```
In [7]: import os
        import sys
        import torch
        import importlib
        from tqdm.auto import tqdm
        current_dir = os.getcwd()
        project_root = os.path.dirname(current_dir)
        sys.path.append(project_root)
        # Import our custom modules
        import src.utils as utils
        import src.plots as plots
        import src.neural_network_scratch as nn_scratch
        importlib.reload(utils)
        importlib.reload(plots)
        importlib.reload(nn_scratch)
        from src.utils import load_transform_split_mnist, per_class_accuracy
        from src.plots import plot_train_val_curves, plot_confusion_matrix, plot_per_class_acc,plot_learning_curves_with_error_bars
        from src.neural_network_scratch import NeuralNetworkScratch
```

Load Data loaders

```
In [2]: # Using the same utility from Part A, but loading all classes
    train_loader, val_loader, test_loader, _, _, _, _, _= load_transform_split_mnist(
        val_size=0.2,
        classes=None, # None means all 10 classes
        batch_size=64
    )
    print("Data loaders created successfully.")
```

Data loaders created successfully.

Initialize and Train Model

```
In [3]: INPUT_DIM = 28 * 28 # for flattened 28x28 image
        HIDDEN1 = 128
        HIDDEN2 = 64
        OUTPUT_DIM = 10
        LEARNING_RATE = 0.01
        EPOCHS = 20
        N_RUNS = 5
        all_histories = []
        final_models = []
        print(f"Starting {N_RUNS} training runs for error bar analysis...")
        print("#" * 60)
        i=0
        for i in range(N_RUNS):
            print(f"--- Starting Run {i+1}/{N_RUNS} (Seed={i}) ---")
            model = NeuralNetworkScratch(INPUT_DIM, HIDDEN1, HIDDEN2, OUTPUT_DIM)
            history = model.fit(train_loader, val_loader, epochs=EPOCHS, lr=LEARNING_RATE)
            all_histories.append(history)
            final_models.append(model) # Save the model from this run
            print(f"Run {i+1} complete.")
        print("#" * 60)
        print("All training runs complete!")
```

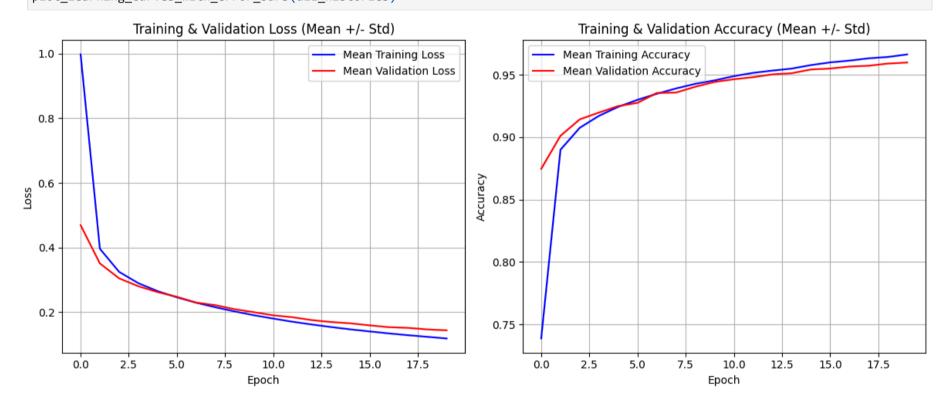
```
--- Starting Run 1/5 (Seed=0) ---
                                                                          Val Acc: 87.47%
Epoch 1/20 |
             Train Loss: 0.9976, Train Acc: 73.87% | Val Loss: 0.4694,
             Train Loss: 0.3965, Train Acc: 89.00%
                                                                          Val Acc: 90.12%
Epoch 2/20
                                                     Val Loss: 0.3512,
             Train Loss: 0.3250, Train Acc: 90.76%
                                                                          Val Acc: 91.43%
Epoch
      3/20
                                                     Val Loss: 0.3050,
Epoch
      4/20
             Train Loss: 0.2899, Train Acc: 91.72%
                                                     Val Loss: 0.2806,
                                                                          Val Acc: 91.98%
             Train Loss: 0.2654, Train Acc: 92.44%
      5/20
Epoch
                                                     Val Loss: 0.2624,
                                                                          Val Acc: 92.50%
      6/20
             Train Loss: 0.2463, Train Acc: 93.00%
                                                     Val Loss: 0.2479,
                                                                          Val Acc: 92.76%
Epoch
             Train Loss: 0.2297, Train Acc: 93.49%
Epoch 7/20
                                                     Val Loss: 0.2300,
                                                                          Val Acc: 93.55%
Epoch 8/20
             Train Loss: 0.2155, Train Acc: 93.91% |
                                                     Val Loss: 0.2220,
                                                                          Val Acc: 93.58%
Epoch 9/20
             Train Loss: 0.2027, Train Acc: 94.28%
                                                     Val Loss: 0.2096,
                                                                          Val Acc: 94.05%
Epoch 10/20
             Train Loss: 0.1909, Train Acc: 94.56%
                                                     Val Loss: 0.2002,
                                                                          Val Acc: 94.43%
             Train Loss: 0.1806, Train Acc: 94.90%
                                                     Val Loss: 0.1906,
                                                                          Val Acc: 94.65%
Epoch 11/20
                                                      Val Loss: 0.1848,
Epoch 12/20
             Train Loss: 0.1708, Train Acc: 95.16%
                                                                          Val Acc: 94.82%
             Train Loss: 0.1623, Train Acc: 95.34%
Epoch 13/20
                                                                          Val Acc: 95.04%
                                                      Val Loss: 0.1759,
Epoch 14/20
             Train Loss: 0.1545, Train Acc: 95.50%
                                                     Val Loss: 0.1700,
                                                                          Val Acc: 95.13%
Epoch 15/20
             Train Loss: 0.1472, Train Acc: 95.79%
                                                                          Val Acc: 95.43%
                                                     Val Loss: 0.1659,
                                                                          Val Acc: 95.51%
Epoch 16/20
             Train Loss: 0.1409, Train Acc: 96.00%
                                                     Val Loss: 0.1597,
Epoch 17/20
             Train Loss: 0.1347, Train Acc: 96.14%
                                                     Val Loss: 0.1540,
                                                                          Val Acc: 95.67%
             Train Loss: 0.1292, Train Acc: 96.33% |
                                                                          Val Acc: 95.73%
Epoch 18/20
                                                     Val Loss: 0.1519,
             Train Loss: 0.1241, Train Acc: 96.44% | Val Loss: 0.1470,
                                                                          Val Acc: 95.91%
Epoch 19/20
Epoch 20/20
             Train Loss: 0.1191, Train Acc: 96.64% | Val Loss: 0.1443,
                                                                          Val Acc: 95.99%
Run 1 complete.
--- Starting Run 2/5 (Seed=1) ---
                                                                          Val Acc: 87.47%
Epoch 1/20
             Train Loss: 0.9976, Train Acc: 73.87%
                                                    | Val Loss: 0.4694,
Epoch 2/20
             Train Loss: 0.3965, Train Acc: 89.00%
                                                     Val Loss: 0.3512,
                                                                          Val Acc: 90.12%
             Train Loss: 0.3250, Train Acc: 90.76%
Epoch 3/20
                                                     Val Loss: 0.3050,
                                                                          Val Acc: 91.43%
             Train Loss: 0.2899, Train Acc: 91.72%
      4/20
                                                     Val Loss: 0.2806,
                                                                          Val Acc: 91.98%
Epoch
             Train Loss: 0.2654, Train Acc: 92.44%
                                                                          Val Acc: 92.50%
Epoch
      5/20
                                                     Val Loss: 0.2624,
Epoch
      6/20
             Train Loss: 0.2463, Train Acc: 93.00%
                                                      Val Loss: 0.2479,
                                                                          Val Acc: 92.76%
Epoch 7/20
             Train Loss: 0.2297, Train Acc: 93.49%
                                                      Val Loss: 0.2300,
                                                                          Val Acc: 93.55%
                                                      Val Loss: 0.2220,
      8/20
             Train Loss: 0.2155, Train Acc: 93.91%
                                                                          Val Acc: 93.58%
Epoch
             Train Loss: 0.2027, Train Acc: 94.28%
Epoch 9/20
                                                     Val Loss: 0.2096,
                                                                          Val Acc: 94.05%
             Train Loss: 0.1909, Train Acc: 94.56%
                                                                          Val Acc: 94.43%
Epoch 10/20
                                                     Val Loss: 0.2002,
Epoch 11/20
                                                     Val Loss: 0.1906,
             Train Loss: 0.1806, Train Acc: 94.90%
                                                                          Val Acc: 94.65%
Epoch 12/20
             Train Loss: 0.1708, Train Acc: 95.16%
                                                     Val Loss: 0.1848,
                                                                          Val Acc: 94.82%
                                                                          Val Acc: 95.04%
Epoch 13/20
             Train Loss: 0.1623, Train Acc: 95.34%
                                                     Val Loss: 0.1759,
Epoch 14/20
             Train Loss: 0.1545, Train Acc: 95.50%
                                                      Val Loss: 0.1700,
                                                                          Val Acc: 95.13%
Epoch 15/20
             Train Loss: 0.1472, Train Acc: 95.79%
                                                                          Val Acc: 95.43%
                                                     Val Loss: 0.1659,
             Train Loss: 0.1409, Train Acc: 96.00%
                                                     Val Loss: 0.1597,
                                                                          Val Acc: 95.51%
Epoch 16/20
Epoch 17/20
             Train Loss: 0.1347, Train Acc: 96.14%
                                                     Val Loss: 0.1540,
                                                                          Val Acc: 95.67%
Epoch 18/20
             Train Loss: 0.1292, Train Acc: 96.33% | Val Loss: 0.1519,
                                                                          Val Acc: 95.73%
             Train Loss: 0.1241, Train Acc: 96.44% | Val Loss: 0.1470,
                                                                          Val Acc: 95.91%
Epoch 19/20
Epoch 20/20 | Train Loss: 0.1191, Train Acc: 96.64% | Val Loss: 0.1443,
                                                                          Val Acc: 95.99%
Run 2 complete.
--- Starting Run 3/5 (Seed=2) ---
                                                                          Val Acc: 87.47%
Epoch 1/20
             Train Loss: 0.9976, Train Acc: 73.87%
                                                     Val Loss: 0.4694,
             Train Loss: 0.3965, Train Acc: 89.00%
                                                                          Val Acc: 90.12%
Epoch
      2/20
                                                     Val Loss: 0.3512,
             Train Loss: 0.3250, Train Acc: 90.76%
                                                     Val Loss: 0.3050,
                                                                          Val Acc: 91.43%
Epoch
      3/20
Epoch
      4/20
             Train Loss: 0.2899, Train Acc: 91.72%
                                                     Val Loss: 0.2806,
                                                                          Val Acc: 91.98%
Epoch
      5/20
             Train Loss: 0.2654, Train Acc: 92.44%
                                                     Val Loss: 0.2624,
                                                                          Val Acc: 92.50%
             Train Loss: 0.2463, Train Acc: 93.00%
                                                                          Val Acc: 92.76%
      6/20
                                                     Val Loss: 0.2479,
Epoch
Epoch
      7/20
             Train Loss: 0.2297, Train Acc: 93.49%
                                                     Val Loss: 0.2300,
                                                                          Val Acc: 93.55%
Epoch
      8/20
             Train Loss: 0.2155, Train Acc: 93.91%
                                                      Val Loss: 0.2220,
                                                                          Val Acc: 93.58%
Epoch 9/20
             Train Loss: 0.2027, Train Acc: 94.28%
                                                     Val Loss: 0.2096,
                                                                          Val Acc: 94.05%
Epoch 10/20
             Train Loss: 0.1909, Train Acc: 94.56%
                                                     Val Loss: 0.2002,
                                                                          Val Acc: 94.43%
             Train Loss: 0.1806, Train Acc: 94.90%
                                                     Val Loss: 0.1906,
                                                                          Val Acc: 94.65%
Epoch 11/20
                                                     Val Loss: 0.1848,
Epoch 12/20
             Train Loss: 0.1708, Train Acc: 95.16%
                                                                          Val Acc: 94.82%
Epoch 13/20
             Train Loss: 0.1623, Train Acc: 95.34%
                                                     Val Loss: 0.1759,
                                                                          Val Acc: 95.04%
                                                                          Val Acc: 95.13%
             Train Loss: 0.1545, Train Acc: 95.50%
Epoch 14/20
                                                     Val Loss: 0.1700,
Epoch 15/20
             Train Loss: 0.1472, Train Acc: 95.79%
                                                      Val Loss: 0.1659,
                                                                          Val Acc: 95.43%
                                                      Val Loss: 0.1597,
Epoch 16/20
             Train Loss: 0.1409, Train Acc: 96.00%
                                                                          Val Acc: 95.51%
                                                      Val Loss: 0.1540,
                                                                          Val Acc: 95.67%
Epoch 17/20
             Train Loss: 0.1347, Train Acc: 96.14%
             Train Loss: 0.1292, Train Acc: 96.33%
Epoch 18/20
                                                     Val Loss: 0.1519,
                                                                          Val Acc: 95.73%
             Train Loss: 0.1241, Train Acc: 96.44% | Val Loss: 0.1470,
Epoch 19/20
                                                                          Val Acc: 95.91%
Epoch 20/20 | Train Loss: 0.1191, Train Acc: 96.64% | Val Loss: 0.1443,
                                                                          Val Acc: 95.99%
Run 3 complete
--- Starting Run 4/5 (Seed=3) ---
Epoch 1/20 | Train Loss: 0.9976, Train Acc: 73.87% | Val Loss: 0.4694,
                                                                          Val Acc: 87.47%
                                                                          Val Acc: 90.12%
Epoch 2/20
             Train Loss: 0.3965, Train Acc: 89.00% | Val Loss: 0.3512,
Epoch 3/20
             Train Loss: 0.3250, Train Acc: 90.76% | Val Loss: 0.3050,
                                                                          Val Acc: 91.43%
             Train Loss: 0.2899, Train Acc: 91.72% | Val Loss: 0.2806,
Epoch 4/20
                                                                          Val Acc: 91.98%
Epoch 5/20
             Train Loss: 0.2654, Train Acc: 92.44% | Val Loss: 0.2624,
                                                                          Val Acc: 92.50%
Epoch 6/20
             Train Loss: 0.2463, Train Acc: 93.00% | Val Loss: 0.2479,
                                                                          Val Acc: 92.76%
             Train Loss: 0.2297, Train Acc: 93.49% | Val Loss: 0.2300,
Epoch 7/20
                                                                          Val Acc: 93.55%
Epoch 8/20
             Train Loss: 0.2155, Train Acc: 93.91% | Val Loss: 0.2220,
                                                                          Val Acc: 93.58%
             Train Loss: 0.2027, Train Acc: 94.28% | Val Loss: 0.2096,
                                                                          Val Acc: 94.05%
Epoch 9/20
                                                     Val Loss: 0.2002,
Epoch 10/20
             Train Loss: 0.1909, Train Acc: 94.56%
                                                                          Val Acc: 94.43%
             Train Loss: 0.1806, Train Acc: 94.90%
                                                     Val Loss: 0.1906,
Epoch 11/20
                                                                          Val Acc: 94.65%
             Train Loss: 0.1708, Train Acc: 95.16% | Val Loss: 0.1848,
Epoch 12/20
                                                                          Val Acc: 94.82%
Epoch 13/20
             Train Loss: 0.1623, Train Acc: 95.34% | Val Loss: 0.1759,
                                                                          Val Acc: 95.04%
Epoch 14/20
             Train Loss: 0.1545, Train Acc: 95.50% | Val Loss: 0.1700,
                                                                          Val Acc: 95.13%
Epoch 15/20
             Train Loss: 0.1472, Train Acc: 95.79% | Val Loss: 0.1659,
                                                                          Val Acc: 95.43%
             Train Loss: 0.1409, Train Acc: 96.00% | Val Loss: 0.1597,
Epoch 16/20
                                                                          Val Acc: 95.51%
Epoch 17/20
             Train Loss: 0.1347, Train Acc: 96.14% | Val Loss: 0.1540,
                                                                          Val Acc: 95.67%
Epoch 18/20 |
             Train Loss: 0.1292, Train Acc: 96.33% | Val Loss: 0.1519,
                                                                          Val Acc: 95.73%
```

```
Epoch 19/20 | Train Loss: 0.1241, Train Acc: 96.44% | Val Loss: 0.1470,
                                                                        Val Acc: 95.91%
Epoch 20/20 | Train Loss: 0.1191, Train Acc: 96.64% | Val Loss: 0.1443,
                                                                        Val Acc: 95.99%
Run 4 complete.
--- Starting Run 5/5 (Seed=4) ---
Epoch 1/20 | Train Loss: 0.9976, Train Acc: 73.87% | Val Loss: 0.4694,
                                                                         Val Acc: 87.47%
                                                                         Val Acc: 90.12%
Epoch 2/20 |
             Train Loss: 0.3965, Train Acc: 89.00% | Val Loss: 0.3512,
Epoch 3/20 |
             Train Loss: 0.3250, Train Acc: 90.76% | Val Loss: 0.3050,
                                                                         Val Acc: 91.43%
Epoch 4/20
             Train Loss: 0.2899, Train Acc: 91.72% | Val Loss: 0.2806,
                                                                        Val Acc: 91.98%
                                                                        Val Acc: 92.50%
Epoch 5/20
             Train Loss: 0.2654, Train Acc: 92.44% | Val Loss: 0.2624,
Epoch 6/20
             Train Loss: 0.2463, Train Acc: 93.00% | Val Loss: 0.2479,
                                                                        Val Acc: 92.76%
Epoch 7/20
             Train Loss: 0.2297, Train Acc: 93.49% | Val Loss: 0.2300,
                                                                        Val Acc: 93.55%
Epoch 8/20 | Train Loss: 0.2155, Train Acc: 93.91% | Val Loss: 0.2220,
                                                                         Val Acc: 93.58%
Epoch 9/20 | Train Loss: 0.2027, Train Acc: 94.28% | Val Loss: 0.2096,
                                                                        Val Acc: 94.05%
                                                                         Val Acc: 94.43%
             Train Loss: 0.1909, Train Acc: 94.56% | Val Loss: 0.2002,
Epoch 10/20
Epoch 11/20
                                                                         Val Acc: 94.65%
             Train Loss: 0.1806, Train Acc: 94.90% | Val Loss: 0.1906,
Epoch 12/20
             Train Loss: 0.1708, Train Acc: 95.16% | Val Loss: 0.1848,
                                                                         Val Acc: 94.82%
Epoch 13/20 |
             Train Loss: 0.1623, Train Acc: 95.34% | Val Loss: 0.1759,
                                                                        Val Acc: 95.04%
Epoch 14/20
             Train Loss: 0.1545, Train Acc: 95.50% | Val Loss: 0.1700,
                                                                        Val Acc: 95.13%
Epoch 15/20
             Train Loss: 0.1472, Train Acc: 95.79% | Val Loss: 0.1659,
                                                                        Val Acc: 95.43%
             Train Loss: 0.1409, Train Acc: 96.00% | Val Loss: 0.1597,
Epoch 16/20 |
                                                                         Val Acc: 95.51%
Epoch 17/20 |
             Train Loss: 0.1347, Train Acc: 96.14% | Val Loss: 0.1540,
                                                                         Val Acc: 95.67%
Epoch 18/20 |
             Train Loss: 0.1292, Train Acc: 96.33% | Val Loss: 0.1519,
                                                                        Val Acc: 95.73%
Epoch 19/20
             Train Loss: 0.1241, Train Acc: 96.44% | Val Loss: 0.1470,
                                                                        Val Acc: 95.91%
Epoch 20/20 | Train Loss: 0.1191, Train Acc: 96.64% | Val Loss: 0.1443, Val Acc: 95.99%
Run 5 complete.
```

All training runs complete!

Performance Visualization

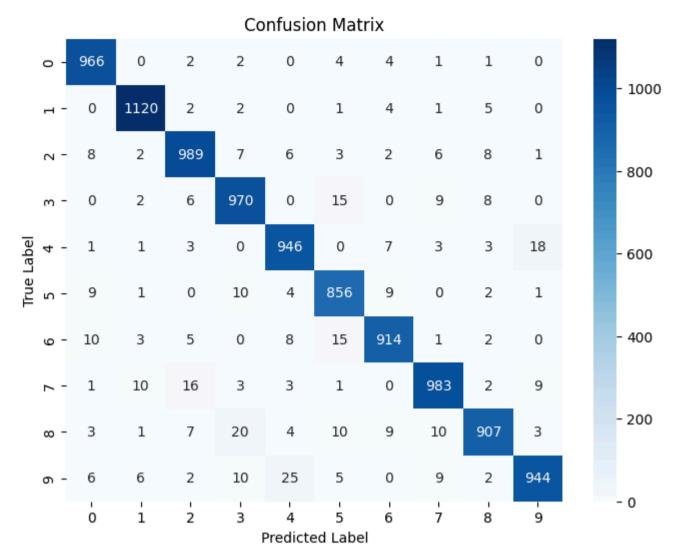
In [4]: # Plot Training and validation loss/accuracy over epochs
plot_learning_curves_with_error_bars(all_histories)



Final Test Set Evaluation

```
In [6]:
        import numpy as np
        # Get predictions for the entire test set
        y_{\text{test}} = []
        y_pred_test = []
        model.eval() # Set model to evaluation mode
        with torch.no_grad():
            for X, y in test_loader:
                 preds = model.predict(X)
                y_test.extend(y.numpy())
                y_pred_test.extend(preds.numpy())
        # Plot Confusion Matrix
        print("Generating Confusion Matrix for Test Set...")
        cm = plot_confusion_matrix(y_test, y_pred_test)
        # Per-class accuracy analysis
        print("\nGenerating Per-Class Accuracy for Test Set...")
        df_acc = per_class_accuracy(cm)
        plot_per_class_acc(df_acc)
```

Generating Confusion Matrix for Test Set...



Generating Per-Class Accuracy for Test Set...

