

### Paramagnetic Susceptibilities and Electronic Structures of Aqueous Cations of Elements 92 to 95

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### Paramagnetic Susceptibilities and Electronic Structures of Aqueous Cations of Elements 92 to 95

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Magnetic susceptibilities per gram atomic weight of elements 92 to 95 in most of their oxidation states were measured at 20°C on 0.1 ml of solution which was 0.005 to 0.09M in heavy element. The values obtained (all paramagnetic) in units ×10° were: U(IV), 3690; Np(VI), 2060; Np(V), 4120; Np(IV), 4000; Pu(IV), 1610; Pu(III), 370; Am(III), 720. The results could be interpreted only on the basis of electronic configurations  $5f^n$ , even though susceptibilities were generally lower than the theoretical values and lower than experimental values for corresponding lanthanide  $4f^n$  cations. The lower values should be expected as a result of the Stark effect produced by electric fields of anions and of water dipoles. Failure of the Russell-Saunders approximation to the coupling between electrons may account for some of the error in the theoretical calculations. That the susceptibilities of Pu(III) and Am(III) are manyfold lower than those of Sm(III) and Eu(III), respectively, is attributed to wider multiplet splitting in the actinide atoms.

HEMICAL and physical properties and theoretical calculations have indicated that elements of about Z=90 and higher constitute a series in which the 5f orbitals are filled as Z increases. These heavy elements have been called actinides in analogy to the name lanthanides for the rare earth elements.2 It was of interest to determine whether corresponding aqueous cations of actinide and lanthanide elements have the same outer electronic configurations even though the actinide concept might not require that they be identical.

If an atom has its electrons in question (i.e., those in addition to the inert gas structure) in inner orbitals, the electrons may be electrostatically shielded from neighboring atoms to the extent that the magnetic susceptibility of a solution of such atoms can be deduced from will yield a unique answer. The method was successful

quantum numbers of the ground state of the electronic configuration. Sometimes the converse, deduction of ground state quantum numbers from the susceptibility,

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for the lanthanide tripositive ions which have as outer configurations  $4f^{1-14}5s^25p^6$ .

Susceptibilities of U(IV) and U(III) solutions were reported by Lawrence.3 Solid uranium compounds have been studied by numerous investigators.4 At room temperature the susceptibility of U(IV) solutions and salts approximates the theoretical value derived from the spin magnetic moment of atoms with two unpaired electrons. Since this type of calculation was successful in accounting for the susceptibility of the first row transition element ions which have partially filled 3d electron orbitals, the observed susceptibility of U(IV) was usually interpreted as evidence for a  $5d^2$  electron configuration. This deduction was inconsistent with the fact that the observed susceptibilities of cations of heavier transition elements (those with partially filled 4d or 5d orbitals) are generally manyfold smaller than the "spin only" calculations, and later studies of general properties of U, Np, and Pu made 6d configurations improbable. Hutchison and Elliott<sup>5</sup> have interpreted their recent measurements of uranium(IV) susceptibilities on the basis of a  $5f^2$  structure.

Shortly after plutonium became available, the susceptibilities of dilute Pu(VI), Pu(V), Pu(IV), and

<sup>&</sup>lt;sup>2</sup> Some of the properties of the recently discovered heavy transition elements were reviewed and the name actinides was suggested by G. T. Seaborg, Chem. and Eng. News 23, 2190 (1945); Science 104, 379 (1946). W. H. Zachariasen, Phys. Rev. 73, 1104 (1948) used the name actinide for the +3 ions only, thorides for +4 ions, etc., in reporting his x-ray diffraction studies which showed that the solid compounds have the crystal structures and ionic radii consistent with assumption of 5f electronic configurations. We use Seaborg's nomenclature.

<sup>&</sup>lt;sup>3</sup> R. W. Lawrence, J. Am. Chem. Soc. 56, 776 (1934).

<sup>&</sup>lt;sup>4</sup> See reference 5 for keys to this literature. <sup>5</sup> C. A. Hutchison, Jr., and N. Elliott, J. Chem. Phys. 16, 920 (1948).

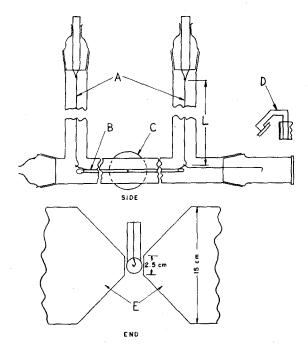


Fig. 1. Apparatus for measurement of magnetic susceptibility: A, glass fibers, 0.005×140 cm; B, glass capillary, 0.2×16 cm; C, magnet pole faces, 2.5 cm diam; D, mirror and microscope; E, magnet pole pieces, 15 cm diam.

Pu(III) solutions were measured with the expectation that they might closely parallel those of Pr(III) through Sm(III) if the actinide element ions also had  $f^n$  electronic configurations. The measurement of Pu(V)was very crude because of the instability of that state. For the other three plutonium oxidation states there was no close agreement with expectations of particular electronic structures. More actinide elements which exist in one or more oxidation states could be used in the present study.

### **EXPERIMENTAL**

Magnetic susceptibility measurements were made on 0.1 ml samples which were of the order of 0.01M in heavy element by use of a bifilar suspension method developed from one described by Theorell.8 A divided glass capillary was suspended as shown in Fig. 1. A solution was in the left compartment; distilled water was in the right or rear compartment. The capillary moved a distance of the order of 0.1 cm when the current through the magnet coils was 40 amp. (Field strength directly between the pole faces was about 17,000 Gauss.)

The horizontal force, F, on the capillary very nearly

<sup>6</sup> M. Calvin, Plutonium Project Report CK-2411 (1944). Calvin, Kasha, and Sheline, AECD-2002 (1948).

<sup>7</sup> Connick, Kasha, McVey, and Sheline, "The +5 oxidation state of plutonium," Plutonium Project Record, Vol. 14B, No. 3.15 (to be published).

<sup>8</sup> H. Theorell, Arkiv f. Kemi. Min. Geol. 16A, No. 1 (1943). Our apparatus was essentially the one used but not described by G. N. Lewis, and M. Calvin, J. Am. Chem. Soc. 67, 1232 (1945). equals wD/L, where w is the weight of the capillary, L is the fiber length, and D is the horizontal displacement which was observed in a microscope equipped with a traveling cross hair. One scale division on the knob corresponded to a distance of 8×10<sup>-5</sup> cm or to a force of  $6 \times 10^{-7}$  g if the load was a 0.5-g capillary.

Each solution was measured several times at magnet coil currents of 20, 30, and 40 amp. in order to establish that susceptibilities were always independent of field

The molar susceptibility,  $\chi$ , of a substance equals  $I_m/H$  where  $I_m$  is the magnetic moment of a gram atomic weight of the bulk material and H is the magnetic field strength. The total force acting on a long cylinder of solution with cross section A and whose axis passes through an inhomogeneous field is

$$wD/L = F = \chi MA(H_2^2 - H_1^2)/2000,$$
 (1)

where M is the molar concentration and  $H_1$  and  $H_2$  are the field strengths on the ends of the solution.

Equation (1) would hold only for a homogeneous sample; it was used for rough estimation of the field strength  $H_2$  from the displacements of nickel chloride solutions. Susceptibilities of other substances were calculated on the assumption that the displacement of a given filled capillary was proportional to  $\chi M$  if  $H_1$  and H<sub>2</sub> were held constant. The displacement was measured for each actinide element solution in the same capillary and at the same magnet coil current (±0.2 amp.) as was done for a standard nickel chloride solution. Correction for diamagnetism of the solvent (including anions) and for non-uniformity of the capillary was made by subtraction of an experimentally determined displacement for the solvent only in the rear compartment. If the molar susceptibility of nickel chloride at 20°C is taken as 4436×10-6 units,9 then for any cation

$$\chi = 4436 \times 10^{-6} D' M_{\text{NiCl}_2} / (MD'_{\text{NiCl}_2}),$$
 (2)

where D' is the displacement after application of the correction.

The U(IV) solution was prepared by dissolution of weighed, distilled UCl4 in oxygen-free hydrochloric acid solution. The last step in the preparation of the neptunium, plutonium, and americium solutions was dissolution of a hydroxide which had been precipitated with ammonium hydroxide. The plutonium concentraions were based on a weighing. The neptunium and americium solutions were assayed by measurement of the rate of alpha-particle emission of a small aliquot. The specific activities in counts minutes<sup>-1</sup> micrograms<sup>-1</sup> were taken as 790 for Np10 and 3.36×106 for Am11 if a thin sample is mounted on platinum and a counter

<sup>9</sup> H. R. Nettleton, and S. Sugden, Proc. Roy. Soc. (London)

A173, 313 (1939).

10 L. B. Magnusson, and T. J. LaChapelle, J. Am. Chem. Soc.

<sup>70, 3534 (1948).

11</sup> B. B. Cunningham, Plutonium Project Report CC-3876, Sect. 2.2 (1948).

TABLE I. Typical data; displacement of capillary for 40-ampere magnet coil current.

| Material in  | Displacement   |      | Suscept.   |
|--|----------------|------|------------|
| rear compart.  | D              | D'   | units ×106 |
| 0.36M HCl<br>0.0392M NiCl <sub>2</sub> in 0.36M HCl  | -030<br>+991   | 1021 | 4436ª      |
| 0.50 <i>M</i> HCl<br>0.0600 <i>M</i> Pu(III) in 0.5 <i>M</i> Cl <sup>-</sup>                       | $-030 \\ +099$ | 129  | 370        |
| $0.50M \text{ H}_2\text{SO}_4$<br>$0.0507M \text{ Pu}(\text{IV}) \text{ in } 0.5M \text{ HSO}_4^-$ | $-089 \\ +389$ | 478  | 1610       |

a Magnetic standard, reference 9.

geometry of "50 percent" is used. 12 These values are said to be better than  $\pm 5$  percent. If other specific activities are reported at a later date, the magnetic susceptibilities should be corrected proportionately. The quantity of neptunium or plutonium which was not in the desired oxidation state was shown to be less than 1 percent by measurement of the characteristic optical absorption maxima<sup>13</sup> on a Beckman spectrophotometer.

The 0.03920M nickel chloride solution which served as magnetic standard was prepared by dissolution of 0.2301 g of nickel rod (Johnson Matthey and Company, 99.97 percent Ni) in 5 ml of refluxing 10M HCl. After the solution had been diluted to 100.0 ml, the excess HCl concentration was found to be 0.360M.

Although the measured displacements were reproducible to about one scale division, the precision for determination of the molar susceptibilities is about 2 percent or 30×106 units, whichever is larger, because of the direct dependence upon determination of actinide element concentration and because of the presence in the solutions of an unknown amount of diamagnetic ammonium ion. The large negative displacements found for some examples of solvent only in the rear compartments were due to non-uniformity of the glass capillary. These large negative subtractions do not increase the percent error if the gross displacement of the actinide solution is positive.

### RESULTS AND INTERPRETATION

Some typical data are given in Table I, and the results are summarized in Table II. In Fig. 2 experimental  $\chi$  of the actinide element cations are compared with simple theoretical  $\chi_J$  for the assumed ground quantum states of the electronic configurations  $5f^n$ and  $5f^{n-1}6d$ . The experimental  $\chi$  follow the  $\chi_J$  for configurations  $f^n$  to a significant degree, though not as closely as had been found for most of the lanthanide

cations. 14, 15 The susceptibility of Am(III) is much higher than the theoretical value of zero, but that is also true of the corresponding lanthanide ion, Eu(III). It will be discussed in a later section of this paper. The susceptibilities of the cations are, of course, dependent upon the anion to a secondary degree.3

The ground states of the cations Np(VI), Np(V), Np(IV), Pu(IV), Pu(III), and Am(III) were concluded to be those on which the theoretical curve B was based, i.e.,  ${}^{2}F_{5/2}$ ,  ${}^{3}H_{4}$ ,  ${}^{4}I_{9/2}$ ,  ${}^{5}I_{4}$ ,  ${}^{6}H_{5/2}$ , and  ${}^{7}F_{0}$  respectively as nis 1 through 6.

While the atomic quantum numbers of a state may be those which are expected for a definite configuration,  $f^n$ , the state can belong partly to another configuration of the same parity.16 Susceptibility measurements can show only that the ground state has certain L, S, and Jquantum numbers; identification of the state with a configuration is a useful approximate concept. To the extent that quantum states of complicated atoms can be attributed to a single electronic configuration, the known aqueous cations of uranium and higher elements must have as the outer part of their ground configurations,  $5f^n6s^26p^6$  (n5f electrons which are more or less inside the configuration for the inert gas element 86).

### APPROXIMATE NATURE OF THEORETICAL CALCULATIONS

The factors which account for the limited accuracy of our theoretical calculations should be mentioned.

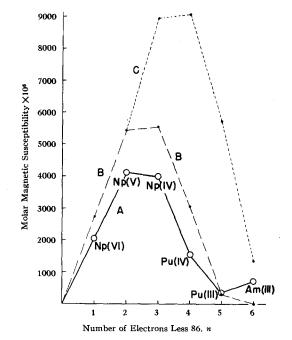


Fig. 2. Comparison at 20°C of magnetic susceptibilities of actinide elements cations with theoretical susceptibilities: A, experimental; B, theoretical for ground states of  $5f^n$ ; C, theoretical for ground states of  $5f^{n-1}6d$ .

<sup>12</sup> About 52 percent of the disintegrations are counted, Cunningham, Ghiorso, and Hindman, "Back-scattering of Pu<sup>229</sup> alphaparticles from platinum," Plutonium Project Record, Vol. 14B, No. 16.3 (to be published).

13 I. C. Hindman, and D. P. Ames, "Absorption spectra of ionic

<sup>18</sup> J. C. Hindman, and D. P. Ames, "Absorption spectra of ionic species of plutonium," Plutonium Project Record, Vol. 14B, No. 4.1; Hindman, Magnusson, and LaChapelle, "Chemistry of element 93, III. Absorption spectrum studies of aqueous ions of spectrum." Third No. 15.2 neptunium," Ibid., No. 15.2.

I<sup>4</sup> F. Hund, Zeits. f. Physik **33**, 855 (1925).
 I<sup>5</sup> J. H. Van Vleck, Phys. Rev. **31**, 587 (1928).
 E. U. Condon, Phys. Rev. **36**, 1121 (1930).

Quantum statistically the susceptibility is given by the

$$\chi = \frac{I_m}{H} = \frac{N_0}{H} \frac{\Sigma \partial W_i / \partial H \exp(-W_i / kT)}{\Sigma \exp(-W_i / kT)},$$
 (3)

where  $N_0$  is Avogadro's number and the summations are over-all quantum states of energies  $W_i$ . If the energy levels are simply those resulting from the Zeeman splitting of an isolated (on the energy scale) state of a free atom, their energies might be assumed to be

$$W_i - W_i^0 = Hg\beta M, \tag{4}$$

where  $\beta = eh/4\pi mc$  and M = J, J - 1,  $\cdots - J$ . Since  $2Hg\beta J\ll kT$  Eq. (3) yields

$$\chi_J = Ng^2\beta^2 J(J+1)/3kT.^{17}$$
 (5)

If the angular momenta of the several electrons are coupled according to the Russell-Saunders scheme (LS coupling)

$$g = [3J(J+1)+S(S+1)-L(L+1)]/2J(J+1).$$
 (6)

Equations (5) and (6) were used to calculate the theoretical points of Fig. 2. The ground state of a configuration was assumed by application of Hund's rules. The limited agreement of theoretical and experimental susceptibilities indicates that each paramagnetic atom interacts with other surrounding atoms as well as with the external magnetic field used for the measurements. Since most of the surrounding atoms are diamagnetic, the interaction is generally electrostatic in nature.

Penney and Schlapp attempted to calculate the effect of crystal electric fields on the magnetic susceptibility of iron group compounds and rare earth salts.18,19 Qualitatively it is a Stark splitting which is of the order of kT whereas the Zeeman splitting is small compared to kT. Although the calculations are not perfected,20 it is clear that the summation (3) can be much smaller than its evaluation by Eq. (5). Similarly in solutions the electric fields of neighbor anions and water dipoles will lower the magnetic susceptibility of

an actinide element cation compared to its corresponding lanthanide ion since the 5f electrons of the former should be outside the valence shell more often than are the 4f electrons in the latter. Since Np(VI) is essentially a one-electron case, the complications to be mentioned later cannot be important, and the 25 percent lowering of the susceptibility from the theoretical  $\chi_J$ must be due to the Stark splitting. It might be assumed tentatively that the Stark effect is the most important single complication tending to lower the susceptibility of all the actinide element cations.

Our theoretical calculations may be inadequate also on account of incorrect assumptions about the interactions between the several 5f electrons within one actinide atom. Ground quantum states of the  $4f^n$ configurations were deduced by Hund<sup>14</sup> from rules which are correct for atoms of small Z in which case it is a good approximation to derive atomic states from the states of individual electrons by means of the LS or Russell-Saunders coupling model (vanishingly weak spin-orbit interaction). In the spectra of gaseous uranium<sup>21, 22</sup> the multiplet splitting is wider than the separation of the centers of gravity of LS states. By definition this is strong spin-orbit interaction. The experimental g's of low lying states of the 5f36d7s2 configuration of uranium are fairly close to g<sub>LS</sub>, however.

It is interesting to see what happens to the energy levels as the spin-orbit interaction increases and the interelectronic interaction approaches the limiting case of jj coupling. Column 2 of Table III lists some states which should lie very low in the configurations  $5f^{1-6}$ . The state listed first lies deepest according to Hund's rules. For  $5f^2$ ,  $5f^3$ , and  $5f^4$  the state listed second was selected because it belongs both to the next group according to LS coupling and to the lowest group of jj coupling states. The ground state of  $5f^5$  or of  $5f^6$  becomes more isolated as jj coupling is approached. In the case of  $5f^6$  the two lowest multiplets of  $^7F$  were selected because the spacing between J=0 and J=1 would be only 1/21 of the total multiplet splitting according to

TABLE II. Molar susceptibilities of actinide element cations at 20°C in aqueous solution.

| Cation in solution | Anion in solution       | Cation suscept<br>units ×10 <sup>6</sup> |
|--------------------|-------------------------|--|
| U(IV)              | 0.5M Cl <sup>-</sup>    | 3690 <sup>a</sup>                        |
| Np(VI)             | $0.5M~\mathrm{HSO_4}^-$ | 2060                                     |
| Np(V)              | 0.2M Cl <sup>-</sup>    | 4120a                                    |
| Np(IV)             | $0.2M~\mathrm{HSO_4}^-$ | 4000b                                    |
| Pu(IV)             | $0.5M~\mathrm{HSO_4}^-$ | 1610                                     |
| Pu(III)            | 0.5M Cl <sup>-</sup>    | 370                                      |
| Am(IIÍ)            | $0.5M \text{ NO}_3^-$   | 720                                      |

 $<sup>^</sup>a$  For Pu(VI) (same number of electrons as U(IV) and Np(V)) susceptibility is 3540  $\times 10^{-6}$ , reference 6.  $^b$  For U(III) (same number of electrons as Np(IV)), susceptibility is 4340  $\times 10^{-6}$ , reference 3.

<sup>&</sup>lt;sup>17</sup> The small contribution to susceptibility from the atomic magnetic moment induced by the applied field was not added to the theoretical  $\chi_J$ 's. It would be only about  $-50 \times 10^{-6}$  for monatomic ions represented by Pu<sup>43</sup> and Am<sup>43</sup> and possibly as much as  $+50 \times 10^{-6}$  for molecular types such as NpO<sub>2</sub><sup>+</sup> and NpO<sub>2</sub><sup>++</sup>.

<sup>18</sup> W. G. Penny, and R. Schlapp, Phys. Rev. 41, 194 (1932); R. Schlapp and W. G. Penny, Ibid. 42, 667 (1932). These authors

pointed out the absence of any fundamental significance of the pointed out the absence of any fundamental significance of the empirical Weiss-Curie relation,  $\chi = C/(T + \Delta)$ . Many investigators have calculated "effective atomic magnetic moments" as  $\mu_{eff} = (Ck/N)^{\frac{1}{2}}$  and compared this "experimental" moment with  $\mu = g\beta[J(J+1)]^{\frac{1}{2}}$ . These  $\mu_{eff}$  can have no more meaning than C, which sometimes approaches  $N\mu^2/3k$  when  $\Delta$  is nearly zero. It seems preferable to present all results as susceptibilities and then compare theoretical values with the directly observed quantities even though the discrepancies appear twice as great when the

device of square root extraction is not used.

19 A. Frank, Phys. Rev. 48, 765 (1935).

20 For more recent discussions see W. G. Penny, and G. J. Kynch, Proc. Roy. Soc. (London) A170, 112 (1939) and L. J. F. Broer, Physica 12, 642 (1946).

<sup>&</sup>lt;sup>21</sup> Kiess, Humphreys, and Laun, J. Opt. Soc. Am. 36, 357 (1946);
J. Research Nat. Bur. Standards 37, 57 (1946).
<sup>22</sup> Ph. Schuurmans, Physica 11, 475 (1946); Schuurmans, van den Bosch, and Dijkwel, Ibid. 13, 117 (1947).

Table III. Theoretical susceptibilities of possible low energy states of actinide ions.

| Assumed<br>elect.<br>config.  | Possible<br>low energy<br>states | Theor. $\chi_J$ 's LS coupl. 20°C | Theor. $x_j$ 's $jj$ coupl. 20°C |
|---|----------------------------------|-----------------------------------|----------------------------------|
| 5 <i>f</i> ¹  | ${}^{2}F_{5/2}$                  | 2730                              | 2730                             |
| 5f <sup>1</sup><br>5f <sup>2</sup><br>5f <sup>4</sup><br>5f <sup>6</sup><br>5f <sup>6</sup> | ${}^{3}H_{4}; {}^{3}F_{2}$       | 5420; 1130                        | 6210; 1870                       |
| 5f3   | ${}^4I_{9/2}; {}^4G_{5/2}$       | 5540; 1210                        | 7680; 2730                       |
| 5f4   | ${}^{5}I_{4}; {}^{5}G_{2}$       | 3040; 280                         | 6210; 1870                       |
| 5f5   | $^6H_{5/2}$                      | 300                               | 2730                             |
| 5 <b>f</b> 6  | ${}^{7}F_{0}; {}^{7}F_{1}$       | 0: 1900                           | 0; 1900                          |
| 5f6d  | ${}^{3}H_{4}; {}^{3}G_{3}$       | 5420; 2860                        | , .                              |
| $5f^26d$  | ${}^{4}K_{11/2}; {}^{4}I_{9/2}$  | 8950; 5540                        |                                  |
| $5f^36d$  | ${}^{5}L_{6}; {}^{5}K_{5}$       | 9070; 5670                        |                                  |
| $5f^46d$  | $^{6}L_{11/2};  ^{6}K_{9/2}$     | 5730; 3130                        |                                  |
| 5f⁵6d   | ${}^{7}K_{4}; {}^{7}I_{3}$       | 1350; 320                         |                                  |

the Landé interval rule. The relative importance of the probably second lowest states is not known at the present time except that  ${}^{7}F_{1}$  must be significantly populated in Am(III) at 20°C.

Theoretical  $\chi_J$ 's for each ground state of the  $5f^n$  configurations were calculated for both coupling approximations, and the two results diverge as n increases from 2 to 5. Since the two  $\chi_J$ 's differ directly as  $g_{LS}^2$  and  $g_{jj}^2$  differ, the experimental  $\chi$  of Pu(III), the example of  $5f^{6}$   $^{6}H_{5/2}$ , shows unambiguously that g is much nearer to  $g_{LS}$  than to  $g_{jj}$ . This is consistent with previously mentioned results for the gaseous uranium atom.

Equation (5) depends on the validity of Eq. (4) for the Zeeman splitting. For each low energy state of Sm(III) and Eu(III) it was necessary<sup>23</sup> to use a more complete equation for  $\chi_J$  which had been derived by Van Vleck<sup>15</sup> from considerations equivalent to taking the Zeeman splitting to the second-order terms in H. He obtained Eq. (5) with the following added on the right:

$$\frac{N\beta^{2}}{6(2J+1)} \left\{ \frac{f(J)}{h\nu(J-1:J)} + \frac{f(J+1)}{h\nu(J+1;J)} \right\}, \quad (5a)$$

where  $f(J) = [(S+L+1)^2-J^2][J^2-(S-L)^2]/J$ . For sufficiently large  $h\nu$ 's this addition is negligible except that when S and L are large and J is small the  $f/h\nu$  terms are extremely large. In the examples Pu(III) and Am(III) the susceptibilities are greater than theoretical  $\chi_J$ 's for  ${}^6H_{5/2}$  and  ${}^7F_0$  as obtained with Eq. (5). The  $f/h\nu$  terms must be significant for low lying states of

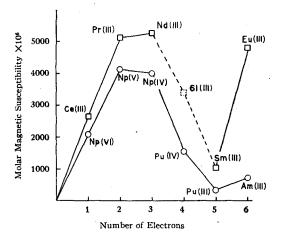


Fig. 3. Comparison of experimental magnetic susceptibilities of lanthanide and actinide element cations at 20°C. The values for the lanthanides were calculated from some of the "effective magnetic moments" compiled by Yost, Russell, and Garner, *The Rare Earth Elements and Their Compounds* (John Wiley, and Sons, Inc., New York, 1947), p. 14. The point for 61(III) is from the theoretical calculation by Van Vleck and Frank (see reference 23).

both cations. While the  ${}^7\!F_1$  state must be well populated in Am(III), it is much less so than in Eu(III) where the multiplet splitting is narrower. Thus the same discrepancies with simplest theory that were important in Sm(III) and in Eu(III) can be detected in Pu(III) and Am(III). The analogy is shown clearly in Fig. 3 where experimental susceptibilities of lanthanide and actinide element cations are compared directly.

#### ACKNOWLEDGMENT

The neptunium and americium were available for this study through the cooperation of T. J. LaChapelle, L. B. Magnusson, L. B. Asprey, and Dr. B. B. Cunningham, who had isolated these materials in very pure form for various research purposes. Many others contributed, of course, to the production of these special materials.<sup>24</sup> We are especially grateful to Professor G. T. Seaborg for his efforts toward making the work reported here possible.

This paper is based on work performed under the auspices of the AEC at the Radiation Laboratory, University of California.

<sup>&</sup>lt;sup>23</sup> J. H. Van Vleck, and A. Frank, Phys. Rev. 34, 1494, 1625 (1929).

<sup>&</sup>lt;sup>24</sup> Note added in proof: See Plutonium Project Record, Volume 14B. This collection of papers has recently been published under the title *The Transuranium Elements*, Seaborg, Katz, and Manning, Ed., (McGraw Hill Book Company, Inc., New York, 1949)