

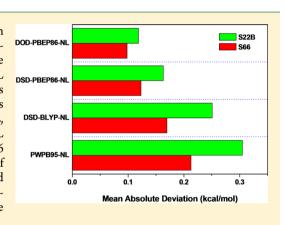
Spin-Component-Scaled Double-Hybrid Density Functionals with Nonlocal van der Waals Correlations for Noncovalent Interactions

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Supporting Information

ABSTRACT: Nonlocal (NL) van der Waals correlation has been incorporated into the spin-component and spin-opposite scaled doublehybrid density functionals (DHDFs) for noncovalent interactions. The short-range attenuation parameters for the tested DHDFs with the NL correlations are optimized by minimizing the mean absolute deviations (MADs) against the S66 database. And consequently, the obtained DHDFs with the NL correlations are denoted as PWPB95-NL, DSD-BLYP-NL, DSD-PBEP86-NL, and DOD-PBEP86-NL. These four DHDFs with the NL correlations are further assessed with the S22B, NCCE31, and ADIM6 databases. On the basis of our benchmark computations, the cooperation of the NL correlation and the spin-component and spin-opposite scaled DHDFs is successful for noncovalent interactions. However, the performances of the four aforementioned DHDFs with the NL correlations on the charge transfer interactions are less than satisfactory.



1. INTRODUCTION

Noncovalent interactions play important roles in the physical and life sciences, and therefore, extensive investigations have been performed to understand different types of noncovalent interactions. 1-6 Density functional theory (DFT) has become a promising methodology for studying noncovalent interactions.^{7–18} Among various density functionals, double-hybrid density functionals (DHDFs) are much more powerful. 19-26 However, additional corrections for the standard density functionals and/or specially devised density functionals are needed for practical applications. 7-18,20-22

Different revisions of dispersion corrections for various density functionals (DFT-D) are efficient and popular methods for noncovalent interactions.²⁷⁻³³ The revision of Grimme's DFT-D3 is generally recommended to investigate various noncovalent interactions with different essences. 30,31 Note that there are two different versions of the Grimme's DFT-D3. The DFT-D3 version with zero damping is denoted as DFT-D3(0),³⁰ whereas the DFT-D3 version with Becke–Johnson damping^{34–36} is dubbed as DFT-D3(BJ).³¹ Moreover, the DFT-D3 refers to a generic notation for both the DFT-D3(0) and DFT-D3(BJ) in this paper. van der Waals density functional theory paves another way for studying noncovalent interactions. $^{37-44}$ In this method, a nonlocal (NL) correlation functional based on the electron density is utilized to describe the dispersion interaction. Simple NL van der Waals density functionals have been developed by Vydrov and Van Voorhis. 40-44 The advanced NL correlation part 44 has also been applied to different density functionals including the DHDFs, and thus, the density functionals with the NL correlations are generally denoted as DFT-NL. 45-47 According to extensive benchmark computations, the DFT-NL method is accurate as the DFT-D3 method for both thermochemistry and noncovalent interactions. 46,47 Furthermore, noncovalent interactions can also be investigated with the exchange-hole dipolemoment model, ^{48–52} pseudopotentials, ^{53–59} and Buckingham— Hirshfeld method. ⁶⁰ Additionally, the long-range van der Waals interactions are able to be well characterized even for complicated condensed matters. ^{61–67} A lot of specially devised density functionals can also be employed to study noncovalent interactions. ⁶⁸⁻⁸¹ For example, we have optimized two DHDFs of B2NC-PLYP and mPW2NC-PLYP without any further correction for noncovalent interactions. 81 However, the limit of accuracy for some aforementioned methods has been presented by Mardirossian and Head-Gordon.⁸²

Recently, dispersion corrected, spin-component and spinopposite scaled DHDFs known as DSD-DFT and DOD-DFT methods have been developed by Martin and co-workers. 83-85 The spin-component and spin-opposite scaled MP2 approaches (SCS-MP2 and SOS-MP2)^{86,87} were applied within the DSD-DFT framework, and moreover, Grimme's DFT-D models including DFT-D2²⁹ and DFT-D3(BJ)³¹ were employed for dispersion corrections. The exchange-correlation energy E_{xc} for the general DSD-DFT method^{83–85} was expressed as

$$\begin{split} E_{xc} &= (1 - c_x) E_x^{\text{DFT}} + c_x E_x^{\text{HF}} + c_c E_c^{\text{DFT}} + c_o E_o^{\text{MP2}} \\ &+ c_s E_s^{\text{MP2}} + E_D \end{split} \tag{1}$$

Received: July 19, 2014 Published: September 16, 2014

Table 1. Exchange Functionals, Correlation Functionals, and Parameters for the DHDFs Tested in This Work^a

DHDF	exchange	correlation	c_x	$c_{\rm c}$	$c_{\rm s}$	$c_{\rm o}$	b	ref
PWPB95-NL	PW	B95	0.50	0.731	0	0.269	11.1	88, ^b 90, 91,
DSD-BLYP-NL	B88	LYP, VWN3	0.69	0.54	0.37	0.46	12.0	83, ^b 102-104
DSD-PBEP86-NL	PBE	P86, VWN5	0.69	0.44	0.22	0.52	14.2	84, 85, ^b 104-106
DOD-PBEP86-NL	PBE	P86, VWN5	0.65	0.47	0	0.54	10.4	85, ^b 104–106

 ${}^{a}c_{sy}$ HF exchange parameter; c_{sy} DFT correlation parameter; c_{sy} same spin parameter for the MP2-like perturbative correlation; c_{oy} opposite spin parameter for the MP2-like perturbative correlation; and b_{sy} , short-range attenuation parameter. The parameter b_{sy} is optimized for each DHDF within the framework of the NL correlation, ${}^{44-46}$ and the long-range parameter C_{sy} is kept as 0.0093 for all the tested DHDFs. b Key reference for the listed parameters except b_{sy} , which is utilized in the NL correlation.

In this formula, the $E_{\rm o}^{\rm MP2}$ and $E_{\rm s}^{\rm MP2}$ were defined as the opposite spin and same spin MP2-like perturbative correlation energies, respectively. In addition, the $E_{\rm D}$ was the dispersion energy obtained with Grimme's DFT-D2²⁹ and DFT-D3(BJ) methods. The DSD-DFT and DOD-DFT functionals performed very well on thermochemistry, thermochemical kinetics, noncovalent interaction, and so on. S3-85 Similarly, the PTPSS-D3(0) and PWPB95-D3(0) functionals were DHDFs fitted with the DFT-D3(0) correction simultaneously by Goerigk and Grimme. The SOS-MP2 procedure was applied for the perturbative correlation. For the PTPSS-D3(0) functional, the first letter "P" denoted "perturbative," and the TPSS exchange and correlation s9 with revised parameters were utilized. As to the PWPB95-D3(0) functional, the second letter "P" implied "perturbative," and the reparameterized PW exchange and B95 correlation were employed.

In this work, we try to employ the NL correlation 44-46 to replace the DFT-D methods 29-31 in the PWPB95-D3(0), 88 DSD-BLYP-D2/D3(0), 83,88 DSD-PBEP86-D3(BJ), 84,85 and DOD-PBEP86-D3(BJ) 55 functionals for noncovalent interactions. The corresponding performances are assessed with the S22 (set 22), 92-95 S66 (set 66), 96,97 NCCE31 (noncovalent complexation energies), 9,98,99 and ADIM6 (interaction energy database for six *n*-alkane dimers) databases. 88,100,101 The S22 database contains 22 small model complexes for noncovalent interactions, 92 whereas the S66 database is much more comprehensive. These two databases were designed by Hobza and co-workers for noncovalent interactions relevant to biochemistry. 92,96 The NCCE31 database is related to diverse nonbonded interactions, 98,99 and this database has been utilized to parametrize and assess density functionals by Truhlar's group. Moreover, the ADIM6 database was designed to study the London-dispersion correction by Grimme et al. In the field of theoretical and computational chemistry, more accurate methods are expected to study noncovalent interactions. And thus, the major aim of this work is to examine the cooperation of the DFT-NL method and the DHDFs using the SCS-MP2 and SOS-MP2 procedures for noncovalent interactions.

2. COMPUTATIONAL METHODS

The databases of S22, 92–95 S66, 96,97 NCCE31, 9,98,99 and ADIM6^{88,100,101} were employed for our benchmark computations. Note that the interaction energies in ref 95 (denoted as S22B) and ref 97 for the S22 and S66 databases were utilized, respectively. The signed mean deviation (MD), mean absolute deviation (MAD), root-mean-square deviation (RMSD), and mean absolute percent deviation (MA%D) were used to assess the performances of the tested methods. The definitions of these four deviations were described in detail in ref 11. The

parameters for the PWPB95-NL, DSD-BLYP-NL, DSD-PBEP86-NL, and DOD-PBEP86-NL functionals are listed in Table 1, and the specific exchange and correlation functionals $^{89-91,102-106}$ were also presented. The Hartree–Fock (HF) exchange parameter (c_x) , DFT correlation parameter (c_c) , and same (c_s) and opposite (c_o) spin coefficients for the MP2like correlation were taken from the related references. 83-85,88 With the framework of the DFT-NL method, 44-47 the shortrange attenuation parameter b for each functional was optimized by minimizing the MAD with the S66 database. Meanwhile, the long-range parameter C was kept as 0.0093. 44,46 which had been proven to be reasonable for the DHDFs. 47 The NL correlation was added non-self-consistently, because the improvement of the self-consistent procedure was negligible. 46 Subsequently, these four obtained functionals with the NL correlations were further assessed with the S22B, NCCE31, and ADIM6 databases. As comparisons, the MP2 method was also examined with the four databases mentioned above.

All the computations in this work were carried out with the ORCA program. ¹⁰⁸ The quadruple- ζ def2-QZVP¹⁰⁹ basis set was utilized for single-point energy computations. On the basis of previous works, ^{88,101} this large basis set was competent for benchmark computations, and the basis set superposition errors for the tested methods could be ignored. The resolution of the identity (RI-JK^{110,111} and RI¹¹²) methods were employed with the auxiliary basis sets of def2-QZVP/JK¹¹³ and def2-QZVP/ C114 to accelerate the self-consistent-field (SCF) and perturbative correlation computations, respectively. The integration grid for the Kohn–Sham SCF computations was Grid6^{115,116} in the ORCA program, whereas vdwGrid4 was used for the NL correlation computations. According to the original work, 83-85,88 the MP2-like computations for the DSD-PBEP86-NL and DOD-PBEP86-NL functionals were performed with the frozen core option, and those for the PWPB95-NL and DSD-BLYP-NL functionals were carried out with correlating all electrons. As to the total energies of molecules, the accuracy of our proposed functionals with the NL correlations was relatively low even for small molecules against the $CCSD(T)^{117-119}$ results (Table S1 in the Supporting Information). Note that the errors of the density functionals for computing the total energies are generally large, and the errors of the total energies are about 1 hartree for medium-sized molecules. 120 In addition, the MP2 computations were also performed with the frozen core option, and the relative costs for the MP2 method and our proposed functionals with the NL correlations were presented in the Supporting Information (Table S2).

3. RESULTS AND DISCUSSION

3.1. Assessment of the PWPB95-NL, DSD-BLYP-NL, DSD-PBEP86-NL, and DOD-PBEP86-NL Functionals with

the S66 and S22B Databases. The short-range attenuation parameters for the PWPB95-NL, DSD-BLYP-NL, DSD-PBEP86-NL, and DOD-PBEP86-NL functionals were determined by minimizing the corresponding MADs with the S66 database. The obtained short-range attenuation parameters have been listed in Table 1. The performances of these four functionals with NL correlations on the S66 and S22B databases are presented in Table 2. As shown in Table 2,

Table 2. Performances of the Tested Methods on the S66 and S22B Databases^a

method	MD	MAD	RMSD	MA%D			
S66 database							
PWPB95-NL	0.13	0.21	0.29	3.9			
DSD-BLYP-NL	-0.03	0.17	0.21	4.0			
DSD-PBEP86-NL	-0.03	0.12	0.15	3.1			
DOD-PBEP86-NL	-0.01	0.10	0.12	2.3			
MP2	-0.57	0.59	0.87	16.3			
revPBE0-DH-NL ^b	-0.04	0.19		4.1			
$B2PLYP-NL^b$	-0.12	0.20		3.6			
S22B database							
PWPB95-NL	0.12	0.31	0.46	4.3			
DSD-BLYP-NL	-0.19	0.25	0.32	6.2			
DSD-PBEP86-NL	-0.13	0.16	0.20	4.2			
DOD-PBEP86-NL	-0.04	0.12	0.15	3.0			
MP2	-1.00	1.02	1.60	23.3			

^aThe MD (kcal/mol), MAD (kcal/mol), RMSD (kcal/mol), and MA %D (%) are employed to evaluate the performances, and the def2-QZVP basis set is used for single-point energy computations. ^bResults taken from ref 47.

these four functionals with NL correlations perform well on both the S66 and S22B databases, because the training set selected in this work is the well designed S66 database. The performance trend of these four functionals with the NL correlations for the S22B database is same as that for the S66 database. Furthermore, the DOD-PBEP86-NL functional is the best performer for both the S66 and S22B databases. The MADs of the DOD-PBEP86-NL/def2-QZVP level against the S66 and S22B databases are only 0.10 and 0.12 kcal/mol, respectively.

With the large def2-QZVP basis set, the MAD of the PWPB95-NL functional (0.21 kcal/mol) is close to those of the revPBE0-DH-NL (0.19 kcal/mol) and B2PLYP-NL (0.20 kcal/ mol) functionals for the S66 database.⁴⁷ The revPBE,¹²¹ a revised version of PBE, in the revPBE0-DH-NL functional was proposed by Zhang and Yang, which was different from the original PBE developed by Perdew and co-workers. 105 Moreover, the DSD-BLYP-NL functional (with an MAD of 0.17 kcal/mol) performs slightly better than the revPBE0-DH-NL and B2PLYP-NL functionals. However, the improvements of the DSD-PBEP86-NL and DOD-PBEP86-NL functionals are more significant. The MADs of the PWPB95-D3(0) and PWPB95-D3(BJ) functionals for the S66 database are 0.19 and 0.22 kcal/mol, respectively. 122 The MAD of the PWPB95-NL functional falls in between these two values. Similarly, the MADs of the DSD-BLYP-D3(0) and DSD-BLYP-D3(BJ) functionals against the S66 database are 0.21 and 0.23 kcal/mol, respectively. The DSD-BLYP-NL functional performs slightly better than these two DFT-D3 methods.

There are three different subsets in the S66 and S22 databases. The concrete subsets are hydrogen-bonded (HB)

complexes, dispersion-dominated (DD) complexes, and complexes with mixed (MX) influence. The assignments of the complexes are determined on the basis of the original refs92 and 96. The MDs and MADs for the subsets of both the S66 and S22B databases are presented in Figure 1. Note that the

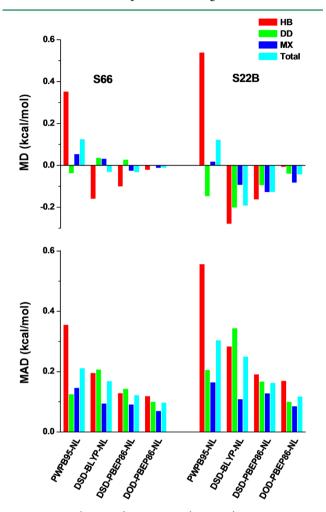


Figure 1. MDs (kcal/mol) and MADs (kcal/mol) for the subsets of both the S66 and S22B databases. The subsets are hydrogen-bonded (HB) complexes, dispersion-dominated (DD) complexes, and complexes with mixed (MX) influence.

reference interaction energies in the S66 and S22B databases are negative values. As illustrated in Figure 1, the DOD-PBEP86-NL functional is the best performer for all the subsets of both the S66 and S22B databases. Compared with the DD and MX subsets, the PWPB95-NL functional performs worse on the HB subsets, and this functional generally tends to overestimate the interaction energies, i.e., underestimate the binding energies for the HB subsets according to the positive MDs.

3.2. Performances of the Four Tested Functionals with the NL Correlations on the NCCE31 Database. In this section, the four tested functionals with the NL correlations are assessed with the NCCE31 database, which has been developed by Truhlar's group. ^{9,98,99} The detailed subsets for the NCCE31 database are six HB (HB6) complexes, seven charge transfer (CT7) complexes, six dipole interaction (DI6) complexes, seven weak interaction (WI7) complexes, and five π - π stacking (PPS5) complexes. The reference binding

energies are positive values, which are different from the S66 and S22B databases. As listed in Table 3, the range of the

Table 3. Assessment of the Tested Methods against the NCCE31 Database^a

method	MD	MAD	RMSD	MA%D
PWPB95-NL	0.11	0.25	0.37	18.2
DSD-BLYP-NL	0.25	0.30	0.44	16.2
DSD-PBEP86-NL	0.23	0.25	0.39	12.5
DOD-PBEP86-NL	0.18	0.20	0.33	8.1
MP2	0.32	0.36	0.61	25.0
revPBE0-DH-NL b	0.15^{c}	0.25		16.4
B2PLYP-NL b	0.35 ^c	0.42		14.5

^aThe MD (kcal/mol), MAD (kcal/mol), RMSD (kcal/mol), and MA %D (%) are utilized to assess the performances, and these results are computed with the def2-QZVP basis set. ^bResults taken from ref 47. ^cThe MDs have been converted with respect to the positive reference binding energies.

MADs for the tested functionals with the NL correlations is 0.20–0.30 kcal/mol, and the DOD-PBEP86-NL functional is also the best performer for the NCCE31 database. As comparisons, the MADs of the revPBE0-DH-NL and B2PLYP-NL functionals are 0.25 and 0.42 kcal/mol, respectively.⁴⁷

As shown in Figure 2, the four tested functionals with the NL correlations perform worst on the CT7 subset of the NCCE31 database, and the MADs for the CT7 subset are within a range of 0.45–0.57 kcal/mol. For each functional with the NL correlation, the MAD for the CT7 subset is identical to the corresponding MD. With respect to the positive reference binding energies in the NCCE31 database, the meaning of the MD for this database is opposite that for the S66 or S22B databases. As a result, the four tested functionals with the NL correlations tend to overestimate the binding energies for the CT7 subset.

3.3. Assessment of the Four Tested Functionals with the NL Correlations against the ADIM6 Database. We now further examine the performances of the four tested functionals with the NL correlations on the ADIM6 database. 88,100,101 The reference energies in the ADIM6 database are binding energies as the NCCE31 database. The six *n*-alkane dimers in the ADIM6 database are remarkable complexes with dispersion effect, and thus, the performances of the DHDFs using the SCS-MP2 and SOS-MP2 procedures combined with the NL correlations on the dispersion effect will be presented much more clearly.

As illuminated in Table 4, the PWPB95-NL and DOD-PBEP86-NL functionals perform better than the DSD-BLYP-NL and DSD-PBEP86-NL functionals on the ADIM6 database. Compared with the performances of the PWPB95, PWPB95-D3(0), DSD-BLYP without any dispersion correction, and DSD-BLYP-D3(0) functionals, the improvement of the NL correlation is similar to that with Grimme's DFT-D3(0) correction. 88,123

3.4. Comments on the Four Tested Functionals with the NL Correlations. On the basis of our benchmark computations, the MADs of the DOD-PBEP86-NL functional for the S66, S22B, and NCCE31 databases are 0.10, 0.12, and 0.20 kcal/mol, respectively. Therefore, this functional with the NL correlation is highly recommended to study noncovalent interactions. Moreover, the other three functionals with the NL

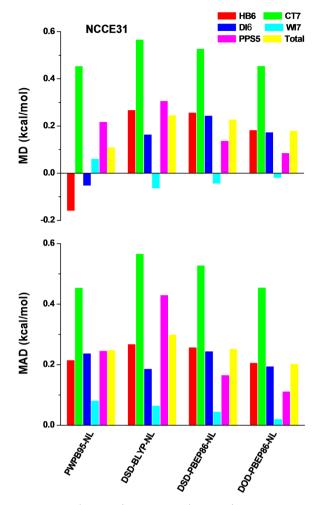


Figure 2. MDs (kcal/mol) and MADs (kcal/mol) for the subsets of the NCCE31 database. The subsets are six hydrogen-bonded (HB6) complexes, seven charge transfer (CT7) complexes, six dipole interaction (DI6) complexes, seven weak interaction (WI7) complexes, and five $\pi-\pi$ stacking (PPS5) complexes.

Table 4. Performances of the Tested Methods on the ADIM6 Database a

method	MD	MAD	RMSD	MA%D
PWPB95-NL	0.08	0.13	0.14	4.0
DSD-BLYP-NL	-0.34	0.34	0.35	11.8
DSD-PBEP86-NL	-0.25	0.25	0.27	8.0
DOD-PBEP86-NL	-0.13	0.13	0.15	4.5
MP2	0.29	0.29	0.34	7.5
PWPB95 ^b	-1.69	1.69	1.86	
PWPB95-D3 $(0)^{b}$	0.36	0.36	0.40	
DSD-BLYP b,c	-1.89	1.89	2.06	
DSD-BLYP-D3 $(0)^b$	-0.13	0.13	0.13	

^aThe MD (kcal/mol), MAD (kcal/mol), RMSD (kcal/mol), and MA %D (%) are utilized to evaluate the performances, and these results are obtained with the def2-QZVP basis set. ^bResults taken from ref 123. ^cWithout any dispersion correction.

correlations tested in this work also perform well on noncovalent interactions. However, the performances of these four functionals with the NL correlations on the charge transfer interactions are unsatisfactory, and they tend to overestimate the binding energies of the charge transfer complexes. The reason may be that the NL correlation optimized with the S66

database generally overestimates the dispersion components of the charge transfer interactions. Therefore, further efforts should be made on this issue in the future. As far as we know, range-separated density functionals with additional dispersion corrections may be suitable for the charge transfer interactions. ^{70,78,79,124–130} With respect to the charge transfer effect, noncovalent interactions involving open-shell species ^{126,131} are suggested for the relevant databases under construction.

The fraction of Fock-exchange for the PWPB95 functional is only 50%. See As demonstrated by Goerigk and Grimme, this fraction is reasonable for general chemistry. Moreover, this relatively low fraction of Fock exchange makes the PWPB95 functional much more stable for complicated electronic structures. On the basis of the good performance of the PWPB95-D3(0) functional on the comprehensive GMTKN30 database, the PWPB95-NL functional is expected to perform well on other chemical properties beyond noncovalent interactions, especially for the complicated electronic structures.

4. CONCLUSIONS

Four DHDFs with the NL correlations denoted as PWPB95-NL, DSD-BLYP-NL, DSD-PBEP86-NL, and DOD-PBEP86-NL have been proposed for investigating noncovalent interactions. Among them, the DOD-PBEP86-NL functional is highly recommended. More importantly, this functional with the NL correlation performs very well on the hydrogenbonded, dispersion-dominated, and mixed influence complexes. However, based on the benchmark computations with the NCCE31 database, the performances of these four density functionals with the NL correlations on the charge transfer interactions are less than satisfactory compared with other types of noncovalent interactions. In practical applications, the DHDFs with the DFT-D3(0) and/or DFT-D3(BJ) corrections may be employed for cross validations.

ASSOCIATED CONTENT

S Supporting Information

Total energies (hartree) of the selected molecules computed with CCSD(T) and our proposed methods (Table S1) and relative costs for MP2 and our proposed methods (Table S2). This material is available free of charge via the Internet at http://pubs.acs.org.

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Notes

The authors declare no competing financial interest.

ACKNOWLEDGMENTS

This work was financially supported by the Xi'an Technological University (No. XAGDXJJ1030). Partial computations were carried out at the Supercomputing Center of Qingdao Institute of Bioenergy and Bioprocess Technology.

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