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Research Article

Modeling and Optimization of Fluoride and Cadmium Trapping in Phosphogypsum Using Design Methodology

The manufacturing of phosphoric acid from natural calcium phosphate generates a solid residue containing 25-30% humidity. This solid residue (phosphogypsum) generates acidic solution (pH \approx 2.5) containing several toxic ionic species, that coat its grains. Fluorides and heavy metals such as cadmium are considered the most harmful species contained in the released solution from phosphogypsum. The purpose of this work is to study the trapping of fluorides and cadmium in phosphogypsum as well as effluent neutralization before its discharge into natural recipient. Therefore, calcium carbonate finely ground was added and fully mixed with wet phosphogypsum. A four factors central composite design was used to model and to optimize the operating parameters that govern the process. The studied factors were temperature, reaction time, mass, and grains size of CaCO₃. Considered responses were pH, F⁻, and Cd²⁺ concentrations in the released solution after reaction with CaCO₃. The optimum operating conditions were quite efficient to trap, respectively, 99% Cd²⁺ and 97% of F with a final pH of 6.66. So an original, easy, simple, and cost effective method to trap some toxic species on phosphogypsum through CaCO₃ addition would likely to be integrated in phosphoric acid manufacturing plant.

Keywords: Cadmium; Calcium carbonate; Central composite design; Fluoride; Neutralization; Phosphogypsum

Received: December 16, 2009; revised: May 22, 2010; accepted: June 30, 2010

DOI: 10.1002/clen.200900284

1 Introduction

Phosphogypsum is a residue of $\rm H_3PO_4$ manufacturing industry by the wet process. It's a very fine wet powder containing 25–30% moisture. Phosphogypsum valorization has been studied by several researchers that would help to solve an enormous environmental problem [1, 2].

In fact, phosphoric acid production process leads to the rejection of 1.7 t of phosphogypsum per ton of treated phosphate rock, which corresponds to 5 t of phosphogypsum per produced ton of P_2O_5 [3]. This residue ranks in the category of hazardous and toxic wastes [4]. Even after washing, the residue remains impregnated with an acid solution which pH is between 2 and 3 [5]. Phosphogypsum also contains impurities coming from phosphate rock [2, 6–9] such as cadmium and fluoride. Consequently, there are environmental risks associated with phosphogypsum storage methods. Indeed, during its storage the phosphogypsum liberates a part of its impregnation water. This effluent is highly acidic and contains some ionic entities that may affect the environment (soil and ground water).

Therefore it would be very beneficial to develop a procedure that neutralize the solution and prevent toxic entities to come into

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contact with the natural environment. Accordingly, the addition of a reactive alkaline solid into wet phosphogypsum was adopted. This choice was dictated by the results of our earlier work related to the interaction of an industrial effluent (solution released by phosphogypsum) with groundwater [10]. This work highlighted particularly the neutralization of the acidic solution and the formation of a precipitate (CaF₂) able to retain heavy metals, especially cadmium. Consequently, it is foreseeable that an alkaline solid would play the same role as the groundwater (slightly alkaline) and leads to the precipitation of calcium fluoride and trapping of some heavy metals. Indeed preliminary tests showed the neutralization of the phosphogypsum impregnation solution and trapping of heavy metals in the solid matrix. This result easily conceivable could be explained by the formation of CaF₂ after the attack of calcium carbonate by the acidic solution and simultaneous retention of heavy metal by the formed product. Thus, further to these events the phosphogypsum released solution would be neutral and free of toxic ionic entities and hence less harmful to the natural environment.

With regard to the above-mentioned observations, the aim of this work was to determine the optimum conditions for trapping toxic entities (fluoride and cadmium) and neutralization of the released solution through ${\rm CaCO_3}$ addition.

Hence a four factors central composite design was chosen. The studied factors were temperature, reaction time, $CaCO_3$ added mass, and finally the grains size of calcium carbonate. The selected responses are pH, concentrations of fluoride and cadmium ($|F^-|$

and $[Cd^{2+}]$). In fact each response depends on several factors as reported in the literature [11–13].

2 Materials and Methods

2.1 Experimental Protocol

A predetermined mass of $CaCO_3$ finely crushed was added to each sample of wet phosphogypsum. The resulting mixture was kept at a defined constant temperature for a specified period of time.

The experimental protocol is as follows:

- (1) Weight 200 g of phosphogypsum.
- (2) Add the necessary mass of CaCO₃.
- (3) Mix well the previous reagents for 10 min.
- (4) Immerse the mixture in a water bath at a specified constant temperature and for a preset time.
- (5) Filter the mixture under pressure of 7 bar to retrieve the liquid phase.
- (6) Analyze chemically the filtrate for cadmium and fluoride ions and determine the pH of the liquid phase.

2.2 Analysis Techniques

A pH meter (691-pH Meter, Metrohm), with a combined glass electrode was used to measure the pH (±0.01). The ion meter (781-pH/Ion Meter, Metrohm) equipped with a crystalline membrane electrode 6.0502.150 was used to determine fluoride ion concentrations and the error is less than 1%. A potentiometer (TTTRINO DMS 716 of Metrohm) was used to determine chloride. The sulfate ions were determined by the gravimetric method. Cl $^-$ and $\mathrm{SO_4}^{2-}$ ions concentrations were determined with an error ranging from 0.1 to 0.2%. Flame atomic absorption spectrometer (AAS Vario 6) was used for Cd, Ca, Mg, Co, Zn, Al, Fe, and Cr determinations. A flame photometer was used for K and Na determinations. Finally the spectroscopy UV–VIS was used for the determination of phosphate ions, Perkin-Elmer UV–VIS Lambda 20 spectrometer was employed. All the above ions were determined with an error less than 1%. Further more additional method was adopted to analyze Cd^{2+} ions.

3 Results and Discussion

3.1 Properties of Phosphogypsum

The phosphogypsum impregnating solution (moisture 25–30%) was separated from the solid matrix by filtration under 7 bar pressure and then analyzed. The analytical results are listed in Tab. 1.

The composition, of phosphogypsum free solution, shown in Tab. 1 is not a mean composition but it is timely one, since it varies slightly depending on the plant progress. The above values remain within the same order of magnitude of those yearly measured. Table 1 shows without doubt that the solution is highly acidic and contains several chemical entities including heavy metals; thus the toxic character of this solution and its harm to the natural environment are quite noticed (Tunisian standard N.T.106.002: $6.5 < \mathrm{pH} < 8.5, \, \mathrm{F}^- \leq 3.00 \, \mathrm{mg} \, \mathrm{L}^{-1}, \, \mathrm{Cd}^{2+} \leq 0.005 \, \mathrm{mg} \, \mathrm{L}^{-1}).$

Phosphogypsum has been characterized by X-ray diffraction and examined under a binocular microscope (20 times). Figures 1 and 2 represent the obtained results.

The diffractogram shows essentially synthetic gypsum (CaSO $_4\cdot 2$ H $_2$ O) containing fluorapatite traces (Ca $_5$ (PO $_4$) $_3$ F).

Table 1. Composition of phosphogypsum free solution.

| Element | Free solution concentrations |
|--|------------------------------|
| pH | 2.35 |
| Conductance (mS) | 15.170 |
| Density | 1.018 |
| Dry residue (g L^{-1}) | 19.981 |
| $\operatorname{Cl}^{-}(\operatorname{gL}^{-1})$ | 5.663 |
| $F^-(gL^{-1})$ | 0.685 |
| $SO_4^{2-}(gL^{-1})$ | 3.723 |
| $PO_4^{3-} (gL^{-1})$ | 3.310 |
| $K^{+}(gL^{-1})$ | 0.147 |
| $Na^{+} (g L^{-1})$ | 5.551 |
| $Ca^{2+} (g L^{-1})$ | 1.643 |
| $Mg^{2+} (g L^{-1})$ | 0.49 |
| $Cd^{2+} (mg L^{-1})$ | 1.770 |
| $Co (mg L^{-1})$ | 0.219 |
| $\operatorname{Zn}\left(\operatorname{mg}\operatorname{L}^{-1}\right)$ | 1.789 |
| Al (mg L^{-1}) | 0.147 |
| Fe (mg L^{-1}) | 0.277 |
| $\operatorname{Cr}\left(\operatorname{mg}\operatorname{L}^{-1}\right)$ | 1.048 |

Figure 2 illustrates the image of a phosphogypsum sample examined under a binocular microscope. This image shows a mass of gypsum containing unattacked apatite grains. This is in agreement with the above X-ray analysis.

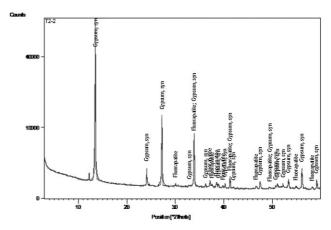


Figure 1. Diffractogram of a phosphogypsum sample.



Figure 2. Microscopic image of phosphogypsum (20 times).

3.2 Studied Factors and Experimental Domains

According to a preliminary work, four factors and their fields were adopted in this study. Table 2 illustrates the selected four factors and their fields.

The chosen responses were pH, cadmium and fluoride concentrations, designated by Y_1 (pH), Y_2 (mg L⁻¹), and Y_3 (mg L⁻¹), respectively.

3.3 Experimental Matrix and Models

The purpose of this work is to model and to optimize the selected responses $(Y_1, Y_2, \text{ and } Y_3)$. A central composite matrix is seemed necessary to achieve this goal (Tab. 3). As indicated in this table, the central composite matrix is built on sixteen (four factors: $2^n = 2^4 = 16$) (from 1 to 16) experiences (levels +1 and -1), eight experiences (from 17 to 24) named star points (levels +2 and -2), and finally eight identical repeated tests performed at the center and named center points (level zero) (from 25 to 32) with the purpose of calculating the experimental variance.

The model equation of second order is given below:

$$Y_{\mathrm{i}} = b_0 + \sum b_{\mathrm{j}} X_{\mathrm{j}} + \sum_{j \neq k} b_{\mathrm{j}k} X_{\mathrm{j}} X_{\mathrm{k}} + \sum b_{\mathrm{j}\mathrm{j}} X_{\mathrm{j}}^2$$

Where Y_i is the chosen response i, b_j the estimation of the significant factor effect j and X_j is its level. Table 4 summarizes the factor effects estimation for the three responses. As it can be seen, the significant factors are: CaCO₃ mass (b_2) , Setting time (b_3) , two quadratic terms $(b_{33}$ and $b_{44})$, and an interaction term (b_{23}) to the response pH (Y_1) , CaCO₃ mass (b_2) , and a quadratic term (b_{22}) to the response cadmium concentration (Y_2) and CaCO₃ mass (b_2) , Setting time (b_3) , Temperature (b_4) , two quadratic terms $(b_{11}$ and $b_{22})$, and an interaction (b_{34}) to the response fluoride concentration (Y_3) .

The resulted models are given by the following equations:

(1) pH:

$$\begin{split} Y_1 &= b_0 + b_2 X_2 + b_3 X_3 + b_{33} X_3^2 + b_{44} X_4^2 + b_{23} X_2 X_3 \\ Y_1 &= 5.355 + 0.918 X_2 + 0.294 X_3 + 0.178 X_3^2 + 0.275 X_4^2 + 0.395 X_2 X_3 \end{split}$$

Table 2. Studied factors and experimental domains.

| Effect | Factors | -2 | -1 | 0 | +1 | +2 | Increment |
|-------------|---|---------|----------|----------|----------|-----------|-----------|
| X_1 X_2 | Grain diameter of $CaCO_3$ (D_G) (μm) $CaCO_3$ mass (M_G) (g) | 69 2 | 106 4 | 143 6 | 180 8 | 217 10 | 37 2 |
| X_3 | Reaction time (T_r) (h) | 3 | 10 | 17 | 24 | 31 | 7 |
| X_4 | Temperature (T) (°C) | 23 | 26 | 29 | 32 | 35 | 3 |

Table 3. Central composite matrix and results.

| No of Exp. | $D_{G}\left(X_{1}\right)$ | $M_G(X_2)$ | $T_{\mathrm{r}}\left(X_{3}\right)$ | $T(X_4)$ | pH (Y ₁) | $[Cd] (10) (mg L^{-1}) (Y_2)$ | $[F] (mg L^{-1}) (Y_3)$ |
|------------|----------------------------|------------|-------------------------------------|----------|----------------------|-------------------------------|-------------------------|
| 1 | -1 | -1 | -1 | -1 | 4.65 | 3.60 | 30.80 |
| 2 | +1 | -1 | -1 | -1 | 4.71 | 3.56 | 37.20 |
| 3 | -1 | +1 | -1 | -1 | 6.39 | 0.15 | 19.30 |
| 4 | +1 | +1 | -1 | -1 | 6.53 | 0.21 | 21.60 |
| 5 | -1 | -1 | +1 | -1 | 4.84 | 3.35 | 28.60 |
| 6 | +1 | -1 | +1 | -1 | 4.56 | 3.11 | 33.60 |
| 7 | -1 | +1 | +1 | -1 | 7.33 | 0.13 | 16.90 |
| 8 | +1 | +1 | +1 | -1 | 7.41 | 0.17 | 22.60 |
| 9 | -1 | -1 | -1 | +1 | 5.36 | 3.25 | 32.40 |
| 10 | +1 | -1 | -1 | +1 | 5.63 | 3.57 | 35.80 |
| 11 | -1 | +1 | -1 | +1 | 5.82 | 0.31 | 20.70 |
| 12 | +1 | +1 | -1 | +1 | 6.46 | 0.46 | 23.80 |
| 13 | -1 | -1 | +1 | +1 | 4.74 | 3.54 | 22.10 |
| 14 | +1 | -1 | +1 | +1 | 5.09 | 2.98 | 24.10 |
| 15 | -1 | +1 | +1 | +1 | 7.95 | 0.11 | 14.90 |
| 16 | +1 | +1 | +1 | +1 | 7.71 | 0.13 | 16.60 |
| 17 | -2 | 0 | 0 | 0 | 6.45 | 0.12 | 26.50 |
| 18 | +2 | 0 | 0 | 0 | 5.22 | 1.56 | 33.30 |
| 19 | 0 | -2 | 0 | 0 | 3.25 | 9.29 | 65.50 |
| 20 | 0 | +2 | 0 | 0 | 6.25 | 1.30 | 32.10 |
| 21 | 0 | 0 | -2 | 0 | 5.15 | 1.25 | 17.30 |
| 22 | 0 | 0 | +2 | 0 | 6.64 | 0.16 | 8.90 |
| 23 | 0 | 0 | 0 | -2 | 6.15 | 2.75 | 16.90 |
| 24 | 0 | 0 | 0 | +2 | 6.42 | 1.10 | 11.40 |
| 25 | 0 | 0 | 0 | 0 | 5.55 | 0.49 | 14.10 |
| 26 | 0 | 0 | 0 | 0 | 5.04 | 0.68 | 17.90 |
| 27 | 0 | 0 | 0 | 0 | 5.21 | 0.74 | 20.40 |
| 28 | 0 | 0 | 0 | 0 | 5.62 | 1.26 | 15.60 |
| 29 | 0 | 0 | 0 | 0 | 4.92 | 0.35 | 16.30 |
| 30 | 0 | 0 | 0 | 0 | 4.87 | 1.47 | 19.20 |
| 31 | 0 | 0 | 0 | 0 | 5.68 | 0.78 | 15.10 |
| 32 | 0 | 0 | 0 | 0 | 5.95 | 1.16 | 18.50 |

Table 4. Factors signification for the three responses pH, [Cd] and [F].

| Coefficient | Value | Standard deviation | t-exp | Signification |
|----------------------|-----------------|-----------------------|--------|---------------|
| рН | | | | |
| b_0 | 5.355 | 0.155 | 34.47 | < 0.01*** |
| b_1 | -0.060 | 0.090 | -0.67 | 51.3 |
| b_2 | 0.918 | 0.090 | 10.23 | < 0.01*** |
| b_3 | 0.294 | 0.090 | 3.28 | 0.442** |
| b_4 | 0.120 | 0.090 | 1.34 | 19.9 |
| b_{11} | 0.163 | 0.081 | 2.01 | 6.0 |
| b_{22} | -0.108 | 0.081 | -1.34 | 19.8 |
| b_{33} | 0.178 | 0.081 | 2.20 | 4.19* |
| b_{44} | 0.275 | 0.081 | 3.41 | 0.336** |
| b_{12} | 0.014 | 0.110 | 0.13 | 90.2 |
| b_{13} | -0.075 | 0.110 | -0.68 | 50.4 |
| b_{23} | 0.395 | 0.110 | 3.60 | 0.223** |
| b_{14}^{-} | 0.064 | 0.110 | 0.58 | 56.9 |
| b_{24} | -0.111 | 0.110 | -1.01 | 32.5 |
| b_{34} | 0.022 | 0.110 | 0.20 | 84.0 |
| $[Cd]$ $(mg L^{-1})$ | | | | |
| b_0 | 0.866 | 0.189 | 4.58 | 0.0266*** |
| b_1 | 0.109 | 0.109 | 1.00 | 33.1 |
| b_2 | -1.720 | 0.109 | -15.76 | < 0.01*** |
| b_3^2 | -0.159 | 0.109 | -1.45 | 16.4 |
| b_4 | -0.135 | 0.109 | -1.23 | 23.4 |
| b_{11}^{-1} | -0.074 | 0.098 | -0.75 | 46.4 |
| b_{22}^{11} | 1.040 | 0.098 | 10.57 | < 0.01*** |
| b_{33} | -0.107 | 0.098 | -1.09 | 29.2 |
| b_{44} | 0.197 | 0.098 | 2.01 | 6.1 |
| b_{12} | 0.050 | 0.134 | 0.37 | 71.4 |
| b_{13} | -0.077 | 0.134 | -0.58 | 57.3 |
| b_{23} | 0.025 | 0.134 | 0.19 | 85.2 |
| b_{14}^{23} | 0.007 | 0.134 | 0.05 | 96.1 |
| b_{24}^{14} | 0.039 | 0.134 | 0.29 | 77.6 |
| b_{34}^{24} | -0.004 | 0.134 | -0.03 | 97.4 |
| $[F] (mg L^{-1})$ | | | | |
| b_0 | 17.138 | 0.947 | 18.09 | < 0.01*** |
| b_1 | 0.967 | 0.547 | 1.77 | 9.5 |
| b_2 | -6.458 | 0.547 | -11.81 | < 0.01*** |
| b_3 | -2.458 | 0.547 | -4.49 | 0.0320*** |
| b_4 | -1.300 | 0.547 | -2.38 | 2.95* |
| b_{11} | 1.911 | 0.493 | 3.88 | 0.121** |
| b_{22} | 7.886 | 0.493 | 15.99 | < 0.01*** |
| b_{33} | -1.039 | 0.493 | -2.11 | 5.0 |
| b_{44} | -0.776 | 0.493 | -1.57 | 13.4 |
| b_{12} | -0.770 -0.250 | 0.670 | -0.37 | 71.4 |
| $b_{12} \\ b_{13}$ | -0.250 -0.050 | 0.670 | -0.07 | 94.1 |
| $b_{13} \\ b_{23}$ | 0.837 | 0.670 | 1.25 | 22.8 |
| b_{14} | -0.575 | 0.670 | -0.86 | 40.3 |
| | -0.575 0.713 | 0.670 | 1.06 | 30.2 |
| b ₂₄ | -1.737 | 0.670 | -2.59 | 30.2 1.89* |
| b_{34} | -1./3/ | 0.070 | -4.39 | 1.05 |

^{* ** ***} Represent the signification level.

(2) Cadmium concentration:

$$Y_2 = b_0 + b_2 X_2 + b_{22} X_2^2$$

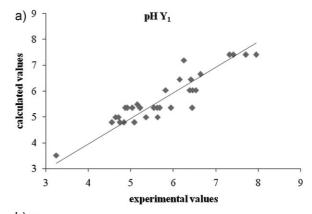
 $Y_2 = 0.866 - 1.720 X_2 + 1.040 X_2^2$

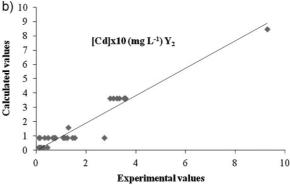
(3) Fluoride concentration:

$$\begin{split} Y_3 &= b_0 + b_2 X_2 + b_3 X_3 + b_4 X_4 + b_{11} X_1^2 + b_{22} X_2^2 + b_{34} X_3 X_4 \\ Y_3 &= 17.138 - 6.458 X_2 - 2.458 X_3 - 1.300 X_4 + 1.911 X_1^2 \\ &\quad + 7.886 X_2^2 - 1.737 X_3 X_4 \end{split}$$

3.4 Analysis of Residue

Figure 3 reveals the distribution of the calculated versus experimental values for the three responses $(Y_1, Y_2, \text{ and } Y_3)$. Figures 3a-c show, that the points are almost randomly distributed about the line





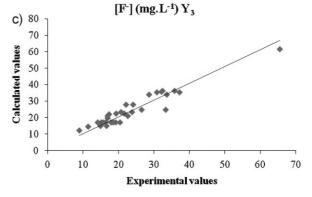


Figure 3. (a) Calculated versus experimental values graph for pH, (b) calculated versus experimental values graph for $[Cd^{2+}]$, and (c) calculated versus experimental values graph for $[F^-]$.

representing exact agreement providing little evidence of lack-offit for the three quadratic models. The deviations in the graphs correspond to root mean square errors of 0.409, 0.5049, and 3.299 for the responses Y_1 , Y_2 , and Y_3 , respectively. The maximum value that the standardized residuals take are 1.095 and 1.884 for the responses Y_1 and Y_2 , it means that about 95% of them should fall within ± 2 . However the maximum standardized residuals value of Y_3 response is 5.798 which exceeds the value 2. Hence it is necessary to go through a variance analysis of Y_3 response as it is beneficial to confirm the validity of Y_1 and Y_2 responses.

3.5 Analysis of Variance

Table 5 summarizes the variance analysis of the chosen responses Y_1 , Y_2 , and Y_3 . The main results for Y_1 , Y_2 , and Y_3 are, respectively, 0.211,

Table 5. Variance analysis.

| Source of variation | SS | DF | MS | Ratio | Signification |
|---------------------------|----------|----|---------|---------|---------------|
| Y ₁ pH | | | | | |
| Regression | 27.874 | 5 | 5.575 | 28.249 | < 0.01*** |
| Residual | 5.131 | 26 | 0.197 | | |
| Lack of fit | 4.018 | 19 | 0.211 | 1.331 | 36.700 |
| Pure error | 1.113 | 7 | 0.159 | | |
| Total | 33.005 | 31 | | | |
| $Y_2 (\text{mg L}^{-1})$ | | | | | |
| Regression | 103.455 | 2 | 51.728 | 186.584 | < 0.01*** |
| Residual | 8.040 | 29 | 0.277 | | |
| Lack of fit | 6.963 | 22 | 0.317 | 2.058 | 16.600 |
| Pure error | 1.077 | 7 | 0.154 | | |
| Total | 111.495 | 31 | | | |
| $Y_3 (\text{mg L}^{-1})$ | | | | | |
| Regression | 3184.885 | 6 | 530.814 | 37.473 | < 0.01*** |
| Residual | 354.130 | 25 | 14.165 | | |
| Lack of fit | 320.351 | 18 | 17.797 | 3.688 | 4.3* |
| Pure error | 33.779 | 7 | 4.826 | | |
| Total | 3539.015 | 31 | | | |

^{*, **, ***} Signification levels.

SS, sum square; DF, degree of freedom; MS, mean square.

0.317, and 17.797 as lack of fit mean square and 0.159, 0.154, and 4.826 as estimation of experimental variance. Thus, the values of the ratios between the lack of fit mean square and the estimation of experimental variance 1.331 and 2.058 for the responses Y_1 and Y_2 are inferior to tabled $F_{19.7}^{0.05}$ and $F_{22.7}^{0.05}$, respectively. However, the value for the response Y_3 (3.688) is only slightly larger than the tabled $F_{18.7}^{0.05}$. Consequently, it is possible to confirm the validity of the three quadratic elaborated models. In addition, the values of the ratios between the regression mean square and the residual mean square for the three responses Y_1 , Y_2 , and Y_3 (28.249, 186.584, and 37.473) are superior to the tabled $F_{5.0.5}^{0.05}$, $F_{2.0.5}^{0.05}$, respectively. Thus, the significant variables, applied to elaborate the three models, have a large significance on their responses.

3.6 The Response Surfaces

The use of the NemrodW software [14] enabled us to obtain the response surfaces and it is possible to superpose the curves of the responses Y_2/Y_1 and Y_3/Y_1 which are shown in Figs. 4a and b. This procedure enables the determination of the optimum conditions in order to guarantee maximum retention of cadmium and fluoride.

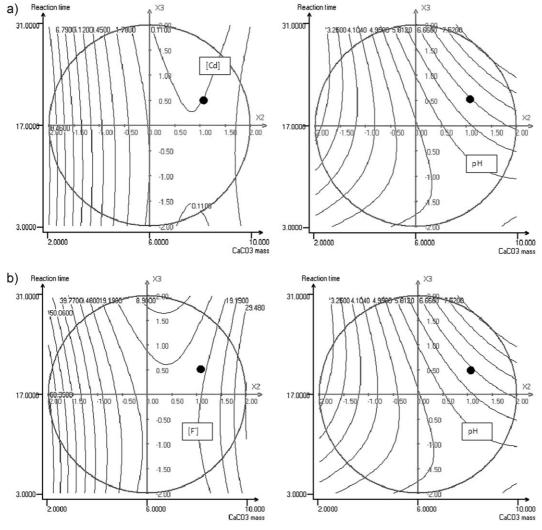


Figure 4. Isoresponse curves variation as function of factors grains mass (X2) and reaction time (X3): (a) Cadmium-pH and (b) Fluoride-pH.

Table 6. Tested optimal conditions and optimal conditions verification.

| (a) Tested optimal | l conditions | _ |
|----------------------|----------------------------|-------|
| Effect | Name | Value |
| $\overline{X_1} = 0$ | Particles size (μm) | 143 |
| $X_2 = 1$ | CaCO ₃ mass (g) | 8 |
| $X_3 = 0.5$ | Reaction time (h) | 20.5 |
| $X_4 = 0.33$ | Temperature (°C) | 30 |

| Parameter | Solution 1 | Solution 2 | Solution 3 |
|-------------------------------|------------|------------|------------|
| рН | 6.64 | 6.60 | 6.65 |
| $[F^-]$ (mg L ⁻¹) | 16.68 | 17.21 | 16.58 |
| $[Cd^{2+1}](mqI^{-1})$ | 0.021 | 0.017 | 0.018 |

Those conditions are: $X_1=0$: particles size = 143 µm; $X_2=1$: CaCO $_3$ mass = 8 g; $X_3=0.5$: setting time = 20.5 h $X_4=0.33$: temperature = 30°C. Under the established conditions the resulted responses are pH 6.66, [Cd $^{2+}$] = 0.018 mg L $^{-1}$, and [F $^{-}$] = 16.54 mg L $^{-1}$ which reveals that 98% of cadmium and 97% of fluoride were extracted. Used calcium carbonate (CaCO $_3$) mass represents 4% of the total mass of treated phosphogypsum which corresponds to 40 kg of calcium carbonate per ton of treated phosphogypsum. In order to confirm the validity of the established three models, the determined optimal conditions were experienced three times on phosphogypsum and the resulted solutions (solutions 1–3) were analyzed. Table 6a exhibits the experimental conditions and Tab. 6b shows the obtained responses.

It is clear that the experimental results fit well with the calculated ones; the established tree models are therefore in good agreement with the experimental performed work.

4 Concluding Remarks

A four factors central composite design was employed in order to model and optimize the chosen responses (pH, cadmium concentration, and fluoride concentration). According to the four factors fields, three valid models were established.

According to these models, the addition of 40 kg of calcium carbonate per ton of phosphogypsum permits under the established conditions (particles size = 143 μm ; CaCO $_3$ mass = 8 g, setting time = 20.5 h, temperature = 30°C), to neutralize the released solution (pH 6.66 in accordance with TN 106.002) and to reduce the concentrations of cadmium ([Cd $^{2+}$] = 0.018 mg L $^{-1}$) and fluoride ([F $^-$] = 16.54 mg L $^{-1}$). The previous values are not compliant to Tunisian norm (F $^ \leq$ 3.00 mg L $^{-1}$, Cd $^{2+}$ \leq 0.005 mg L $^{-1}$) but they correspond to a retention of 98% cadmium and of 97% fluoride. These

results, despite the fact that they are under the permitted limits, they represent a good achievement, given that currently the total effluent goes into the natural environment. However, we believe that the established process can very probably be improved by studying the effect of new reagents.

Finally this work permits to make available an original, easy, simple, and cost effective method to trap some toxic species on phosphogypsum through CaCO₃ addition. This procedure may be used to prevent natural recipient pollution when phosphogypsum is stored. To implement this procedure in industrial practice, it is conceivable to insert a mixing step (wet phosphogypsum + CaCO₃) before discharge and storage of wet phosphogypsum in natural environment.

The authors have declared no conflict of interest.

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