



# Sketching in augmented reality

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Spring 2019

# Change of plans...

- Initially I planned to do a “then & now” re-photography app. The goal was to use augmented reality combined with other computer vision techniques to align photos and explore the results.



[https://www.swiss-miss.com/wp-content/uploads/2010/02/4355405531\\_e9daccfdc6-480x326.jpg](https://www.swiss-miss.com/wp-content/uploads/2010/02/4355405531_e9daccfdc6-480x326.jpg)



<http://www.bluedotmagazine.com/2016/05/18/london-during-the-blitz-then-and-now-photographs/>



Wikipedia

- However, many technical difficulties, and way too many moving parts for <10 weeks.

# Augmented reality basics

- Device has to build a map of the environment, then determine its location within that environment.
- Virtual images are determined by aligning the virtual camera's pose with the real camera's pose.
- Google ARCore SDK does this automatically using a process it has patented as “concurrent odometry and mapping”
  - At a high level, it detects feature points from multiple images and uses them to build a 3D visual representation of the environment.
  - Combined with information from the IMU (inertial measurement unit), camera pose is estimated.
- ARCore obscures how many functions work.

# Sketch-based modeling

- In contrast to CAD, sketch-based modeling turns 2D sketches into 3D models.

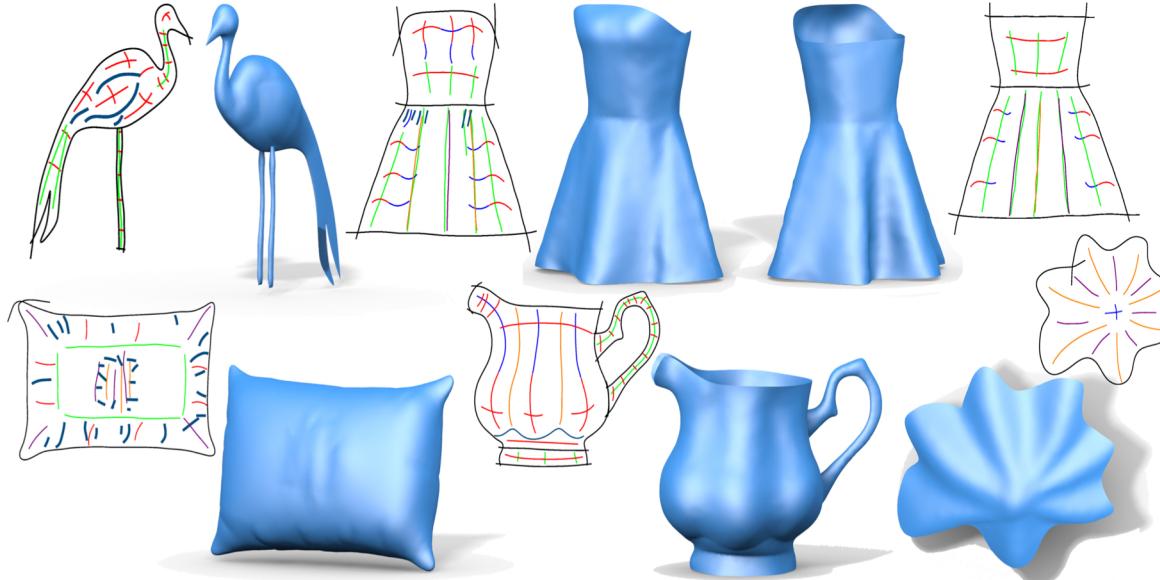
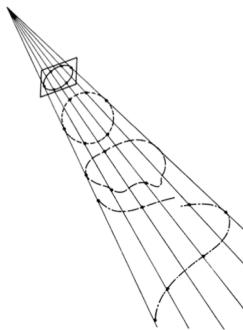


Image from Li et al, *BendSketch*, 2017.

- With AR, user can also view the resulting model within their current context.

- 2D → 3D: infinite number of possibilities



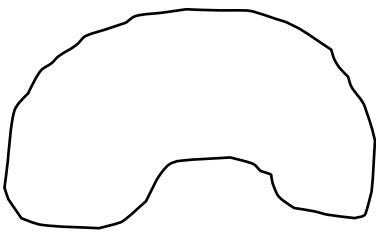
All 3D curves map to the ellipse  
in the image plane.

- In VR, users can sculpt/draw in 3D, and ideally in AR as well (although difficulties with depth and hand-tracking.)
- But user may not know exactly where in 3D space they want points to go, or they want something quick & convenient with little overhead.
- Follow *Teddy: A Sketching Interface for 3D Freeform Design* by Igarashi, Matsuoka, and Tanaka (1999), which uses an inflation-based approach.

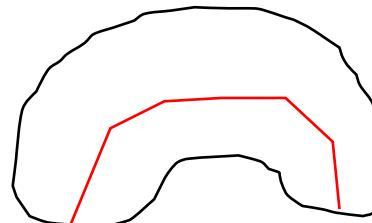
# *Teddy* (1999) overview

Simple idea:

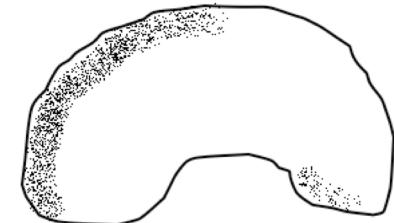
We have a 2D shape:



Determine its “skeleton”:



Inflate:



# *Teddy* (1999) overview

- User draws 2D closed curves (curves are automatically closed otherwise.)
- The closed region is “inflated” in both directions. Wide areas become fat, and narrow areas become thin. A free-form shape is generated.

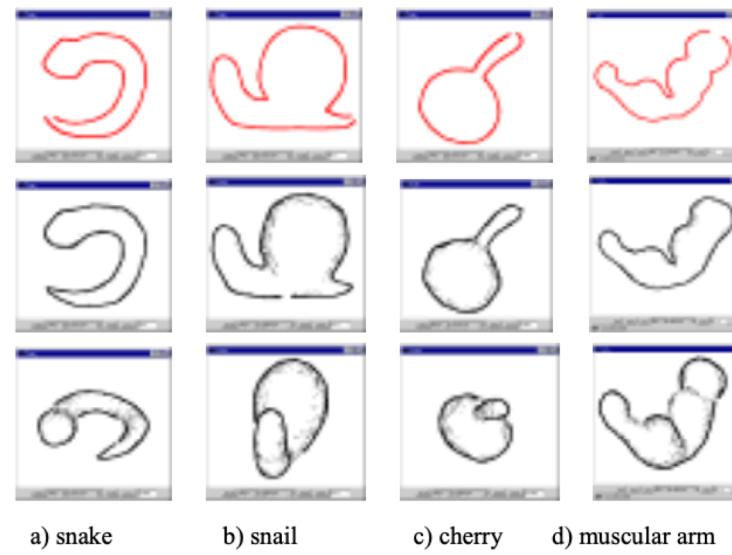


Figure 5: Examples of creation operation (top: input stroke, middle: result of creation, bottom: rotated view).

- Cons: models must have spherical topology, no self-intersecting curves.

# Algorithm overview

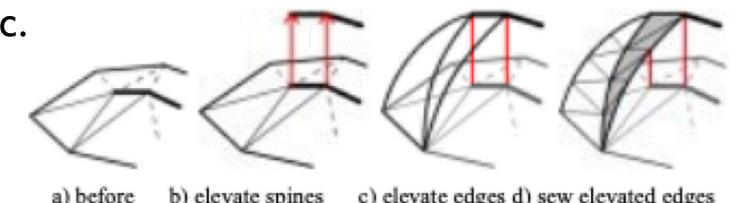
- Start with a closed 2D polygon.
  - Resample and make all edges some unit length.
- Determine the “spine” the polygon using the *chordal axis*.
  - Perform constrained Delaunay triangulation (CDT) on the polygon.
  - Obtain the chordal axis by connecting the midpoints of internal edges.
  - Prune insignificant branches.
  - Re-triangulate the mesh.
- Elevate the vertices of the spine by an amount proportional to their distance from the polygon.
  - Elevate each vertex on the spine by a distance proportional to the average distance between the vertex and the external vertices directly connected to it.
  - Convert each internal non-spinal edge to a quarter oval, and elevate along with the spine.
  - Sew together the neighboring elevated edges.
  - Copy the elevated mesh to the other side to make the mesh closed and symmetric.
  - Remove short edges and small triangles.



a) initial 2D polygon    b) result of CDT    c) chordal axis



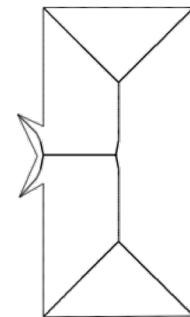
d) fan triangles    e) resulting spine    f) final triangulation



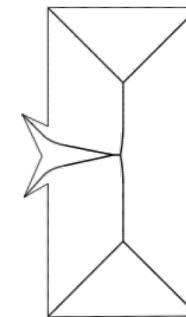
a) before    b) elevate spines    c) elevate edges d) sew elevated edges

# Skeleton construction - CDT

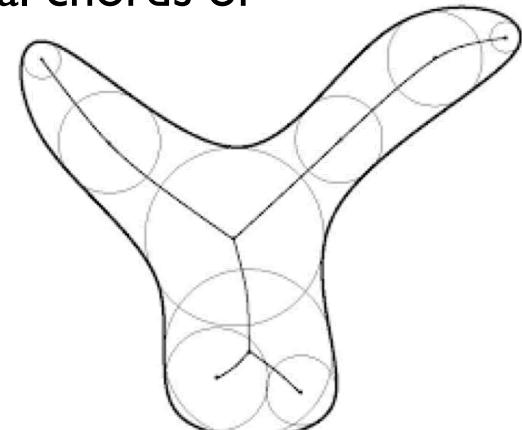
- A *maximal disc* is a circle contained in the interior of the shape, that is tangent to its boundary at at least 2 points.
- A *maximal chord of tangency* of a maximal disc is a chord that
  - (i) connects two points of tangency (of the disc with the shape boundary)
  - (ii) at least one of the two arcs subtended by the chord has no points of tangency.
- The *chordal axis transform* is the set of all pairs  $(p, d)$ , where either:
  - (i)  $p$  and  $d$  are the midpoint and half the length of a maximal chord of tangency, resp.
  - or, (ii)  $p$  and  $d$  are the center and radius of a maximal disc with three maximal chords of tangency that form an acute triangle.



(d) CAT skeleton



(e) MAT



# Skeleton construction - CDT

- In the discrete case, *maximal discs* are replaced by *empty circles* that pass through  $\geq 3$  polygon vertices.
  - *Empty circles* do not contain any vertex of the polygon that are *visible* to the any 2 vertices on the circle (*visible* = the line segment joining the 2 vertices is entirely in the interior of the polygon.)
- *Maximal chords of tangency* are replaced by the line that joins 2 non-neighboring vertices of the polygon iff an *empty circle* passes through both these vertices.
  - This is equivalent to a Constrained Delaunay Triangulation (CDT.)
  - A Delaunay Triangulation is a decomposition of a polygon into triangles s.t. the circumcircle of each triangle is empty.
  - Results in 3 types of triangles: *terminal*, *sleeve*, and *junction*

# Skeleton construction - CDT

- After the CDT, we obtain “terminal” (2 boundary edges), “sleeve” (1) and “junction”(0) triangles.
- The chordal axis is obtained by connecting the midpoints of the interior edges.
- However, we then want to obtain an “inflatable-friendly” triangulation.
- We remove insignificant branches and round the extremities via a “fanning” process.



a) initial 2D polygon



b) result of CDT



c) chordal axis



d) fan triangles



e) resulting spine



f) final triangulation

# Skeleton construction – fanning & pruning

- We want the final mesh to be as smooth as possible.
- We want to round the extremities of each branch (which are indicated by terminal triangles.)
- We do this by fitting a hemispherical cap at the end of each branch, and determining the center around which to fan the triangles.

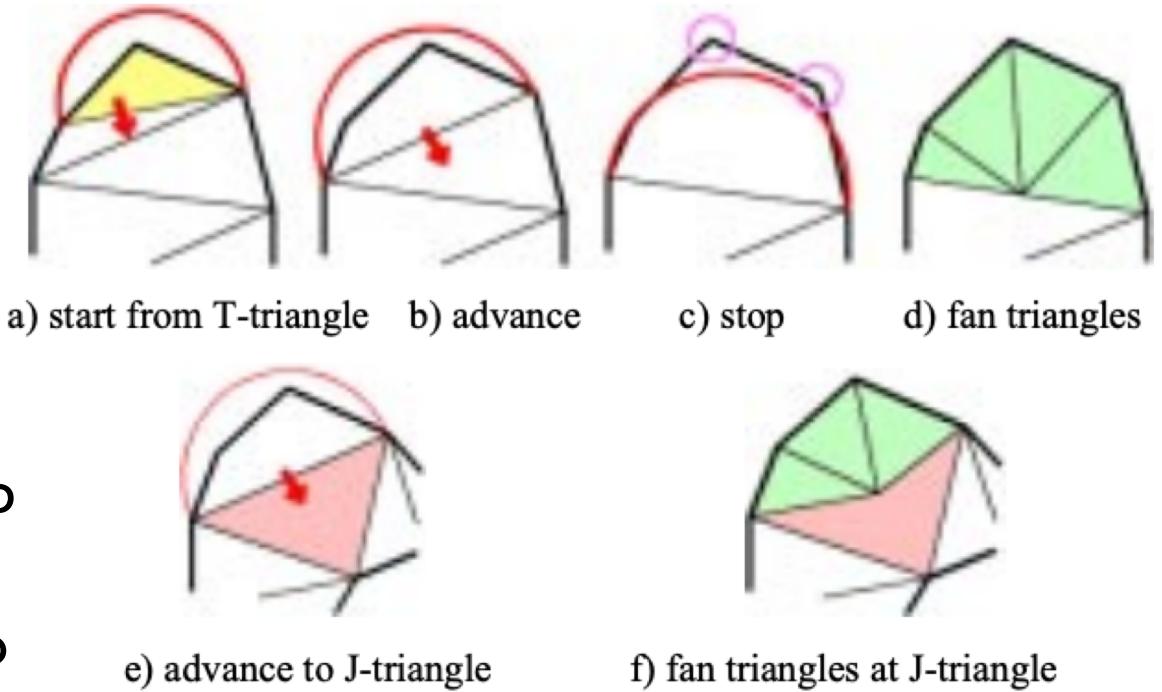
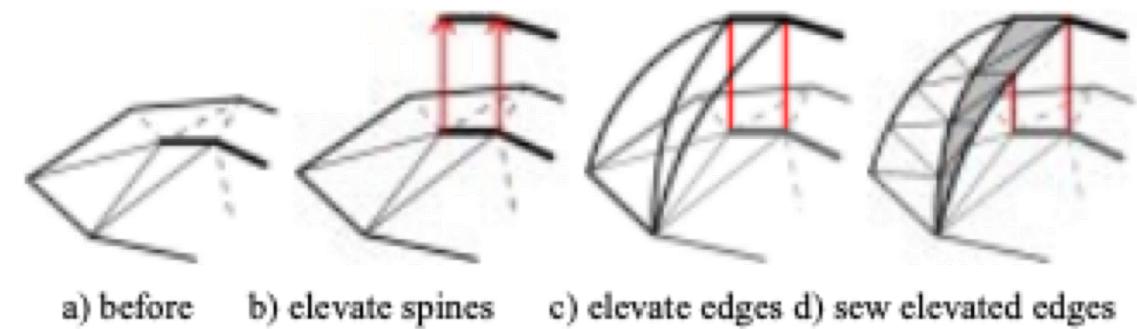
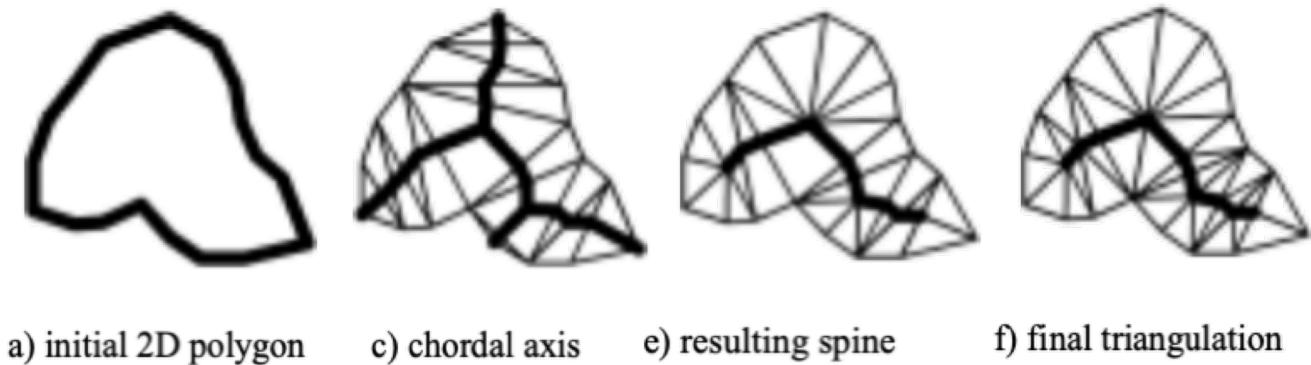


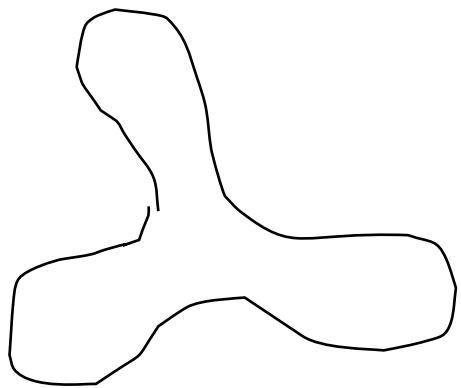
Figure 14: Pruning.

# Mesh construction – re-triangulation

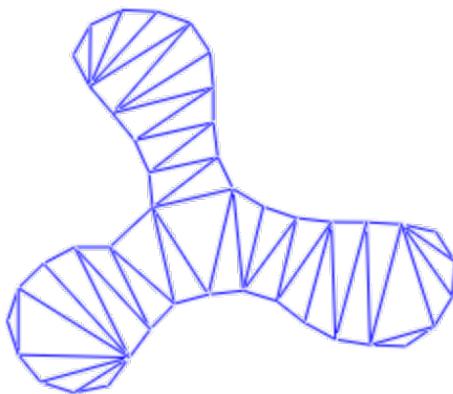
- After fanning and pruning, we connect the resulting internal points and midpoints of internal edges to obtain the spine we want.
- We then construct the final triangulation such that all interior edges are between the spine and the boundary.
- First we elevate the spine a distance proportional to the average length of its adjacent edges.
- Then we sew together each triangle with several smaller triangles, and elevate them such that each edge approximate a quarter-ellipse.



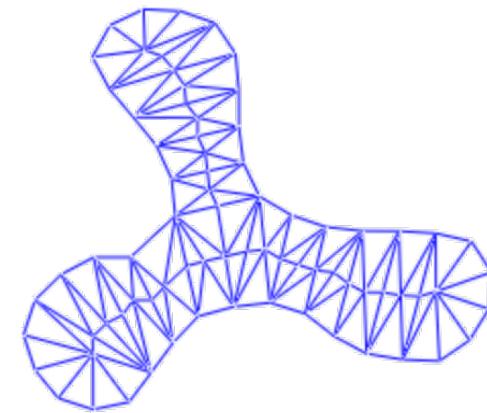
Draw in 2D:



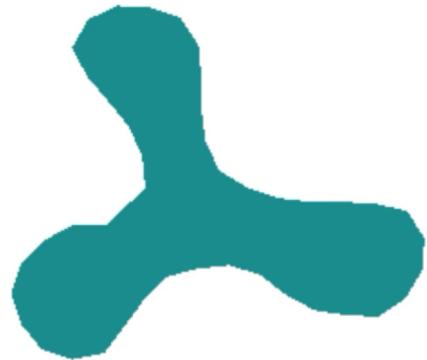
CDT:



After pruning and  
re-triangulation:



Final mesh:



# Implementation

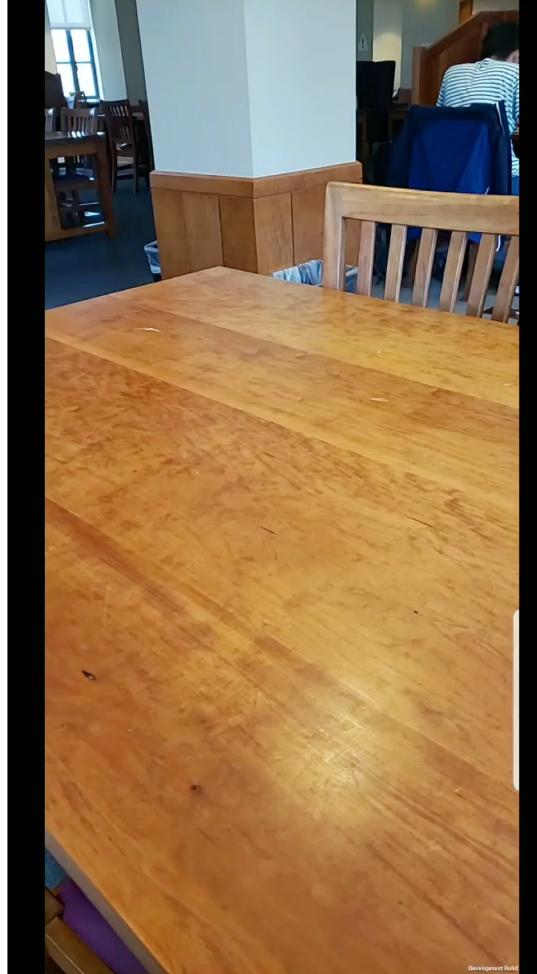
- Implement halfedge data structure for performing manipulations on mesh
- Implement constrained Delaunay triangulation
- Implement drawing interface, which:
  - Takes in 2D drawing input
  - Resamples drawn curve
  - Performs CDT
  - Prunes insignificant edges from the chordal axis
  - Re-triangulates
  - Elevates the spine
  - Elevates each of the interior edges, and stitches them together as a mesh
- Have ARCore detect planes on which to place the newly created object.
- Implement mesh manipulation (drag and drop)
- Optionally support other mesh operations.

# Other implementation details

- Google ARCore comes with environmental light estimation, so we use this in our shaders to adjust the lighting of the mesh.
  - Source code is not available, but my guess is that it computes some average of pixel intensities across frames to provide the light estimates.
- ARCore also comes with a plane detection feature, which we use to anchor our mesh.

# Implementation

Code available at: <https://github.com/nzfeng/CS174>



**Currently supported operations:** mesh creation, pinch enlarge / shrink

**Cons:** too slow on smartphone

# Goals of project

- Implement a sketch-based modeling algorithm
- Develop app that demonstrates using AR to extend an existing application
- Develop app using newly-released AR SDK for smartphone, where there is little existing work and sparse documentation / example usage.

# Future directions

- Support other types of drawing and modeling.
  - Other types of inference, for example from orthographic projections
- Allow further manipulation of existing objects, such as cutting, extrusion, etc. although operations are too slow on my smartphone.

# References

- H.G. Barrow and J.M. Tenenbaum, *Interpreting Line Drawings as Three-Dimensional Surfaces*, 1980.
- Igarashi, Matsuoka, Tanaka, *Teddy: A Sketching Interface for 3D Freeform Design*, 1999.
- Lakshman Prasad, *Morphological Analysis of Shapes*, 1997.
- Google patent: <https://patentimages.storage.googleapis.com/4d/af/08/b9351479700bcf/US20170336511A1.pdf>
- <https://developer.android.com>