERCISE**

1. Calculate the distance in nautical miles between the following points

- a) A( $20^{\circ}\text{S}$ ,  $40^{\circ}\text{E}$ ) and B( $85^{\circ}\text{S}$ ,  $40^{\circ}\text{E}$ )

Soln;

Both points A and B lie on the same longitude ( $40^{\circ}\text{E}$ ) which is a great circle

$$L = 60a$$

$a$  = difference in latitudes

$$= 85 - 20$$

$$= 65^{\circ}$$

$$L = 60 \times 65$$

$$= \text{-----} \text{ nm}$$

- b) P( $0^{\circ}$ ,  $36^{\circ}\text{E}$ ) and B( $0^{\circ}$ ,  $113^{\circ}\text{E}$ )

Soln;

Both points P and Q lie on the same latitude ( $0^{\circ}$ ) equator which is a great circle

$$L = 60a$$

$a$  = difference in longitudes

$$= 113 - 36$$

$$= 77^{\circ}$$

$$L = 60 \times 77$$

$$= \text{-----} \text{ nm}$$

- c) X( $30^{\circ}\text{N}$ ,  $15^{\circ}\text{W}$ ) and Y( $72^{\circ}\text{S}$ ,  $15^{\circ}\text{W}$ )

Soln;

Both points X and Y lie on the same longitude ( $15^{\circ}\text{W}$ ) which is a great circle

X and Y lie on the opposite sides of equator and hence latitude difference is the sum of latitudes

$$L = 60a$$

$a$  = sum of angles of latitudes

$$= 72 + 30$$

$$= 102^{\circ}$$

$$L = 60 \times 102$$

$$= \text{----- nm}$$

- d) K( $0^{\circ}$ ,  $16^{\circ}$ E) and L( $0^{\circ}$ ,  $54^{\circ}$ W)

Soln;

Both points K and L lie on Equator and on the opposite sides of Prime meridian. Hence longitude difference is the sum of longitudes

$$L = 60a$$

a = sum of angles of longitudes

$$= 54 + 16$$

$$= 70^{\circ}$$

$$L = 60 \times 70$$

$$= \text{----- nm}$$

2. A plane flew northwards from a base V( $20^{\circ}$ N,  $50^{\circ}$ W) to a base W covering 1500 nm. Find the

a) Latitude difference

b) Position of W

Soln;

When a body moves northwards or southwards, it follows a great circle; hence the formula to apply is

$$L = 60a$$

$$\text{a) } 1500 = 60a$$

$$a = \frac{1500}{60}$$

$$a = 25^{\circ}$$

b) Moving from  $20^{\circ}$ N northwards, the angle of latitude increases by  $25^{\circ}$

$$\text{New latitude} = 20 + 25$$

$$= 45^{\circ}\text{N}$$

$$\text{Position of W } (45^{\circ}\text{N}, 50^{\circ}\text{W})$$

3. A plane flew southwards from a base H( $10^{\circ}$ N,  $30^{\circ}$ W) to a base J covering 3900 nm. Find the

a) Latitude difference

b) Position of J

Soln;

When a body moves northwards or southwards, it follows a great circle; hence the formula to apply is  $L = 60a$

$$\text{a) } L = 60a$$

$$3900 = 60a$$

$$a = \frac{3900}{60}$$

$$a = 65^{\circ}$$

b) Since  $65^{\circ}$  is greater than  $10^{\circ}$  (latitude) then J is in South of equator

$$\text{New latitude} = 65 - 10$$

$$= 55^{\circ}\text{S}$$

$$\text{Position of J } (55^{\circ}\text{S}, 30^{\circ}\text{W})$$

### **EXERCISE**

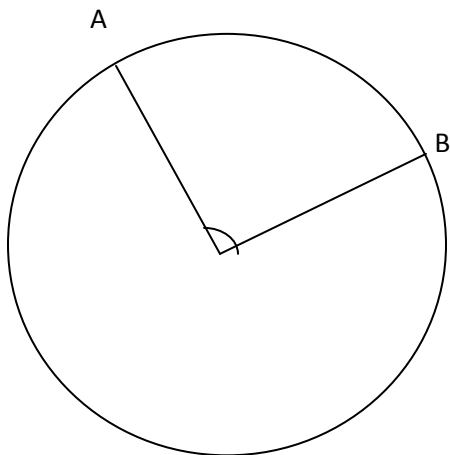
1. Calculate the distance in nautical miles between the following points.

	A	B
a)	(30°N, 18°W)	(70°N, 18°W)
b)	(14°S, 10°E)	(2°S, 10°E)
c)	(25°N, 32°W)	(16°S, 32°W)
d)	(0°, 142°W)	(0°, 78°W)
e)	(0°, 58°E)	(0°, 96°W)
f)	(25.6°N, 140°E)	(82°N, 140°E)

2. A plane flew northwards from a base situated at (70°S, 10°E) for a distance of 2160 nm to another base. Find its new
- Latitude
  - Position
3. A ship sailed from a harbor H(15°N, 36°E) to another harbor J situated to the south of H. If it covered 2700 nm, find the position of J.
4. A jet flew northwards from a base P(30°S, 100°E) for 1800 nm to a base Q. From Q it flew westwards to another base R for a further distance of 9000 nm. Find the position of Q and R.

### **DISTANCE ALONG A GREAT CIRCLE IN KILOMETRES**

- Consider the circle below of radius R.



- Arc AB subtends an angle of  $a^\circ$  at the centre O.
- The length of the arc AB is given by the formula

$$L = \frac{a}{360} \times \text{circumference}$$

$$L = \frac{a}{360} \times 2\pi R$$

- Similarly, if points A and B lie on a great circle and R is the radius of the earth, the distance along a great circle in kilometers is given by the formula

$$L = \frac{a}{360} \times 2\pi R \quad \text{where} \quad \text{(i) } R \text{ is the radius of the earth, } R = 6370 \text{ km}$$

(ii)  $a$  is the latitude difference or longitude difference (for points on the equator)



### **WORKED EXAMPLES**

Take  $\pi = 22/7$  and  $R = 6370$  km

1. Find the distance in km between the given point

a) K( $30^\circ\text{N}$ ,  $0^\circ$ ), L( $60^\circ\text{N}$ ,  $0^\circ$ )

Soln;

K and L lie on the same longitude  $0^\circ$ , hence on a great circle

$$L = \frac{a}{360} \times 2\pi R$$

a = latitude difference

$$= 60 - 30$$

$$= 30^\circ$$

$$L = \frac{30}{360} \times 2 \times \frac{22}{7} \times 6370$$

$$L = \dots\dots\dots \text{ Km}$$

b) F( $20^\circ\text{S}$ ,  $112^\circ\text{W}$ ), G( $25^\circ\text{N}$ ,  $112^\circ\text{W}$ )

Soln;

F and G lie on the same longitude  $112^\circ\text{W}$ , hence on a great circle and on opposite sides of equator

$$L = \frac{a}{360} \times 2\pi R$$

a = latitude difference (sum)

$$= 20 + 25$$

$$= 45^\circ$$

$$L = \frac{45}{360} \times 2 \times \frac{22}{7} \times 6370$$

$$L = \dots\dots\dots \text{ km}$$

c) A( $0^\circ$ ,  $50^\circ\text{E}$ ), B( $0^\circ$ ,  $100^\circ\text{W}$ )

Soln;

A and B lie on the Equator (great circle) and on opposite sides of Prime meridian

$$L = \frac{a}{360} \times 2\pi R$$

a = longitude difference (sum)

$$= 50 + 100$$

$$= 150^\circ$$

$$L = \frac{150}{360} \times 2 \times \frac{22}{7} \times 6370$$

$$L = \dots\dots\dots \text{ Km}$$

2. A ship sailed southwards from a port T(80°N, 20°E) to another port S 10010 km away. Find
- Its new latitude
  - Position of S

Soln

The ship followed a great circle

$$L = \frac{a}{360} \times 2\pi R$$

$$a = \frac{360l}{2\pi R}$$

$$a = \frac{360 \times 10010}{2 \times \frac{22}{7} \times 6370}$$

$$a = \dots\dots\dots$$

$$\text{New latitude} = \dots\dots\dots$$

$$\text{b) Position of S} = \dots\dots\dots$$

### **EXERCISE**

In this exercise take  $\pi = \frac{22}{7}$  and radius of the earth  $R = 6370$  km

1. Find the distance in km between the following points

	A	B
a)	(40°N, 10°E)	(86°N, 10°E)
b)	(0°, 50°W)	(0°, 10°W)
c)	(36°S, 90°E)	(54°N, 90°E)
d)	(0°, 15°W)	(0°, 60°E)
e)	(40°S, 20°W)	(78°S, 20°W)

2. A jet flew eastwards from a base P(0°, 54°W) to another base Q covering 20020 km. Find the
- longitude difference between P and Q.
  - position of Q.
3. Two points X and Y lie on longitude 80°W and they are 1280 km apart. If the position of X(6°S, 80°W), find
- to 1 decimal place, the latitude difference
  - the latitude of Y and hence its position

### **DISTANCE ALONG A SMALL CIRCLE IN NAUTICAL MILES (nm)**

- The distance along a small circle (circle of latitude) is given by the formula
- $$L = 60a \cos \theta \quad \text{where } a = \text{longitude difference and } \theta = \text{angle of latitude}$$

### **WORKED EXAMPLES**

1. Find the distance in nautical miles between the following points
- P(40°N, 20°E) Q(40°N, 120°E)

Soln;

P and Q lie on the same latitude  $40^{\circ}\text{N}$  (small circle)

$$L = 60a\cos\theta$$

$a$  = longitude difference

$$= 120 - 20$$

$$= 100^{\circ}$$

$$L = 60 \times 100 \times \cos 40^{\circ}$$

$$L = \dots\dots\dots \text{ nm}$$

b)

U( $60^{\circ}\text{S}$ ,  $10^{\circ}\text{E}$ )   V( $60^{\circ}\text{S}$ ,  $30^{\circ}\text{W}$ )

Soln;

U and V lie on the same latitude  $60^{\circ}\text{S}$  (small circle) and on the opposite sides of [Prime meridian]

$$L = 60a\cos\theta$$

$a$  = longitude difference

$$= 10 + 30$$

$$= 40^{\circ}$$

$$L = 60 \times 40 \times \cos 60^{\circ}$$

$$L = \dots\dots\dots \text{ nm}$$

2. Two points lying on the same latitude have a longitude difference of  $80^{\circ}$  and are 2400 nm apart. Find their latitude.

Soln

$$L = 60a\cos\theta \quad a = 80^{\circ}$$

$$\cos\theta = L \div (60a)$$

$$\cos\theta = 2400 \div (60 \times 80)$$

$$\cos\theta = 0.5$$

$$\theta = \cos^{-1}0.5$$

$$\theta = 60^{\circ}$$

Latitude is  $60^{\circ}\text{N}$  or  $60^{\circ}\text{S}$

3. P and Q lie on the same latitude to the south of equator. P is on longitude  $20^{\circ}\text{E}$  and Q is on  $70^{\circ}\text{E}$ . If they are 2700 nm apart, find their latitude to the nearest tenth of a degree

Soln;

$$L = 60a \cos \Theta \quad a = 70 - 20 = 50^\circ$$

$$\cos \Theta = L \div (60a)$$

$$\cos \Theta = 2700 \div (60 \times 50)$$

$$\cos \Theta = 0.9$$

$$\Theta = \cos^{-1} 0.9$$

$$\Theta = 25.84^\circ$$

Latitude is  $25.8^\circ \text{S}$

### **EXERCISE**

1. Calculate the distance in nautical miles between the following points.

	P	Q
a)	( $20^\circ \text{S}$ , $40^\circ \text{E}$ )	( $20^\circ \text{S}$ , $100^\circ \text{E}$ )
b)	( $60^\circ \text{N}$ , $20^\circ \text{W}$ )	( $60^\circ \text{N}$ , $70^\circ \text{E}$ )
c)	( $10^\circ \text{S}$ , $100^\circ \text{W}$ )	( $10^\circ \text{S}$ , $15^\circ \text{W}$ )
d)	( $64^\circ \text{N}$ , $12^\circ \text{W}$ )	( $64^\circ \text{N}$ , $88^\circ \text{E}$ )

2. Two points lying on the same latitude south of equator are 1500 nm apart. Their longitude difference is 800. Find their latitude to the nearest degree.

DISTANCE ALONG A SMALL CIRCLE IN KILOMETRES (KM)

- Distance along a small circle (circle of latitude) is given by the formula

$$L = \frac{a}{360} \times 2\pi R \cos \Theta$$

Where  $a$  = longitude difference

$R$  = radius of the earth

$\Theta$  = angle of latitude

### **WORKED EXAMPLES**

Take  $\pi = 22/7$ ,  $R = 6370 \text{ km}$

1. Calculate the distance in km between the following points.

a) J( $20^\circ \text{N}$ ,  $18^\circ \text{E}$ ), L( $20^\circ \text{N}$ ,  $115^\circ \text{E}$ )

Soln;

J and L lie on the same latitude  $20^\circ \text{N}$  (small circle)

$$L = \frac{a}{360} \times 2\pi R \cos \Theta$$

$a$  = longitude difference

$$= 115 - 18$$

$$= 97^\circ$$

$R = 6370 \text{ km}$

$$\Theta = 20^\circ$$

$$L = \frac{97}{360} \times 2 \times \frac{22}{7} \times 6370 \times \cos 20^\circ$$

$$L = \dots\dots\dots \text{ km}$$

- b) C(35°S, 25°W), D(35°S, 90°E)

Soln;

C and D lie on the same latitude 35°S (small circle)

$$L = \frac{a}{360} \times 2\pi R \cos \theta$$

a = longitude difference

$$= 25 + 90$$

$$= 115^\circ$$

$$R = 6370 \text{ km}$$

$$\theta = 35^\circ$$

$$L = \frac{115}{360} \times 2 \times \frac{22}{7} \times 6370 \times \cos 35^\circ$$

$$L = \dots\dots\dots \text{ km}$$

2. X and Y are two points on the same latitude north of equator. They are 3336.67 km apart and their longitude difference is 60°. Find their latitude.

Soln;

$$L = \frac{a}{360} \times 2\pi R \cos \theta$$

$$\cos \theta = 360l \div (2a\pi R)$$

$$= 360 \times 3336.67 \div (2 \times 60 \times \frac{22}{7} \times 6370)$$

$$= 0.5$$

$$\theta = \cos^{-1} 0.5$$

$$\theta = 60^\circ \text{N}$$

### **EXERCISE**

Find the distance in km between the following points. Take  $\pi = \frac{22}{7}$ ,  $R = 6370 \text{ km}$

	X	Y
a)	(40°S, 40°E)	(40°S, 160°E)
b)	(27°N, 20°W)	(27°N, 70°E)
c)	(80°S, 130°W)	(80°S, 15°W)
d)	(64°N, 12°W)	(64°N, 98°E)
e)	(16°S, 56°E)	(16°S, 27°W)

### **SHORTEST DISTANCE BETWEEN TWO POINTS ON THE EARTH'S SURFACE**

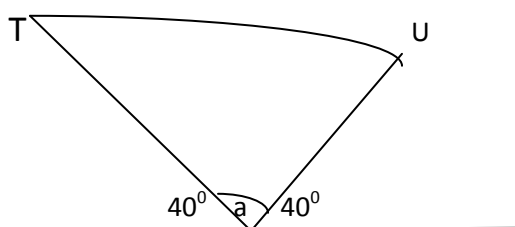
- If the sum of longitudes of two points is  $180^\circ$ , the two points lie on the same great circle, e.g. P( $60^\circ\text{N}$ ,  $125^\circ\text{E}$ ), Q( $34^\circ\text{N}$ ,  $55^\circ\text{W}$ )
- The sum of longitudes of A and B is  $125^\circ + 55^\circ = 180^\circ$
- Therefore the two points lie on the same great circle
- The shortest distance between such points is along the great circle

### WORKED EXAMPLES

1. The positions of T and U are T( $40^\circ\text{N}$ ,  $84^\circ\text{E}$ ) and U( $40^\circ\text{N}$ ,  $96^\circ\text{W}$ ). Calculate the shortest distance between them in nautical miles.

Soln;

Sum of longitudes =  $84 + 96 = 180^\circ$ , hence the two points lie on the same great circle.



$$a = 180 - (40 + 40)$$

$$= 100^\circ$$

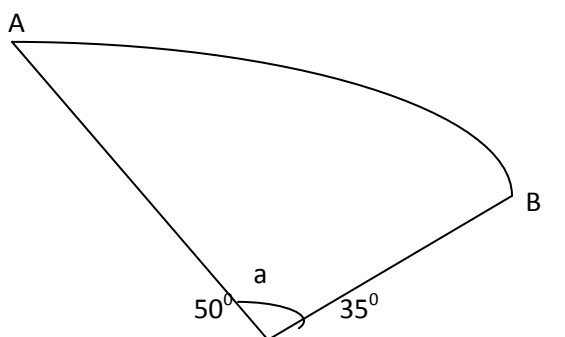
$$L = 60a$$

$$= 60 \times 100$$

$$= 6000 \text{ nm}$$

2. Find the shortest distance between the following points A( $35^\circ\text{S}$ ,  $60^\circ\text{W}$ ) and B ( $50^\circ\text{S}$ ,  $120^\circ\text{E}$ )

Soln.



$$\text{Sum of longitudes} = 60 + 120$$

$$= 180$$

$$a = 180 - (35 + 50)$$

$$= 95^\circ$$

$$L = 60a$$

$$= 60 \times 95$$

$$= \dots\dots\dots \text{ nm}$$

3. The positions of G and H are G( $50^\circ\text{N}$ ,  $102^\circ\text{E}$ ) and H( $50^\circ\text{N}$ ,  $78^\circ\text{W}$ ). Calculate the shortest distance between them in nautical miles,
  - a) Along the parallel of latitude
  - b) Along the great circle.

Soln

$$\text{a) } L = 60a \cos \theta$$

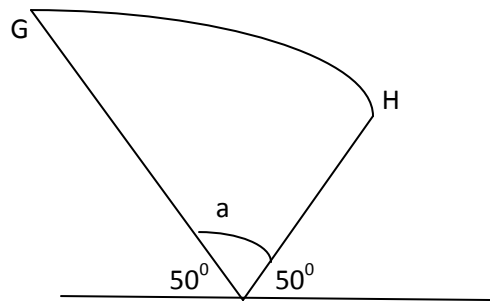
$$a = 102 + 78 = 180$$

$$\theta = 50^\circ$$

$$L = 60 \times 180 \times \cos 50^\circ$$

$$L = \dots\dots\dots \text{ Nm}$$

b)



$$a = 180 - (50 + 50)$$

$$= 80^\circ$$

$$l = 60a$$

$$= 60 \times 80$$

$$= \dots\dots\dots \text{ Nm}$$

### **EXERCISE**

1. Find the shortest distance in nautical miles between the following points
  - a) A(63°N, 100°E) and B(63°N, 80°W).
  - b) C(25°S, 115°W) and D(50°S, 65°E).
  - c) E(10°N, 45°W) and F(10°N, 135°E).
  - d) G(75°S, 86°E) and H(20°S, 94°W).
2. Two points P and Q lie on the latitude 25°N. The sum of their longitudes is 180°. Find in nautical miles the distance between them
  - a) Along the parallel of latitude
  - b) Along the great circle.

### **SPEED IN KNOTS**

- A knot is a unit of speed used by airmen and sailors.
- A speed of one nautical mile per hour is called a knot
- Speed (knots) =  $\frac{\text{distance in nautical miles}}{\text{Time taken in hours}}$

N.B. Distance in nautical miles = Speed in knots x Time in hours

### **WORKED EXAMPLES**

1. A plane covered 1800 nm in 9 hours. Find its speed in knots.

Soln;

$$\begin{aligned} S &= \frac{D}{T} \\ &= \frac{1800 \text{ nm}}{9 \text{ hr}} \\ &= 200 \text{ knots} \end{aligned}$$

2. A ship covered a certain distance in 4 hours at a speed of 35.8 knots. Find the distance covered.

Soln;

$$\begin{aligned} D &= S \times T \\ &= 35.8 \times 4 \\ &= \dots\dots\dots \text{ nm} \end{aligned}$$

### **EXERCISE**

1. Find the speed in knots in each of the following cases.

	Distance (nm)	Time (hrs)	Speed (knots)
a)	100	2	
b)	50	0.5	
c)	9840	7	
d)	0.5	0.25	

2. Find the distance covered in nautical miles.

	Speed (knots)	Time(hours)	Distance
a)	20	6	
b)	150	8	
c)	40.6	10	
d)	85	11	

### **LONGITUDE AND TIME**

- The earth rotates through 360° in every 24 hours.
- This means in 360° change in longitude, there is a change of 1440 minutes.
- In short for 1° change in longitude, there is a change in time of 4 minutes.
- This means if two longitudes differ by 1°, there is a time difference of 4 minutes.
- This is equivalent to a time difference of 1 hour between two longitudes 15° apart.
- All places on the same longitude have the same local time.
- The local time on Greenwich meridian is known as Greenwich Mean Time(GMT)
- All longitudes to the west of Greenwich meridian lag behind in time
- Likewise, all meridians to the east of Greenwich meridian are ahead in time.

### **WORKED EXAMPLES**

1. The local time of a town A(63°N, 40°E) is 11.30 am. What is the local time of the following towns.
  - a) Town B(34°N, 82°E).
  - b) town C(55°S, 10°W)

Soln;

$$\begin{aligned} \text{a) longitude difference} &= 82 - 40 \\ &= 42^\circ \end{aligned}$$

$$\begin{aligned} \text{Time difference} &= 42 \times 4 \\ &= 168 \text{ minutes} \\ &= 2 \text{ hrs } 48 \text{ minutes} \end{aligned}$$

Town B is to the east of town A, hence ahead of local time of town A. Therefore add

$$\begin{array}{r} \text{Local time of town B} = 11.30 \\ + 2.48 \\ \hline 13.78 \\ \underline{1 - 60} \\ 1418 \end{array}$$

Local time of town B is 1418h or 2.18 pm

$$\begin{aligned} \text{b) longitude difference} &= 40 + 10 \\ &= 50^\circ \end{aligned}$$

$$\begin{aligned} \text{Time difference} &= 50 \times 4 \\ &= 200 \text{ minutes} \\ &= 3 \text{ hrs } 20 \text{ minutes} \end{aligned}$$

Town C is to the West of town A, hence lag behind local time of town A. Therefore subtract

$$\text{Local time of town C} = 11.30$$



$$\frac{-3.20}{8.10}$$

Local time of town C is 8.10 am.

### **EXERCISE**

- Given that the local time of a city P A(0°, 30°W) is 12.00 pm. What is the local time of the following cities.
  - Q(10°S, 60°W)
  - R(24°N, 10°W)
  - S(33°S, 20°E)
  - T(81°N, 81°W)
- Three towns X, Y and Z have positions X(42°S, 15°E), Y(8°N, 15°E) and Z(10°S, 60°E). A jet left town X at 10.00 am for town Y moving at a speed of 600 knots. What was the local time of town Z when the jet landed at town Y.

### **SUMMARY OF FORMULAE**

- $L = 60a$  (distance along a great circle in nautical miles)
- $L = 60a \cos \theta$  (distance along a small circle in nautical miles)
- $L = \frac{a}{360} \times 2\pi R$  (distance along a great circle in kilometres)
- $L = \frac{a}{360} \times 2\pi R \cos \theta$  (distance along a small circle in kilometres)
- $r = R \cos \theta$  (radius of a circle of latitude, R is the radius of the earth and  $\theta$  is the angle of latitude)

### **REVISION QUESTIONS**

- A passenger plane takes off from airport A(60°N, 5°E) and flies directly to another airport B(60°N, 17°E) and then flies due North for 600 nautical miles (nm) another airport C
  - Find the position of airport C (3mks)
  - Find the distance between airport A and B in nautical miles (3mks)
  - If the plane at an average speed of 300 knots, find total flight time (2mks)
  - Given that the plane left air port A at 9.20am. Find the local time of arrival at airport C (2mks)
- A plane take of from airport P at (0°, 40°W) and flies 1800 nautical miles due East to Q then 1800 nautical miles due South to R and finally 1800 nautical miles due West before landing at S.
  - Find to the nearest degree the latitudes and longitudes of Q, R and S. (4mks)
  - If the total flight time is 16 hours, find the average speed in knots for the whole journey. (3mks)
  - Find the time taken to fly from R to S, given that this was two hours shorter than the time

taken from P to Q to R.

(3mks)

3. Calculate the shortest distance in nautical miles between M( $45^{\circ}\text{N}$ ,  $38^{\circ}\text{E}$ ) and N( $45^{\circ}\text{N}$ ,  $142^{\circ}\text{W}$ ). (3mks)
4. A plane leaves an airport P ( $10^{\circ}\text{S}$ ,  $62^{\circ}\text{E}$ ) and flies due north at 800km/h.
- (a) Find its position after 2 hours (3 Marks)
- (b) The plane turns and flies at the same speed due west. It reaches longitude Q,  $12^{\circ}\text{W}$ .
- (i) Find the distance it has traveled in nautical miles. (3 Marks)
- (ii) Find the time it has taken (Take  $\pi = \frac{22}{7}$ , the radius of the earth to be 6370km and 1 nautical mile to be 1.853km) (2 Marks)
- (c) If the local time at P was 1300 hours when it reached Q, find the local time at Q when it landed at Q (2 Marks)
5. An aircraft leaves A ( $60^{\circ}\text{N}$ ,  $13^{\circ}\text{W}$ ) at 1300 hours and arrives at B ( $60^{\circ}\text{N}$ ,  $47^{\circ}\text{E}$ ) at 1700 hrs
- (a) Calculate the average speed of the aircraft in knots (3 Marks)
- (b) Town C ( $60^{\circ}\text{N}$ ,  $133^{\circ}\text{W}$ ) has a helipad. Two helicopters S and T leaves B at the same time. S moves due West to C while T moves due North to C. If the two helicopters are moving at 600kts. Find
- (i) The time taken by S to reach C (2 Marks)
- (ii) The time taken by T to reach C (2 Marks)
- (c) The local time at a town D ( $23^{\circ}\text{N}$ ,  $5^{\circ}\text{W}$ ) is 1000 hours. What is the local time at B. (3 Marks)