

Ionization of gases by a pulsed electron beam as studied by selffocusing. II. Polyatomic gases

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Citation: [The Journal of Chemical Physics](#) **75**, 2723 (1981); doi: 10.1063/1.442341

View online: <http://dx.doi.org/10.1063/1.442341>

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Ionization of gases by a pulsed electron beam as studied by self-focusing. II. Polyatomic gases

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(Received 5 March 1981; accepted 27 May 1981)

In order to analyze data on the self-focusing of a pulsed electron beam in polyatomic gases, the net current I_{net} in H_2 , N_2 , and CH_4 was computed self-consistently as functions of time in the pressure range between 5 and 300 Torr of these gases by using swarm parameters. The computational result indicates that the larger dose D_{obs} , observed by a piled dosimeter on the beam axis, is attributed to the larger I_{net} , which is mainly determined by a mean ionization time t_i for secondary ionization by the electric field induced by the pulsed beam. When values of D_{obs} for different gases are compared at the same pressure, the larger D_{obs} is given by the larger t_i . This relationship is demonstrated for several polyatomic gases by estimating t_i from various parameters in a function of secondary electron energy or E/p such as the electron drift velocity, the first Townsend ionization coefficient, the ionization cross section, and so on. For the short pulse duration of a Febetron 706, electron-ion recombination processes scarcely affect I_{net} except at high pressures of some polyatomic gases, while the effect of electron-attachment processes is appreciable in SF_6 , CCl_2F_2 , and N_2O .

INTRODUCTION

In a preceding paper (part I),¹ it has been shown that, for monatomic gases, the maximum dose (D_{obs}) of the depth-dose curve in a piled dosimeter given by a pulsed electron beam of a Febetron 706 (tube 5515)² can be interpreted in terms of the net current I_{net} , which is mainly determined by a mean ionization time t_i . The value of I_{net} has been calculated with the following equations:

$$I_{\text{net}}(t) = I_b(t) + I_{\text{back}}(t), \quad (1)$$

$$I_{\text{back}}(t) = \pi r_0 E_z(t) \sigma_e(t), \quad (2)$$

$$E_z(t) = -\frac{2}{c^2} \left(\frac{1}{2} + \ln \frac{R}{r_0} \right) \frac{dI_{\text{net}}(t)}{dt}, \quad (3)$$

$$\sigma_e(t) = \frac{e^2 n_e(t)}{n_0 (2m)^{1/2} Q_m(\bar{\epsilon}) \bar{\epsilon}^{1/2}}, \quad (4)$$

$$\frac{dn_e(t)}{dt} = \frac{n_0 \sigma_{\text{ion}}(E_b) I_b(t)}{\pi r_0^2 e} + \frac{n_e(t)}{t_i(t)}, \quad (5)$$

where I_b is the beam current assumed as in part I, I_{back} the plasma backward current, r_0 the beam radius assumed to be 0.6 cm, R the chamber radius (6.4 cm), E_z the longitudinal electric field induced along the beam coordinate z by the pulsed beam, c the velocity of light, σ_e the plasma conductivity of the irradiated medium gas, m the electron rest mass, e the electron charge, n_0 the number density of gas molecules, n_e the number density of secondary electrons, and Q_m the momentum transfer cross section for electrons with mean kinetic energy $\bar{\epsilon}$. The total ionization cross section $\sigma_{\text{ion}}(E_b)$ for the beam electron with energy E_b is estimated for $\bar{E}_b = 480$ keV from the Rieke-Prepejchal parameters.³ The mean ionization time t_i for secondary ionization has been determined as a function of E/p for some gases by Felthenthal and Proud.⁴ For other gases, t_i can be estimated by⁴

$$1/(p t_i) = w(\alpha/p - \eta/p), \quad (6)$$

where α is the first Townsend ionization coefficient, η

the electron-attachment coefficient, and w the electron drift velocity. It has been demonstrated from the calculated I_{net} that D_{obs} can be expressed approximately as

$$D_{\text{obs}} \propto \int \frac{I_b(t) I_{\text{net}}(t)}{\epsilon_b^2} dt, \quad (7)$$

where $\pi \epsilon_b$ is the beam emittance. Thus, the larger D_{obs} corresponds to the larger I_{net} , which is given by the smaller I_{back} for $dI_{\text{net}}/dt > 0$ from Eqs. (1)–(3). This means that the larger D_{obs} is given by a gas with the larger t_i for $dI_{\text{net}}/dt > 0$.

The similar computation was carried out for H_2 , N_2 , and CH_4 . In the present paper, data on D_{obs} for various polyatomic gases^{5–7} are discussed on the basis of the computational result for these gases.

COMPUTATION FOR H_2 , N_2 , and CH_4

In the computation, the parameters r_0 , $I_b(t)$, and $\sigma_{\text{ion}}(E_b)$ were used on the same assumptions as made in part I.¹ Literature values were used for the following parameters; w ,⁸ α/p ,⁹ D_L/μ ,¹⁰ and Q_m ¹¹ for H_2 ; w ,⁸ α/p ,¹² D_L/μ ,¹³ and Q_m ¹¹ for N_2 ; and w ,^{14–16} α/p ,¹⁷ D_L/μ ,¹⁸ and Q_m ^{19,20} for CH_4 . The value of $\bar{\epsilon}$ was estimated from data on D_L/μ on the assumption of the Maxwellian. For polyatomic gases, Eq. (5) was revised as

$$\begin{aligned} \frac{dn_e}{dt} = & \frac{n_0 \sigma_{\text{ion}}(E_b)}{e} \cdot \frac{I_b(t)}{\pi r_0^2} + \frac{n_e(t)}{t_i(t)} \\ & \text{(term 1)} \quad \text{(term 2)} \\ & - \alpha_r n_e(t) n_i(t) - \alpha_{ra} n_e(t) n_a(t), \end{aligned} \quad (8)$$

$$\frac{dn_i}{dt} = \frac{n_0 \sigma_{\text{ion}}(E_b)}{e} \cdot \frac{I_b(t)}{\pi r_0^2} + \frac{n_e}{t_i} - \alpha_r n_e n_i - k_d n_i n_0^2, \quad (9)$$

$$\frac{dn_a}{dt} = k_d n_i n_0^2 - \alpha_{ra} n_e n_a, \quad (10)$$

where α_r and α_{rd} are the recombination coefficients (cm^3/s) between electron-ion and electron-dimer ion, respectively, and k_d is the rate constant of dimer ion formation. The number densities of ions and dimer ions are represented by n_i and n_d , respectively. We have assumed that the variation of α_r and α_{rd} with $\bar{\epsilon}$ is expressed as

$$\alpha_r(\text{H}_2^+) = 4.7 \times 10^{-8} \bar{\epsilon}^{-0.40} \quad (\text{Ref. 21}),$$

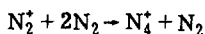
$$\alpha_r(\text{N}_2^+) = 5.5 \times 10^{-8} \bar{\epsilon}^{-0.65}, \quad \text{for } \bar{\epsilon} > 1 \text{ eV (Ref. 22)},$$

$$\alpha_{rd}(\text{N}_4^+) = 3.7 \times 10^{-7} \bar{\epsilon}^{-0.65}, \quad \text{for } \bar{\epsilon} > 1 \text{ eV (Ref. 22)},$$

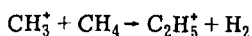
$$\alpha_r(\text{CH}_3^+) = 5.5 \times 10^{-8} \bar{\epsilon}^{-0.93}, \quad \text{for } \bar{\epsilon} > 0.8 \text{ eV (Ref. 23)},$$

$$\alpha_{rd}(\text{C}_2\text{H}_5^+) = 9.5 \times 10^{-8} \bar{\epsilon}^{-0.75}, \quad \text{for } \bar{\epsilon} > 1 \text{ eV (Ref. 23)},$$

and for formation processes of N_4^+ and C_2H_5^+ :



$$(k_d = 8 \times 10^{-29} \text{ molecule}^{-2} \text{ cm}^6 \text{ s}^{-1}) \quad (\text{Ref. 24}),$$



$$(k_d = 1 \times 10^{-9} \text{ cm}^3/\text{s}) \quad (\text{Ref. 25}).$$

For hydrogen, only the association reaction of H^+ leading to H_3^+ is known.²⁴ However, the yield of H^+ is small in comparison with that of H_2^+ (about several percent).^{26,27} Thus, the recombination of electron- H_3^+ was neglected in the calculation for H_2 . Only the formation of CH_3^+ and C_2H_5^+ was assumed in the calculation for methane.

Computational results of $I_{\text{net}}(t)$ for H_2 , N_2 , and CH_4 are shown in Figs. 1, 2, and 3, respectively. They show that the calculated value of I_{net} at lower pressure is nearly constant after a certain time, as has been assumed previously as the t_B model.⁵ The value of D_{obs} increases at first with increasing pressure in the low pressure region, and after passing the maximum it decreases abruptly at a certain pressure (usually 1–5 Torr) but increases again with further increasing pressure.^{6,7} The curve of $I_{\text{net}}(t)$ varies according to the t_B

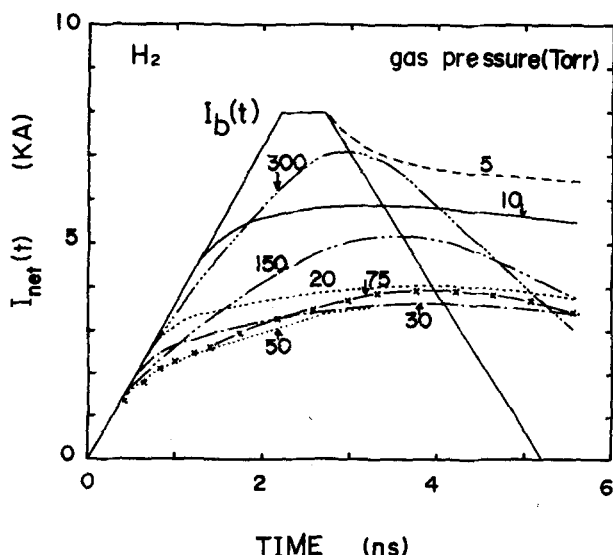


FIG. 1. The calculated net current $I_{\text{net}}(t)$ as a function of time for various pressures of H_2 . The solid straight lines indicate the beam current $I_b(t)$.

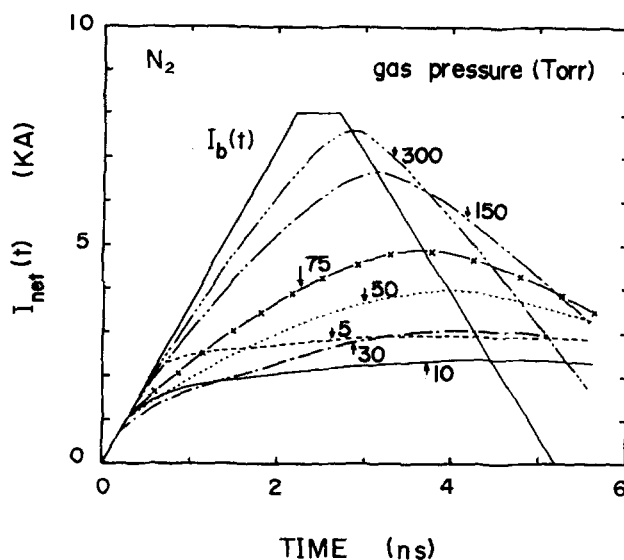


FIG. 2. The calculated net current $I_{\text{net}}(t)$ as a function of time for various pressures of N_2 .

model up to the pressure giving the minimum D_{obs} . In this region, $I_{\text{net}}(t)$ decreases with increasing pressure.

In the present paper, we are most interested in the higher pressure region in which D_{obs} increases gradually after passing the minimum. In this region, in Figs. 1–3, $I_{\text{net}}(t)$ increases appreciably with the lapse of time and also increases with increasing pressure. According to Eq. (7), D_{obs} should be proportional to the value of $\int I_b(t) I_{\text{net}}(t) dt$ if the variation of ϵ_0 is ignored. In Fig. 4, values of this integral are plotted in an arbitrary unit by solid symbols for H_2 , N_2 , and CH_4 by using the calculated values of I_{net} in Figs. 1, 2, and 3, respectively, together with the curves of D_{obs} shown by open symbols. The curve of the integral represents fairly well the aspect of the curve of D_{obs} . However, when both the curves are compared at the pressure giving the minimum, the value

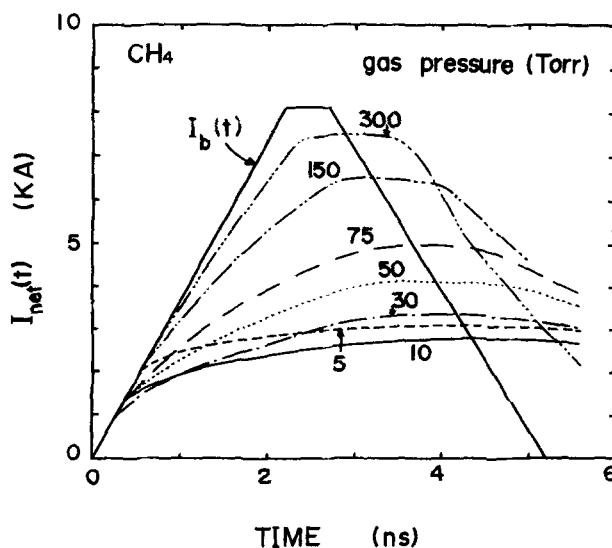


FIG. 3. The calculated net current $I_{\text{net}}(t)$ as a function of time for various pressures of CH_4 .

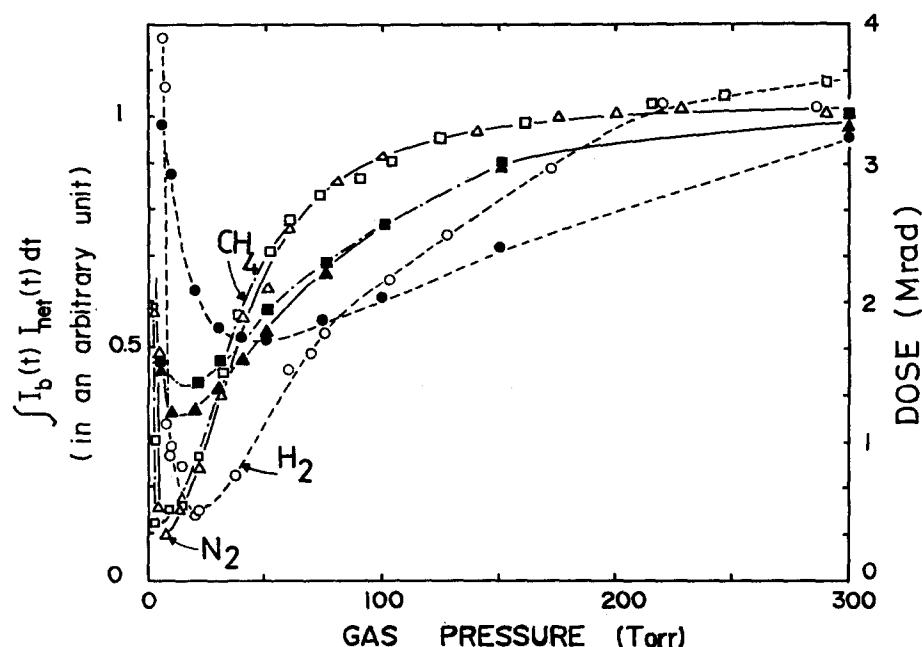


FIG. 4. D_{obs} at various pressures of H_2 , N_2 , and CH_4 : \circ (H_2), \triangle (N_2), and \square (CH_4). Solid marks [\bullet (H_2), \blacktriangle (N_2), and \blacksquare (CH_4)] indicate the values of the integral in Eq. (7) in an arbitrary unit.

of the integral is relatively larger than that of D_{obs} . This can be fitted by using the correct value of ϵ_b as has been discussed in part I.¹ Consequently, the present computational result represents fairly well the phenomena induced by the pulsed beam in a gas chamber so that the calculated values of parameters such as I_{net} , n_e , and E/p , which are not easy to be measured, might be used semiquantitatively.

Curves of E_z/p calculated from the values of I_{net} in Figs. 1, 2, and 3 are shown as functions of t in Figs. 6, 7, and 8 for H_2 , N_2 , and CH_4 , respectively. In the

present computation, values of $\bar{\epsilon}$ are estimated from data on D_L/μ on the assumption of the Maxwellian as functions of the calculated E_z/p shown in Figs. 6–8. Such values of $\bar{\epsilon}$ at pressure of 30 Torr for three gases, as

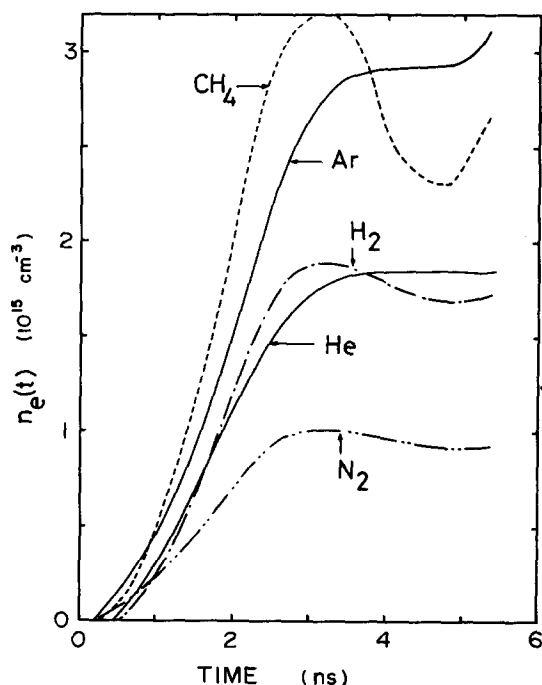


FIG. 5. The calculated number density $n_e(t)$ of produced secondary electrons as functions of time at 50 Torr of He (—), Ar (—), H_2 (---), N_2 (----), and CH_4 (-----).

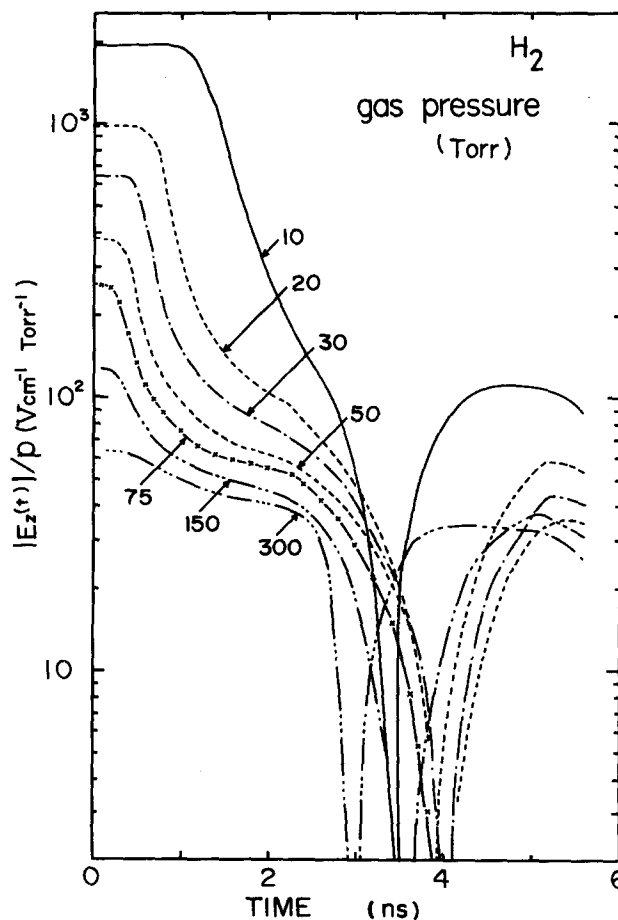


FIG. 6. The calculated $|E_z(t)|/p$ [$E_z(t)$: the induced longitudinal electric field] as functions of time for various pressures of H_2 .

the representative, are shown as functions of t in Fig. 9, because we are interested mainly in the pressure region between 10 and 50 Torr in the present paper. Curves in Figs. 6–8 show that the value of E_z/p decreases abruptly for a short period. However, the actual value of $\bar{\epsilon}$ for this period might not so decrease as shown in Fig. 9 so that the value of t_i for this period may not vary abruptly according to such a calculated E_z/p because of the presence of the relaxation time of $\bar{\epsilon}$. The present computation, however, was carried out straightforwardly according to the calculated E_z/p without any correction.

The calculated value of $n_e(t)$ increased with increasing pressure and became the maximum at 75 Torr of H_2 , 50 Torr of N_2 , and 30 Torr of CH_4 . The value decreased slightly with further increasing pressure. The value of n_e became the maximum at the pressure for which D_{obs} is nearly equal to 1 Mrad. Such a relationship of $n_e(t)$ between p or D_{obs} is common with He and Ar, whose curves are shown in detail in part I.¹ Then, the curve of $n_e(t)$ becomes almost the same irrespective of pressure for D_{obs} higher than 1 Mrad. Curves of $n_e(t)$ at 50 Torr are shown as functions of t in Fig. 5.

The contribution of each term to the total n_e in Eq. (8) is as follows, although the computation was carried out for a discrete value of p : The contribution of direct ionization (term 1) is less than 10% of electron avalanching (term 2) at 20–150 Torr of H_2 , 5–50 Torr of N_2 , and 5–100 Torr of CH_4 . Furthermore, the contribution of recombination precesses (terms 3 and 4) at the peak of

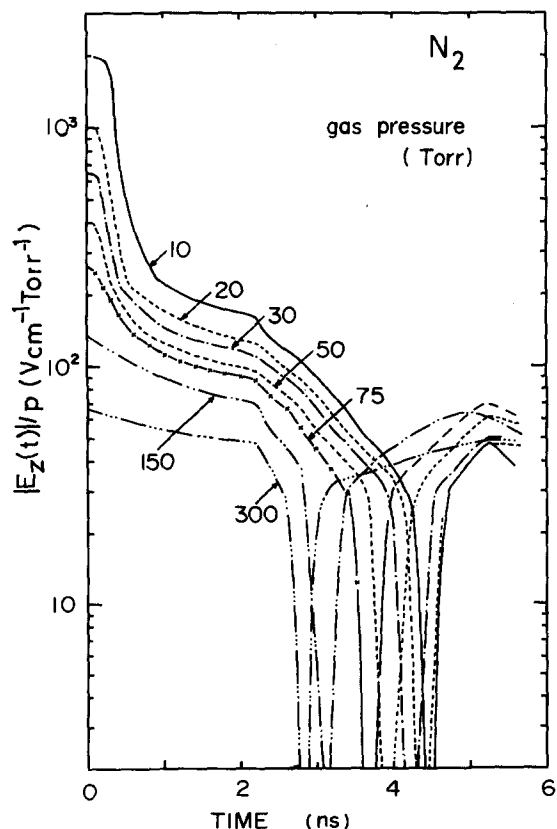


FIG. 7. The calculated $|E_z(t)|/p$ as functions of time for various pressures of N_2 .

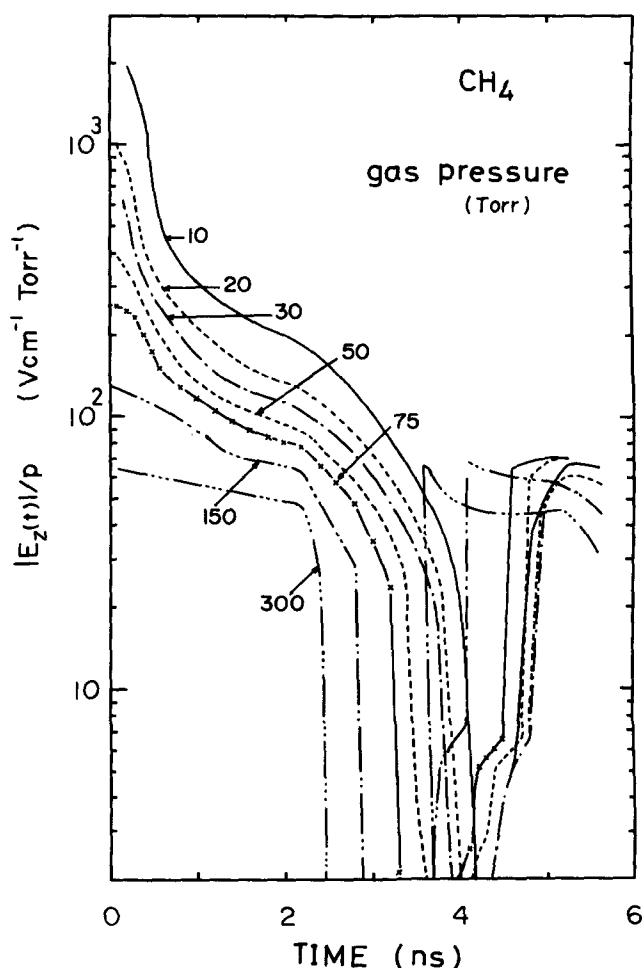


FIG. 8. The calculated $|E_z(t)|/p$ as functions of time for various pressures of CH_4 .

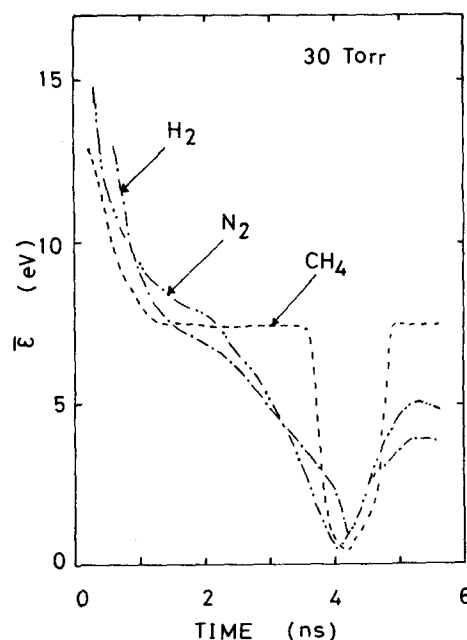


FIG. 9. The mean electron energy estimated at 30 Torr of H_2 (---), N_2 (-·-·-), and CH_4 (----) as functions of time.

the pulsed beam (2.2 ns) is less than 10% of the total n_e at pressures below 300 Torr of the three gases. At higher pressure, however, the recombination contribution became large at 3 ns due to decreasing $\bar{\epsilon}$ in the low- E/p region and due to the large amount of dimer-ion formation. Some results are shown in Figs. 10 and 11. The number densities of secondary electrons (n_e), $N_2^+(n_i)$, and $N_4^+(n_d)$ at 30 and 300 Torr of N_2 are shown as functions of t in Fig. 10. At 300 Torr, most of N_2^+ becomes N_4^+ without recombination for the pulse duration. The similar curves of n_e , $n_i(\text{CH}_3^+)$, and $n_d(\text{C}_2\text{H}_5^+)$ at 30 and 300 Torr of CH_4 are shown in Fig. 11.

Generally speaking, since n_e is on the order of 10^{15} cm^{-3} as seen in Fig. 5, the half-life of secondary electrons for electron-ion recombination processes is less than 1 ns for α , larger than $10^{-6} \text{ cm}^3 \text{ s}^{-1}$. Such large rate constants, are reported only for N_4^+ ,²⁸ O_4^+ ,²⁸ and CH_4^+ or CH_3^+ ²³ for thermal electrons and N_2O^+ ²⁹ for 0.04 eV electrons. Apparent recombination coefficients for N_2 , CO_2 , CH_4 , and C_3H_8 for thermal electrons³⁰ are also larger than $10^{-6} \text{ cm}^3 \text{ s}^{-1}$ at 50 Torr. When α is reduced according to the $\bar{\epsilon}^{-0.5}$ law, the value may be on the order of $10^{-7} \text{ cm}^3 \text{ s}^{-1}$ even for these gases for the present experiments. Therefore, we can ignore the electron-ion recombination process at least for the ns pulse duration in the pressure region of interest.

DISCUSSION

It is concluded from Fig. 4 that the larger D_{obs} is given by the larger I_{net} which is due to the smaller I_{back} or $\sigma_e E_x$ from Eqs. (1), (2), and (7). From Eq. (4), $\sigma_e E_x$ is pro-

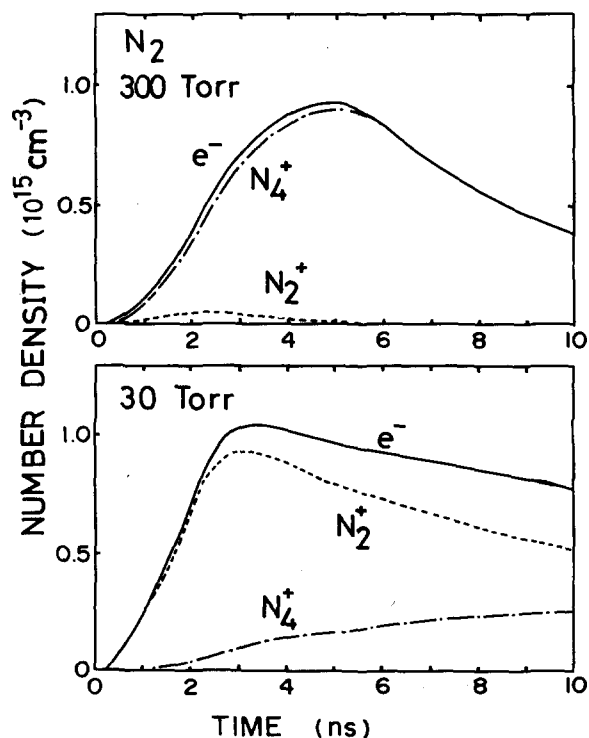


FIG. 10. The calculated number densities of secondary electrons e^- , monomer ion N_2^+ , and dimer ion N_4^+ as functions of time for 30 and 300 Torr of N_2 .

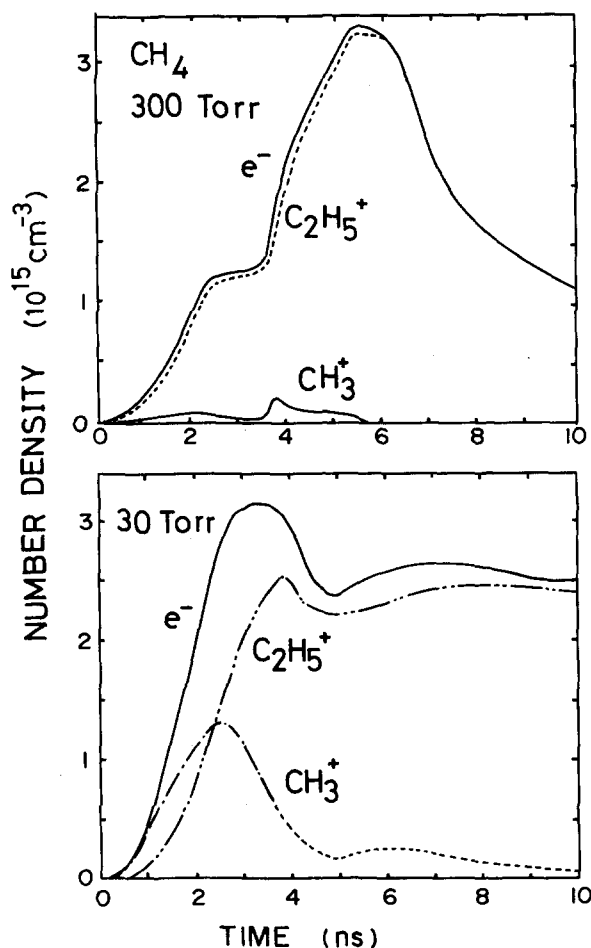


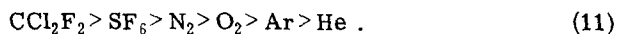
FIG. 11. The calculated number densities of secondary electrons e^- , monomer ion CH_3^+ , and dimer ion C_2H_5^+ as functions of time for 30 and 300 Torr of CH_4 .

portional to the product of $n_e/Q_m \bar{\epsilon}^{1/2}$ and E_x/p . The value of $Q_m(\bar{\epsilon}) \bar{\epsilon}^{1/2}$ increases with increasing $\bar{\epsilon}$ and usually becomes nearly constant from a certain $\bar{\epsilon}$. Such plateau values are $(2-3) \times 10^{-15} \text{ cm}^2 \text{ eV}^{0.5}$ for 1-10 eV of $\bar{\epsilon}$ (5-300 $\text{V cm}^{-1} \text{ Torr}^{-1}$ of E/p) for H_2 , $(2.5-4.5) \times 10^{-15} \text{ cm}^2 \text{ eV}^{0.5}$ for 2-10 eV of $\bar{\epsilon}$ (1-150 $\text{V cm}^{-1} \text{ Torr}^{-1}$ of E/p) for N_2 , and $6.5 \times 10^{-15} \text{ cm}^2 \text{ eV}^{0.5}$ for 7.4 eV (24-136 $\text{V cm}^{-1} \text{ Torr}^{-1}$ of E/p) for CH_4 . In Figs. 6-8, these E/p regions giving the plateau value are covered by the major part of the pulse duration. The difference of $Q_m(\bar{\epsilon}) \bar{\epsilon}^{1/2}$ among gases must be noticed but the plateau values are not much different among gases except CH_4 . Then, the aspect of D_{obs} can be analyzed mainly by E/p and n_e .

Since the larger I_{net} induces the larger E_x from Eq. (3), at the same pressure, the larger D_{obs} is associated with the larger E_x/p in spite of the smaller I_{back} because the larger D_{obs} corresponds to the smaller I_{back} as pointed out above. From Eqs. (2) and (4), this means that the larger D_{obs} is given by a gas with the smaller $n_e/Q_m \bar{\epsilon}^{1/2}$ at the same pressure. The smaller n_e is given by a gas with the larger t_i because, in Eq. (8), term 2 is dominant for the major part of the pulse duration in the pressure region of interest, as described already. Therefore, if we ignore the variation of $Q_m \bar{\epsilon}^{1/2}$ among gases,

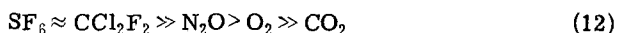
the larger D_{obs} is given by a gas with the larger t_i or pt_i at the same pressure under the larger E/p , as described above. This is the principal conclusion on the relationship between D_{obs} and t_i . Hereafter, data on D_{obs} for various polyatomic gases will be analyzed on the basis of this conclusion. The value of D_{obs} can give information on t_i for the pulse duration, which is difficult to be measured directly.

The E/p - pt_i curves for several gases have been obtained experimentally by Felsenthal and Proud⁴ as seen in Fig. 16 of Ref. 4 in which pt_i increases with decreasing E/p . The above conclusion suggests that the E/p - pt_i curve for a gas giving the larger D_{obs} at the same pressure must be placed at the upper side in such a figure. In fact, in Fig. 16 of Ref. 4, the values of E/p at the same pt_i are in the order

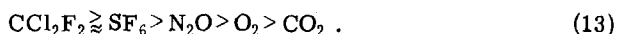


This is the same order as for D_{obs} at the same pressure as seen in Figs. 6 and 7 of Ref. 5. The relationship between He and Ar has been discussed in part I.¹

As demonstrated by Felsenthal and Proud,⁴ the value of t_i for a gas with no experimental value of t_i can be determined by Eq. (6) from swarm parameters (w , α/p , and η/p). Values of η/p have been measured as functions of E/p for some gases. According to references, values of η/p are in the order³¹⁻³⁴



and ratios of η/α are in the order



For $E/p > 60 \text{ V cm}^{-1} \text{ Torr}^{-1}$, the ratio of η/α is negligibly small for O_2 and CO_2 . On the other hand, since the number density of gas molecules is $3.3 \times 10^{18} \text{ cm}^{-3}$ at 20°C and 100 Torr, the half-life of secondary electrons for electron-attachment processes is less than 1 ns for the rate constant larger than $2 \times 10^{-10} \text{ cm}^3/\text{s}$. Such large rate constants are reported for O_2 ($3.4 \times 10^{-10} \text{ cm}^3/\text{s}$ at 6.7 eV^{35}), N_2O ($9.2 \times 10^{-10} \text{ cm}^3/\text{s}$ at 2.4 eV^{35}), SF_6 ($2 \times 10^{-7} \text{ cm}^3/\text{s}$ at thermal energy³⁶), and CCl_2F_2 ($5.6 \times 10^{-9} \text{ cm}^3/\text{s}$ at 1.08 eV^{36}). Then, the contribution of electron-attachment processes may be important in CCl_2F_2 , SF_6 , and N_2O . In fact, as seen in Fig. 7 of Ref. 5, values of D_{obs} in these gases are larger than in other gases; they are in the order



as predicted from the ordering (12) and (13). This fact suggests that t_i is lengthened due to the large η/p in Eq. (6).

For the gas with no appreciable electron-attachment process, the value of pt_i can be estimated as $p/w\alpha$. Although E/p varies with t and p , from Figs. 6-8, we attempt to estimate the value of $p/w\alpha$ at $100 \text{ V cm}^{-1} \times \text{Torr}^{-1}$ as the representative value for gas pressures between 20 and 50 Torr. From data on w and α/p in Ref. 8, values of $p/w\alpha$ are in the order



This order is almost the same with the order of D_{obs} in

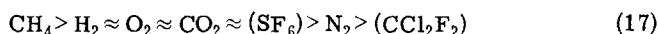
Fig. 7 of Ref. 5 except CH_4 because D_{obs} for CH_4 is rather larger than for N_2 . This fact supports the present conclusion on the relationship between D_{obs} and t_i . D_{obs} for CH_4 is attributed to the large value of $Q_m \bar{\epsilon}^{1/2}$ for CH_4 as described already.

On the other hand, for the gas with no electron-attachment process, the value of pt_i can also be estimated by the following equation instead of $p/w\alpha$:

$$\frac{1}{n_0 t_i} = \left(\frac{2}{m} \right)^{1/2} \int_{\text{I.P.}}^{\infty} \epsilon^{1/2} \sigma_i(\epsilon) F(\epsilon) d\epsilon , \quad (16)$$

where I. P. is the ionization potential of a gas, $\sigma_i(\epsilon)$ the total ionization cross section of a gas for electrons with energy ϵ , and $F(\epsilon)$ the distribution function of ϵ . Data on σ_i for lower-energy electrons are given by Rapp and Englander-Golden.²⁶ Equation (16) indicates that, at the same pressure, the larger D_{obs} or t_i is given by the gas with the higher I. P., the slower initial slope of σ_i , and the larger distribution of ϵ at the lower energy.

There are few available data on $F(\epsilon)$ in the E/p region of interest. We can find some data on D_L/μ as functions of E/p between 50 and $100 \text{ V cm}^{-1} \text{ Torr}^{-1}$ for estimation of $\bar{\epsilon}$ for H_2 ,¹⁰ N_2 ,¹³ O_2 ,³⁷ CO_2 ,³⁸ CH_4 ,¹⁸ SF_6 ,³⁹ and CCl_2F_2 .⁴⁰ Values of $\bar{\epsilon}$ for these gases estimated on the assumption of the Maxwellian are about 7-8 eV except CCl_2F_2 (5.5 eV) at $100 \text{ V cm}^{-1} \text{ Torr}^{-1}$ and are in the order



at $50 \text{ V cm}^{-1} \text{ Torr}^{-1}$. The values for SF_6 and CCl_2F_2 are extrapolated from data at E/p above $100 \text{ V cm}^{-1} \text{ Torr}^{-1}$.

Let us suppose that ϵ is lowered by $Q_t f$, where Q_t is the total collision cross section and f the mean fractional energy loss per collision which is given by⁴¹

$$f = 1.74 \times 10^{-14} w^2 / k_T , \quad (18)$$

where k_T is the Townsend energy factor ($k_T = 39.8 D_L/\mu$ at 20°C^{41} for the Maxwellian). Values of $Q_t f$ from Eq. (18) are shown as functions of $\bar{\epsilon}$ in Fig. 12. Data on $Q_t f$ are cited from references as follows; H_2 ,⁴² N_2 ,²⁰ O_2 ,^{43,44} CO_2 ,²⁰ CH_4 ,¹⁹ and SF_6 .⁴⁵ When the curves in Fig. 12 are compared with the ordering (17), the high value of $Q_t f$ for CH_4 at lower E/p is attributed to the small value of D_L/μ at lower $\bar{\epsilon}$ because of the special dependence of D_L/μ on E/p ¹⁸; the low value of $\bar{\epsilon}$ for N_2 is attributed to the large value of $Q_t f$, and the intermediate values for O_2 , CO_2 , and SF_6 are also understood by their curves of $Q_t f$ from Eq. (18). This means that $Q_t f$ from Eq. (18) is useful to estimate $F(\epsilon)$ qualitatively, though there is some problem for the application of Eq. (18) to the higher E/p region.

Now, we examine the order of D_{obs} as seen in Fig. 7 of Ref. 5 on the basis of Eq. (16). When data on I. P. and σ_i are compared for N_2O and N_2 , t_i for N_2O must be smaller than for N_2 because of the large $Q_t f$ for N_2 . However, D_{obs} for N_2O is larger than for N_2 . This fact suggests that D_{obs} or t_i for N_2O may be affected appreciably by the electron-attachment process which is ignored in Eq. (16). Similarly, in the comparison between CH_4 and N_2 , D_{obs} for CH_4 rather larger than for N_2 can be explained only by the large $Q_m(\bar{\epsilon})\bar{\epsilon}^{1/2}$ for CH_4 . The value

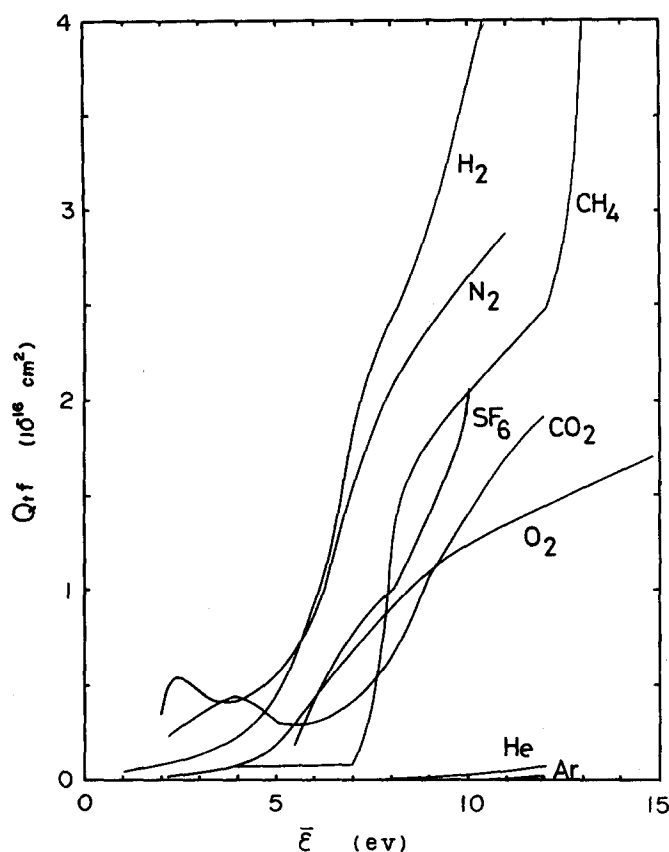


FIG. 12. The estimated values of $Q_i f$ (Q_i : total collision cross section for electrons; and f : mean fractional energy loss per collision) as functions of the mean electron energy.

of D_{obs} for N_2 rather larger than for CO_2 is attributed to the higher I. P., the smaller σ_i , and the larger $Q_i f$ for N_2 than for CO_2 . The value of D_{obs} for O_2 smaller than for CO_2 is attributed to the lowest I. P. among gases compared in the ordering (15). On the other hand, for H_2 , the value of D_{obs} is the lowest among polyatomic gases as seen in Fig. 7 of Ref. 5. This fact can be interpreted in terms of $p/w\alpha$ as seen in the ordering (15) because of the largest α/p for H_2 at $100 \text{ V cm}^{-1} \text{ Torr}^{-1}$. However, the largest α/p cannot be derived from Eq. (16) because H_2 has a high I. P., a small σ_i , and a large $Q_i f$.

ACKNOWLEDGMENTS

The authors wish to express their thanks to Sin-ichi Sato and Minoru Maeda of Fujitsu Ltd. at the Computing Center of Tokai Research Establishment, JAERI for their valuable advice and help in programming and computation.

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