## **Problem Set**

## Problem 1

A small foundry needs to schedule the production of four different castings during the next week. The production requirements of each casting are summarized in the following table:

Product	Unit production times (minutes)					
Product	Pouring	Cleaning	Grinding	Inspection	Packing	
Α	3	8	10	1	3	
В	1	12	6	1	5	
С	2	6	9	1	3	
D	1	7	7	1	2	

The unit profit for products A, B, C, and D are \$18, \$15, \$13, and \$14, respectively. Current demands indicate that all castings that are made can be sold; however, contracts dictate that at least 200 units of Product A and 300 units of Product D must be produced. The estimated times available for each of the operations during the next week are:

Pouring	40 hours
Cleaning	80 hours
Grinding	80 hours
Inspection	20 hours
Packing	40 hours

Determine how many of each of the products should be produced next week to maximize the total profit. Formulate the linear model for this problem; clearly define the variables, and state the objective function and constraints.

## **Problem 2**

An agriculture mill manufactures feed for cattle, sheep, and chickens. This is done by mixing the following main ingredients: corn, limestone, soybeans, and fish meal. These ingredients contain the following nutrients: vitamins, protein, calcium, and crude fat. The contents of the nutrients in each kilogram of the ingredients is summarized below:

Ingradiant	Nutrient					
Ingredient	Vitamins	Protein	Calcium	Crude fat		
Corn	3	8	10	1		
Limestone	1	12	6	1		
Soybeans	2	6	9	1		
Fish meal	1	7	7	1		

The mill contracted to produce 10, 6, and 8 tons of cattle feed, sheep feed, and chicken feed. Because of shortages, a limited amount of the ingredients is available-namely, 6 tons of corn, 10 tons of limestone, 4 tons of soybean, and 5 tons of fish meal. The price per kilogram of these ingredients is respectively \$0.2, \$0.12, \$0.24, and \$0.12. The minimal and maximal units of the various nutrients that are permitted is summarized below for a kilogram of the cattle feed, the sheep feed, and the chicken feed.

	Nutrient							
	Vita	mins	Protein		Calcium		Crude fat	
Product	Min	Max	Min	Max	Min	Max	Min	Max
Cattle feed	6	8	6	∞	7	8	4	8
Sheep feed	6	8	6	∞	6	8	4	6
Chicken feed	4	6	6	∞	6	8	4	6

Formulate this feed-mix problem so that the total cost is minimized.

## Problem 3

A corporation has \$30 million available for the coming year to allocate to its three subsidiaries. Because of commitments to stability of personnel employment and for other reasons, the corporation has established a minimal level of funding for each subsidiary. These funding levels are \$3 million, \$5 million, and \$8 million, respectively. Owing to the nature of its operation, subsidiary 2 cannot utilize more than \$17 million without major new capital expansion. The corporation is unwilling to undertake such expansion at this time. Each subsidiary has the opportunity to conduct various projects with the funds it receives. A rate of return (as a percent of the investment) has been established for each project. In addition, certain of the projects permit only limited investment. The data for each project are given below.

Subsidiary	Project	Rate of return	Upper limit of investment
1	1	8%	\$6 million
	2	6%	\$5 million
	3	7%	\$9 million
2	4	5%	\$7 million
	5	8%	\$10 million
	6	9%	\$4 million
3	7	10%	\$6 million
	8	6%	\$3 million

Formulate this problem as a linear program.