

Exercise 9.1 (May 29, 2020)

-B9TB1707

Question:

- A, B, C and D are the last 4 digits from your student number (see Exercise 4.1)
- In an area of a country, it is known that earthquakes occur $0.7 \cdot (A+1)$ times in $B+1$ days in an average sense since the dawn of the history
- However, there were $10+C+D$ earthquakes in the last four weeks
- Calculate the probability of $10+C+D$ and more earthquakes occurring in four consecutive weeks

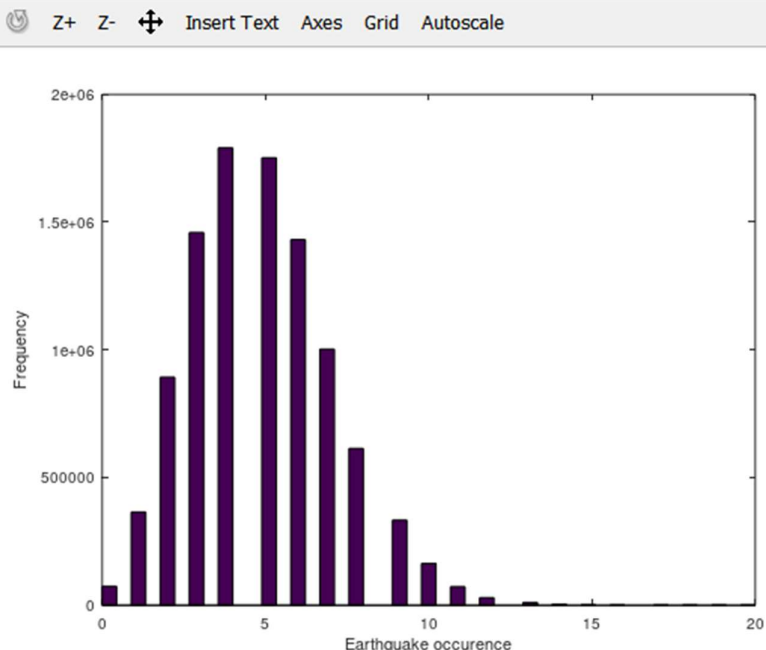
Solution:

My code for the solution is as follows:

```
CAPS_09_B9TB1707_9.1.m
1 A = 1, B = 7, C = 0, D = 7;
2 l = .7*(A+1)*28/(B+1);
3 t = 10+C+D;
4 occurrence=randp(l,10000000,1);
5 hist(occurrence,45);
6 xlabel('Earthquake occurrence');
7 ylabel('Frequency');
8 n=occurrence>=t;
9 p=sum(n)/length(n);
10 printf("The probability is earthquakes occurring %d times or more in 28 days is %d",t,p);
```

The output is as follows:

```
Command Window
>> The probability is earthquakes occurring 17 times or more in 28 days is 1.4e-05
```



Where $A = 1$, $B = 7$, $C = 0$, $D = 7$.

The probability that the event happened k times in this specified interval is given by;

$$P(X = k) = \frac{\lambda^k e^{-\lambda}}{k!}$$

And the expected value of the event defined $E[X]$ is equal to λ .

This is the Poisson distribution equation, and I will use this equation to solve this problem.

How it works:

1. Line 1 declares the variables A, B, C, D.
2. Line 2 declares the variable to hold the value of lambda for the Poisson equation.
3. Line 3 declares the variable to hold the unusual occurrences of earthquakes, the threshold value.
4. A Poisson distribution is generated by randp function of length 10000000
5. Line 5 generates a histogram based on the Poisson distribution.
6. Line 6 and 7 labels the histogram.
7. Line 8 filters the data in the distribution and keeps only the values equal to or greater than the threshold, by using a simple relational operator `>=`.
8. Line 9 calculates the probability
9. Line 10 displays the results.

Conclusion:

The program above uses the `randp()` function to generate the Poisson distribution. One could use an iterative approach to solve this problem, but I feel that this way is too inefficient and cumbersome to code, so I stuck with the `randp()` function.