

测量金属杨氏模量 (1) 3.20 CCD

北京地重力加速度 $g = 9.801 \text{ m.s}^{-2}$

$$E = \frac{4mgL}{\pi d^2 \Delta L}$$

m - 砝码质量

L - 标尺

d - 平均直径

$$L = 126.0 \text{ mm} - 23.9 \text{ mm} = 102.1 \text{ mm}$$

$$L = 101.80 \text{ mm} - 22.40 \text{ mm} = 79.40 \text{ mm}$$

测量金属丝直径

$$d_0 = 0.00 \text{ mm}$$

i	1	2	3	4	5	6	7	8	9	10
d_i/mm	0.323	0.322	0.322	0.322	0.321	0.324	0.323	0.322	0.325	0.322

~~平均~~

$$\bar{d} = 0.322 \text{ mm} \quad \sigma_d = 0.006 \text{ mm}$$

测量金属丝受外力拉伸后的伸长量数据表

i	$\frac{m_i}{g}$	m_i/g	r_i/mm	r_i'/mm	\bar{r}/mm	$\Delta L = (\bar{r}_{i+5} - \bar{r}_i)/\text{mm}$
0	—	0.00	2.20	2.19	—	—
1	199.99	199.99	2.34	2.33	—	—
2	199.76	199.75	2.49	2.46	2.475	0.465
3	199.91	199.66	2.60	2.59	2.595	0.455
4	199.99	199.65	2.71	2.70	2.705	0.455
5	199.73	199.38	2.80	2.83	2.815	0.465
6	199.55	198.93	2.95	2.93	2.940	—
7	199.63	198.56	3.05	3.05	3.050	—
8	199.94	198.50	3.17	3.15	3.160	—
9	199.67	198.17	3.28	3.28	3.280	—

$$\bar{m} = 199.7979 \quad \sigma_m = 0.06 \text{ g}$$

$$\bar{\Delta L} = 0.460 \text{ mm}$$

$$\sigma_{\Delta L} = 0.002 \text{ mm}$$

$$\Rightarrow \bar{E} = \frac{4mgL}{\pi d^2 \Delta L} = 1.6536 \times 10^{11} \text{ Pa}$$

$$\sigma_{\bar{E}} = \bar{E} \sqrt{\left(\frac{\sigma_m}{\bar{m}}\right)^2 + \left(\frac{\sigma_L}{\bar{L}}\right)^2 + 4\left(\frac{\sigma_d}{\bar{d}}\right)^2 + \left(\frac{\sigma_{\Delta L}}{\bar{\Delta L}}\right)^2} = 0.13 \times 10^{11} \text{ Pa}$$

2.20

测金属的杨氏模量 (二) 3.22 高曲梁

$$E = \frac{Gl^3}{4\lambda ah^3} \quad G = mg$$

l - 钢尺 ~~0.1 cm~~ ^{0.1 cm} 测 10 次 (两侧相等) $l = 27.85 \text{ cm}$ $\sigma_l = 0.06 \text{ cm}$

~~a - 钢尺 0.01 cm 测 10 次 $a = 1.50 \text{ cm}$~~

h - 千分尺 ~~0.01 mm~~ ^{0.01 mm} $d_0 = -0.002 \text{ mm}$

i	1	2	3	4	5	$(\bar{h} - h_0)$
h/mm	1.530	1.523	1.531	1.514	1.532	$(\bar{h} - d_0) = 1.528 \text{ mm}$

a - 游标卡尺 0.05 mm

$$\sigma_a = 0.007 \text{ mm}$$

i	1	2	3	4	5	\bar{a}
a/mm	14.90 14.90	14.90 14.90	14.95 14.95	14.90 14.93	14.90 14.90	$\bar{a} = 14.92 \text{ mm}$ $\sigma_a = 0.03 \text{ mm}$

测量误差 λ

i	m/g	X_i/mm	X_i'/mm	Δ/mm	λ'/mm
0	0.00	45.50	45.4	0.0	0.0
1	200.39 (199.56)	44.6	44.5	0.9	0.9
2	399.95 (200.94)	43.7	43.6	1.8	1.8
3	600.89 (200.66)	42.8	42.7	2.7	2.7
4	801.55 (200.08)	41.9	41.8	3.6	3.6
5	1001.63 (200.13)	41.0	40.9	4.5	4.5
6	1201.76	40.0	40.0	5.5	5.4

小数点位置有误差

$$\lambda = \frac{gl^3}{4Eah^3} \Rightarrow E = \frac{gl^3}{4\lambda ah^3}$$

$$k = 4.4925 \times 10^{-4} \quad r = 0.99999976 \quad \sigma_k = 0.0014 \times 10^{-4}$$

$$\Rightarrow \bar{E} = 2.2134 \times 10^{11} \text{ Pa}$$

2.21 3.22