

Database review 12

2 min

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Linear Hashing

Key Notes: I = MSB, N = #Buckets

Linear Hashing: ALGORITHM

$i = \text{MSB}$

$N = \# \text{Buckets}$

Split if : $\frac{\# \text{ of full Buckets}}{\# \text{ of Buckets}} > \text{load}$

(2) Overflow Block is full

When do you use an overflow block?

If Bucket is full but Not

$\frac{\# \text{ Buckets full}}{\# \text{ Buckets}} > \text{load}$

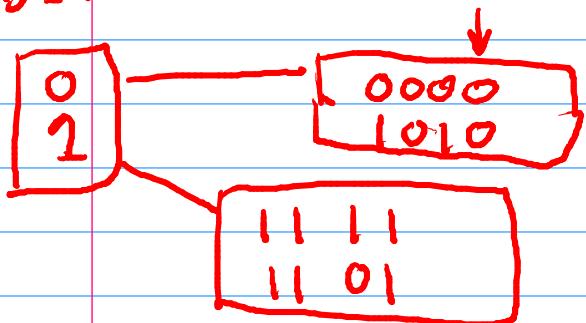
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00
01
10
00
01
10
11

\Rightarrow Use overflow

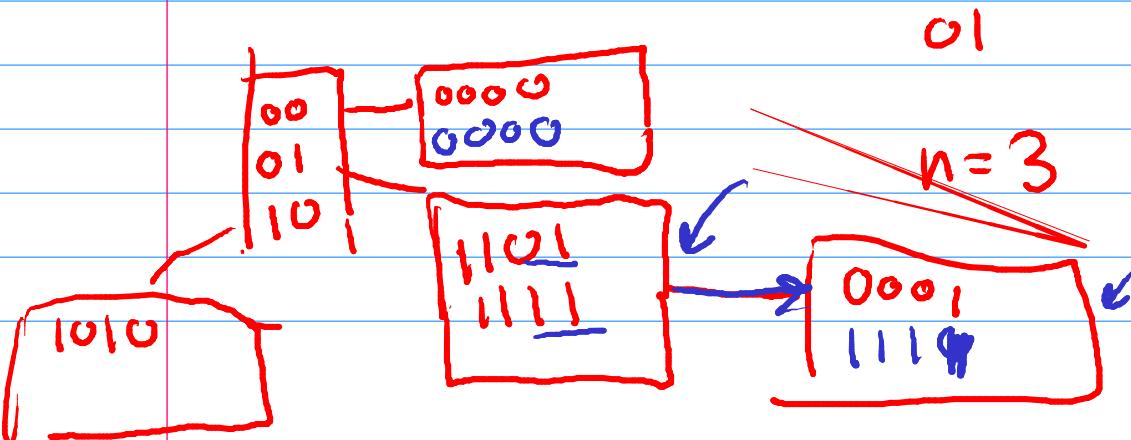
using linear hashing, with an overflow of 0.9
add these values

MSB = 1

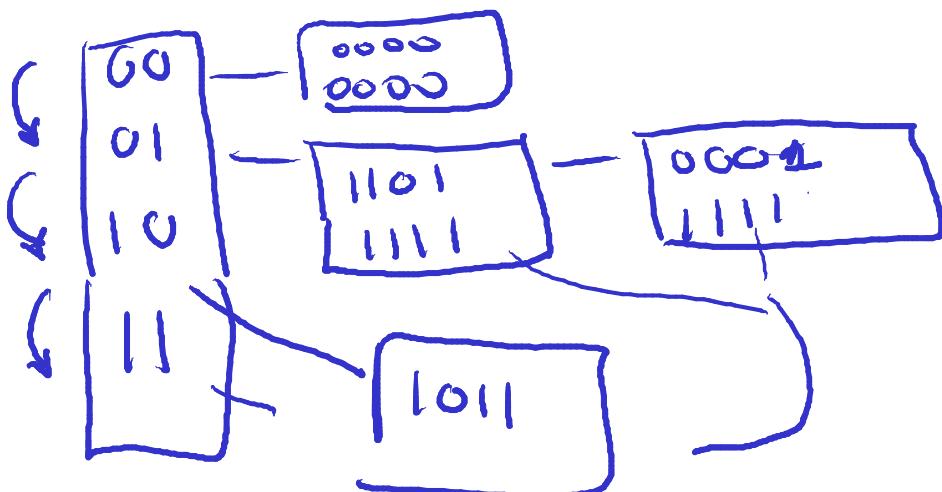


• 0000
→ • 1010
→ • 1111
→ • 1101 ← 0001
• 0001 ↑
→ • 0000 } extra
• 1111 ↗

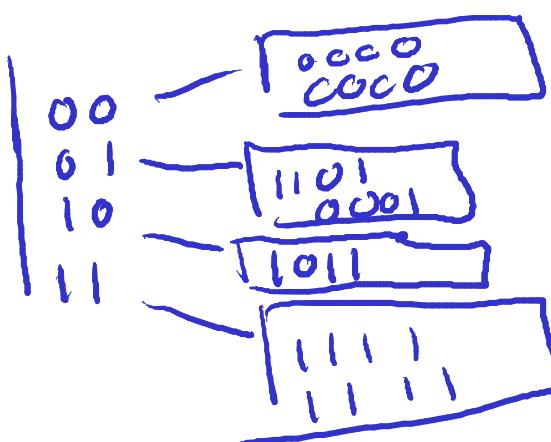
$\text{MSB} + 1 = 2$



$1/3 = 0.33$
 $0.9 > 0.3$



$$MSB+1$$
$$= 3$$



mod X = Binary

Extendible hashing

Algorithm : take mod of value then
Convert Binary fit into bucket
If # in Bucket > records \Rightarrow MSB + 1

Using an extendible hashing thingy, write the structure:

$h(x) = x \bmod 5$ each bucket can hold 4
 Indexes Joey-Issa-2024

2, 7, 3, 4, 5, 11, 17, 20, 22, 14, 9

$$2 \bmod 5 = 2 \quad 010^*$$

$$7 \bmod 5 = 2 \quad 010^*$$

$$3 \bmod 5 = 3 \quad 011^*$$

$$11 \bmod 5 = 1 \quad 001$$

$$17 \bmod 5 = 2 = 010$$

$$20 \bmod 5 = 0 = 000$$

$$22 \bmod 5 = 2 = 010$$

$$0 \rightarrow 2, 17 \checkmark \quad 22 \bmod 5 + 1$$

$$\rightarrow 7 \quad 20$$

$$1 \rightarrow 3$$

$$14 \bmod 5 = 4 \\ = 100$$

$$00 \rightarrow 20, 9, 14$$

$$10 \rightarrow 2, 7, 17, 22$$

$$01 \rightarrow 11,$$

$$11 \rightarrow 3$$

$$4 \checkmark \quad 9 \bmod 5 = 100 \\ = 4$$

B + trees

me ↗
↗

Average
HASH MAP



Average
B-TREE MAP



Tips: $n = \text{value}$

$n=4$

$n-1 = \# \text{Values in box}$

so You can have n children

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Minimum element :

2 for $n=5$
1 for $n=4$

value in
Branch
found in leaf
to the
> side.

How do we know this?

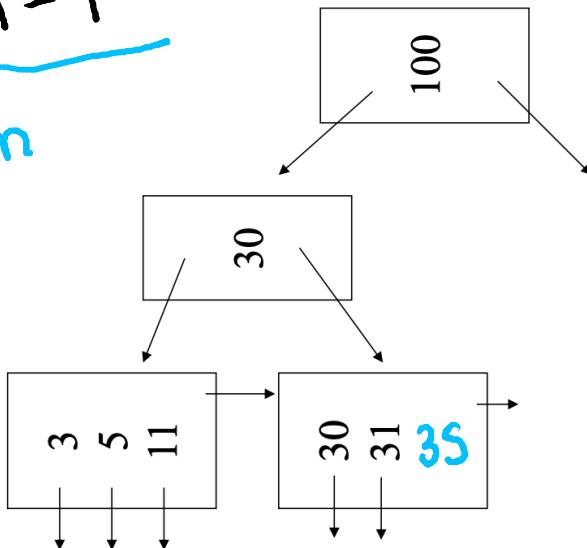
$$\rightarrow \text{ceil} \left\lceil \frac{n}{2} \right\rceil - 1$$

$$\text{ceil} \left[\frac{5}{2} \right] = 2$$

Insert 35

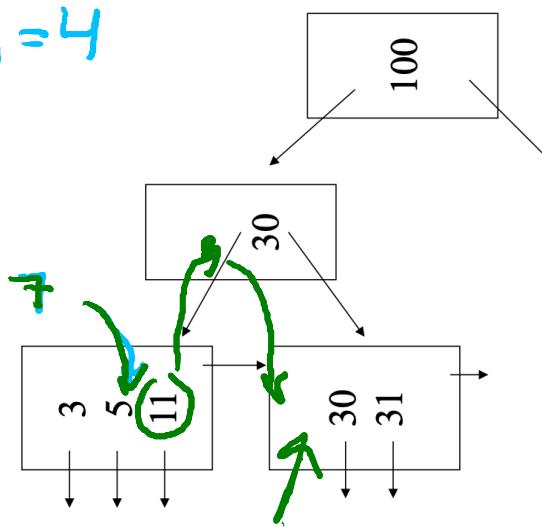
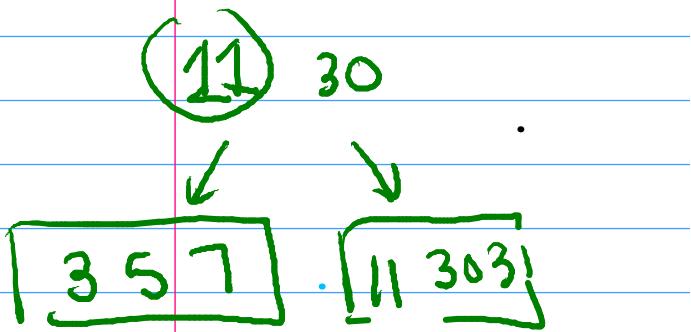
$n=4$

3 elem



Insert >

$n=4$

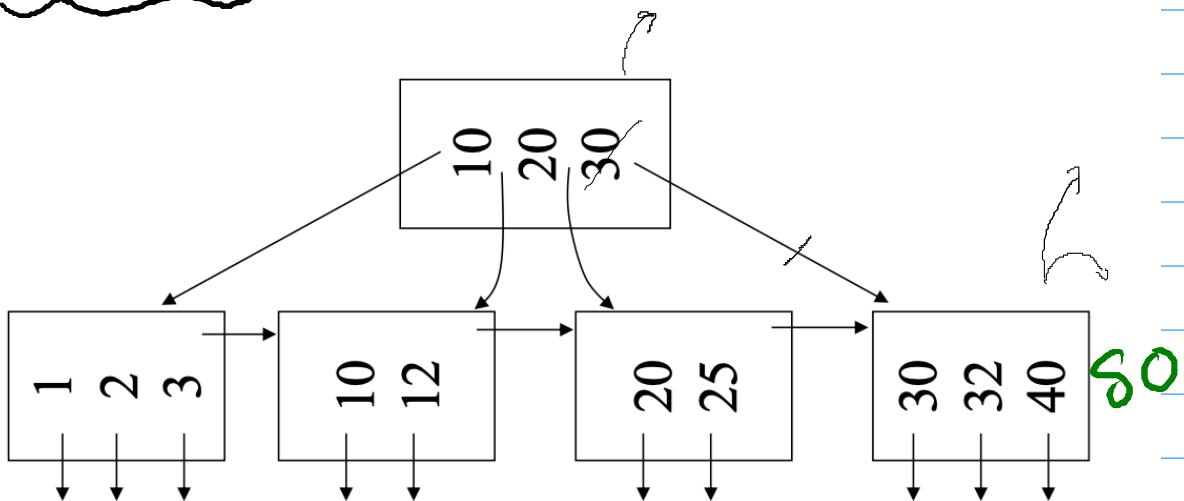


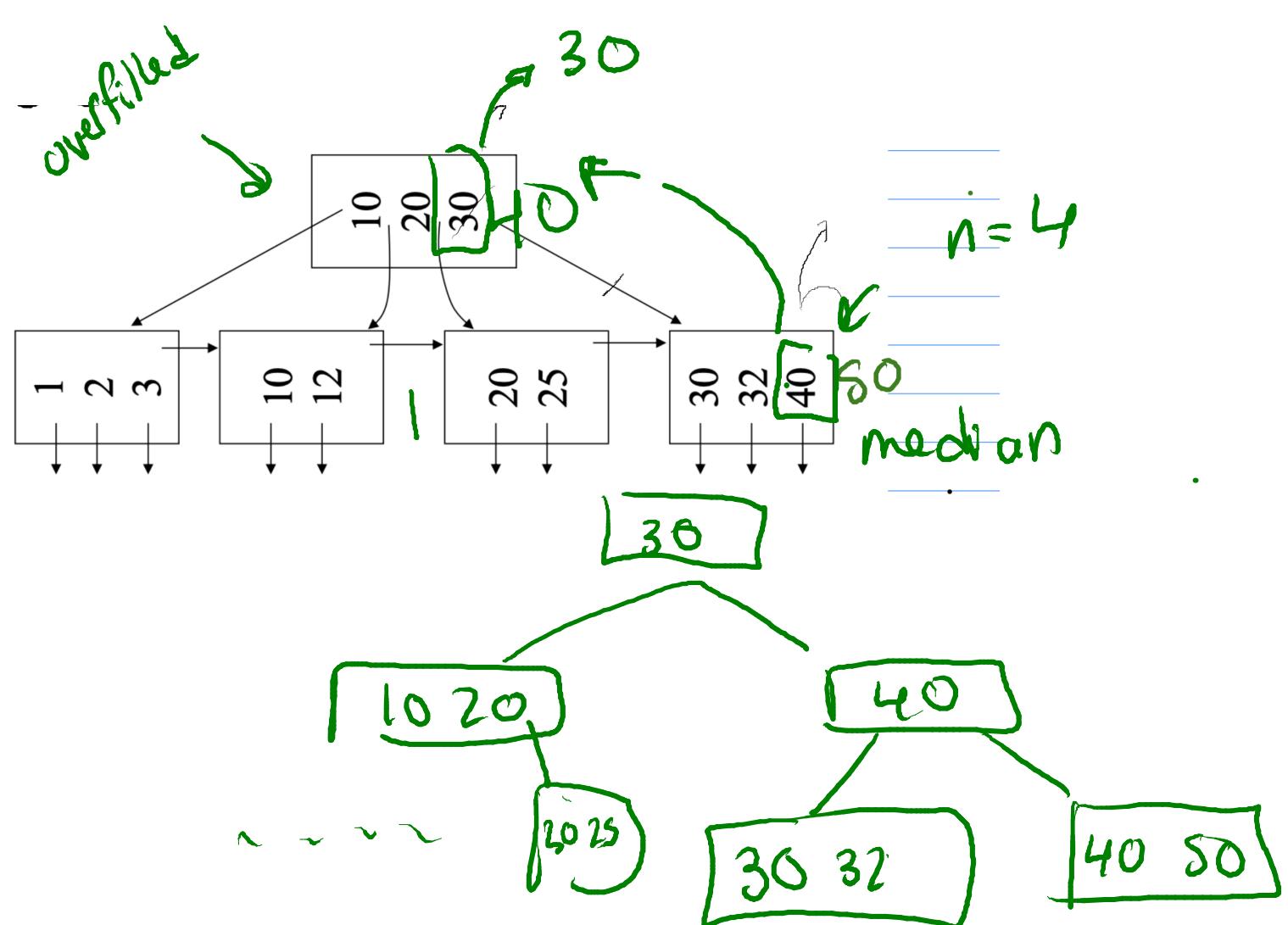
More examples in slides

1 more important addition (new root)

Insert 50

$n=4$

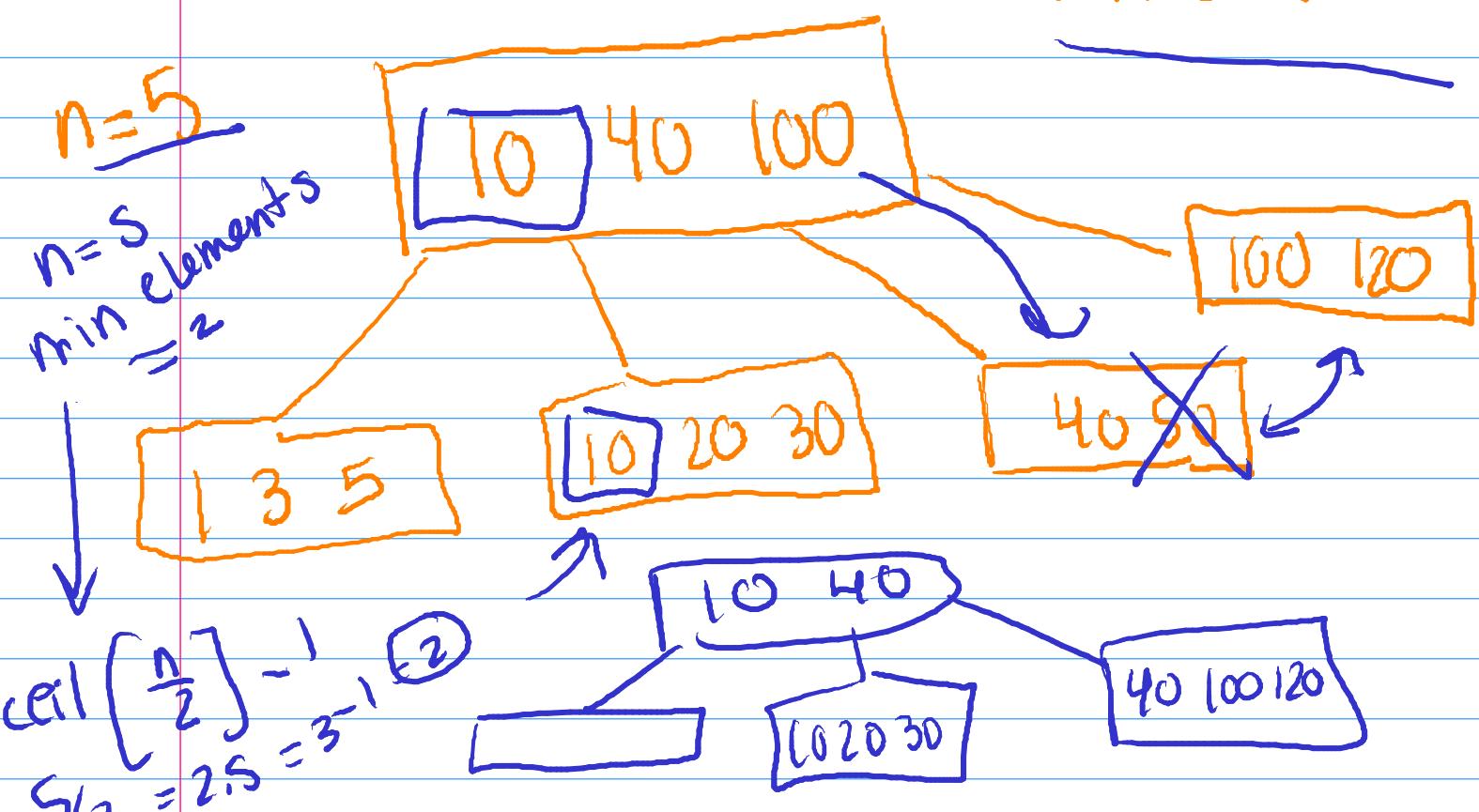




Deletion

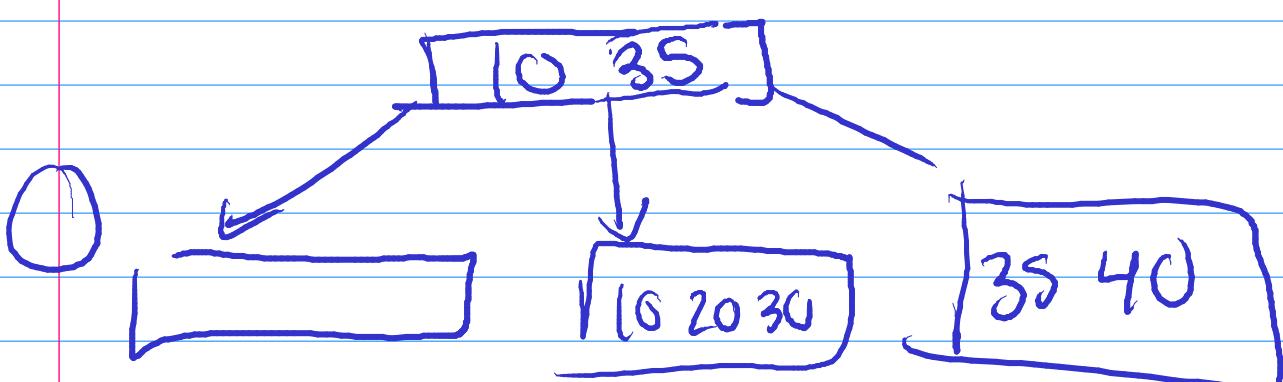
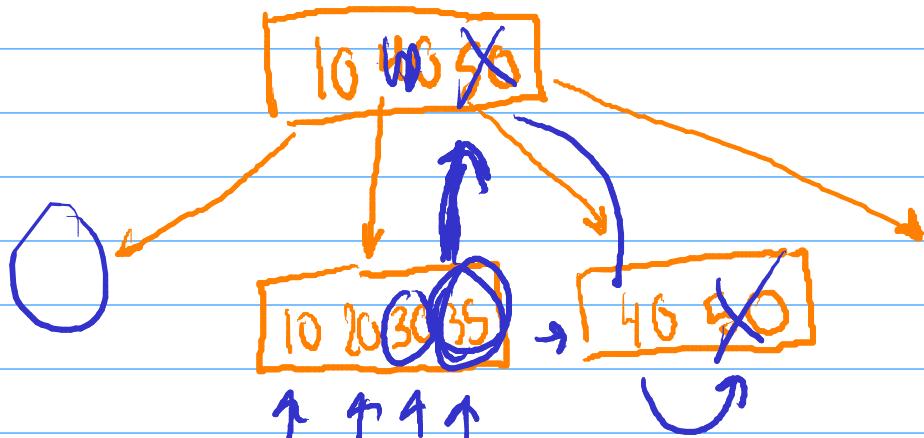
B+ tree

Delete 50



Delete 50

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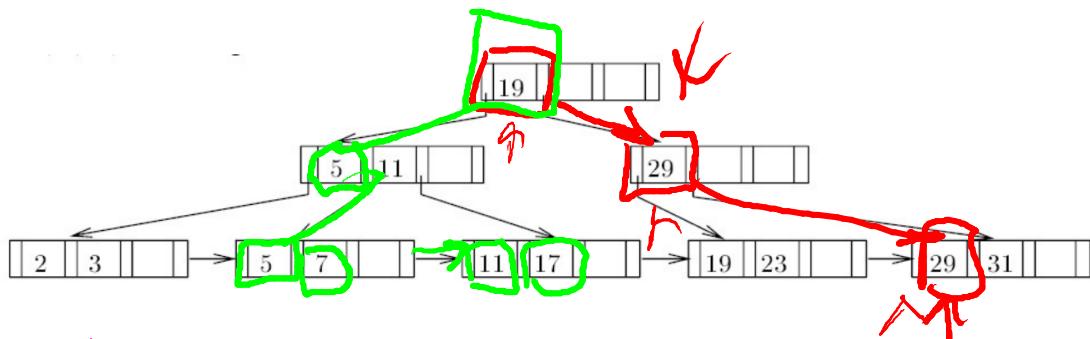


find record with Key ≈ 29

Junk drawer :

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Assume that the following B+ tree is given:



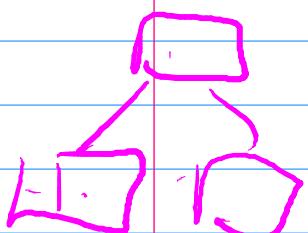
find values from 5 to 17 inclusive

5 7 11 17

(A lot more examples in notes)

Some formulas : $\# \text{ leaf} = \left\lceil \frac{\text{records}}{\text{keys}} \right\rceil$

$\# \text{ Blocks in level} = \left\lceil \frac{\text{leaves}}{\text{keys} + 1} \right\rceil$



\rightarrow (B) until 2
then + 1

- Assume a relation R(A,B,C,D) with 1000 records and a B+tree index on C. There are 14 keys per index block. How many leaf blocks does the index have?

$$\# \text{ leaf} = \left\lceil \frac{1000}{14} \right\rceil \quad \begin{matrix} \text{ceil} \\ \text{round up} \end{matrix}$$

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- Assume a B+tree index with 83 leaves and 6 keys per index block. How many levels does the tree have?

83 leaves 6 key

$$\# \text{ Blocks} = \left\lceil \frac{\text{leaves}}{\text{keys}+1} \right\rceil$$

$$\# = \left\lceil \frac{12}{7} \right\rceil \quad \rightarrow \quad = \left\lceil \frac{83}{7} \right\rceil$$

$$= (2) \quad \quad \quad = 12$$

$$\# \quad 1 + 2 + 12 + 83 \quad \quad \quad = 12$$

file & storage Mgmt

✓ Slides
Chapter

⇒ read Slides

?? max rotational delay??

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$$= \frac{1}{7200} \text{ (rev/min)}$$

1. Consider a disk with a sector size of 512 bytes, 100 sectors per track. Given a rotational speed of 7200 revolutions per minute, what is the maximum rotational delay to the start of a sector? Assuming that one track of data can be transferred per revolution, what is the transfer rate?

Rotational delay

$$\frac{1 \text{ track}}{\text{rev}}$$

$$= 1 / \text{rev/min}$$

$$= 1 / 7200$$

$$\Rightarrow \frac{\text{bytes}}{\text{sector}} \times \frac{\text{sectors}}{\text{track}} \times \frac{\text{revolutions}}{\text{min}} \times \frac{\text{track}}{\text{rev}}$$

bytes/min

$$TR = \frac{512 \text{ bytes}}{\text{sector}} \times 100 \times 7200 \times \frac{1 \text{ track}}{\text{rev}}$$

Normalization

Consider the following functional dependencies for the relation scheme R(A,B,C,D,E):

$$A \rightarrow BC$$

$$CD \rightarrow E$$

$$B \rightarrow D$$

$$E \rightarrow A.$$

FD

* Rules in slides make this E2

Show that all the attributes of R are functionally dependent on each of the following sets of attributes:

i) A

ii) BC

$$A = \{B, C, D, E, A\} \quad A \rightarrow BC$$

$$A \rightarrow C$$

$$E \rightarrow A$$

$$A \rightarrow A$$

A^{FD}

$$A \rightarrow B, A \rightarrow C$$

$$B \rightarrow D, A \rightarrow B$$

$$\Rightarrow A \rightarrow D$$

$$CD \rightarrow A \quad A \rightarrow C, A \rightarrow D$$

$$A \rightarrow C, A \rightarrow D, CD \rightarrow E = A \rightarrow E$$

Rules

- $A \rightarrow B \wedge B \rightarrow C \text{ then } A \rightarrow C$
- $B \subseteq A, A \rightarrow B$
- $A \rightarrow BC \text{ then } A \rightarrow B \wedge A \rightarrow C$
- * $CD \rightarrow A, A \rightarrow C, A \rightarrow D \Rightarrow A \rightarrow A$

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- $A \rightarrow B \text{ then } XA \rightarrow XB$
- $A \rightarrow B \wedge B \rightarrow C \text{ then } A \rightarrow C$
- $A \rightarrow B \wedge CD \rightarrow D, AC \rightarrow D$

BC

$CD \rightarrow E$

$B \rightarrow D$

$CB \rightarrow E$

$E \rightarrow A$

Also

$\cancel{CB} \rightarrow A$

~~FD~~

Which FD do not hold in table?

Key things : $mk = \text{multi attribute primary Key}$

case 1:

$Mk \rightarrow Mk$ X Bad

subset primary key ↑
subset prim. key

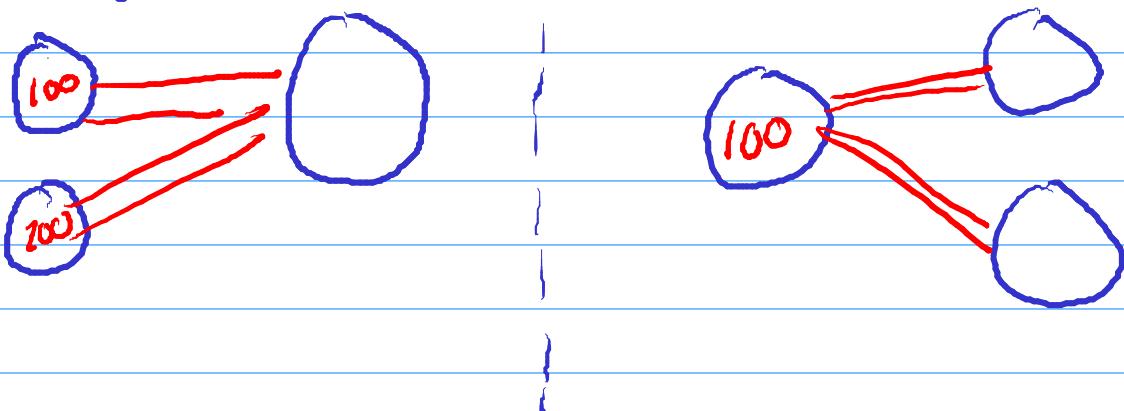
case 2:

Look @ table

If mk , you don't have unique

primary key
(Not unique for all tuples)

LS



Tips Define Superkey - A set where you can uniquely ID every row

Superkey = {A, B, C}
 $\times \{A, B\}$

Candidate Key - A superkey that does not \subseteq inside that is also a superkey

Primary Key - A candidate key ... User defined

Duplicated $100 \rightarrow \text{value}$

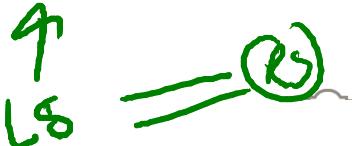
Consider the following table called CSP

C#	CName	P#	PName	Type	Colour	S#	Sname	Date	Qty
100	dupont	10	wheel	a32	black	30	doe	10.10	25
100	dupont	20	tyre	b12	black	30	doe	10.10	30
200	martin	50	door	x21	white	10	minty	20.9	50
200	martin	20	tyre	b12	black	10	minty	20.9	50
300	dupont	70	bumper	a10	grey	30	doe	20.9	20

Of the following dependencies which definitely do not hold in CSP?

- a. $C\# \rightarrow P\#$ ~~hold~~
- b. $C\# \rightarrow CName$ ✓
- c. $P\# \rightarrow Type$ ✓
- d. $Colour \rightarrow PName$ ~~X~~
- e. $S\# \rightarrow Qty$

$LS \rightarrow RS$



Consider again the CSP relation:

C#	CName	P#	PName	Type	Colour	S#	Sname	Date	Qty
100	dupont	10	wheel	a32	black	30	doe	10.10	25
100	dupont	20	tyre	b12	black	30	doe	10.10	30
200	martin	50	door	x21	white	10	minty	20.9	50
200	martin	20	tyre	b12	black	10	minty	20.9	50
300	dupont	70	bumper	a10	grey	30	doe	20.9	20

Not just
a subset

Suppose that $(C\#, P\#, Date)$ is the primary key of CSP and that the following FDs hold in CSP:

- $C\# \rightarrow CName$
- $P\# \rightarrow PName$
- $S\# \rightarrow Sname$
- $PName \rightarrow Type$
- $PName \rightarrow Colour$
- $C\#, P\# \rightarrow S\#$

\hookrightarrow 2NF Non key element fully dependant on primary key
 \hookrightarrow (not just a subset)

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Show that CSP is not 2NF ↪

CName only depends on a subset of a primary key

Give lossless decomp :

* Algorithm

- $L \rightarrow RS \quad R(LS, RS)$
- $LS, LS \rightarrow RS \quad R(LS, LS, RS)$

element not found RS

→ whole primary key $R(R.\text{key}, RS)$

A relation is in 2NF if it has No Partial Dependency, i.e., no non-prime attribute (attributes that are not part of any candidate key) is dependent on any proper subset of any candidate key of the table. In other words,

If the proper subset of the candidate key determines a non-prime attribute, it is called partial dependency. The normalization of 1NF relations to 2NF involves the removal of partial dependencies. If a partial dependency exists, we remove the partially dependent attribute(s) from the relation by placing them in a new relation along with a copy of their determinant.



Consider again the CSP relation:

C#	CName	P#	PName	Type	Colour	S#	Sname	Date	Qty
100	dupont	10	wheel	a32	black	30	doe	10.10	25
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200	martin	20	tyre	b12	black	10	minty	20.9	50
300	dupont	70	bumper	a10	grey	30	doe	20.9	20

Suppose that $(C\#, P\#, Date)$ is the primary key of CSP and that the following FDs hold in CSP:

$$\begin{array}{l} C\# \rightarrow CName \\ P\# \rightarrow PName \\ S\# \rightarrow Sname \\ PName \rightarrow Type \\ PName \rightarrow Colour \\ C\#, P\# \rightarrow S\# \end{array}$$

$R(C\#, CName)$

LS primary key

Duplicated

$R(S, Sname)$

Give a lossless decomposition of CSP into 2NF relation schemes.

$\rightarrow R(P, PName, type, Color)$

$\rightarrow R(C, P, S)$

$R(C, P, Date, Qty)$

Definitions

key

Phone #: 613

1NF No atomic values
↳ value composed of two values

(unique)

2NF Non key element fully
dependent on primary key

any
P.K → RS
unique element D.Key

2NF

3NF Key attribute depends on
transitivity

$A \rightarrow B, B \rightarrow C$
 $A \rightarrow C$

BCNF
LS
Must key

if intersection holds R_1, R_2
⇒ then lossless

Not Covered 3NF, BCNF

SQL ⇒ Do Practice in Slides

given database : easy - intermediate → hard

Consider the Sailors-Boats-Reserves database.

$\exists [s(sid, sname, rating, age)$
 $b(bid, bname, color)$
 $r(sid, bid, date)]$

Write each of the following queries in SQL.

SQL
DC
Domain
color column

1. Find the colors of boats reserved by Albert.

$(\prod_{color} ((\sigma_{sname=Albert} S \bowtie b) \bowtie r))$

Select from s, b, r
where s.sid = r.sid and
b.bid = r.bid
and
 $s.sname = "Albert"$

2. Find all sailor id's of sailors who have a rating of at least 8 or reserved boat 103.

(Select sid from s where rating > 8)

U

(Select sid from r where bid = 103)

$\prod_{sid} ((\sigma_{rating > 8} s) \cup \prod_{sid} (\sigma_{bid=103} r))$

Relational Algebra

* Symbols :

π project 6 - select

ex. "6 dept-name = "Physics" (instructor)"

Natural join $r \bowtie s$ Ex: $\Pi_{\text{branch-name}}$ (deposit)

- result removes duplicates (if both tables have)
- extending table (combining them) them

Relations r, s:

A	B	C	D
a	1	a	a
b	2	y	a
y	4	b	b
a	1	y	a
b	2	b	b

r

B	D	E
1	a	a
3	a	b
1	a	y
2	b	b
3	b	c

s

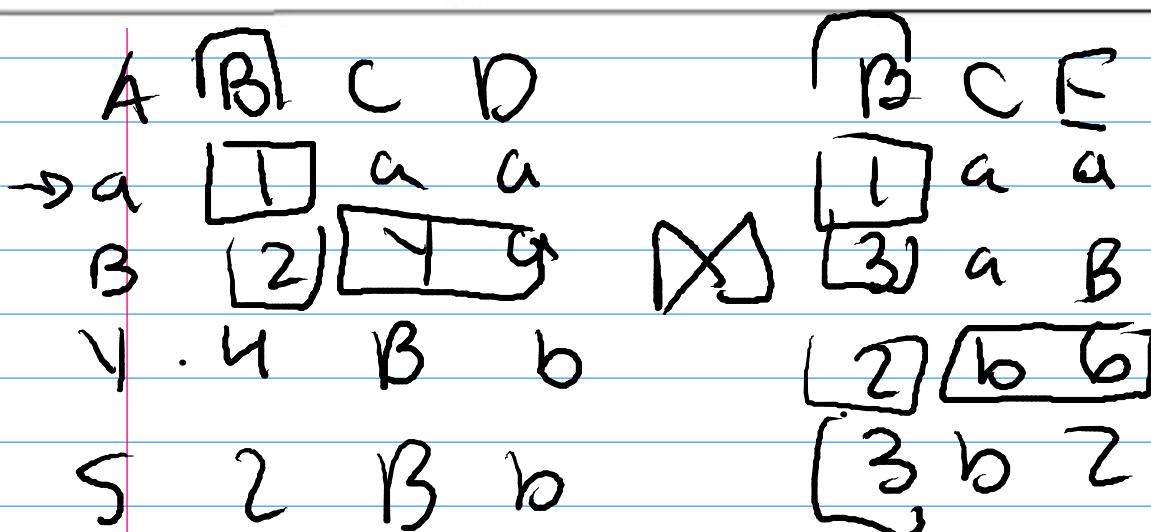
if no match (only include it if between tables it matches row from another table)
it gets ignored

$r \bowtie s$

A	B	C	D	E
a	1	a	a	a
b	2	a	a	b
a	1	y	a	a
a	1	y	a	y
b	2	b	b	b

* Key is:
column in R & S must have
Same name.

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A B C D E

a z a a a

B 2 Y a e

B 2 Y b 6

BCNF



3NF

SQL

LS P.Key

decomposition

ID 3NF

Conversion
decomposition

FD → What is FD?

normal form?

$\{F^3\}^+$ → Decomposed relations

B+ tree → inserting + Delete

Liner extendible hashing

• ordering indexes, insert, overflow