

# Hashing

Why we need Hashing

- Hashing can achieve  $O(1)$  time complexity
- Hash Table is created to store elements in which hashing is performed
- Hash function

↓

$$h(k) = k \bmod m$$

↑  
address in hash table

↑  
key to be stored

↑  
Size of Hash Table

Size of Hash Table

key to be stored

Hash Table

Array

Hash Function

if  $m = 5$

$k = 20, 21, 22, 23, 32$

$$h(20) = 20 \bmod 5 = 0$$

$$h(21) = 21 \bmod 5 = 1$$

$$h(22) = 22 \bmod 5 = 2$$

$$h(23) = 23 \bmod 5 = 3$$

$$h(32) = 32 \bmod 5 = 2$$

Hash Table

Index

element

0

20

1

21

2

22

3

23

4

22

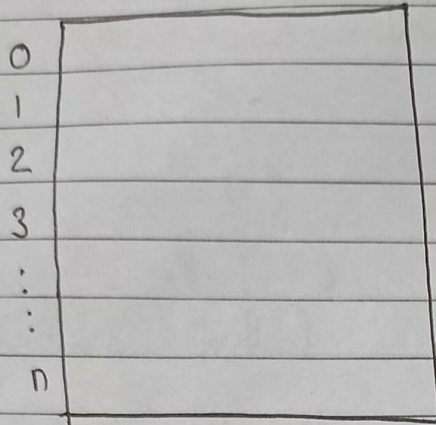
:

collision occurred

We cannot put 32 at address 2 as it is already occupied, this is two values of hash function are same i.e. value of 22 & 32 and this process is called collision.



# Solution to Callisiew is DAT Direct Address Table



## - Diff b/w Hash Table & DAT 5★

⇒ Hash Function - It is a mathematical formula <sup>used</sup> to ~~map~~ the map a given key within hash table

Types of Hash function

⇒ Divid. Division Method -  $h(k) = k \text{ mod } m$

⇒ Mid square Method -  $k^2$  ie  $k=25 \Rightarrow k^2=625$  remove ~~elem~~ values from left & right and value at centre is the index of the element in this case  $k^1$  is 25 and  $k^2$  is 625 after removing values from the left & right most value which is 6 & 5, we got 2 as index of element. If  $k^2=6024$  then index is 0 (Remove 1 from Left) & (Remove 2 from Right)

⇒ Folding Method -  $K = 12, 34, 56$

1  
12

34

56

102

Reject carry 1

and index is 02 or 2 for your element.



# Collision

Date

When more than one key point to the same slot in Hash table then it is called collision

Hash Table

$$h(k) = k \bmod m$$

$$k = 20, 30$$

$$h(20) = 20 \bmod 5 = 0$$

$$h(30) = 30 \bmod 5 = 0$$

collision occurred

## Collision Resolution Technique

- Chaining Method
- Probing Method

⇒ Chaining Method

Hash Table

3	
2	
1	
0	

$$k = 20, 30, 40, 50, 11, 21, 31$$

$$h(k) = k \bmod m$$

$$h(20) = 0$$

$$h(30) = 0$$

$$h(40) = 0$$

$$h(50) = 0$$

$$h(11) = 1$$

$$h(21) = 1$$

$$h(31) = 1$$

20

11 → 21 → 31 → NULL

20 → 30 → 40 → 50 → NULL

In Hash Table address is stored of the starting node. In this case address of 20 is stored at index 0 of Hash Table.



## Probing

- Linear Probing
- Quadratic Probing
- Double Hashing

### ⇒ Linear Probing

$$h'(k) = (h(k) + i) \bmod m \quad h'(k) = (h(k) + i) \bmod m$$

where  $h(k) = k \bmod m$

$m$  = No. of slots in Hash Table

$i$  = Probe No. = 0, 1, 2, ...

$k$  = 20, 30, 32, 41, 51

$$h'(20) = ((20 \bmod 5) + 0) \bmod 5 = (0 + 0) \bmod 5 = 0$$

$$h'(30) = ((30 \bmod 5) + 0) \bmod 5 = (0 + 0) \bmod 5 = 0$$

We cannot store 30 at index 0 as it is occupied by 20. So Now we are going to again call probe function for  $h'(30)$  where  $i = 1$

$$h'(30) = ((30 \bmod 5) + 1) \bmod 5 = (0 + 1) \bmod 5 = 1$$

There was collision b/w 20 & 30 key. And it is solved using prob function

### Chaining Method

1	30
0	20

### Problem of Linear Probing

- In probing in order to solve the problem of collision we calculate the index of hash table using linear probing function. While calculating the index we start by comparing the values from the start i.e. 0, 1, 2 Ex. This process is known as Primary Clustering



## Quadratic Probing

$$h'(k) = (h(k) + C_1 i + C_2 i^2) \bmod m$$

$C_1, C_2 = \text{constants}$

$$h(k) = k \bmod m$$

$$i = 0, 1, 2, \dots$$

$$C_1 = 1, C_2 = 3$$

$$\text{keys} = 20, 30, 32, 41, 51$$

$$\begin{aligned} 1) \quad h'(20) &= ((20 \bmod 5) + 1(0) + 3(0)^2) \bmod 5 \\ &= ((0) + 0 + 0) \bmod 5 \\ &= 0 \end{aligned}$$

$$\begin{aligned} 2) \quad h'(30) &= ((30 \bmod 5) + 1(0) + 3(0)^2) \bmod 5 \\ &= ((0) + 0 + 0) \bmod 5 \\ &= 0 \end{aligned}$$

Again run for  $h'(30)$  but  $i=1$

$$\begin{aligned} 3) \quad h'(30) &= ((30 \bmod 5) + 1(1) + 3(1)^2) \bmod 5 \\ &= ((0) + 1 + 3) \bmod 5 \\ &= 4 \bmod 5 \\ &= 4 \end{aligned}$$

$$\begin{aligned} 4) \quad h'(32) &= ((32 \bmod 5) + 1(0) + 3(0)^2) \bmod 5 \\ &= ((2) + 0 + 0) \bmod 5 \\ &= 2 \bmod 5 \\ &= 2 \end{aligned}$$

⇒ Problem with Quadratic Probing  
Secondary Clustering

# Double Hashing

$$h'(k) = (h_1(k) + i h_2(k)) \bmod m$$

$$h_1(k) = k \bmod m \quad \left. \begin{array}{l} h_1 \text{ \& } h_2 \text{ are hash function} \end{array} \right\}$$

$$h_2(k) = k \bmod m \quad \left. \begin{array}{l} \text{we can use any Method like} \\ \text{divide function, Mid square, Folding} \\ \text{Method} \end{array} \right\}$$

$$Q = h_1(k) \quad m = 5$$

$$h_2(k) \quad m = 3$$



# Question on Double Hashing 5★

★ given keys 71, 29, 38, 61, 100 map these keys in a hash table of size 5 with  $h_1 = k \bmod 5$  &  $h_2 = k \bmod 4$

~~$h(29) =$~~

$$\Rightarrow h(k) = [(h_1(k) + i \cdot h_2(k)) \bmod 5]$$

$$h(71) = [(71 \bmod 5) + 0 \cdot (71 \bmod 4)] \bmod 5$$

$$h(71) = [1 + 0] \bmod 5$$

$$h(71) = 1$$

$$\Rightarrow h(29) = [(29 \bmod 5) + 0 \cdot (29 \bmod 4)] \bmod 5$$

$$h(29) = [4 + 0 \cdot (1)] \bmod 5$$

$$h(29) = 4$$

$$\Rightarrow h(38) = [(38 \bmod 5) + 0 \cdot (38 \bmod 4)] \bmod 5$$

$$h(38) = [3 + 0] \bmod 5$$

$$h(38) = 3$$

$$h(38) = [(38 \bmod 5) + 1(38 \bmod 4)] \bmod 5$$

$$h(38) = 3$$

$$\Rightarrow h(61) = [(61 \bmod 5) + 0(61 \bmod 4)] \bmod 5$$

$$= [1 + 0] \bmod 5$$

$$= 1 \quad \text{collision}$$

$$\Rightarrow h(61) = [(61 \bmod 5) + 1(61 \bmod 4)] \bmod 5$$

$$= [1 + 1] \bmod 5$$

$$= 2$$

$$\Rightarrow h(100) = [(100 \bmod 5) + 0(100 \bmod 4)] \bmod 5$$

$$= 0 + 0 \bmod 5$$

$$= 0$$

Hash Table  
using double hashing

4	29
3	38
2	61
1	71
0	100