

Formation of Abundant $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ by Ligand-Exchange Reaction between $[\text{Pb}(\text{N}_2)_n]^{2+}$ ($n = 1-3$) and H_2O

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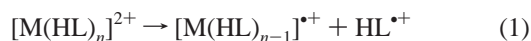
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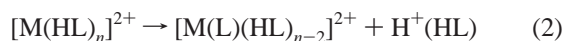
Doubly charged lead monohydrate, $[\text{Pb}(\text{H}_2\text{O})]^{2+}$, was predicted to be unstable in the gas phase, but it has recently been observed to form in low yield via ligand change between $[\text{Pb}(\text{CH}_3\text{CN})]^{2+}$ and H_2O [Shi, T.; Orlova, G.; Guo, J.; Bohme, D. K.; Hopkinson, A. C.; Siu, K. W. M. *J. Am. Chem. Soc.* **2004**, *126*, 7975–7980]. Here we report that *abundant* $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ is formed in the gas phase by ligand-exchange reaction between $[\text{Pb}(\text{N}_2)_n]^{2+}$ ($n = 1-3$) and water after collisional activation. Density functional theory has been used to examine the ligand-exchange reaction profile. A comparison of the potential-energy surfaces between $[\text{Pb}(\text{N}_2)]^{2+}$ and $[\text{Pb}(\text{CH}_3\text{CN})]^{2+}$ reacting with H_2O provides strong evidence that the ligand-exchange reaction of $[\text{Pb}(\text{N}_2)]^{2+}$ with H_2O to form $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ is more efficient than that of $[\text{Pb}(\text{CH}_3\text{CN})]^{2+}$ with H_2O .

Introduction

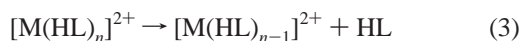
Whether doubly charged metal hydrates, $[\text{M}(\text{H}_2\text{O})]^{2+}$, can exist in the gas phase or not has received a lot of attention in the past decade.^{1–15} The classical technique of attaching a water molecule to M^{2+} to form $[\text{M}(\text{H}_2\text{O})]^{2+}$ failed except for $\text{M} = \text{Ba}, \text{Sr}, \text{and Ca}$,¹⁶ metals whose second ionization energies (IEs) are lower than the first IE of water at 12.6 eV.¹⁷ For M whose second IEs are higher than the first IE of water, a spontaneous dissociative electron transfer occurs, resulting in M^{+} and H_2O^{+} . It turns out that the route to $[\text{M}(\text{H}_2\text{O})]^{2+}$ is through collision-induced dissociation (CID) of $[\text{M}(\text{H}_2\text{O})_n]^{2+}$ ($n \geq 4$), which are abundantly produced via electrospraying an aqueous solution of the M^{2+} .^{1,2,11} To date, most $[\text{M}(\text{H}_2\text{O})]^{2+}$ of divalent M , including $[\text{Cu}(\text{H}_2\text{O})]^{2+}$ (Cu has the highest second IE of all divalent metals), have been observed, at least within the tens of microsecond observation window in a tandem mass spectrometry (MS/MS) experiment.^{10,11,18} A driving force behind the reactivity of $[\text{M}(\text{H}_2\text{O})_n]^{2+}$ and in general $[\text{M}(\text{HL})_n]^{2+}$, where HL is a generic ligand, is its high charge density, especially when n is small. A classical view is that withdrawal of electron density from the ligand to the formally doubly charged metal ion provides some stabilization and causes partial delocalization of the 2+ charge onto the ligands. This delocalization predisposes the complex to dissociation as a result of Coulombic repulsion. Dissociation can take place concomitantly with electron transfer:



or with proton transfer:



These two channels compete with ligand elimination:



In general, dissociative electron and/or proton transfer are/is more prevalent than ligand elimination in the CID of $[\text{M}(\text{HL})_n]^{2+}$ where n is small.

For $\text{HL} = \text{H}_2\text{O}$, high-level *ab initio* calculations performed on $[\text{M}(\text{H}_2\text{O})]^{2+}$ for a number of alkaline earth and transition metal ions have all predicted the presence of sizable activation barriers in the dissociative electron-transfer reactions into M^{+} and H_2O^{+} , and that the $[\text{M}(\text{H}_2\text{O})]^{2+}$ is either stable or metastable.^{7–9} Beyer et al.⁷ showed using density functional theory (DFT) that alkaline earth metal dihydrates $[\text{M}(\text{H}_2\text{O})_2]^{2+}$ dissociate preferentially via proton transfer to give MOH^{+} and H_3O^{+} . The $[\text{M}(\text{H}_2\text{O})_2]^{2+}$ complexes are nonetheless stable as the activation energies for dissociative proton transfer are larger than 33 kcal/mol.⁷

Despite electrospray's success in producing $[\text{M}(\text{H}_2\text{O})]^{2+}$ of most divalent metals, attempts to produce $[\text{Pb}(\text{H}_2\text{O})_n]^{2+}$ ions by electrospraying lead(II) salt solutions were unsuccessful. By contrast, the complexes $[\text{Pb}(\text{CH}_3\text{CN})_n]^{2+}$,¹⁵ $[\text{Pb}(\text{D-glucose})_n]^{2+}$,¹⁹ and $[\text{Pb}(\text{DMSO})_n]^{2+}$ ²⁰ have been produced by electrospray. Stace et al.²¹ using the "pick-up" technique, also failed to detect any $[\text{Pb}(\text{H}_2\text{O})_n]^{2+}$ ions in the gas phase, but did observe doubly charged ions $[\text{Pb}(\text{ROH})_n]^{2+}$, where ROH was propan-1-ol or butan-1-ol. These experiments, complemented by DFT calculations, allowed them to deduce that the stability of $[\text{Pb}(\text{ROH})_4]^{2+}$ could be explained by the hard–soft acid–base principle and led them to the conclusion that complexes of smaller alcohols and water with Pb^{2+} are too unstable to exist. However, very recently, we provided proof that doubly charged lead monohydrate does exist and can be synthesized, albeit in very low yield, by the ligand-exchange reaction between $[\text{Pb}(\text{CH}_3\text{CN})]^{2+}$ and water in the collision cell of a tandem mass spectrometer.¹⁵ DFT calculations show strong evidence that $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ is stable, while $[\text{Pb}(\text{H}_2\text{O})_2]^{2+}$ and $[\text{Pb}(\text{H}_2\text{O})_3]^{2+}$ are metastable against dissociative proton transfer.

Here we report that abundant $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ can be produced via the ligand-exchange reaction between $[\text{Pb}(\text{N}_2)_n]^{2+}$ ($n = 1-3$) and water. By comparison with the reaction between $[\text{Pb}(\text{CH}_3\text{CN})]^{2+}$ and water, factors that lead to efficient production of $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ are presented and discussed.

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complex	% of total ion signal				precursor ion
	Pb ²⁺	PbOH ⁺	Pb ²⁺	[Pb(H ₂ O)] ²⁺	
[Pb(CH ₃ CN)] ²⁺	51.0	3.7	3.7	0.08	32.9
[Pb(N ₂)] ²⁺	25.4	18.6	18.1	14.7	23.2
[Pb(N ₂) ₂] ²⁺	20.5	29.1	7.3	21.8	3.1
[Pb(N ₂) ₃] ²⁺	13.6	37.2	3.4	22.8	2.4

Experimental Section

Computational Section

Results and Discussion

Under a declustering potential of 80–120 eV, electrospraying an acetonitrile solution of lead(II) nitrate produced Pb^{2+} in high abundance. A small fraction of the Pb^{2+} , after supersonic jet expansion, associated with N_2 , the curtain gas, a minute fraction

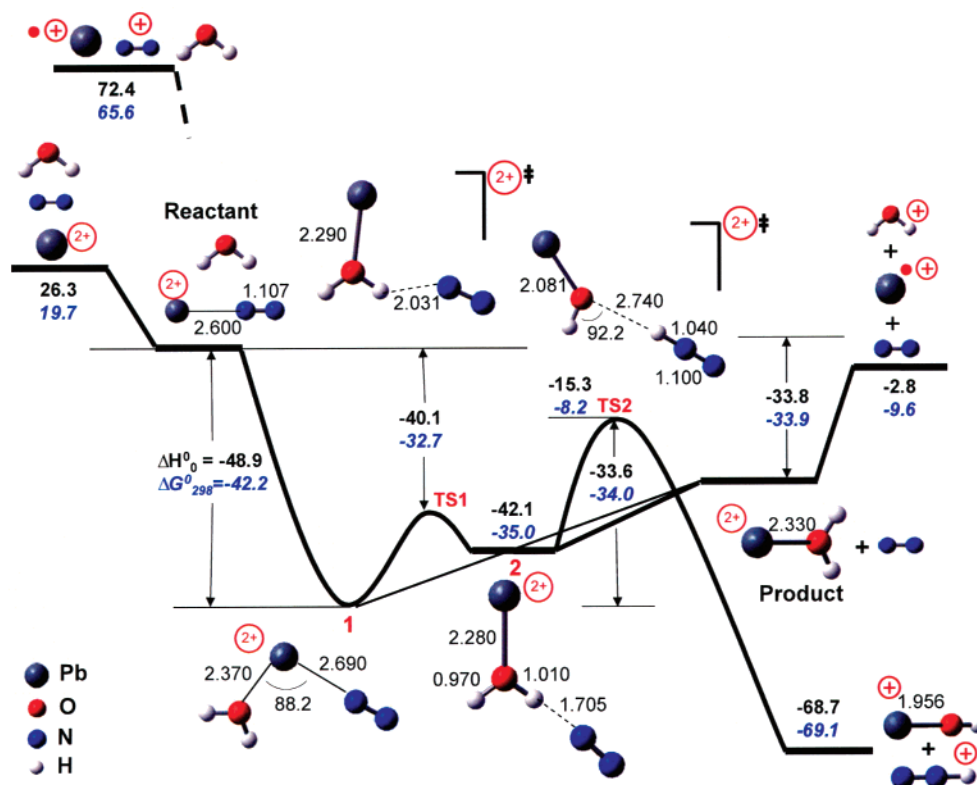
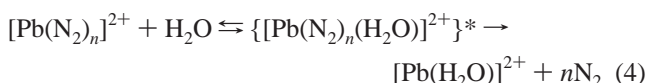


Figure 2. Reaction profiles of $[\text{Pb}(\text{N}_2)_2]^{2+}$ and water at B3LYP/sdd/6-31++G**. The upper values are relative enthalpies at 0 K (ΔH°_0); the lower, italicized values are relative free energies at 298 K (ΔG°_{298}). All energies are in kcal/mol.

of which was also sampled along with Pb^{2+} and other ions. Up to three nitrogen molecules could be attached, resulting in $[\text{Pb}(\text{N}_2)_n]^{2+}$ ($n = 1-3$). Mass-selecting $[\text{Pb}(\text{N}_2)_n]^{2+}$ ($n = 1-3$) by Q1, colliding with wet nitrogen in q2, and mass-analyzing by Q3 resulted in a number of product ions, including Pb^+ , PbOH^+ , $[\text{Pb}(\text{N}_2)]^{2+}$, Pb^{2+} , and $[\text{Pb}(\text{H}_2\text{O})]^{2+}$. Their relative abundances are summarized in Table 1; mass spectra for $^{206}\text{Pb}(\text{N}_2)_2^{2+}$, $^{208}\text{Pb}(\text{N}_2)_2^{2+}$, $^{206}\text{Pb}(\text{N}_2)_3^{2+}$, and $^{208}\text{Pb}(\text{N}_2)_3^{2+}$ are shown in Figure 1. Table 1 also summarizes the results of colliding $[\text{Pb}(\text{CH}_3\text{CN})]^{2+}$ with wet nitrogen; it is readily apparent that more $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ was produced from $[\text{Pb}(\text{N}_2)_n]^{2+}$ ($n = 1-3$) than from $[\text{Pb}(\text{CH}_3\text{CN})]^{2+}$. The relative abundance of $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ increased from the latter to the former by a factor of ca. 180 for $n = 1$ and ca. 280 for $n = 3$. In an earlier paper, we reported the synthesis of $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ via colliding $[\text{Pb}(\text{CH}_3\text{CN})]^{2+}$ with room air of relative humidity of 50–58%.¹⁵ Although the moisture content of the wet nitrogen used in the current study is unknown, it is unlikely that it is as high as that of room air. This conjecture is in accordance with the measured relative abundance of $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ at 0.08% (Table 1), which is lower than that measured previously at 0.4%.¹⁵ By contrast, with $[\text{Pb}(\text{N}_2)_n]^{2+}$ as reagent, $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ is a major product ion with relative abundance ranging from 14.7 to 22.8% from $n = 1$ to $n = 3$. As in our earlier proposal,¹⁵ we are hypothesizing here that the abundant $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ observed in this study was a result of ligand-exchange reaction between the Pb^{2+} complex, herein $[\text{Pb}(\text{N}_2)_n]^{2+}$, and H_2O :



where the asterisk (*) denotes vibronical excitation. The higher yield of $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ from $[\text{Pb}(\text{N}_2)_3]^{2+}$ than from $[\text{Pb}(\text{N}_2)]^{2+}$ may be attributed to, first, a longer lifetime of the $\{[\text{Pb}(\text{N}_2)_3-$

$(\text{H}_2\text{O})]^{2+}\}^*$ complex than that of the $\{[\text{Pb}(\text{N}_2)(\text{H}_2\text{O})]^{2+}\}^*$ complex because of the increased degrees of freedom by having two additional nitrogen molecules and, second, a more efficient deactivation of $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ because of the presence of two additional nitrogen molecules into which the excess energy may be distributed after dissociation.

Prior to examining the reaction channels of $[\text{Pb}(\text{N}_2)_n]^{2+}$ with water, it is instructive to examine the properties of the nitrogen molecule. For comparison, we will also examine the properties of acetonitrile. N_2 has a triple bond, which is much stronger (226.2 ± 0.1 kcal/mol) than the C–C bond of acetonitrile (145.9 ± 0.5 kcal/mol),¹⁷ suggesting that, unlike acetonitrile, ligand fragmentation will not occur with N_2 in $[\text{Pb}(\text{N}_2)_n]^{2+}$. The bond enthalpy, ΔH°_0 , for the M–ligand bond in $[\text{Pb}(\text{N}_2)]^{2+}$ is 26.3 kcal/mol (see below), 65.6 kcal/mol lower than that in $[\text{Pb}(\text{CH}_3\text{CN})]^{2+}$ at 91.9 kcal/mol.¹⁵ Thus the loss of the nitrogen molecule is much easier than that of acetonitrile. That is, the stabilities of $[\text{Pb}(\text{N}_2)_n]^{2+}$ are much lower than those of $[\text{Pb}(\text{CH}_3\text{CN})_n]^{2+}$. Indeed, in MS scans, we found that the abundances of $[\text{Pb}(\text{N}_2)_n]^{2+}$ are lower and more sensitive to orifice voltages than those of $[\text{Pb}(\text{CH}_3\text{CN})_n]^{2+}$. In addition, the IE of N_2 (15.6 eV) is slightly higher than the second IE of Pb (15.0 eV), while the IE of CH_3CN (12.2 eV) is lower.¹⁷ This means that electron transfer from the nitrogen molecule to doubly charged lead is unlikely. The wet nitrogen contains traces of water and oxygen. The IEs of H_2O (12.6 eV) and O_2 (12.1 eV) are lower than the second IE of lead.¹⁷ Thus electron transfer from water and oxygen to Pb^{2+} in the transient complexes formed after collision is exothermic and will be efficient, unless the barrier against electron transfer is large. Indeed, O_2^{+*} was reported in the earlier, $[\text{Pb}(\text{CH}_3\text{CN})]^{2+}$ work.¹⁵

The following reaction channels are apparent in the collision of $[\text{Pb}(\text{N}_2)]^{2+}$ with wet nitrogen: (1) ligand elimination, $[\text{Pb}(\text{N}_2)]^{2+} + \text{M} \rightarrow \text{Pb}^{2+} + \text{N}_2 + \text{M}$ (where M is a collision partner,

N_2 , O_2 , or H_2O); (2) complexation followed by dissociative electron transfer, $\text{Pb}^{2+} + \text{O}_2$ (or H_2O) $\rightarrow \{[\text{Pb}(\text{O}_2 \text{ or } \text{H}_2\text{O})]^{2+}\}^* \rightarrow \text{Pb}^{+} + \text{O}_2^{+}$ (or H_2O^{+}); (3) complexation followed by dissociative proton transfer, $[\text{Pb}(\text{N}_2)]^{2+} + \text{H}_2\text{O} \rightarrow \{[\text{Pb}(\text{N}_2)(\text{H}_2\text{O})]^{2+}\}^* \rightarrow \text{PbOH}^{+} + \text{N}_2\text{H}^{+}$; (4) ligand exchange, $[\text{Pb}(\text{N}_2)]^{2+} + \text{H}_2\text{O} \rightarrow \{[\text{Pb}(\text{N}_2)(\text{H}_2\text{O})]^{2+}\}^* \rightarrow [\text{Pb}(\text{H}_2\text{O})]^{2+} + \text{N}_2$. All ions >30 Th with the exception of O_2^{+} have been detected (Figure 1); the absence of O_2^{+} (32 Th) is likely due to scattering and poor confinement within q_2 .

The reaction profile between $[\text{Pb}(\text{N}_2)]^{2+}$ and H_2O is shown in Figure 2, where the upper values are ΔH°_0 and the lower, italicized values are ΔG°_{298} . As we have shown experimentally that $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ exists in the gas phase, our focus here is on the mechanism of the ligand-exchange reaction between $[\text{Pb}(\text{N}_2)]^{2+}$ and H_2O . Reaction of $[\text{Pb}(\text{N}_2)]^{2+}$ and H_2O leads first to the formation of vibronically excited $[\text{Pb}(\text{N}_2)(\text{H}_2\text{O})]^{2+}$, structure **1**, which then dissociates either directly into $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ and N_2 , or indirectly after promoting the ligated nitrogen from the first to the second solvation shell via the transition state **TS1** to form $[\text{Pb}(\text{H}_2\text{O})]^{2+}(\text{N}_2)$, structure **2**, which then dissociates to form $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ and N_2 (channel 4). Both dissociations from the vibronically excited structure **1** are expected to be barrierless. Alternatively, **2** can also dissociate via **TS2**, through which a proton is transferred from the ligated water to the departing nitrogen molecule, to give PbOH^{+} and N_2H^{+} (channel 3). There is competition between nitrogen elimination and dissociative proton transfer; this largely determines the formation efficiency of $[\text{Pb}(\text{H}_2\text{O})]^{2+}$. **TS2** at -15.3 kcal/mol is 18.5 kcal/mol higher in enthalpy than the separated products of $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ and N_2 . Thus formation of $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ is favored over that of PbOH^{+} . By comparison, for $[\text{Pb}(\text{CH}_3\text{CN})(\text{H}_2\text{O})]^{2+}$ the formation of PbOH^{+} is favored over that of $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ by 48.8 kcal/mol, which is the major factor for low $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ abundance in the earlier work.¹⁵ It is noteworthy that the barriers for proton transfer are inversely related to the proton affinities of the ligands: the proton affinity of acetonitrile (186.2 kcal/mol) is much higher than that of nitrogen (118.0 kcal/mol).³³ In addition, the dissociative proton-transfer barrier (in terms of ΔH°_0) in $[\text{Pb}(\text{CH}_3\text{CN})(\text{H}_2\text{O})]^{2+}$, at 22.1 kcal/mol,¹⁵ is 11.5 kcal/mol lower than that of $[\text{Pb}(\text{N}_2)(\text{H}_2\text{O})]^{2+}$, at 33.6 kcal/mol. As formation of $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ involves loss of the ligand originally attached to Pb^{2+} , the binding enthalpies of Pb^{2+} to the ligands are also an important factor. For the ligands N_2 , H_2O , and CH_3CN , the calculated binding enthalpies with Pb^{2+} are, respectively, 26.3, 60.4,¹⁵ and 91.9 kcal/mol.¹⁵ Within the context of relative binding enthalpy, collisionally activated $[\text{Pb}(\text{N}_2)(\text{H}_2\text{O})]^{2+}$ would be expected to lose nitrogen, while $[\text{Pb}(\text{CH}_3\text{CN})(\text{H}_2\text{O})]^{2+}$ lose water. Thus all factors discussed above are consistent with the experimental observation: namely, that ligand exchange between $[\text{Pb}(\text{CH}_3\text{CN})]^{2+}$ and H_2O produces a low abundance of $[\text{Pb}(\text{H}_2\text{O})]^{2+}$; by contrast, ligand exchange between $[\text{Pb}(\text{N}_2)]^{2+}$ and H_2O produces $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ abundantly.

Conclusions

Abundant $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ is produced in the ligand-exchange reaction of $[\text{Pb}(\text{N}_2)]^{2+}$ with water. Compared to our previous observation, where a low abundance of $[\text{Pb}(\text{H}_2\text{O})]^{2+}$ was observed in the reaction of $[\text{Pb}(\text{CH}_3\text{CN})]^{2+}$ with water, the efficiency of ligand exchange in this study is greatly enhanced by having a weakly bound N_2 as the departing ligand. Two properties of the ligand, the proton affinity and the binding enthalpy, contribute toward the formation efficiency of $[\text{Pb}(\text{H}_2\text{O})]^{2+}$.

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Supporting Information Available: Cartesian coordinates and electronic energies for key structures reported. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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