Support Vector Machines-Based Quantitative Structure—Property Relationship for the Prediction of Heat Capacity

C. X. Xue, † R. S. Zhang, †,‡ H. X. Liu, † M. C. Liu, † Z. D. Hu, *,† and B. T. Fan§

Department of Chemistry and Department of Computer Science, Lanzhou University, Lanzhou 730000, China, and Université Paris 7-Denis Diderot, ITODYS 1, Rue Guy de la Brosse, 75005 Paris, France

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The support vector machine (SVM), as a novel type of learning machine, for the first time, was used to develop a Quantitative Structure—Property Relationship (QSPR) model of the heat capacity of a diverse set of 182 compounds based on the molecular descriptors calculated from the structure alone. Multiple linear regression (MLR) and radial basis function networks (RBFNNs) were also utilized to construct quantitative linear and nonlinear models to compare with the results obtained by SVM. The root-mean-square (rms) errors in heat capacity predictions for the whole data set given by MLR, RBFNNs, and SVM were 4.648, 4.337, and 2.931 heat capacity units, respectively. The prediction results are in good agreement with the experimental value of heat capacity; also, the results reveal the superiority of the SVM over MLR and RBFNNs models.

1. INTRODUCTION

The heat capacity of a substance is a measure of how well the substance stores heat. Whenever we supply heat to a material, it will necessarily cause an increase in the material's temperature. The heat capacity is defined as the amount of heat required to raise the temperature of a unit of mass of a substance by a unit change in temperature, so that c = $\Delta Q/(m\Delta T)$, where c is the specific heat capacity in J/(kg °C), ΔO is the change in heat content in Joules, m is the mass in kg, and ΔT is the change in temperature in °C.¹ The heat capacity of the compounds is a subject of interest in terms of understanding the fundamental chemical and physical processes in combustion chemistry. It has also received attention in recent years from the point of view of safety in chemical industrial processes. Experimental heat capacity data are desirable, but due to the advancement of technology in discovery or synthesis of new compounds, there is often a significant gap between the demand for such data and their availability. Of the millions of known substances, heat capacity values are only recorded for a few thousand. Moreover, for some toxic, explosive, or radioactive compounds the experimental determination of the heat capacity is extremely difficult. Hence a reliable theoretical method for predicting the heat capacity is desired.

The quantitative structure—property relationship (QSPR) approach has become very useful in the prediction of many physicochemical properties. The advantage of this approach over other methods lies in the fact that the descriptors used can be calculated from the structure alone and are not dependent on any experimental properties. Once the structure of a compound is known, any descriptor can be calculated no matter whether it is synthesized or not. So once a reliable

model is established, we can use this method to predict the property of compounds. This study can tell us which of the structural factors may play an important role in the determination of a property. The QSPR approach is based on the assumption that the variation of the behavior of the compounds, as expressed by any measured physical or chemical properties, can be correlated with a change in molecular features of the compounds termed descriptors. After the calculation of the molecular descriptors, linear methods, such as multiple linear regression (MLR), principal component regression (PCR), and partial least squares (PLS) or nonlinear methods, e.g. neural networks, can be used in the development of a mathematical relationship between the structural descriptors and the property.

Machine learning techniques have been applied to the QSPR analysis since the late 1980s, mainly in response to increased accuracy demands. The most popular neural networks model is the back-propagation (BP) neural networks due to its simple architecture yet powerful problem-solving ability. However, the BP neural networks suffers from a number of weaknesses which include the need for a large number of controlling parameters, difficulty in obtaining a stable solution, and the danger of overfitting. Other problems with the use of neural networks concern the reproducibility of results, due largely to random initialization of the networks and variation of stopping criteria.² Genetic algorithms can suffer in a similar manner. The stochastic nature of both population initialization and the genetic operators used during training can make results hard to reproduce.³ Owing to the reasons outlined above, there is a continuing need for the application of more accurate and informative techniques in OSPR analysis.

The support vector machine (SVM) is a new algorithm developed from the machine learning community. Due to its remarkable generalization performance, the SVM has attracted attention and gained extensive application, such as pattern recognition problems,^{4–6} drug design,⁷ quantitative

^{*} Corresponding author phone: +86-931-891-2578; fax: +86-931-891-2582; e-mail: huzd@lzu.edu.cn.

Department of Chemistry, Lanzhou University.

[‡] Department of Computer Science, Lanzhou University.

[§] Université Paris 7-Denis Diderot.

structure—activity relationship (QSAR),⁸ and QSPR analysis.^{9–11} Nevertheless, to the best of our knowledge there is no prediction of heat capacity by the QSPR approach based on SVM.

In this work, for the first time, SVM was used for the prediction of heat capacity at 298.15 K of a diverse set of 182 compounds using descriptors calculated by the software CODESSA.¹² The aim was to establish a QSPR model that could be used for the prediction of heat capacity of a diverse set of compounds from their molecular structures alone, to show the flexible modeling ability of SVM and, at the same time, to seek the important structural features related to the heat capacity of compounds. MLR and radial basis function networks (RBFNNs) methods were also utilized to establish quantitative linear and nonlinear relationship to compare with the results obtained by SVM.

2. EXPERIMENTAL SECTION

2.1. Data Preparation. The heat capacity values of 182 compounds were collected from the database and used for this study. The compounds include hydrocarbons, chlorocarbons, alcohols, acids, ketones, aldehydes, ethers, esters, amines, nitriles, sulfide, and thios. A complete list of the compounds' names and corresponding experimental heat capacities was given in Table 1. The data set was randomly divided into two subsets: the training set (2,3,4,6,7,8,10...) and the test set (1,5,9...) (136 and 46 points, respectively). The training set was used to adjust the parameters of the models, and the test set was used to evaluate its prediction ability. Leave-one-out (LOO) cross-validation was performed on the training set to select the parameters of RBFNNs and SVM.

2.2. Descriptor Calculation. All structures of the molecules were drawn with the HyperChem program and exported in a file format suitable for MOPAC.14 The final geometries were obtained with the semiempirical PM3 method in the MOPAC 6.0 program.¹⁵ All the geometries had been fully optimized without symmetry restrictions. In all cases frequency calculations had been performed in order to ensure that all the calculated geometries correspond to true minima. The resulted geometry was transferred into software CODESSA that can calculate constitutional, topological, geometrical, electrostatic, and quantum-chemical descriptors. The constitutional descriptors reflect the molecular composition of the compound without using the geometry or electronic structure of the molecule. The topological descriptors describe the atomic connectivity in the molecule. The geometrical descriptors describe the size of the molecule and require 3D-coordinates of the atoms in the given molecule. The electrostatic descriptors reflect characteristics of the charge distribution of the molecule. The quantum-chemical descriptors add important information to the conventional descriptors.

3. METHODOLOGY

3.1. Feature Selection and Regression Analysis. Once descriptors were generated, in this work, the correlation analysis of descriptors was performed first. In the process of correlation analysis, pairwise correlations between descriptors were examined so that only one descriptor was retained from a pair contributing similar information (cor-

relation coefficients greater than 0.85). After the correlation analysis of the descriptors, descriptor-screening methods were used to select the most relevant descriptor to establish the models for prediction of the molecular property. Here, the forward stepwise regression method was used to choose the subset of the molecular descriptors. Forward stepwise regression starts with no model terms, and at each step it adds the most statistically significant term (the one with the highest F-statistic or lowest P-value) until there are none left.

After the descriptor was selected, multiple linear regression was used to develop the linear model of the property of interest, which takes the form below:

$$Y = b_0 + b_1 X_1 + b_2 X_2 + \dots + b_n X_n \tag{1}$$

In this equation, Y is the property, that is, the dependent variable, X_1-X_n represents the specific descriptor, while b_1-b_n represents the coefficients of those descriptors, and b_0 is the intercept of the equation. The statistical evaluation of the data was obtained by the software SPSS.

3.2. Radial Basis Function Neural Networks Theory. The theory of RBFNNs has been extensively presented in the paper of Yao et al. 16,17 Here only a brief description of the RBFNNs principle was given. The RBFNNs consist of three layers: the input layer, the hidden layer, and the output layer. The input layer does not process the information; it only distributes the input vectors to the hidden layer. Each neuron on the hidden layer employs a radial basis function (RBF) as a nonlinear transfer function to operate on the input data. In general, there are several radial basis functions: linear, cubic, thin plate spline (TPS), Gaussian, multiquadratic, and inverse multiquadratic. The most often used RBF is the Gaussian function that is characterized by a center (c_i) and width (r_i) . In this study, Gaussian was selected as the radial basis function. The operation of the output layer is linear, which is given in eq 2

$$y_k(x) = \sum w_{ki} h_i(x) + bk \tag{2}$$

where y_k is the kth output unit for the input vector x, w_{kj} is the weight connection between the kth output unit and the jth hidden layer unit, and h_j is the notation for the output of the jth RBF unit.

The training procedure when using RBF involves selecting centers, width, and weights. In this paper, the forward subset selection routine was used to select the centers from training set samples. ^{18,19} The adjustment of the connection weight between the hidden layer and the output layer was performed using a least-squares solution after the selection of centers and width of radial basis functions.

3.3. Support Vector Machines. 3.3.1. Structural Risk Minimization.^{20,21} Previous approaches to statistical learning have tended to be based on finding functions to map vector-encoded data to their respective classes. The conventional minimization of the empirical risk over the training data does not, however, imply a good generalization to the novel test data. Indeed, there could be a number of different functions which all give a good approximation to a training set. It is nevertheless difficult to determine a function which best captures the true underlying structure of the data distribution. Structural risk minimization (SRM) aims to address this

Table 1. Compounds and the Predicted Results of the Heat Capacity (J $K^{-1}\ Mol^{-1}$)

$\begin{array}{c} 1^d \\ 2 \\ 3 \\ 4 \\ 5^d \\ 6 \\ 7 \\ 8 \\ 9^d \\ 10 \\ 11 \\ 12 \\ 13^d \\ 14 \\ 15 \\ 16 \\ 17^d \\ 18 \\ 19 \\ 20 \\ 21^d \\ 22 \\ 23 \\ 24 \\ 25^d \\ 26 \\ 27 \\ 28 \\ 29^d \\ 30 \\ 31 \\ 32 \\ \end{array}$	methane methyl chloride methylene chloride chloroform carbon tetrachloride carbon monoxide carbon dioxide methyl alcohol formic acid methylamine ethylene acetylene ethane ethene, 1,2-dichloro-, (Z)- ethyl chloride ethene, 1,1-dichloro- ethane, 1,1-dichloro- ethane, 1,1-dichloro- ethane, 1,2-dichloro- ethane, 1,2-dichloro- ethane, 1,1-dichloro- ethane, 1,2-dichloro- ethane, 1,2-dichloro- eterachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol dimethyl ether	35.695 40.740 50.950 63.521 82.888 29.141 37.135 44.101 45.801 50.050 42.883 44.036 52.487 53.680 64.890 65.640 66.560 67.123 76.320 77.320 94.919 47.850 55.320 63.440	33.940 43.198 55.602 68.926 84.111 31.318 39.439 42.440 43.767 47.203 44.149 36.795 53.637 56.431 66.495 66.057 66.688 69.695 79.673 76.657 90.931 43.559	32.859 41.321 54.339 65.452 72.643 31.404 40.608 43.623 45.387 48.229 41.901 35.804 50.415 55.348 64.238 64.445 64.388 67.210 76.552 74.190 77.904	35.220 42.724 53.248 66.950 83.012 31.756 38.574 44.502 43.541 48.738 43.909 45.922 52.594 53.864 62.883 63.587 63.583 67.128 77.964	76 77 ^d 78 79 80 81 ^d 82 83 84 85 ^d 86 87 88 89 ^d 90 91	2-butene, (Z)- 1-butyne 1-butene 2-butene, (E)- 1-propene, 2-methyl- isobutane butane butane, 1-chloro- butane, 2-chloro- propane, 2-chloro- 2-methyl- furan furan, 2,3-dihydro- cyclobutanone furan, tetrahydro- 2-oxetanone,	80.150 81.820 85.560 87.670 88.090 96.650 98.490 107.940 110.220 111.950 65.400 74.310 76.634 84.410	87.298 80.360 87.847 87.772 90.592 100.336 97.168 108.139 110.281 115.254 65.182 74.802 76.074 84.024 78.190	85.953 78.747 86.564 86.481 88.379 98.730 96.452 107.770 109.28 112.76 68.176 74.024 76.812 80.161 83.385	85.523 78.316 86.127 86.023 88.775 98.505 95.579 107.970 109.958 114.230 67.715 74.092 78.704 80.556
3 4 5 ^d 6 7 8 9 ^d 10 11 11 12 13 ^d 14 15 16 17 ^d 18 19 20 21 ^d 22 22 23 24 25 ^d 27 28 30 31 31 31 31 31 31 31 31 31 31 31 31 31	methylene chloride chloroform carbon tetrachloride carbon monoxide carbon dioxide methyl alcohol formic acid methylamine ethylene acetylene ethane ethene, chloroethene, 1,2-dichloro-, (Z)-ethyl chloride ethene, 1,1-dichloroethane, 1,1-dichloroethane, 1,2-dichlorotetrachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	50.950 63.521 82.888 29.141 37.135 44.101 45.801 50.050 42.883 44.036 52.487 53.680 64.890 65.640 66.560 67.123 76.320 77.320 94.919 47.850 51.750 55.320	55.602 68.926 84.111 31.318 39.439 42.440 43.767 47.203 44.149 36.795 53.637 56.431 66.495 66.057 66.688 69.695 79.673 76.657 90.931 43.559	54.339 65.452 72.643 31.404 40.608 43.623 45.387 48.229 41.901 35.804 50.415 55.348 64.238 64.445 64.388 67.210 76.552 74.190	53.248 66.950 83.012 31.756 38.574 44.502 43.541 48.738 43.909 45.922 52.594 53.864 62.883 63.587 63.583 67.128	78 79 80 81 ^d 82 83 84 85 ^d 86 87 88 89 ^d 90	1-butene 2-butene, (E)- 1-propene, 2-methyl- isobutane butane, 1-chloro- butane, 2-chloro- propane, 2-chloro- 2-methyl- furan furan, 2,3-dihydro- cyclobutanone furan, tetrahydro- 2-oxetanone,	85.560 87.670 88.090 96.650 98.490 107.940 110.220 111.950 65.400 74.310 76.634	87.847 87.772 90.592 100.336 97.168 108.139 110.281 115.254 65.182 74.802 76.074 84.024	86.564 86.481 88.379 98.730 96.452 107.770 109.28 112.76 68.176 74.024 76.812 80.161	86.127 86.023 88.775 98.505 95.579 107.970 109.958 114.230 67.715 74.092 78.704 80.556
4 5 ^d 6 7 8 9 ^d 10 11 12 13 ^d 14 15 16 17 ^d 18 19 20 21 ^d 22 23 224 25 ^d 26 27 28 29 ^d 30 31 32	chloroform carbon tetrachloride carbon monoxide carbon dioxide methyl alcohol formic acid methylamine ethylene acetylene ethane ethene, chloro- ethene, 1,2-dichloro-, (Z)- ethyl chloride ethene, 1,1-dichloro- ethane, 1,1-dichloro- ethane, 1,2-dichloro- ethane, 1,2-dichloro- ethane, 1,1-dichloro- ethane, 1,2-dichloro- ethane, 1,2-dichloro- etrachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	63.521 82.888 29.141 37.135 44.101 50.050 42.883 44.036 52.487 53.680 64.890 65.640 66.560 67.123 76.320 77.320 94.919 47.850 51.750 55.320	68.926 84.111 31.318 39.439 42.440 43.767 47.203 44.149 36.795 53.637 56.431 66.495 66.057 66.688 69.695 79.673 76.657 90.931 43.559	65.452 72.643 31.404 40.608 43.623 45.387 48.229 41.901 35.804 50.415 55.348 64.238 64.238 67.210 76.552 74.190	66.950 83.012 31.756 38.574 44.502 43.541 48.738 43.909 45.922 52.594 53.864 62.883 63.587 63.583 67.128	79 80 81 ^d 82 83 84 85 ^d 86 87 88 89 ^d 90	2-butene, (E)- 1-propene, 2-methyl- isobutane butane, 1-chloro- butane, 2-chloro- propane, 2-chloro- 2-methyl- furan furan, 2,3-dihydro- cyclobutanone furan, tetrahydro- 2-oxetanone,	87.670 88.090 96.650 98.490 107.940 110.220 111.950 65.400 74.310 76.634	87.772 90.592 100.336 97.168 108.139 110.281 115.254 65.182 74.802 76.074 84.024	86.481 88.379 98.730 96.452 107.770 109.28 112.76 68.176 74.024 76.812 80.161	86.023 88.775 98.505 95.579 107.970 109.958 114.230 67.715 74.092 78.704 80.556
5^d 6 7 8 9^d 10 11 12 13^d 14 15 16 17^d 18 19 20 21^d 22 23 24 25^d 26 27 28 29^d 30 31 32	carbon tetrachloride carbon monoxide carbon dioxide methyl alcohol formic acid methylamine ethylene acetylene ethane, chloro- ethene, 1,2-dichloro-, (Z)- ethyl chloride ethene, 1,1-dichloro- ethane, 1,1-dichloro- ethane, 1,2-dichloro- ethane, 1,2-dichloro- ethane, 1,1-dichloro- ethane, 1,1-dichloro- ethane, 1,2-dichloro- ethane, 1,2-dichloro- etrachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	82.888 29.141 37.135 44.101 45.801 50.050 42.883 44.036 52.487 53.680 64.890 65.640 66.560 67.123 76.320 77.320 94.919 47.850 51.750 55.320	84.111 31.318 39.439 42.440 43.767 47.203 44.149 36.795 53.637 56.431 66.495 66.057 66.688 69.695 79.673 76.657 90.931 43.559	72.643 31.404 40.608 43.623 45.387 48.229 41.901 35.804 50.415 55.348 64.238 64.238 67.210 76.552 74.190	83.012 31.756 38.574 44.502 43.541 48.738 43.909 45.922 52.594 53.864 62.883 63.587 63.583 67.128	80 81 ^d 82 83 84 85 ^d 86 87 88 89 ^d 90	1-propene, 2-methyl- isobutane butane, 1-chloro- butane, 2-chloro- propane, 2-chloro- 2-methyl- furan furan, 2,3-dihydro- cyclobutanone furan, tetrahydro- 2-oxetanone,	88.090 96.650 98.490 107.940 110.220 111.950 65.400 74.310 76.634	90.592 100.336 97.168 108.139 110.281 115.254 65.182 74.802 76.074 84.024	88.379 98.730 96.452 107.770 109.28 112.76 68.176 74.024 76.812 80.161	88.775 98.505 95.579 107.970 109.958 114.230 67.715 74.092 78.704 80.556
$\begin{matrix} 6 \\ 7 \\ 8 \\ 9^d \\ 10 \\ 11 \\ 12 \\ 13^d \\ 14 \\ 15 \\ 16 \\ 17^d \\ 18 \\ 19 \\ 20 \\ 21^d \\ 22 \\ 23 \\ 24 \\ 25^d \\ 26 \\ 27 \\ 28 \\ 29^d \\ 30 \\ 31 \\ 32 \end{matrix}$	carbon monoxide carbon dioxide methyl alcohol formic acid methylamine ethylene acetylene ethane ethene, 1,2-dichloro-, (Z)- ethyl chloride ethene, 1,1-dichloro- ethane, 1,1-dichloro- ethane, 1,2-dichloro- ethane, 1,2-dichloro- ethane, 1,1-dichloro- ethane, 1,2-dichloro- ethane, 1,2-dichloro- ethane, 1,2-dichloro- etrachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	29.141 37.135 44.101 45.801 50.050 42.883 44.036 52.487 53.680 64.890 65.640 66.560 67.123 76.320 77.320 94.919 47.850 51.750 55.320	31.318 39.439 42.440 43.767 47.203 44.149 36.795 53.637 56.431 66.495 66.057 66.688 69.695 79.673 76.657 90.931 43.559	31.404 40.608 43.623 45.387 48.229 41.901 35.804 50.415 55.348 64.238 64.445 64.388 67.210 76.552 74.190	31.756 38.574 44.502 43.541 48.738 43.909 45.922 52.594 53.864 62.883 63.587 63.583 67.128	81 ^d 82 83 84 85 ^d 86 87 88 89 ^d 90	isobutane butane, 1-chloro- butane, 2-chloro- propane, 2-chloro- 2-methyl- furan furan, 2,3-dihydro- cyclobutanone furan, tetrahydro- 2-oxetanone,	96.650 98.490 107.940 110.220 111.950 65.400 74.310 76.634	100.336 97.168 108.139 110.281 115.254 65.182 74.802 76.074 84.024	98.730 96.452 107.770 109.28 112.76 68.176 74.024 76.812 80.161	98.505 95.579 107.970 109.958 114.230 67.715 74.092 78.704 80.556
$egin{array}{cccccccccccccccccccccccccccccccccccc$	carbon dioxide methyl alcohol formic acid methylamine ethylene acetylene ethane ethene, chloro- ethene, 1,2-dichloro-, (Z)- ethyl chloride ethene, 1,1-dichloro- ethane, 1,1-dichloro- ethane, 1,2-dichloro- tetrachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	37.135 44.101 45.801 50.050 42.883 44.036 52.487 53.680 64.890 65.640 66.560 67.123 76.320 77.320 94.919 47.850 51.750 55.320	39.439 42.440 43.767 47.203 44.149 36.795 53.637 56.431 66.495 66.057 66.688 69.695 79.673 76.657 90.931 43.559	40.608 43.623 45.387 48.229 41.901 35.804 50.415 55.348 64.238 64.445 64.388 67.210 76.552 74.190	38.574 44.502 43.541 48.738 43.909 45.922 52.594 53.864 62.883 63.587 63.583 67.128	82 83 84 85 ^d 86 87 88 89 ^d 90	butane butane, 1-chloro- butane, 2-chloro- propane, 2-chloro- 2-methyl- furan furan, 2,3-dihydro- cyclobutanone furan, tetrahydro- 2-oxetanone,	98.490 107.940 110.220 111.950 65.400 74.310 76.634	97.168 108.139 110.281 115.254 65.182 74.802 76.074 84.024	96.452 107.770 109.28 112.76 68.176 74.024 76.812 80.161	95.579 107.970 109.958 114.230 67.715 74.092 78.704 80.556
9^d 10 11 12 13^d 14 15 16 17^d 18 19 20 21^d 22 23 24 25^d 26 27 28 29^d 30 31 32	formic acid methylamine ethylamine ethylene acetylene ethane ethene, chloro- ethene, 1,2-dichloro-, (Z)- ethyl chloride ethene, 1,2-dichloro-, (E)- ethene, 1,1-dichloro- ethane, 1,1-dichloro- ethane, 1,2-dichloro- tetrachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	45.801 50.050 42.883 44.036 52.487 53.680 64.890 65.640 66.560 67.123 76.320 77.320 94.919 47.850 51.750 55.320	43.767 47.203 44.149 36.795 53.637 56.431 66.495 66.057 66.688 69.695 79.673 76.657 90.931 43.559	45.387 48.229 41.901 35.804 50.415 55.348 64.238 64.445 64.388 67.210 76.552 74.190	43.541 48.738 43.909 45.922 52.594 53.864 62.883 63.587 63.583 67.128	84 85 ^d 86 87 88 89 ^d 90	butane, 2-chloro- propane, 2-chloro- 2-methyl- furan furan, 2,3-dihydro- cyclobutanone furan, tetrahydro- 2-oxetanone,	110.220 111.950 65.400 74.310 74.310 76.634	110.281 115.254 65.182 74.802 76.074 84.024	109.28 112.76 68.176 74.024 76.812 80.161	109.958 114.230 67.715 74.092 78.704 80.556
$\begin{array}{c} 10 \\ 11 \\ 12 \\ 13^d \\ 14 \\ 15 \\ 16 \\ 17^d \\ 18 \\ 19 \\ 20 \\ 21^d \\ 22 \\ 23 \\ 24 \\ 25^d \\ 26 \\ 27 \\ 28 \\ 29^d \\ 30 \\ 31 \\ 32 \\ \end{array}$	methylamine ethylene acetylene ethane ethene, chloro- ethene, 1,2-dichloro-, (Z)- ethyl chloride ethene, 1,1-dichloro- ethane, 1,1-dichloro- ethane, 1,1-dichloro- ethane, 1,2-dichloro- tetrachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	50.050 42.883 44.036 52.487 53.680 64.890 65.640 66.560 67.123 76.320 77.320 94.919 47.850 51.750 55.320	47.203 44.149 36.795 53.637 56.431 66.495 66.057 66.688 69.695 79.673 76.657 90.931 43.559	48.229 41.901 35.804 50.415 55.348 64.238 64.445 64.388 67.210 76.552 74.190	48.738 43.909 45.922 52.594 53.864 62.883 63.587 63.583 67.128	85 ^d 86 87 88 89 ^d 90	propane, 2-chloro- 2-methyl- furan furan, 2,3-dihydro- cyclobutanone furan, tetrahydro- 2-oxetanone,	111.950 65.400 74.310 74.310 76.634	115.254 65.182 74.802 76.074 84.024	68.176 74.024 76.812 80.161	67.715 74.092 78.704 80.556
$\begin{array}{c} 11 \\ 12 \\ 13^d \\ 14 \\ 15 \\ 16 \\ 17^d \\ 18 \\ 19 \\ 20 \\ 21^d \\ 22 \\ 23 \\ 24 \\ 25^d \\ 26 \\ 27 \\ 28 \\ 29^d \\ 30 \\ 31 \\ 32 \\ \end{array}$	ethylene acetylene ethane ethene, chloro-ethene, 1,2-dichloro-, (Z)-ethyl chloride ethene, 1,1-dichloro-ethane, 1,1-dichloro-ethane, 1,1-dichloro-ethane, 1,2-dichloro-tetrachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	42.883 44.036 52.487 53.680 64.890 65.640 66.560 67.123 76.320 77.320 94.919 47.850 51.750 55.320	44.149 36.795 53.637 56.431 66.495 66.057 66.688 69.695 79.673 76.657 90.931 43.559	41.901 35.804 50.415 55.348 64.238 64.445 64.388 67.210 76.552 74.190	43.909 45.922 52.594 53.864 62.883 63.587 63.583 67.128	86 87 88 89 ^d 90	2-methyl- furan furan, 2,3-dihydro- cyclobutanone furan, tetrahydro- 2-oxetanone,	65.400 74.310 74.310 76.634	65.182 74.802 76.074 84.024	68.176 74.024 76.812 80.161	67.715 74.092 78.704 80.556
$\begin{array}{c} 12 \\ 13^d \\ 14 \\ 15 \\ 16 \\ 17^d \\ 18 \\ 19 \\ 20 \\ 21^d \\ 22 \\ 23 \\ 24 \\ 25^d \\ 26 \\ 27 \\ 28 \\ 29^d \\ 30 \\ 31 \\ 32 \\ \end{array}$	acetylene ethane ethene, chloro- ethene, 1,2-dichloro-, (Z)- ethyl chloride ethene, 1,1-dichloro- ethene, 1,1-dichloro- ethane, 1,1-dichloro- ethane, 1,2-dichloro- tetrachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	44.036 52.487 53.680 64.890 65.640 66.560 67.123 76.320 77.320 94.919 47.850 51.750 55.320	36.795 53.637 56.431 66.495 66.057 66.688 69.695 79.673 76.657 90.931 43.559	35.804 50.415 55.348 64.238 64.445 64.388 67.210 76.552 74.190	45.922 52.594 53.864 62.883 63.587 63.583 67.128	87 88 89 ^d 90	furan furan, 2,3-dihydro- cyclobutanone furan, tetrahydro- 2-oxetanone,	74.310 74.310 76.634	74.802 76.074 84.024	74.024 76.812 80.161	74.092 78.704 80.556
13^d 14 15 16 17^d 18 19 20 21^d 22 23 24 25^d 26 27 28 29^d 30 31 32	ethane ethene, chloro- ethene, 1,2-dichloro-, (Z)- ethyl chloride ethene, 1,2-dichloro-, (E)- ethene, 1,1-dichloro- ethane, 1,1-dichloro- ethane, 1,2-dichloro- tetrachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	52.487 53.680 64.890 65.640 66.560 67.123 76.320 77.320 94.919 47.850 51.750 55.320	53.637 56.431 66.495 66.057 66.688 69.695 79.673 76.657 90.931 43.559	50.415 55.348 64.238 64.445 64.388 67.210 76.552 74.190	52.594 53.864 62.883 63.587 63.583 67.128	87 88 89 ^d 90	furan, 2,3-dihydro- cyclobutanone furan, tetrahydro- 2-oxetanone,	74.310 74.310 76.634	74.802 76.074 84.024	74.024 76.812 80.161	74.092 78.704 80.556
14 15 16 17 ^d 18 19 20 21 ^d 22 23 24 25 ^d 26 27 28 29 ^d 30 31 32	ethene, chloro- ethene, 1,2-dichloro-, (Z)- ethyl chloride ethene, 1,2-dichloro-, (E)- ethene, 1,1-dichloro- ethane, 1,2-dichloro- ethane, 1,2-dichloro- tetrachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	53.680 64.890 65.640 66.560 67.123 76.320 77.320 94.919 47.850 51.750 55.320	56.431 66.495 66.057 66.688 69.695 79.673 76.657 90.931 43.559	55.348 64.238 64.445 64.388 67.210 76.552 74.190	53.864 62.883 63.587 63.583 67.128	88 89 ^d 90	cyclobutanone furan, tetrahydro- 2-oxetanone,	74.310 76.634	76.074 84.024	76.812 80.161	78.704 80.556
$\begin{array}{c} 15 \\ 16 \\ 17^d \\ 18 \\ 19 \\ 20 \\ 21^d \\ 22 \\ 23 \\ 24 \\ 25^d \\ 26 \\ 27 \\ 28 \\ 29^d \\ 30 \\ 31 \\ 32 \\ \end{array}$	ethene, 1,2-dichloro-, (Z)-ethyl chloride ethene, 1,2-dichloro-, (E)-ethene, 1,1-dichloro- ethane, 1,1-dichloro- ethane, 1,2-dichloro- tetrachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	64.890 65.640 66.560 67.123 76.320 77.320 94.919 47.850 51.750 55.320	66.495 66.057 66.688 69.695 79.673 76.657 90.931 43.559	64.238 64.445 64.388 67.210 76.552 74.190	62.883 63.587 63.583 67.128	89 ^d 90	furan, tetrahydro- 2-oxetanone,	76.634	84.024	80.161	80.556
17 ^d 18 19 20 21 ^d 22 23 24 25 ^d 26 27 28 29 ^d 30 31 32	ethene, 1,2-dichloro-, (E)- ethene, 1,1-dichloro- ethane, 1,1-dichloro- ethane, 1,2-dichloro- tetrachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	66.560 67.123 76.320 77.320 94.919 47.850 51.750 55.320	66.688 69.695 79.673 76.657 90.931 43.559	64.388 67.210 76.552 74.190	63.583 67.128			84.410	78.190	83 385	01 200
18 19 20 21 ^d 22 23 24 25 ^d 26 27 28 29 ^d 30 31 32	ethene, 1,1-dichloro- ethane, 1,1-dichloro- ethane, 1,2-dichloro- tetrachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	67.123 76.320 77.320 94.919 47.850 51.750 55.320	69.695 79.673 76.657 90.931 43.559	67.210 76.552 74.190	67.128	91				05.505	81.208
19 20 21 ^d 22 23 24 25 ^d 26 27 28 29 ^d 30 31 32	ethane, 1,1-dichloro- ethane, 1,2-dichloro- tetrachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	76.320 77.320 94.919 47.850 51.750 55.320	79.673 76.657 90.931 43.559	76.552 74.190			gamma-butyrolactone	86.100	85.285	86.316	85.491
20 21^{d} 22 23 24 25^{d} 26 27 28 29^{d} 30 31 32	ethane, 1,2-dichloro- tetrachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	77.320 94.919 47.850 51.750 55.320	76.657 90.931 43.559	74.190	77.964	92	1,3-dioxane	89.400	94.065	90.671	90.739
21 ^d 22 23 24 25 ^d 26 27 28 29 ^d 30 31 32	tetrachloroethylene ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	94.919 47.850 51.750 55.320	90.931 43.559			93 ^d	1,4-dioxane	92.100	94.149	90.739	90.585
22 23 24 25 ^d 26 27 28 29 ^d 30 31 32	ethylene oxide ketene acetaldehyde acetic acid methyl formate ethanol	47.850 51.750 55.320	43.559		73.953 89.971	94 95	2-butenal cyclobutanol	93.920 94.470	87.974 85.931	88.369 86.698	88.014 86.309
23 24 25 ^d 26 27 28 29 ^d 30 31 32	ketene acetaldehyde acetic acid methyl formate ethanol	51.750 55.320		50.428	48.045	96	1-butanol	108.030	106.866	109.030	108.569
24 25^{d} 26 27 28 29^{d} 30 31 32	acetaldehyde acetic acid methyl formate ethanol	55.320	50.597	51.832	48.980	97 ^d	ethanol, 1,1-dimethyl-	113.630	114.111	111.140	113.572
26 27 28 29 ^d 30 31 32	methyl formate ethanol	63.440	55.314	56.450	54.992	98	ethyl acetate	113.640	109.717	108.230	108.709
27 28 29 ^d 30 31 32	ethanol		67.743	65.853	66.453	99	ethoxy ethane	119.460	107.809	107.780	116.866
28 29 ^d 30 31 32		64.380	65.442	64.056	63.044	100	pyrrole	71.600	69.931	71.358	72.315
29 ^d 30 31 32	dimethyl ether	65.210	65.117	65.607	65.385	101^{d}	(Z)-2-butenenitrile	83.850	91.827	89.899	80.484
30 31 32	1,2-ethanediol	65.570	65.523	63.583	63.406	102 103	(E)—2-butenenitrile	86.740	92.096	90.140	90.883
31 32	acetonitrile	77.990 52.220	74.685 53.020	74.813 54.409	74.478 52.104	103	1-butanamine 2-butanamine	113.900 120.300	112.327 114.191	114.150 116.720	114.418 115.101
32	dimethylamine	70.500	70.292	70.423	70.891	105^{d}	2-propanamine, 2-methyl-	120.920	119.266	118.010	118.930
	thiirane	53.320	49.635	55.351	53.717	106	thiophene, tetrahydro-	90.860	90.266	91.398	89.515
33^d	ethanethiol	73.008	71.500	73.099	71.892	107	diethyl sulfide	116.570	113.532	117.930	117.130
34	dimethyl sulfide	74.060	71.599	73.208	71.970	108	1-propanethiol, 2-methyl-	118.830	115.463	120.240	118.423
35	disulfide, dimethyl	94.220	88.860	90.835	90.123	109^{d}	2-butanethiol	119.700	115.607	120.440	118.554
36 37 ^d	acetyl chloride	67.860	69.073	67.828	67.391	110	propane, 2-(methylthio)-	120.000	115.870	120.780	118.812
38	urea, methyl- cyclopropene	88.700 52.900	86.850 45.268	84.301 51.496	86.051 48.828	111 112	2-propanethiol, 2-methyl- 1,3-cyclopentadiene	121.130 75.400	120.483 76.144	120.990 74.891	122.912 75.241
39	cyclopropane	55.600	54.311	56.208	55.256	112^{d}	cyclopentene	81.280	85.482	81.253	81.853
40	allene	59.030	61.708	60.269	59.180	114	cyclopentane	82.800	95.084	88.354	89.770
41^d	propyne	60.730	59.142	57.847	56.778	115	cyclobutane, methylene-	87.400	87.497	84.969	84.986
42	propene	64.320	66.974	65.130	64.860	116	1,3-pentadiene, (Z)-	97.180	99.464	98.549	98.431
43	propane	73.600	76.106	74.026	74.118	117^{d}	1,4-pentadiene	98.240	99.412	98.500	98.369
44 45 ^d	propane, 1-chloro-	85.300	86.692	85.311	85.062 88.374	118 119	2-pentene, (Z)-	98.800 99.060	108.921 99.532	109.000	98.212 98.489
46	propane, 2-chloro- oxetane	87.560 61.541	90.125 63.813	87.813 64.398	64.121	120	1,3-pentadiene, (E)- 2,3-pentadiene	99.000	103.085	98.619 102.110	102.648
47	cyclopropanone	64.300	55.493	61.009	60.113		1,2-pentadiene	101.000		102.650	103.305
48	1,3-dioxolane	71.000	73.249	72.991	73.129	122	1,3-butadiene, 2-methyl-	102.690	100.684	99.057	99.320
49^d	beta-propiolactone	71.240	65.136	70.270	68.993	123	2-butene, 2-methyl-	105.020	110.005	109.460	108.905
50	acetone	75.020	79.420	76.476	78.895	124	1,2-butadiene, 3-methyl-	105.250	105.213	103.520	104.586
51	2-propen-1-ol	76.020	76.682	77.235	76.815	125^{d}	cyclopropane, 1,1-	106.370	100.324	100.760	97.931
52 52d	propanal 2-propenoic acid	80.730	87.766	86.474	80.032	126	dimethyl- 2-pentene, (E)-	100 000	109 724	109 700	107 022
53 ^d 54	2-propenoic acid 1,3,5-trioxane	81.800 81.900	78.417 82.852	76.178 82.289	77.036 82.094	126 127	2-pentene, (E)- 1-butene, 2-methyl-	108.900 109.960	108.724 110.500	108.790 110.010	107.932 109.471
55	1-propanol	85.560	85.928	86.283	86.715	128	butane, 2-methyl-	118.900	120.424	120.750	119.504
56	acetic acid, methyl ester	86.030	88.312	85.933	86.438	129^{d}	pentane	120.070	118.196	118.750	117.528
57^d	isopropyl alcohol	89.320	89.171	86.619	88.866	130	propane, 2,2-dimethyl-	120.820	124.813	124.260	123.340
58	ethane, methoxy-	93.300	86.342	84.878	94.486	131	pentane, 1-chloro-	130.580	129.439	129.230	130.431
59	acrylonitrile	63.940	64.260	64.989	62.691	132	2H-pyran, 3,4-dihydro-	92.200	95.340	91.644	91.706
60	1-propanamine	91.170	91.022	91.294	92.181	133^{d}	cyclopentanone	95.330	96.113	97.630	96.602
61 ^d 62	2-propanamine thietane	97.550 68.620	94.306 69.902	92.526 71.181	94.326 71.474	134 135	2H-pyran, tetrahydro- cyclopentanol	99.100 105.430	104.817 105.812	99.354 108.730	98.402 103.496
63	1-propanethiol	94.890	92.553	94.841	94.399	136	2-pentanone	125.900	120.740	125.680	122.521
64	ethane, (methylthio)-	95.060	92.811	95.159	94.707	137^{d}	3-pentanone	129.870	119.471	124.580	131.726
65^d	2-propanethiol	96.150	95.510	95.261	96.288	138	1-pentanol	130.700	128.471	131.070	131.758
66	urea, N,N'-dimethyl-	103.800	107.537	109.300	108.815	139	pyridine	78.230	80.979	81.204	82.931
67	urea, N,N-dimethyl-	107.200	109.485	108.58	109.879	140	1H-pyrrole, 1-methyl-	90.890	92.813	93.662	94.149
68	urea, ethyl-	115.700	108.422	109.080	118.706	141^{d}	(E)—2-pentenenitrile	106.100	106.567	108.950	108.476
69 ^d	cyclobutene	64.410	65.308	65.381	64.955	142	(Z)-2-pentenenitrile	106.100	106.640	109.040	109.016
70 71	cyclobutane methylenecyclopropane	70.600 72.930	74.707 66.971	70.984 68.447	72.007 67.613	143 144	pentanenitrile butanenitrile, 2-methyl-	116.540 121.800	115.683 116.226	120.720 120.930	118.689 118.503
72	1-methylcyclopropene	74.680	67.208	68.600	67.802	144 145^d	propanenitrile, 2,2-	124.220	121.206	120.930	122.466
73 ^d	2-butyne	78.020	79.932	78.323	77.867	5	dimethyl-	220	1.200		2.100
74	1,2-butadiene	79.480	82.479	80.804	80.749	146	thiophene, 2-methyl-	95.370	92.974	92.953	95.048
75	1,3-butadiene	79.810	78.289	76.658	76.155	147	thiophene, 3-methyl-	95.790	93.177	93.131	95.043

Table 1 (Continued)

	heat						heat				
no.	name	capacity	MLR^a	RBFNNs ^b	SVM^c	no.	name	capacity	MLR^a	RBFNNs ^b	SVM^c
148	ethyl propyl sulfide	139.200	135.130	138.150	141.078	165^{d}	2-hexyne	119.650	122.393	122.440	122.995
149^{d}	butane, 1-(methylthio)-	139.790	134.493	137.570	139.282	166	cyclobutane, ethyl-	122.800	117.437	110.460	118.365
150	1-pentanethiol	141.210	134.838	137.880	139.360	167	2-butene, 2,3-dimethyl-	123.600	133.233	133.410	122.452
151	2-butanethiol, 2-methyl-	143.390	139.783	143.920	142.724	168	1-hexyne	125.950	122.697	122.700	123.192
152	propane, 2-methyl-2-	143.800	140.217	144.380	143.432	169^{d}	2-pentene, 3-methyl-, (E)-	126.600	130.988	131.310	130.903
	(methylthio)-					170	2-pentene, 3-methyl-, (Z)-	126.600	131.245	131.530	131.192
153^{d}	benzene	94.100	89.269	86.429	94.947	171	1-hexene	130.830	129.577	129.960	129.259
154	1,4-cyclohexadiene	94.100	96.330	92.379	92.588	172	1-butyne, 3,3-dimethyl-	131.310	127.221	126.300	125.824
155	1,3-cyclohexadiene	94.200	96.716	92.662	92.966	173^{d}	pentane, 3-methylene-	133.600	130.256	130.640	130.011
156	cyclopentene, 4-methyl-	100.000	107.683	104.360	102.903	174	butane, 2,3-dimethyl-	139.400	141.700	140.560	140.004
157^{d}	cyclopentene, 3-methyl-	100.000	108.044	104.650	102.935	175	pentane, 3-methyl-	140.100	140.288	138.850	138.877
158	bicyclo[3.1.0]hexane	100.500	95.349	100.400	92.113	176	butane, 2,2-dimethyl-	141.500	143.422	142.080	140.166
159	cyclopentene, 1-methyl-	101.000	107.514	104.220	102.701	177^{d}	hexane	142.600	139.956	138.230	139.595
160	cyclohexane	105.300	115.230	107.700	107.680	178	1-butene, 2,3-dimethyl-	143.500	132.813	133.020	141.825
161^{d}	cyclopentane, methyl-	109.500	116.769	111.760	108.911	179	phenol	103.220	100.008	100.700	99.857
162	1,3,5-hexatriene, (Z)-	110.170	110.826	109.900	110.723	180	toluene	103.700	112.238	110.490	109.928
163	1,3,5-hexatriene, (E)-	110.620	111.226	110.260	111.200	181^{d}	styrene	151.290	122.248	119.670	149.550
164	3-hexyne	119.500	122.364	122.410	122.960	182	naphthalene	133.020	132.444	132.710	137.580

^a Predicted heat capacity by MLR. ^b Predicted heat capacity by RBFNNs. ^c Predicted heat capacity by SVM. ^d Test set.

problem and provides a well-defined quantitative measure for the capacity of a learned function to generalize over unknown test data. Due to its relative simplicity, the Vapnik-Chervonenkis (VC) dimension in particular has been adopted as one of the more popular measures for such a capacity. By choosing a function with a low VC dimension and minimizing its empirical error to a training data set, SRM can offer a guaranteed minimal bound on the test error.

3.3.2. Theory of SVM for Regression.²² The foundation of Support Vector Machines (SVM) has been developed by Vapnik, and they are gaining popularity due to many attractive features and promising empirical performance. 21,23 The formulation embodies the Structural Risk Minimization (SRM) principle, which has been shown to be superior to the traditional Empirical Risk Minimization (ERM) principle, employed by conventional neural networks. SRM minimizes an upper bound on VC dimension ("generalization error"), as opposed to ERM that minimizes the error on the training data. It is the difference that equips SVM with good generalization performance, which is the goal in statistical learning. Originally, SVM were developed for pattern recognition problems²⁴ and now, with the introduction of ϵ -insensitive loss function, SVM have been extended to solve nonlinear regression estimation. The estimated function is a linear expansion in terms of functions defined on a certain subset of the data (support vectors), and the final number of coefficients in such an expansion does not depend on the dimensionality of the space of input variables. These two properties make SVM an especially useful technique for dealing with very large data sets in a high-dimensional space.

Compared to other neural network regressors, there are three distinct characteristics when SVM are used to estimate the regression function. First of all, SVM estimate the regression using a set of linear functions that are defined in a high-dimensional space. Second, SVM carry out the regression estimation by risk minimization where the risk is measured using Vapnik's ϵ -insensitive loss function. Third, SVM use a risk function consisting of the empirical error and a regularization term which is derived from the structural risk minimization principle of converging to the global optimum and not to a local optimum.

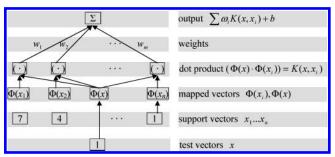


Figure 1. Architecture of a regression machine constructed by the support vector algorithm.²²

Figure 1 contains a graphical overview over the different steps in the regression stage of SVM. In support vector regression (SVR), the basic idea is to map the data x into a higher-dimensional feature space F via a nonlinear mapping Φ and then to do linear regression in this space. Therefore, regression approximation addresses the problem of estimating a function based on a given data set $G = \{(x_i, d_i)\}_i^n$ (x_i is the input vector, d_i is the desired value, and n is the total number of data patterns), and SVM approximate the function using the following equation

$$y = f(x) = w\Phi(x) + b \tag{3}$$

where $\Phi(x)$ is the high-dimensional feature space which is nonlinearly mapped from the input space x. The coefficients w and b are estimated by minimizing

$$R_{\text{SVMs}}(C) = C - \sum_{n_{i=1}}^{1} L_{\epsilon}(d_{i}, y_{i}) + \frac{1}{2} ||w||^{2}$$
 (4)

$$L_{\epsilon}(d,y) = \begin{cases} |d-y| - \epsilon |d-y| \ge \epsilon \\ 0 & \text{otherwise} \end{cases}$$
 (5)

In the regularized risk function given by eq 4, the first term $C(1/n)\sum_{i=1}^{n} L_{\epsilon}(d_{i},y_{i})$ is the empirical error (risk). They are measured by the ϵ -insensitive loss function given by eq 5. This loss function provides the advantage of enabling one to use sparse data points to represent the decision function given by eq 3. The second term $1/2||w||^{2}$, on the other hand, is the regularization term. C is referred to as the regularized

constant, and it determines the tradeoff between the empirical risk and the regularization term. Increasing the value of C will result in the relative importance of the empirical risk with respect to the regularization term to grow. ϵ is called the tube size, and it is equivalent to the approximation accuracy placed on the training data points. Both C and ϵ are user-prescribed parameters.

To obtain the estimations of w and b, eq 4 is transformed to the primal function given by eq 6 by introducing the positive slack variables ξ_i and ξ_i^* as follows:

Minimize
$$R_{SVMs}(w, \xi^{(*)}) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{n} (\xi_i + \xi_i^*)$$

Subject to
$$\begin{cases} d_i - w\Phi(x_i) - b_i \le \epsilon + \xi_i \\ w\Phi(x_i) + b_i - d_i \le \epsilon + \xi_i^* \\ \xi_i, \xi_i^* \ge 0 \end{cases}$$
 (6)

Finally, by introducing Lagrange multipliers and exploiting the optimality constraints, the decision function given by eq 3 has the following explicit form

$$f(x,a_i,a_i^*) = \sum (a_i - a_i^*)K(x,x_i) + b$$
 (7)

where the kernel function K corresponds to $K(x,x_i) =$ $\phi(x)^T \phi(x_i)$. One has several possibilities for the choice of this kernel function, including linear, polynomial, splines, and radial basis function. The elegance of using kernel function lies in the fact that one can deal with feature spaces of arbitrary dimensionality without having to compute the map $\Phi(x)$ explicitly. In the support vector regression, a commonly used kernel function is the Gaussian Radial Basis Function.

The overall performances of RBFNNs and SVM were evaluated in terms of the root-mean-square (rms) error which was defined as below

$$rms = \sqrt{\frac{\sum_{i=1}^{n_s} (y_k - \hat{y}_k)^2}{n_s}}$$
 (8)

where y_k is the desired output and \hat{y}_k is the actual output of the model, and n_s is the number of compounds in the analyzed set.

3.4. RBFNNs and SVM Implementation and Computation Environment. All calculation programs implementing RBFNNs were written in M-file based on the basis MAT-LAB script for RBFNNs. All calculation programs implementing SVM were written in R-file based on the R script for SVM and compiled using an R1.7.1 compiler.²⁵ The scripts were run on a Pentium IV PC with 256M RAM.

4. RESULTS AND DISCUSSION

4.1. Results of MLR. About 600 descriptors were calculated by the CODESSA program. After the correlation analysis of the descriptors, the pool of descriptors was reduced to 227. The stepwise regression routine was used to develop the linear model for the prediction of the heat capacity using calculated structural descriptors. The best linear model contains 4 molecular descriptors. The regression

Table 2. Descriptors, Coefficients, Standard Error, and T-Values for the Linear Modela

chemical meaning	descriptor	coeff	SE	beta	T-value
intercept	(constant)	0.882	1.911		0.461
molecular volume	MV	0.678	0.064	0.502	10.520
number of rings	NR	-12.697	0.942	-0.236	-13.476
number of atoms	NA	2.762	0.267	0.407	10.348
Randic index (order 2)	RI2	4.262	1.048	0.115	4.068

 $^{a}R = 0.988$; $R^{2} = 0.975$; SE of the estimate = 4.268; rms = 4.189; n = 136; F = 1295.787.

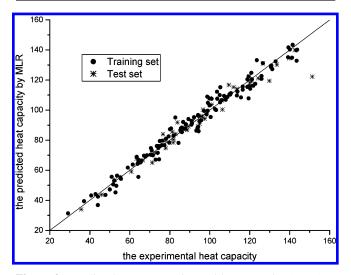


Figure 2. Predicted versus experimental heat capacity (MLR).

coefficients of the descriptors and their physical-chemical meaning were listed in Table 2. The linear correlation coefficient value of each of the two descriptors is <0.85, which means the descriptors were independent in this MLR analysis. The predicted results were given in Table 1. This model gave an rms error of 4.268 heat capacity units for the training set, 5.794 for the test set, and 4.648 for the whole set, and the corresponding correlation coefficients (R) were 0.988, 0.975, and 0.985, respectively. Figure 2 showed these predicted versus experimental heat capacity.

4.2. Result of RBFNNs. From Table 2, it can be seen that the model of MLR was not sufficiently accurate (rms = 4.189, SE = 4.268) and showed the factors influencing the heat capacity were complex and not all of them were a linear correlation with the heat capacity. So, we built the nonlinear prediction models by RBFNNs and SVM to further discuss the correlation between the molecular structure and the heat capacity based on the same descriptor set.

After the establishment of a linear model, RBFNNs were used to develop a nonlinear model based on the same subset of descriptors. Each minimum error on the LOO crossvalidation was plotted versus the width (Figure 3), and the minimum was chosen as the optimal conditions.

Through the above process, the optimum width and the best number of hidden layer units were selected as 2.0 and 20, respectively. From the best network, the inputs in the test set were presented with it, and the results with RBFNNs were obtained. They were shown in Table 1 and Figure 4. The network gave an rms error of 3.422 for the training set, 6.310 for the prediction set, and 4.337 for the whole set, and the corresponding correlation coefficients (R) were 0.987, 0.992, and 0.973, respectively.

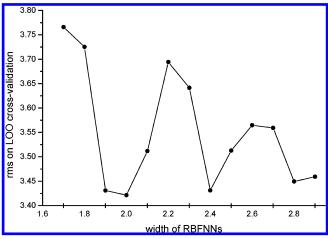


Figure 3. The width of RBFNNs versus rms error on LOO cross-validation.

4.3. Result of SVM. 4.3.1. Selection of the Parameters of the SVM. Analysis of the results obtained by RBFNNs, it can be seen that the model constructed by RBFNNs was not sufficiently accurate and the prediction ability was bad (the rms error for the test set was 6.310), so after the establishment of nonlinear model by RBFNNs, the support vector machines were used to develop an accurate nonlinear model based on the same subset of descriptors.

Similar to other multivariate statistical models, the performances of SVM for regression depend on the combination of several parameters. They are capacity parameter C, ϵ of ϵ -insensitive loss function, the kernel type K, and its corresponding parameters. In this work, LOO cross-validation was performed for parameters selection, 26,27 which probably is the current best-performing approach to the SVM design problem. 28 C is a regularization parameter that controls the tradeoff between maximizing the margin and minimizing the training error. If C is too small, then insufficient stress will be placed on fitting the training data. If C is too large, then the algorithm will overfit the training data. To make the learning process stable, a large value should be set up for C.

The kernel type is another important parameter. For regression tasks, the Gaussian kernel is commonly used. The form of the Gaussian function is as follows

$$\exp(-\gamma * |u - v|^2)$$

where γ is a constant, the parameter of the kernel, and u and v are two independent variables. γ controls the amplitude of the Gaussian function and, therefore, controls the generalization ability of SVM. Each rms error on the LOO cross-validation was plotted versus γ (Figure 5), and the minimum was chosen as the optimal conditions. In this case: $\gamma = 0.008$.

The optimal value for ϵ depends on the type of noise present in the data, which is usually unknown. Even if enough knowledge of the noise is available to select an optimal value for ϵ , there is the practical consideration of the number of resulting support vectors. ϵ -insensitivity prevents the entire training set meeting boundary conditions, and so allows for the possibility of sparsity in the dual formulation's solution. So, choosing the appropriate value of ϵ is critical from theory. To find an optimal ϵ , the rms on

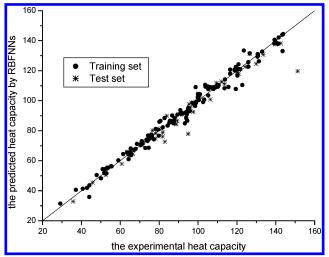


Figure 4. Predicted versus experimental heat capacity (RBFNNs).

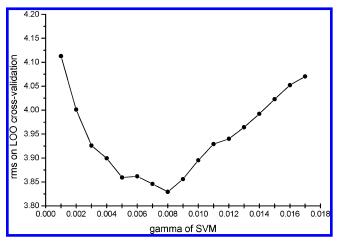


Figure 5. The gamma versus rms error on LOO cross-validation $(C = 100, \epsilon = 0.1)$.

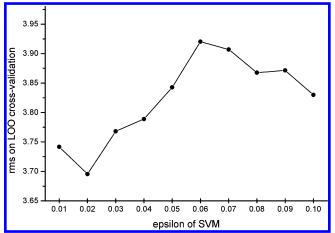


Figure 6. The epsilon versus rms error on validation set (C = 100, $\gamma = 0.008$).

LOO cross-validation on different ϵ was calculated. The curve of rms versus the epsilon was shown in Figure 6. The optimal ϵ was found as 0.02.

The last important parameter is the regularization parameter C, of which the effect on the rms was shown in Figure 7. From Figure 7, the optimal C was found as 100.

4.3.2. The Predicted Results of SVM. Through the above process, the γ , ϵ , and C were fixed to 0.008, 0.02, and 100, respectively, when the support vector number of the SVM

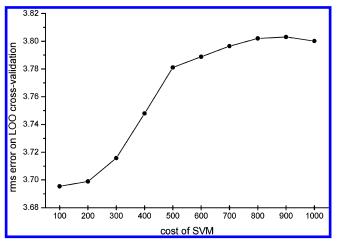


Figure 7. The C versus rms error on validation set ($\gamma = 0.008$, ϵ = 0.02)

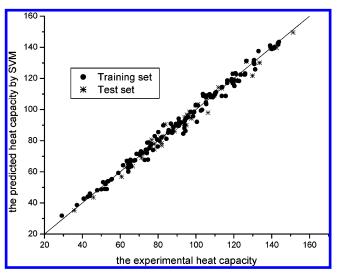


Figure 8. Predicted versus experimental heat capacity(SVM).

model was 19, the predicted results of the optimal SVM were shown in Table 1 and Figure 8. The model gave an rms of 2.880 for the training set, 3.078 for the prediction set, and 2.931 for the whole set, and the corresponding correlation coefficients (R) were 0.994, 0.993 and 0.994, respectively. The performance of SVM is better than MLR and RBFNNs models in Table 1.

4.4. Discussion of the Input Parameters and the Results.

By interpreting the descriptors in the regression model, it is possible to gain some insight into factors that are likely to govern the heat capacity of the compounds. Of the four descriptors, two are constitutional, one is topological, and one is geometrical descriptor. According to the beta values (Table 2), the more relevant descriptor is a geometrical descriptor: molecular volume (MV). MV is a bulk property, which describes the size of a molecule and relates to the dispersion interaction among molecules; this parameter receives a positive regression coefficient in the regression indicating that the larger the molecular volume is, the higher the heat capacity is. The constitutional descriptors include the number of rings (NR) and the number of atoms (NA). NR receives a negative coefficient in the regression, and this indicates that increasing the number of rings leads to a low heat capacity. So, the heat capacity of noncyclic compound is higher than that of cyclic compound. NA receives a

positive coefficient indicating that the heat capacity increases with the increasing of the number of the atoms. The inclusion of topological descriptors: the Randic index (order 2) (RI2), which encodes the size, shape, and degree of branching in the compound and also relates to the dispersion interaction among molecules. It receives a positive coefficient in the regression model indicating the heat capacity increases with increasing the RI2 of the molecule.

Analysis of the results obtained indicated that the models we proposed correctly represent the structural-property relationships of these compounds and that molecular descriptors calculated solely from structures can represent the structural features of the compounds responsible for their heat capacity. Moreover, it seems that the prediction ability of SVM is better than MLR and RBFNNs models. The root cause that SVM can obtain the best results is that SVM adopts the Structural Risk Minimization principle.

5. CONCLUSION

The support vector machine, as a novel type of learning machine, for the first time, was used to develop a QSPR model for the prediction of the heat capacity of a diverse set of 182 compounds based on descriptors calculated from the molecular structure alone. MLR and RBFNNs were also utilized to establish quantitative linear and nonlinear relationships to compare with the results obtained by SVM. Very satisfactory results were obtained with the proposed methods. The models proposed could identify and give some insight into factors that are likely to govern the heat capacity of the compounds. Additionally, nonlinear models using SVM based on the same set of descriptors produced even better models with a good predictive ability than the two other MLR and RBFNNs models. This study of the QSPR model shows that the SVM is a very promising tool in the prediction of heat capacity and exhibits a high speed of leaning when compared with RBFNNs. The training procedure is also simple when using SVM because there are fewer parameters having to be optimized, and only support vectors are used in the generalization process. Besides, the SVM exhibits the better whole performance due to embodying the Structural Risk Minimization principle and some advantages over the other techniques. Furthermore, the proposed approach can also be extended to other QSPR or QSAR investigations.

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