# Electrical Properties and Defect Chemistry of TiO<sub>2</sub> Single Crystal. III. Equilibration Kinetics and Chemical Diffusion<sup>†</sup>

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The equilibration kinetics of high-purity single-crystal TiO<sub>2</sub> were monitored using measurements of electrical conductivity in the temperature range 1073–1323 K and oxygen activity,  $p(O_2)$ , range  $10^{-13}$  to 75 kPa. The kinetics data were used to determine the chemical diffusion coefficient ( $D_{\text{chem}}$ ) within narrow ranges of  $p(O_2)$ . There was observed a complex effect of the  $p(O_2)$  on the  $D_{\text{chem}}$ , which exhibits a maximum at the n-p transition. The effect of the  $p(O_2)$  on the  $D_{\text{chem}}$  was discussed in terms of the defect disorder and the related semiconducting properties. The activation energy of the  $D_{\text{chem}}$ , which also varies with the  $p(O_2)$ , exhibits a maximum at  $p(O_2) = \sim 10^4$  Pa (143 kJ/mol).

#### 1. Introduction

Fujishima and Honda<sup>1</sup> were the first to determine that  $TiO_2$  is a good candidate for the photoelectrochemical conversion of solar energy (sunlight) into chemical energy (hydrogen). While this was a major discovery, its commercialization requires a significant increase in the energy conversion efficiency (ECE) from the  $\sim 0.5\%$  reported by Fujishima and Honda<sup>1</sup> to > 10%, which the U.S. Department of Energy considers as the benchmark for commercialization.<sup>2</sup> Consequently, many laboratories have undertaken research that aims to process  $TiO_2$  with enhanced properties by modifying its nonstoichiometry, defect disorder, and associated photoelectrochemical properties.

The imposition of controlled defect disorder in metal oxides, such as TiO<sub>2</sub>, requires knowledge of the diffusion data and assessment of mass transport kinetics in order to ensure equilibration during processing at elevated temperatures. In particular, these data can be used to determine the required processing conditions, including the time and the temperature of the process. Consequently, a precondition for the fabrication of TiO<sub>2</sub> specimens that are well-defined and reproducible is the determination of diffusion data.

Nonstoichiometry and related defect disorder in nonstoichiometric oxides can be imposed by controlled oxygen activity at the gas—solid interface, which results in the formation of an oxygen chemical potential gradient and the subsequent propagation of the oxygen activity into the bulk. The gradient is the driving force of the equilibration, which is rate-controlled by the transport of defects under the influence of the chemical potential gradient. Consequently, the equilibration aims at annihilation of the concentration gradients. The rate constant of this process, which is the chemical diffusion coefficient  $(D_{\rm chem})$ , may be determined from the equilibration kinetics.<sup>3–7</sup>

The determination of well-defined data for the equilibration kinetics requires the following issues to be addressed: (i) The

initial and the final stages of the equilibration must be well defined. This is the case when these two stages correspond to gas—solid equilibrium. Therefore, the diffusion data may be considered as well-defined when it is demonstrated that gas—solid equilibrium has been achieved. (ii) When the transport kinetics depend on nonstoichiometry, the  $D_{\rm chem}$  must be determined from the equilibration kinetic data within narrow ranges of p(O<sub>2</sub>). (iii) The  $D_{\rm chem}$  must reflect bulk diffusion under the chemical potential gradient and be independent of surface effects. Therefore, knowledge of the effects of the surface on the gas—solid kinetics is required to assess whether the kinetics are controlled by bulk diffusion or by surface reaction.

The reported data for the  $D_{\rm chem}$  of TiO<sub>2</sub> exhibit substantial scatter in both the absolute values and the temperature dependencies. <sup>8–14</sup> The present work demonstrates that, in most cases, the reported data are not well defined because they are reflective of the applied experimental procedures rather than the intrinsic properties of TiO<sub>2</sub>. In the remaining cases, the experimental details, which are required to assess physical meaning of the diffusion data, are not available. Therefore, there is a need to determine well-defined data of the chemical diffusion coefficient for TiO<sub>2</sub>.

Recently, Lee and Yoo<sup>15</sup> reported so-called 2-fold kinetics, which consists of two independent relaxation kinetics. The related kinetic data are considered in terms of the chemical diffusion coefficients of tetravalent Ti interstitials and oxygen vacancies, which assume comparable values and both are relatively rapid. Their interpretation of data is based on the effect of p(O<sub>2</sub>) on electrical conductivity. According to Lee and Yoo, <sup>15</sup> the  $p(O_2)$  exponent dependence of the electrical conductivity is -1/5 and -1/6 at low and high p(O<sub>2</sub>), respectively. Our electrical conductivity data reported in Part I<sup>16</sup> do not confirm this behavior. The authors of the present work also have reported two regimes of the relaxation kinetics; 17 however, the procedure of the determination of the chemical diffusion coefficient and the interpretation of data differ essentially from those of Lee and Yoo15 in terms of the assumed defect disorder model. Therefore, the absolute values of their chemical diffusion coefficient cannot be compared with the data determined in the present work.

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The purpose of the present work is to determine the gas—solid equilibration kinetics for undoped single-crystal  $\text{TiO}_2$  within narrow ranges of p(O<sub>2</sub>), where the diffusion data are well-defined in terms of the defect disorder.

#### 2. Definition Of Terms

**2.1. Defect Disorder.**  $TiO_2$  is a nonstoichiometric compound.<sup>3</sup> Its defect disorder has been considered in terms of both oxygen vacancies and titanium interstitials, which result in the formation of donor centers.<sup>3,11</sup> Therefore,  $TiO_2$  has been considered as an n-type semiconductor. Gravimetric studies have revealed that  $TiO_2$  exhibits an effective deficit of oxygen<sup>3</sup>. Therefore, its formula has been assumed as  $TiO_{2-x}$ , where x varies between  $10^{-2}$  and  $10^{-4}$ .

It has been shown that TiO<sub>2</sub> may exhibit both n- and p-type properties. <sup>17,18</sup> The presence of p-type properties is considered in terms of titanium vacancies, which are formed during prolonged oxidation of TiO<sub>2</sub>. <sup>17</sup> These defects lead to the formation of acceptor centers. Therefore, their imposition in a controlled manner allows the generation of p-type TiO<sub>2</sub> without the incorporation of acceptor-type ions.

Using the Kröger-Vink notation, <sup>19</sup> the following defect equilibria are the most representative for TiO<sub>2</sub>: <sup>20</sup>

$$O_0^x \rightleftharpoons V_0^{\bullet \bullet} + e' + \frac{1}{2}O_2 \tag{1}$$

$$2O_O + Ti_{Ti} \rightleftharpoons Ti_i^{3+} + 3e' + O_2$$
 (2)

$$2O_0 + Ti_{Ti} \rightleftharpoons Ti_i^{4+} + 4e' + O_2$$
 (3)

$$O_2 \rightleftharpoons V_{T_i}^{\prime\prime\prime\prime\prime} + 4h^{\bullet} + 2O_0^x \tag{4}$$

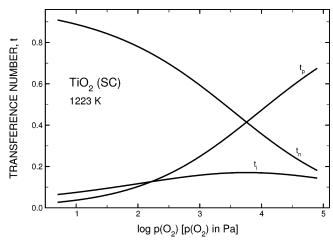
$$\operatorname{nil} \rightleftharpoons e' + h^{\bullet} \tag{5}$$

The relationships between the defect concentrations and the  $p(O_2)$  have been derived previously.<sup>16</sup>

Equilibrium constants of the above equilibria were used for derivation of defect concentration diagrams as a function of the p(O<sub>2</sub>), which indicate that oxygen vacancies, formed according to eq 1, are the majority defects over a wide range of p(O<sub>2</sub>) except under extremely reduced conditions, where the concentration of trivalent titanium interstitials, formed according to eq 2, become the predominant defects.<sup>3,21</sup> It was also shown that the concentration of trivalent Ti interstitials is larger than that of tetravalent Ti interstitials within a wide range of oxygen activities. Moreover, it was shown that Ti vacancies are relatively immobile, and therefore, in the experimental conditions commonly applied in studies of equilibration kinetics, their concentration remains practically constant. Therefore, in the present work, the considerations of the mass transport kinetics during gas—solid equilibration are limited to oxygen vacancies.

Equation 5 represents intrinsic ionization over the band gap. The equilibrium constant of this process was determined elsewhere.<sup>22</sup>

**2.2. Electrical Conductivity.** Properties such as electrical conductivity may be used to verify the defect disorder models for semiconducting oxides<sup>3</sup>. The physical meaning of the electrical conductivity of TiO<sub>2</sub> at elevated temperatures is complex because ions may have an effect on the conductivity.<sup>20</sup> Previous work by the authors<sup>16</sup> indicates that the transference number of ions (subscript *i*) in the n-p transition range reaches a substantial value that cannot be ignored. As seen in Figure 1, the ionic transference number for undoped TiO<sub>2</sub> at 1223 K may reach 20%. Consequently, the electrical conductivity of TiO<sub>2</sub>



**Figure 1.** Transference numbers of electronic  $(t_n, t_p)$  and ionic  $(t_i)$  charge carriers in undoped single-crystal TiO<sub>2</sub> at 1223 K.<sup>16</sup>

at elevated temperatures should be considered to include three components, related to electrons, holes, and ions:

$$\sigma = e(n\mu_{\rm n} + p\mu_{\rm p}) + z[i]\mu_{\rm i} = \sigma_{\rm n} + \sigma_{\rm p} + \sigma_{\rm i}$$
 (6)

where  $\sigma$  is the electrical conductivity, e is the elementary charge, n and p denote the concentrations of quasi-free electrons and electron holes, respectively,  $\mu$  is the mobility of the charge carrier; and the subscripts n and p refer to electrons and electron holes, respectively, z is the valence of the ionic defect, [i] is the concentration of ions, and the subscript i refers to ions.

2.3. Gas-Solid Kinetics. Defect disorder and the related properties in equilibrium for a oxygen-metal oxide system and the related nonstoichiometry are determined by the  $p(O_2)$  in the gas phase and the temperature. Thus, upon equilibration, the concentration of defects is determined by the conditions of equilibrium. When either the p(O<sub>2</sub>) or the temperature is changed over an initially equilibrated oxide crystal (within the stability range of a single-phase), the crystal drives toward a new equilibrium state and related nonstoichiometry. The new concentration of defects is imposed at the surface almost immediately and then is propagated into the bulk phase over time, attaining new chemical potentials throughout the crystal. The rate of propagation is determined by chemical diffusion.<sup>4–7</sup> Knowledge of the chemical diffusion rate is essential for the empirical imposition of a uniform concentration of defects within the crystal, free of concentration gradients. Only then is the crystal well-defined and the related properties can be considered to be materials data. Conversely, when the properties are determined under the influence of concentration gradients, then the data are not well-defined and reflect a combination of materials properties and experimental conditions.

The equilibration kinetics is described by the degree of equilibration  $\gamma$ :<sup>23</sup>

$$\gamma = 1 - \prod_{m=1}^{m=3} \left\{ \sum_{n=\infty}^{n=\infty} \frac{2L_m^2 \left[ \frac{-\beta_n^2 D_{\text{chem}} t}{l_m^2} \right]}{\beta_n^2 (\beta_n + L_m^2 + L_m)} \right\}$$
(7)

where the subscript m refers to the three orthogonal directions of the specimen, L is defined in eq 8,  $\beta$  is the positive root of the equation  $L = \beta \tan \beta$ , t is the time, l is the half-thickness of the specimen's dimensions, and:

$$L = \frac{l_m k}{D_{\text{charp}}} \tag{8}$$

where k is the rate constant of a nondiffusional surface reaction. In the case where the surface reaction is much faster than bulk diffusion, the equilibration is rate-controlled by bulk diffusion which allows the determination of the  $D_{\rm chem}$  from the equilibration kinetics data, as given by Newman:<sup>24</sup>

$$\gamma = 1 - \left(\frac{8}{\pi^2}\right)^3 \left(\sum_{l=0}^{\infty} \frac{1}{(2l+1)^2} \exp\left[\frac{-D_{\text{chem}} (2l+1)^2 \pi^2 t}{a^2}\right]\right)$$

$$\sum_{l=0}^{\infty} \frac{1}{(2l+1)^2} \exp\left[\frac{-D_{\text{chem}} (2l+1)^2 \pi^2 t}{b^2}\right] \qquad (9)$$

$$\sum_{l=0}^{\infty} \frac{1}{(2l+1)^2} \exp\left[\frac{-D_{\text{chem}} (2l+1)^2 \pi^2 t}{c^2}\right]$$

where a, b, and c are the specimen's dimensions. When oxygen vacancies are the majority defect, which is the case under the present experimental conditions,<sup>17</sup> then  $\gamma$  is defined as:

$$\gamma = \frac{[V_0^{\bullet}]_t - [V_0^{\bullet}]_0}{[V_0^{\bullet}]_{\infty} - [V_0^{\bullet}]_0} \tag{10}$$

where the subscripts t, o, and  $\infty$  denote the time, the initial stage of equilibration, and the final stage of equilibration, respectively.

Under conditions of prolonged oxidation of  $TiO_2$ ,  $\gamma$  assumes a form that is more complex than that expressed by eq 10 because the defect disorder involves an increase in the concentration of titanium vacancies.<sup>17</sup> Therefore, the effects of titanium vacancies on the gas—solid kinetics will be considered subsequently.<sup>25</sup> However, because the present work on the equilibration kinetics does not involve prolonged oxidation, these data are considered in terms of oxygen vacancies.

Assuming that the electrical conductivity is proportional to the concentrations of defects, as described in relation to eq 6, the degree of equilibration may be represented by the following relation:

$$\gamma = \frac{\Delta \sigma_t}{\Delta \sigma_{-}} \tag{11}$$

where  $\Delta\sigma_t$  and  $\Delta\sigma_\infty$  denote the electrical conductivity change at time t (counted from the moment when the new gas front reaches the surface of the specimen) and at the time at which the new equilibrium state is attained, respectively.

Using Wagner's theory of the oxidation of metals<sup>26,27</sup> and the associated expressions that derive the total ionic particle flux in a growing oxide scale of formula  $M_aO_b$ , the following equation may be derived:<sup>28</sup>

$$D_{\text{chem}} = -\frac{k_{\text{B}} T \sigma_{\text{i}} t_{\text{el}}}{16e^2} F^{-1}$$
 (12)

where  $k_{\rm B}$  is Boltzman's constant, T is the absolute temperature,  $\sigma_{\rm i}$  is the conductivity component due to ions,  $t_{\rm el}$  is the transference number of electronic charge carriers

TABLE 1: Anisotropy for Atomic Diffusion of Cations and Oxygen in TiO<sub>2</sub> According to literature reports<sup>30–35</sup>

authors	ions	temperature [K]	$m{D}_{ m llc}\!/D_{\perp m c}$
Johnson, 1964 <sup>30</sup>	Li <sup>+</sup>	773	108
Johnson, 1975 <sup>31</sup>	$H^+$	773	150
Wittke, 1966 <sup>32</sup>	$Fe^{3+}$	Not Stated	$D_{llc} > D_{\perp c}$
Sassaki & Peterson, 1984 <sup>33</sup>	$Co^{2+}$	1073	$10^{3}$
Haul & Dumbgen, 1965 <sup>34</sup>	$O^{2-}$	983-1573	$D_{llc} < D_{\perp c}$
Gruenwald & Gordon, 1971 <sup>35</sup>	$O^{2-}$	1079	0.188

 $[t_{\rm el} = (\sigma_{\rm n} + \sigma_{\rm p})/\sigma]$ , and F is:

$$F = \frac{\partial [V_0^{\bullet}]}{\partial \ln p(O_2)} = -\frac{1}{8}(n+p) \tag{13}$$

The factor F describes the relation between  $p(O_2)$  and the change in concentration of the majority defect taking part in the equilibration process. Therefore, the expression for  $D_{\rm chem}$ , represented by eq 12, may be rewritten in a form that includes the concentrations of electronic charge carriers:<sup>28</sup>

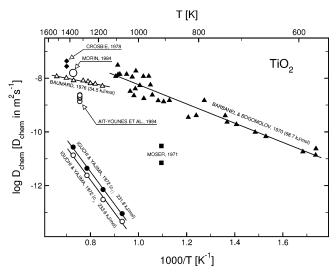
$$D_{\text{chem}} = \frac{k_{\text{B}} T \sigma_{\text{i}} t_{\text{el}}}{2e^2} \frac{1}{n+p}$$
 (14)

Equation 14 is especially useful in assessing chemical diffusion data within the n-p transition for amphoteric semiconductors, such as TiO<sub>2</sub>.

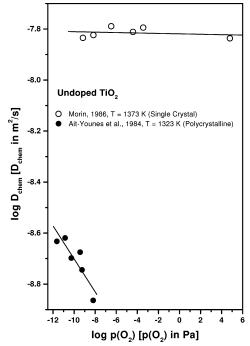
#### 3. Brief Overview of Literature

The crystal structure of rutile, which is the stable high-temperature allotrope of  $\text{TiO}_2$ , exhibits open channels parallel to the c axis, which is a manifestation of the anisotropy of tetragonal  $\text{TiO}_2{}^3$ . The transport of small cations along these channels is faster than that in the direction perpendicular to the c axis. $^{29-33}$  However, oxygen diffusion is faster in the direction perpendicular to the c axis. $^{34,35}$  Reported *atomic* diffusion data for cations and oxygen are shown in Table 1. However, the data of Iguchi and Yajima $^{10}$  indicate that there is little anisotropy in the transport under chemical potential gradient.

The available data for the  $D_{\text{chem}}$  of TiO<sub>2</sub>, most of which were determined using single crystals, are shown in Figure 2.<sup>8–14</sup> Also, most of these data were determined from the equilibration kinetics monitored using electrical conductivity measurements.



**Figure 2.** Arrhenius plot of the chemical diffusion coefficient ( $D_{\text{chem}}$ ) for undoped single-crystal and polycrystalline  $\text{TiO}_2$  reported in the literature.<sup>8–14</sup>



**Figure 3.** Effect of oxygen activity,  $p(O_2)$  on the chemical diffusion coefficient ( $D_{chem}$ ) for undoped single-crystal and polycrystalline TiO<sub>2</sub> at 1323 K according to Ait-Younes et al.<sup>13</sup> and Morin.<sup>14</sup>

These and other publications generally assume that gas—solid equilibrium is attained when the electrical conductivity reaches a constant value over some length of time, typically  $1-2\,h$ . However, this assumption does not take into account the potential for the slope to be only approximately zero and that it might continue to change over an extended time frame. Recent work by the authors on prolonged oxidation of  ${\rm TiO_2}^{17}$  demonstrates that the actual slope of the conductivity—time curve becomes measurable only after several hundred hours at elevated temperatures.

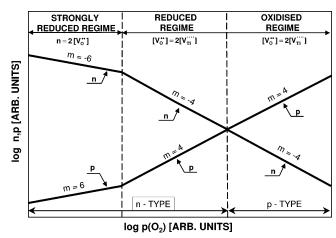
As seen in Figure 2, there are substantial discrepancies between the data of the chemical diffusion coefficient reported so far. The reasons for the discrepancy, concerning both absolute values and their temperature dependence, was outlined in the Introduction.

Barbanel and Bogomolov<sup>8</sup> determined  $D_{\rm chem}$  data using single-crystal TiO<sub>2</sub> previously outgassed in a vacuum at 973 K. The assessment of their data is problematic because they did not provide details concerning the experimental procedure for the determination of the equilibration kinetics. Especially, their kinetics at 580 K seems to be unrealistic.

The experimental details of the diffusion data of Moser,<sup>9</sup> which were reported by Childs and Wagner,<sup>4</sup> are not available. Therefore, physical meaning of these data is not clear.

Iguchi and Yajima<sup>10</sup> reported  $D_{\rm chem}$  data in the range 1073—1373 K. They determined the  $D_{\rm chem}$  for the two main crystal orientations. Figure 2 shows that the  $D_{\rm chem}$  is slightly larger in the direction parallel to the c axis. It was argued that these diffusion data were determined by the transport of oxygen vacancies because (i) they did not observe substantial anisotropy, which would be expected for the transport of cations, and (ii) the activation energies are similar to that determined for oxygen tracer diffusion reported by Haul and Dumbgen.<sup>34</sup>

The study of Baumard<sup>11</sup> reported the equilibration kinetics for single-crystal  $TiO_2$  in the temperature range 1180-1520 K. This study was the first approach to determine the  $D_{\rm chem}$  through in situ monitoring of the equilibration kinetics. Baumard claimed that the  $D_{\rm chem}$  is independent of the  $p(O_2)$ .



**Figure 4.** Defect disorder model for undoped  $TiO_2$  showing the effect of  $p(O_2)$  on the concentration of electronic charge carriers within ranges of  $p(O_2)$  governed by simplified charge neutralities.

Crosbie<sup>12</sup> reported the  $D_{\rm chem}$  for polycrystalline TiO<sub>2</sub> with and without dispersed submicron SiO<sub>2</sub> as a function of annealing time. Because no details of the experimental procedure for the determination of the equilibration kinetics were provided, the physical meaning of the reported diffusion data cannot be assessed.

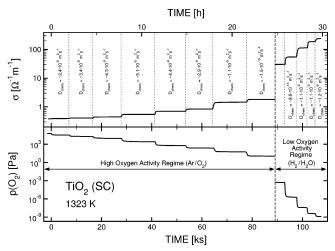
Ait-Younes et al.  $^{13}$  determined the  $D_{\rm chem}$  at 1323 K from the equilibration kinetics determined using the electromotive force of a cell with polycrystalline TiO<sub>2</sub> as an oxygen-sensitive electrode. They reported that the  $D_{\rm chem}$  changed as a function of the p(O<sub>2</sub>) over the range  $10^{-12}$  to  $10^{-8}$  Pa. Their data are shown in Figure 3, along with those of Morin,  $^{14}$  who reported that the  $D_{\rm chem}$  at the same temperature for single-crystal TiO<sub>2</sub> is effectively independent of the oxygen nonstoichiometry over a large p(O<sub>2</sub>) range of  $10^{-8}$  to  $10^{5}$  Pa. Assessment of the kinetic data of Morin  $^{14}$  is not possible because he did not report details of the experimental procedure. It is possible, however, to conclude that the experimental procedures applied by Morin  $^{14}$  are not well-defined.

The overview of the literature indicates that there is a need to verify the available data for the equilibration kinetics for the O<sub>2</sub>—TiO<sub>2</sub> system. The purpose of the present work, and the subsequent work in this series,<sup>25</sup> is to address this need by providing well-defined data for the equilibration kinetics of single-crystal TiO<sub>2</sub>. Preliminary kinetics data by the authors indicate that chemical diffusion in TiO<sub>2</sub> is very complex.<sup>36</sup> It also has been shown that the equilibration kinetics of TiO<sub>2</sub> exhibit two kinetics regimes:<sup>17</sup> (i) kinetics regime I (fast kinetics), where the kinetics are determined by the transport of rapid defects; oxygen vacancies; (ii) kinetics regime II (slow kinetics), where the kinetics are determined by the transport of slow defects, i.e., titanium vacancies

The present work aims at the determination of the equilibration kinetics for single-crystal  ${\rm TiO_2}$  in kinetics regime I and assesses the data of the  $D_{\rm chem}$  in terms of the defect disorder, which was derived based on the measurements of both electrical conductivity<sup>16</sup> and thermoelectric power.<sup>37</sup> This defect disorder is shown in Figure 4 in terms of the effect of oxygen activity,  ${\rm p(O_2)}$ , on the concentration of electronic defects within the  ${\rm p(O_2)}$  regimes, which correspond to the experimental conditions applied in the present work.

# 4. Experimental Procedure

Details of the specimen (high-purity single-crystal TiO<sub>2</sub>), including its impurity analysis, are reported elsewhere. <sup>16</sup> The



**Figure 5.** The monitoring sheet for undoped single-crystal  $\text{TiO}_2$  at 1323 K showing the changes of oxygen activity during subsequent reduction experiments (lower part) and the related changes of the electrical conductivity within individual experimental cycles at high and low  $p(O_2)$ .

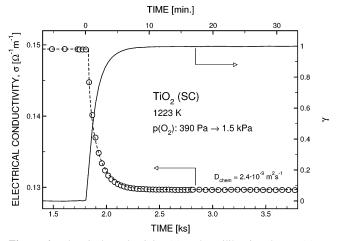
size of the specimen was 2 mm  $\times$  3 mm  $\times$  10 mm; the 3 mm  $\times$  10 mm surface was perpendicular to the c axis.

The facility for the determination of the electrical conductivity, using the dc four-probe technique, and the experimental monitoring sheet recording the oxygen activity, temperature, and the electrical conductivity, are described in detail elsewhere.<sup>38</sup> The equilibration kinetics were determined in two broad p(O<sub>2</sub>) regimes: (i) Low Oxygen Activity Range. The required p(O<sub>2</sub>) in this range was imposed by an H<sub>2</sub>-H<sub>2</sub>O mixtures flowing through the reaction chamber at a constant flow rate of 100 mL/min (set by mass flow controllers). The mixtures were achieved by passing of a mixture of 1%H<sub>2</sub>-99% Ar diluted with pure Ar through deionized water contained in a Drechsel bottle in an ice bath. The p(O2) levels were imposed in the range  $\sim 10^{-13}$  to  $10^{-5}$  Pa within very narrow p(O<sub>2</sub>) ranges. (ii) High Oxygen Activity Range. The oxygen activity in this range was imposed by Ar/O<sub>2</sub> mixtures at a constant flow rate of 100 mL/ min (set by mass flow controllers) in the range 10 Pa to 75 kPa.

The  $p(O_2)$  levels were determined with a zirconia electrochemical oxygen probe. When the  $p(O_2)$  was increased or decreased, the experiments are termed *oxidation* and *reduction*, respectively. The equilibration kinetics were determined for both oxidation and reduction runs at six temperatures: 1073, 1198, 1223, 1248, 1273, and 1323 K. The temperatures monitored during the entire equilibration experiment were reproducible to  $\pm 0.5$  K.

The electrical properties as a function of  $p(O_2)$  were assessed using in situ measurements of electrical conductivity and thermoelectic power (S). <sup>16,38</sup> These measurements also were used to monitor the equilibration kinetics.

Figure 5 shows a monitoring sheet including the changes of the  $p(O_2)$  and electrical conductivity as a function of time within individual cycles of the equilibration during reduction experiments at 1323 K. As seen, the successively reduced  $p(O_2)$  in the gas mixture leads to the imposition of appropriately reduced oxygen activity in the reaction chamber in which the specimen is located. The upper part of Figure 5 shows fragments of the related electrical conductivity changes at 1323 K. As seen, the electrical conductivity exhibits changes within 0.5 h. The electrical conductivity was monitored for  $\sim 20$  h in order to ensure the achievement of equilibrium. In all cases, the electrical conductivity after 2 h reached (within 0.1%) the final electrical



**Figure 6.** Electrical conductivity ( $\sigma$ ) and equilibration degree ( $\gamma$ ) as a function of time during oxidation of undoped single-crystal TiO<sub>2</sub> at 1223 K.

conductivity after 20 h. <sup>16,17</sup> Details of the experimental procedure are reported elsewhere. <sup>16</sup>

The condition of the gas—solid equilibrium, corresponding to stable electrical conductivity within 20 h, is referred to as *operational equilibrium*, at which the concentration of oxygen vacancies and also Ti interstials that exhibit comparable diffusion rate, reaches homogeneity. The *operational equilibrium* should be distinguished from the *effective equilibrium*, at which the concentration of Ti vacancies assumes homogeneous distribution. The later term will be discussed elsewhere.<sup>25</sup>

## 5. Results

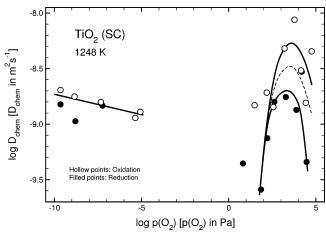
The chemical diffusion coefficient was determined using a computer program that allows minimization of the following error function:

$$E_{\rm f} = \sum \left( \sigma_{\rm exp} - \sigma_{\rm theor} \right)^2 \tag{15}$$

where  $E_{\rm f}$  is the error function,  $\sigma_{\rm exp}$  and  $\sigma_{\rm theor}$  denote the experimental data of the electrical conductivity during oxidation-reduction, and  $\sigma_{ ext{theor}}$  is the theoretical value derived either by the diffusion eqs 7 or 9. In the first attempt, the program adjusted the parameters of eq 7, involving  $D_{\text{chem}}$ , the rate constant, k, and the final conductivity value,  $\sigma_{\infty}$ , in eq 11, to achieve minimum of function  $E_{\rm f}$ . This procedure indicated that the rate constant k is  $\sim$ 20 orders of magnitude larger than that of D<sub>chem</sub>. Therefore, it is concluded that the gas-solid kinetics are determined by bulk diffusion and not surface reaction. Consequently, the  $D_{\text{chem}}$  was determined assuming that bulk diffusion is the rate controlling the gas-solid equilibration. Then eq 9 was applied. In this attempt, the program iteratively adjusted the parameters of eq 9, involving  $D_{\text{chem}}$  and the final conductivity value,  $\sigma_{\infty}$ , to achieve minimum of the error function  $E_{\rm f}$ . The stopping criterion was  $E_{\rm f} < 10^{-5}$ .

The electrical conductivity data taken for calculations were determined as the average of two conductivity values (current directions of opposite polarity). Figure 6 shows isothermal changes in the electrical conductivity ( $\sigma$ ) and the degree of equilibration ( $\gamma$ ) during oxidation at 1223 K. As seen, there is an excellent agreement between the kinetics data of  $\sigma(t)$  and the kinetic eq 9. The data in Figure 6 are representative for the equilibration kinetic data in the entire range 1073–1323 K.

Figures 7 and 8 show the typical scatter of the data for both reduction and oxidation experiments at high and low  $p(O_2)$  ranges at 1248 and 1273 K, respectively. Despite the relatively



**Figure 7.** Chemical diffusion coefficient ( $D_{chem}$ ) for undoped singlecrystal TiO<sub>2</sub> at 1248 K as a function of oxygen activity, p(O<sub>2</sub>), during oxidation and reduction runs; solid lines in the low p(O2) range represent the best fit for oxidation and reduction combined; solid lines in the high p(O<sub>2</sub>) regime represent the best fit for oxidation and reduction separately; dashed line represents combined values.

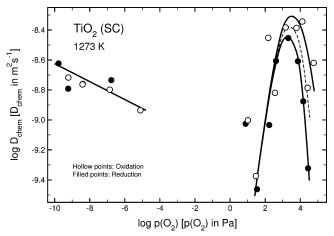


Figure 8. Chemical diffusion coefficient ( $D_{\text{chem}}$ ) for undoped singlecrystal  $TiO_2$  as a function of oxygen activity,  $p(O_2)$ , during oxidation and reduction runs at 1273 K; solid lines in the low p(O2) range represent the best fit for oxidation and reduction combined; solid lines in the high p(O<sub>2</sub>) regime represent the best fit for oxidation and reduction separately; dashed line represents combined values.

large scatter, the reproducibility of the data for successive runs was very good. The scatter of data observed in Figures 7 and 8 is representative for the scatter observed at other temperatures (see Appendix). These data indicate the following: (i) Low  $p(O_2)$  Range. The effect of the  $p(O_2)$  on the  $D_{chem}$  is approximated by a linear dependence for both oxidation and reduction experiments, indicating a weak dependence of the  $D_{\text{chem}}$  on the p(O<sub>2</sub>). The experimental data of the effect of p(O<sub>2</sub>) on the  $D_{\text{chem}}$  for other temperatures (1073, 1198, 1223, and 1323) K) can be seen in the Appendix. (ii) High p(O<sub>2</sub>) Range. Despite the substantial scatter of data showing the effect of  $p(O_2)$  on  $D_{\text{chem}}$ , these data allow observation of several behaviors that are apparent at all temperatures: (a) The oxidation kinetics is faster than those for reduction. This can be explained by the segregation-induced diffusion resistance within the electric field of the surface layer.<sup>39</sup> This effect is not apparent at low  $p(O_2)$ . (b) The effect of the p(O<sub>2</sub>) in this range is significant, showing that the  $D_{\text{chem}}$  increases in the p(O<sub>2</sub>) in which n-type conductivity has been identified, <sup>16</sup> assumes a maximum at the n-p transition point, and then sharply decreases. (3) The n-p transition, which

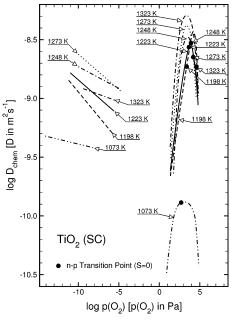


Figure 9. Chemical diffusion coefficient  $(D_{chem})$  as a function of oxygen activity, p(O2), for undoped single-crystal TiO2 in the temperature range 1073-1323 K; data points correspond to the n-p transitions determined from the thermoelectric power (S).

was confirmed using measurements of both electrical conductivity and thermoelectric power, coincides with the maximum in the  $D_{\text{chem}}$ .

The hollow points, representing the data for oxidation, and the filled points, corresponding to reduction, may be approximated by continuous lines, as shown in Figures 7 and 8. In the first approximation, the observed behavior represented by this lines is consistent with the model represented by eq 14. The dashed line, in between these two solid lines, may be used as a general representation of the effect of  $p(O_2)$  on the  $D_{chem}$ for both oxidation and reduction. This dashed line will then be used for the collective representation of the effect of  $p(O_2)$  on the  $D_{\text{chem}}$  in Figure 9.

Figure 9 shows the effect of the  $p(O_2)$  on the  $D_{chem}$  over the entire temperature and p(O<sub>2</sub>) ranges studied in the present work. For the reason of clarity, Figure 9 includes only the averages  $D_{\text{chem}}$  for the oxidation and reduction runs and represented by the dashed line in Figures 7 and 8.

The data in Figure 9 indicate the following behavior: (i) The character of the  $D_{\text{chem}}$  versus  $p(O_2)$  dependencies is similar at all temperatures, with the notable exception of the dependence at 1073 K. (ii) The data can be divided into three regimes: (a) strongly reduced (n-type)  $10^{-10} < p(O_2) < 10^{-5} Pa$ ; (b) reduced (n-type) lower p(O<sub>2</sub>) side of the apexes at  $\sim 10^3 - 10^4$  Pa; (c) Oxidized (p-type) higher p(O<sub>2</sub>) side of the apexes at  $\sim 10^3$  $10^4$  Pa. The data relevant to the effect of the p(O<sub>2</sub>) on the diffusion, including the activation energies, are listed in Table 2. (iii) The n-p transitions determined from the thermoelectric power data<sup>37</sup> are shown as data points. The  $D_{\text{chem}}$  values appear to reach maxima at the n-p transition points, supporting the consistency of the  $D_{\text{chem}}$  data with the model described by eq 14. Thus, this indicates that the minima in the concentrations of the electronic charge carriers at the n-p transition points are responsible for the maxima in the  $D_{\rm chem}$  values at these points. (iii) The capacity to locate accurately the locations of the apexes is limited owing to the scatter of the data and the steepness of the curves. These are likely to be the causes of the discrepancy between the locations of the apexes and the determined n-p transition points. (iv) The effect of the  $p(O_2)$ 

TABLE 2: Chemical Diffusion Coefficient as a Function of Temperature for TiO2-SC within Different Defect Disorder Regimes

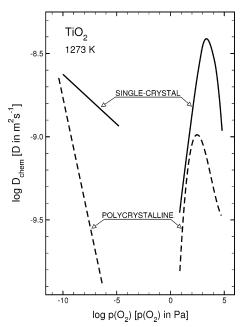
regime	oxygen	chemical diffusion coefficient
	activity [Pa]	$D_{ m chem}$ [m $^2$ s $^{-1}$ ]
strongly reduced	$p(O_2) < 10^{-5}$	$D_{\text{chem}} = 6.21 \times 10^{-6} \exp(-87 \text{ [kJ/mol]}/RT)$
reduced	$10 < p(O_2) < p(O_2)_{n=p}$	$D_{\text{chem}} = 2.04 \times 10^{-3} \exp(-87  [\text{kJ/mol}]/RT)$
		$D_{\text{chem}} = 6.42 \times 10^{-5} \exp(-126 [\text{kJ/mol}]/RT)$
oxidized	$p(O_2) > p(O_2)_{n=p}$	$D_{\text{chem}} = 2.22 \times 10^{-6} \exp(-66 \text{ [kJ/mol]}/RT)$

on the  $D_{\text{chem}}$  may be described according to the following generic expression:

$$D_{\text{chem}} = (D_{\text{chem}})_0 \, \text{p(O}_2)^{1/n} \tag{16}$$

where  $(D_{\text{chem}})_0$  is the  $D_{\text{chem}}$  under standard conditions and 1/nis the slope of the dependence of the log  $D_{\text{chem}}$  versus log p(O<sub>2</sub>) plot. The  $p(O_2)$  exponent (1/n) in the strongly reduced regime is relatively low and varies between -1/15 and -1/40. These values indicate that the  $p(O_2)$  has a very weak effect on the  $D_{\rm chem}$  in this range. Conversely, in the reduced and oxidized regimes, the absolute values of the p(O<sub>2</sub>) exponents are much greater (1/n = 1/2), indicating a significant effect of the p(O<sub>2</sub>) on the  $D_{\text{chem}}$ . These dependencies may be considered in terms of the relevant variables in eq 14, which are electrical conductivity, electronic transference number, and concentrations of electronic charge carriers. (v) The change in the  $D_{\text{chem}}$  at different temperatures is approximately a half order of magnitude over a wide range of  $p(O_2)$  in the strongly reduced regime, while it is over an order of magnitude over narrow ranges of p(O<sub>2</sub>) in the reduced and oxidized regimes. (vi) The effect of temperature on the  $D_{\text{chem}}$  in the strongly reduced regime is consistent, where increasing the temperature increases the  $D_{\text{chem}}$ . The exception is the data for the highest temperature of 1323 K, which are out of sequence. This effect suggests that the mechanism of chemical diffusion of strongly reduced TiO<sub>2</sub> in this case differs from that of the other temperatures, which may be a result of a change in transport mechanism at temperatures >1273 K.

Figure 10 shows the diffusion data for both single-crystal (reported in this work) and polycrystalline  $TiO_2$  at 1273 K.<sup>40</sup> It can be seen that the  $D_{\rm chem}$  values for polycrystalline  $TiO_2$  are



**Figure 10.** Chemical diffusion coefficient ( $D_{\text{chem}}$ ) for undoped single-crystal and polycrystalline<sup>40</sup> TiO<sub>2</sub> as a function of oxygen activity, p(O<sub>2</sub>) at 1273 K.

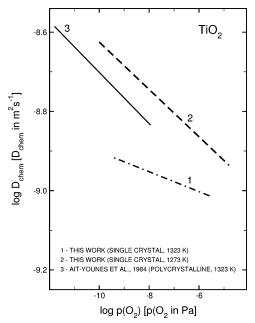
smaller than those of single-crystal  $\text{TiO}_2$ . This difference is likely to be due to grain boundaries acting as weak links for the mass transport during the equilibration. The diffusion in this case is influenced by the grain boundaries, which appear to have a retarding effect on the chemical diffusional transport across grain boundaries

An error analysis was performed for the data of the chemical diffusion coefficient determined within several independent experiments but for the same specimen studied in identical conditions. For example, at the temperature 1323 K, oxygen activity range, 1.6-6.2 kPa, type of experiment, and oxidation, the analysis resulted in  $D_{\rm chem} = (5.4 \pm 0.4) \ 10^{-9} \ {\rm m}^2 \ {\rm s}^{-1}$  (with the confidence interval 95%).

#### 6. Discussion

6.1. Effect of Oxygen Activity. Figure 9 makes it clear that the effect of the  $p(O_2)$  on the  $D_{chem}$  is complex. The following general points can be made: (i) The observed character of the  $D_{\text{chem}}$  versus p(O<sub>2</sub>) dependence is unprecedented and is entirely different from those reported for other widely studied semiconducting transition metal oxides such as NiO,41 CoO,42,43 and FeO.<sup>43</sup> In all of these cases, however, the  $D_{\rm chem}$  data were determined within a regime governed by a single type of charge carrier. Therefore, the main reasons for the observed complex dependence of  $D_{\text{chem}}$  versus  $p(O_2)$  include: large values of nonstoichiometry and the related substantial interactions between defects, and change of the type of the predominant electronic charge carriers within the n-p transition. (ii) The observed nonmonotonic changes in the  $D_{\text{chem}}$  as a function of the p(O<sub>2</sub>) indicate that chemical transport under the influence of a chemical potential gradient exhibits a change in mechanism, which is strongly dependent on the defect disorder, related charge compensation, and concentrations of the predominant charge

The comments concerning the effects illustrated in Figure 9 prompt the following considerations: (i) TiO<sub>2</sub> is a highly nonstoichiometric compound with several types of ionic defects: oxygen vacancies, titanium interstitials, and titanium vacancies. While the present work does not consider the transport of titanium vacancies because they are immobile under the present experimental conditions, these defects must be considered when evaluating charge neutrality. Also, because titanium interstitials are the minority defects, then they also are ignored. Thus, the diffusion data during equilibration are considered solely in terms of the transport of oxygen vacancies. (ii) An interesting feature in the high p(O<sub>2</sub>) range studied is the maxima in the  $D_{\text{chem}}$  data. The consistency between these maxima and the n-p transition points determined from thermoelectric power measurements indicates that the model described by eq 14 may be applied to explain this effect. (iii) As seen, there is a weak dependence of the  $D_{\text{chem}}$  on the p(O<sub>2</sub>) in a low oxygen activity (strongly reduced) regime. This effect may be interpreted in terms of two factors: (a) The model described by eq 14 indicates that the electrical conductivity, electronic transference number, and concentrations of electronic charge carriers concurrently govern the effect of the p(O<sub>2</sub>) on the  $D_{\text{chem}}$ . (b) Oxygen vacancies in strongly reduced TiO<sub>2</sub> are



**Figure 11.** Chemical diffusion coefficient ( $D_{\text{chem}}$ ) as a function of oxygen activity,  $p(O_2)$ , for undoped single-crystal TiO<sub>2</sub> at 1273 K and 1323 K compared to the data for undoped polycrystalline TiO<sub>2</sub> at 1323 K of Ait-Younes et al.<sup>13</sup>

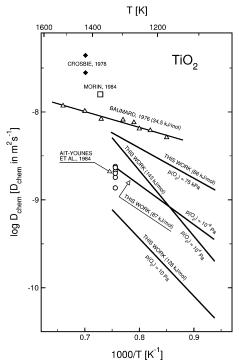
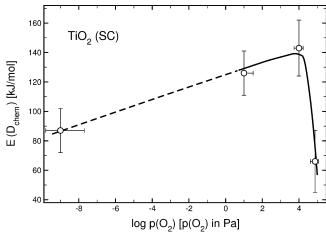


Figure 12. Arrhenius plot of the chemical diffusion coefficient ( $D_{\text{chem}}$ ) for undoped single-crystal TiO<sub>2</sub> along the literature data.

known to form planar defects in the form of shear structures.<sup>3,44</sup> They also are known to interact and form clusters.<sup>45</sup> Consequently, the idealized picture of point defects must be broadened to include larger two- and three-dimensional defect assemblies, which also may have an effect on the dependence of the  $D_{\text{chem}}$  on the p(O<sub>2</sub>).

It is interesting to compare the diffusion data determined in the present work to those elsewhere under comparable experimental conditions. The  $D_{\text{chem}}$  versus p(O<sub>2</sub>) data at 1273 and 1323 K determined in the present work and those reported by Ait-Younes et al. <sup>13</sup> are shown in Figure 11. It can be seen that there



**Figure 13.** Activation energy of chemical diffusion,  $E(D_{\text{chem}})$ , for undoped single-crystal TiO<sub>2</sub> as a function of oxygen activity, p(O<sub>2</sub>), in the temperature range 1073–1323 K.

is clear consistency between the two reports in terms of the effect of  $p(O_2)$  on  $D_{chem}$  and the proximity of their absolute values.

**6.2. Effect of Temperature.** Because the  $D_{\rm chem}$  varies substantially with the p(O<sub>2</sub>), the effect of the temperature on the  $D_{\rm chem}$  should be considered within relatively narrow p(O<sub>2</sub>) ranges. Figure 12 shows Arrhenius plots of  $D_{\rm chem}$  in several ranges of p(O<sub>2</sub>), along with those reported by Baumard<sup>11</sup> measured over a wide range of p(O<sub>2</sub>) and individual data points reported by Crosbie, <sup>12</sup> Ait-Younes et al., <sup>13</sup> and Morin. <sup>14</sup> As seen, the absolute values of our data at p(O<sub>2</sub>) = 75 kPa are slightly smaller than those of Baumard, <sup>11</sup> although our activation energy is twice as large. The consistency between our data and those of Ait-Younes et al. <sup>13</sup> is very good (see Figure 11).

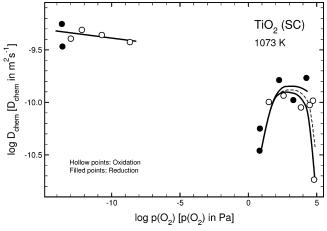
The expressions for the determined  $D_{\rm chem}$  as a function of temperature are shown in Table 2 within the specific defect disorder models. The effect of the p(O<sub>2</sub>) on the activation energies of the  $D_{\rm chem}$ ,  $E(D_{\rm chem})$ , which are shown in Figure 13, confirms that the transport mechanism varies substantially with nonstoichiometry. As seen, the activation energies of the  $D_{\rm chem}$  in the reduced regime reach the highest values of  $126-143~{\rm kJ/mol}$ .

## 7. Conclusions

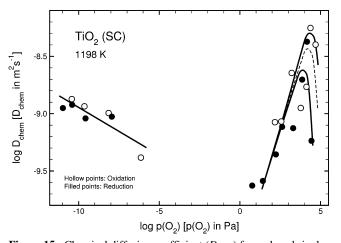
The chemical diffusion coefficient of  $TiO_2$  is related closely to the defect disorder. Therefore,  $D_{\rm chem}$  should not be considered as a single materials-related datum over the entire range of nonstoichiometry, which is the case for other semiconducting oxides such as NiO.<sup>41</sup>

It has been shown that the gas—solid equilibration kinetic for the  $O_2$ — $TiO_2$  system as well as the  $D_{chem}$  exhibit a complex dependence on the  $p(O_2)$ . Therefore, well-defined data for the  $D_{chem}$  of  $TiO_2$  must be determined within narrow ranges of  $p(O_2)$  and be considered in terms of its specific nonstoichiometry, defect disorder, and the associated equilibrium  $p(O_2)$ .

The observed strong effect of the  $p(O_2)$  on the  $D_{chem}$  within the n-p transition range, involving both the reduction and oxidation regimes, may be explained in terms of minima in the concentrations of electronic charge carriers. In the strongly reduced regime, the effect of the  $p(O_2)$  on the  $D_{chem}$  for  $TiO_2$  involves the contribution of several concurrent influences, including electrical conductivity, electronic transference number, and concentrations of electronic charge carrier, leading to a weak dependence of  $D_{chem}$  on  $p(O_2)$ .



**Figure 14.** Chemical diffusion coefficient ( $D_{\text{chem}}$ ) for undoped single-crystal TiO<sub>2</sub> at 1073 K as a function of oxygen activity, p(O<sub>2</sub>), during oxidation and reduction runs; solid lines in the low p(O<sub>2</sub>) range represent the best fit for oxidation and reduction combined; solid lines in the high p(O<sub>2</sub>) regime represent the best fit for oxidation and reduction separately; dashed line represents combined values.



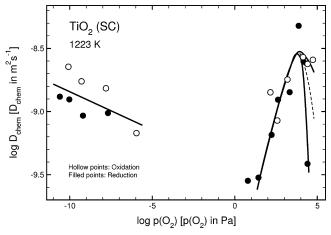
**Figure 15.** Chemical diffusion coefficient ( $D_{\rm chem}$ ) for undoped single-crystal TiO<sub>2</sub> at 1198 K as a function of oxygen activity, p(O<sub>2</sub>), during oxidation and reduction runs; solid lines in the low p(O<sub>2</sub>) range represent the best fit for oxidation and reduction combined; solid lines in the high p(O<sub>2</sub>) regime represent the best fit for oxidation and reduction separately; dashed line represents combined values.

The observed effect of  $p(O_2)$  on the  $D_{chem}$  is consistent with the determined different values of the activation energies for the  $D_{chem}$  in different  $p(O_2)$  regimes. These sets of data may be used for the selection of optimized processing conditions for  $TiO_2$  under controlled  $p(O_2)$ , including the  $p(O_2)$ , temperature, and time required to impose a homogeneous nonstoichiometry and the associated concentration of defects within the specimen.

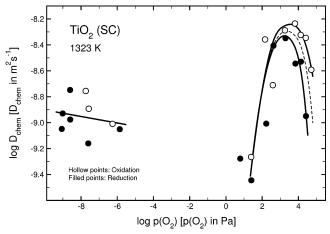
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### A. Appendix

The experimental data on the effect of  $p(O_2)$  on  $D_{chem}$  at 1073, 1198, 1223, and 1323 K are shown in Figures 14–17, respectively.



**Figure 16.** Chemical diffusion coefficient ( $D_{\text{chem}}$ ) for undoped single-crystal TiO<sub>2</sub> at 1223 K as a function of oxygen activity, p(O<sub>2</sub>), during oxidation and reduction runs; solid lines in the low p(O<sub>2</sub>) range represent the best fit for oxidation and reduction combined; solid lines in the high p(O<sub>2</sub>) regime represent the best fit for oxidation and reduction separately; dashed line represents combined values.



**Figure 17.** Chemical diffusion coefficient ( $D_{\text{chem}}$ ) for undoped single-crystal TiO<sub>2</sub> at 1323 K as a function of oxygen activity, p(O<sub>2</sub>), during oxidation and reduction runs; solid lines in the low p(O<sub>2</sub>) range represent the best fit for oxidation and reduction combined; solid lines in the high p(O<sub>2</sub>) regime represent the best fit for oxidation and reduction separately; dashed line represents combined values.

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