

An electronic structure study of H2 and CH4 interactions with MgO and Lidoped MgO clusters

James L. Anchell, Keiji Morokuma, and Anthony C. Hess

Citation: The Journal of Chemical Physics 99, 6004 (1993); doi: 10.1063/1.465899

View online: http://dx.doi.org/10.1063/1.465899

View Table of Contents: http://scitation.aip.org/content/aip/journal/jcp/99/8?ver=pdfcov

Published by the AIP Publishing

Articles you may be interested in

Periodic density functional theory studies of Li-doped polythiophene: Dependence of electronic and structural properties on dopant concentration

J. Chem. Phys. 130, 164904 (2009); 10.1063/1.3109079

Structure and electronic properties of Li-doped vanadium oxide nanotubes

J. Chem. Phys. 128, 224701 (2008); 10.1063/1.2931542

Activation energy for hydrogen abstraction from methane over Li-doped MgO: A density functional theory study

J. Chem. Phys. 125, 074715 (2006); 10.1063/1.2227387

Molecular adsorption of NH3 on MgO(001) and hydrogen abstraction from NH3 on gaseous LiO and Li doped MgO(001). A computational study

J. Chem. Phys. 96, 6281 (1992); 10.1063/1.462619

Interaction of 0.2 to 4.0ev Electron Beams with Cleaved MgO

J. Chem. Phys. **36**, 608 (1962); 10.1063/1.1732580



An electronic structure study of H₂ and CH₄ interactions with MgO and Li-doped MgO clusters

James L. Anchell^{a)} and Keiji Morokuma Institute for Molecular Science, Myodaiji, Okazaki 444, Japan

Anthony C. Hess

Pacific Northwest Laboratory, b) MSIN K1-90, Richland, Washington 99352

(Received 23 March 1993; accepted 29 June 1993)

An ab initio study is presented concerning the chemisorption of hydrogen on a model of the (100) surface of MgO and Li-doped MgO. The local surface environment was modeled employing cubic and tetragonal clusters composed of 8 and 12 atoms, respectively. The lattice constant for the clusters was fixed at the experimentally determined value for bulk MgO and the geometry of the adsorbate was optimized at the unrestricted Hartree–Fock (UHF) level of theory. Correlation energy was treated at the second-order unrestricted Møller–Plesset (UMP2) level at the UHF optimized geometry. It was found that H_2 undergoes heterolytic dissociation at neighboring three-coordinated Mg and O sites (denoted Mg_{3c} and O_{3c}) in MgO with activation energies of 4.2 and 2.4 kcal/mol at the UHF and UMP2 levels, respectively. Li-doped MgO did not support heterolytic dissociation at neighboring Mg and O sites. Instead H_2 was found to dissociate homolytically without barrier at two O_{3c} sites and to undergo hydrogen atom abstraction at O_{3c} and O_{4c} sites. At the UHF/UMP2 level, it was found that at O_{3c} sites, abstraction occurs with a 17.9/3.0 kcal/mol barrier, and at O_{4c} sites, abstraction occurs with a 15.7/0.6 kcal/mol activation energy.

I. INTRODUCTION

Magnesium oxide is known to catalyze a variety of reactions involving hydrocarbons. Some examples of these reactions are the $\rm H_2/D_2$ exchange reaction, ¹ methanol and ethanol decomposition, ^{2,3} alkene hydrogenation, ⁴ the water–gas shift reaction, ⁵ and isomerization of *cis*-2-butene. ^{6,7}

In addition, Li-doped (hereafter referred to as Li/MgO) MgO is known to increase the activity of the MgO catalyst with respect to the high temperature conversion of methane to higher order alkanes^{8,9} and oxidation of C_2 hydrocarbons to form carbon oxides.¹⁰ In this study, ab initio molecular orbital methods are applied to clusters of $(MgO)_n$ and $LiMg_{n-1}O_n$ (n=4 and 6), and a comparative investigation is made of the energetics and chemistry of hydrogen and methane interactions on local surface sites of MgO and Li/MgO.

Because of its industrial importance, and because it is a computationally tractable system at relatively sophisticated levels of theory, numerous theoretical investigations have been carried out on the MgO and Li/MgO systems. Colbourn and Mackrodt¹¹ used self-consistent field (SCF) molecular orbital methods to study the effect of H₂ chemisorption on single ion and six atom clusters of MgO in a finite point ion field chosen to give the correct Madelung potential at the surface. Their calculations predicted that the dissociative chemisorption of hydrogen cannot take

place at a nondefective (001) surface of MgO.

The results of thermal programmed desorption (TPD) experiments, ¹² IR spectra of hydrogen adsorbed on alkaline—earth oxides, ^{13,14} and theoretical investigations ^{12,15,17} has shown that, on the surface of MgO, H_2 dissociates heterolytically at adjacent, low coordinated Mg^{2+} and O^{2-} sites. For brevity, we will use the notation site1—site2 to refer to adjacent sites on the surface on which H_2 dissociates.

From the results of the TPD study cited above, Ito et al. concluded that the activity of the available surface sites increases as

$$O_{4c}-Mg_{3c} < O_{3c}-Mg_{4c} < O_{3c}-Mg_{3c}$$

where the subscripts refer to the coordination number of the atom. In subsequent work, Ito et al. 18,19 showed that methane also dissociates heterolytically at low coordinated Mg-O sites, where CH₃⁻ is bound to Mg, and H⁺ is bound to O.

Kobayashi and Yamaguchi¹⁶ and later Sawabe et al. ^{15,17} carried out ab initio molecular orbital studies on an eight atom (MgO)₄ cubic cluster to represent the local structure of the (100) surface. Møller-Plesset perturbation through second order was used to treat correlation effects. They found that H₂ readily undergoes heterolytic dissociative chemisorption at neighboring Mg_{3c}-O_{3c}. Depending on the size of the basis set employed, this process was found to be exothermic by approximately 30 kcal/mol at the SCF level and proceeded with an activation barrier of about 5 kcal/mol. Although homolytic adsorption at nearest O_{3c}-O_{3c} sites was also found to be exothermic, it is less favorable kinetically, as the SCF estimate of the activation barrier is 68 kcal/mol. A positive cooperativity effect was

a)JSPS fellow. Current address: Pacific Northwest Laboratories, P.O. Box 999, MSIN K1-95, Richland, WA 99352.

b)Pacific Northwest Laboratory is operated for the U.S. Department of Energy by Battelle Memorial Institute under Contract No. DE-AC0C-76RLO 1830.

found with respect to the adsorption of a second H_2 molecule to the cubic cluster—an important consequence with respect to the ability of MgO to catalyze the H_2/D_2 exchange reaction. Although correlation energy was found to alter the energetics considerably (inclusion of correlation often changed the calculated energies by as much as 50%), the qualitative findings regarding H_2 chemisorption onto MgO were unchanged.

With respect to the study of methyl radical formation over Li/MgO, ultrahigh vacuum (UHV) experiments were carried out by Lunsford and co-workers on methane gas passed over MgO and Li/MgO at 500 °C.²⁰ Using an electron paramagnetic resonance (EPR) spectrometer to detect methyl radical formation, they determined that lithium doping increased the catalytic activity of MgO by a factor of 2.6 to 3.5 depending on the surface area of their MgO sample.

Rodriguez et al.²¹ used ab initio SCF methods to study hydrogen atom abstraction from methane by the MgO and LiO diatomic molecules. They found that the process of hydrogen atom abstraction by either MgO or LiO was exothermic by 3 and 1 kcal/mol, respectively, and that the activation barriers were 36 and 25 kcal/mol, respectively. They ascribed the observed enhancement of the activity of the MgO catalyst upon lithium doping to this reduced barrier.

Using semiempirical methods, Mehandru et al.²² estimated the energies involved in hydrogen atom abstraction from methane on a $Mg_{21}O_{20}^{2+}$ cluster. Their study indicated that abstraction proceeded without barrier at three-, four-, and five-centered sites, and that these reactions were exothermic by 6.5, 2.5, and 2.5 kcal/mol, respectively.

In this study, we employ ab initio all-electron methods to investigate the chemisorption and transition state energies of hydrogen bound to three coordinate and four coordinate sites of MgO and Li/MgO clusters. These calculations are intended to provide a semiquantitative evaluation of the energetics involved in hydrogen atom abstraction from methane on local defects sites on the surface of MgO and Li/MgO. By comparison of the two systems, the results obtained give an indication of how lithium doping affects the chemistry (e.g., mapping of active sites, electron populations, and reaction mechanisms) of the MgO catalyst.

II. METHOD

Four clusters have been incorporated in this investigation. These included two cubic clusters (MgO)₄ and LiMg₃O₄, and two tetragonal clusters (MgO)₆ and LiMg₅O₆. These clusters are shown in Fig. 1 and 2.

In all the calculations presented, the Mg-O distance was fixed at its bulk value of 2.106 Å.²³ The relaxation of the distance between the first and second topmost layers of the (100) surface has been studied theoretically via finite cluster²⁴ and infinite slab methods,²⁵ and has been estimated to deviate 1%-2% from the bulk value. Experimental investigations of the same phenomenon predict that the relaxation is from 0% to 3%.²⁶⁻²⁸ As the purpose of employing the MgO cluster is to model the local environment of a surface defect on MgO, we did optimize the cluster as

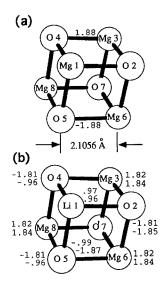


FIG. 1. (a) $(MgO)_4$. The numbers shown are the natural populations of symmetry inequivalent atoms. (b) LiMg₃O₄. Populations of all the atoms are given. The upper set of numbers are the populations for the 2A_1 state of the cluster and the lower set are for the symmetry broken $^2A'$ state.

is the case in other studies in which the relevant issue is the investigation of the electronic and geometric structure of gas phase (MgO)_n clusters.²⁹

For Li/MgO, the lithium atom was assumed to occupy the position of the magnesium atom that it replaced without relaxation. UHF calculations on the lithium trapped-hole center predicted that the ${\rm Li^+-O^{2-}}$ distance expands by about 10%, and that the ${\rm Li^+l-O^{-1}}$ center contracts by about 8% relative to the bulk Mg-O distance. As these calculations were carried out on small clusters without the rigid environment of neighboring bulk atoms, we presume that these expansions are representative of an upper bound to any actual geometrical distortions.

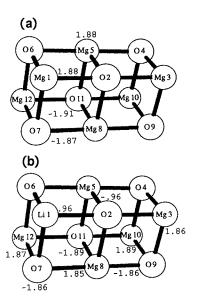


FIG. 2. (a) $(MgO)_6$; (b) $LiMg_5O_6$. The numbers shown are the natural populations of symmetry inequivalent atoms.

In Sec. III C, we evaluate the energetics for the process of hydrogen atom extraction from H₂ or CH₄ by various sites of the different model clusters. An example of such a reaction is

$$CH_4 + (MgO)_4 \rightarrow CH_3 + H - MgO_4$$
.

The evaluation of the reaction energy requires the calculation of energies for all the products and reactants in the above equation. However, the computation of the optimized geometries and energies of the reactants and CH_3 . needs to be carried out only once for the many different reactions. The product $H\text{-}Mg_4O_4$ only requires optimizing the three degrees of freedom of the hydrogen atom relative to the cluster.

For the study of chemisorption of CH₄ on MgO and Li/MgO and related transitions states, which involve the breaking of the C-H bond (Sec. III B), we used H₂ as the probe molecule rather than CH₄. The justification for this computationally less expensive approximation is that the C-H and H-H bonds are similar in nature. They are both nonpolar covalent and have similar bond strengths [103.3 kcal/mol for H₂ (Ref. 31) and 103.2 kcal/mol for CH₄ (Ref. 32)]. Additionally, in their study of the chemisorption of methane on the surface of MgO, Ito *et al.* ¹⁸ found that for both the transition and product states, the structure of the CH₃ group was essentially unchanged.

An investigation of the basis set dependence of H_2 chemidissociation on $(MgO)_4$, including split valence $(3\text{-}21G)_4$ and $(3\text{-}21G)_4$, polarized split valence $(6\text{-}31G^{**})_4$, and triple split valence basis sets $(6\text{-}311G)_4$, was carried out by Sawabe. Is It was found that the calculation of H_2 adsorption energies and optimized geometries derived from the 3-21G basis set were qualitatively the same as the results for larger basis sets. However, for some weakly physisorbed configurations of H_2 on $(MgO)_4$, diffuse s and p functions on oxygen $(\alpha_0=0.0845)$ and diffuse s functions on hydrogen $(\alpha_H=0.036)$ were necessary to accurately describe the optimized geometries. Hence, the basis employed in these calculations is a 3-21G type augmented with the diffuse functions described above.

The correlation energy of systems involving hydrogen interactions with $(MgO)_4$ and $LiMg_3O_4$ was treated at the second-order unrestricted Møller–Plesset (UMP2) level at the unrestricted Hartree–Fock (UHF) optimized geometry. Preliminary calculations indicated that the difference in the geometries and energies obtained from full UMP2 optimizations did not, for our purposes, differ significantly from the MP2 single-point method. For the remainder of this paper, we will use the notation $E_{\rm UHF}/E_{\rm UMP2}$ to report optimized UHF and single-point UMP2 energies for a given system. All energies are expressed in kilocalories per mole and distances are given in Angstroms.

These calculations were carried out using the software package GAUSSIAN 90.³⁵

III. RESULTS

Section III is divided into three parts. In Sec. III A, we give a description of the electronic states of the bare clusters employed in this study. This is necessary for pedagog-

ical reasons and also to facilitate the efforts of those who may want to try to reproduce these results. In Sec. III B, we presents results for the chemisorption of H_2 onto the cluster surfaces, and in Sec. III C, we discuss the abstraction of H from H_2 and CH_4 .

In each of the sections III A, III B, and III C, we discuss results for each of the clusters employed in this study in the following order: (MgO)₄, LiMg₃O₄, (MgO)₆, and LiMg₅O₆. (MgO)₄ and LiMg₃O₄ are employed to directly compare the effect of clusters with and without lithium. (MgO)₆ and LiMg₅O₆ are included to assess the cluster size effect on our results and to explore the chemistry of four-coordinate sites that are not present in the smaller clusters.

A. Bare clusters

The symmetry of $(MgO)_4$ belongs to the T_d point group. The ground state for this system was found to be 1A_1 .

A Mulliken population analysis of this cluster assigns a -1.30|e| charge to the oxygen atoms and a 1.30|e| charge to the magnesium atoms. The natural population analysis (NPA) of Weinhold and co-workers, ³⁶ which is a population analysis based on a localized orbital scheme, assigns a charge of -1.88|e| to the oxygen atoms and 1.88|e| to the magnesium atoms [see Fig. 1(a)]. Mulliken populations are known to give physically unreasonable results for ionic compounds ³⁷ as the off-diagonal elements of the density matrix can contribute "shared" electron density to the cations, thereby assigning too much electron density to cations and too little electron density to the anions. Therefore, all populations reported in the remainder of this paper are derived from the NPA.

The symmetry of LiMg₃O₄ is classified by the C_{3v} point group. For this cluster, the lowest energy eigenstate was found to be of broken symmetry in which the wave function was a $^2A'$ state belonging to the C_s subgroup. The lowest doublet state of nonbroken symmetry was found to be the 2A_1 state, which lies 29.5/16.9 kcal/mol higher in energy than the $^2A'$ state. The valence electronic configuration of this state is

$${}^{2}A_{1}:a_{1}^{2}a_{1}^{2}e^{4}a_{1}^{2}e^{4}a_{1}^{2}e^{4}a_{2}^{2}e^{4}a_{1}^{1}e^{4}.$$

The symmetry broken state arises when the half-filled a_1 orbital accepts an electron from the filled degenerate highest-occupied molecular orbital (HOMO). A natural population analysis of the $^2A'$ state of LiMg₃O₄ showed that the hole created by the lithium resides on one of the symmetry equivalent oxygens [O5 in Fig. 1(b); charge = -0.96]. For the 2A_1 state, the hole is found on the symmetry unique oxygen [O7 in Fig. 1(b); charge = -0.99]. $\langle S^2 \rangle$ for these systems is 0.75, but due to spin contamination inherent in the UHF wave function, $\langle S^2 \rangle$ was 0.762 and 0.758 for the 2A_1 and $^2A'$ states, respectively.

The tetragonal cell $(MgO)_6$ has D_{2h} symmetry, and the ground electronic state was found to be ${}^1A_{1g}$ [see Fig. 2(a)].

For the Li-doped analog to (MgO)₆, LiMg₅O₆, one may consider substituting a lithium atom for a three-

TABLE I. The energy of chemisorption of H₂ onto various neighboring sites in (MgO)₄, LiMg₃O₄, MgO₆, and LiMg₅O₆ NI=not investigated; NTF=no transition state found.

| Cluster | Pair site | Chemisorption energy (kcal/mol) | Transition state energy (kcal/mol) |
|----------------------------------|----------------------------------|---------------------------------|------------------------------------|
| (MgO) | O _{3c} -O _{3c} | -33.5/-22.5 | 71.7/59.5 |
| | $O_{3c}-Mg_{3c}$ | -30.4/-13.8 | 2.4/4.2 |
| LiMg ₃ O ₄ | $O_{3c}-O_{3c}$ | -114.2/-98.5 | NTF |
| | $O_{3c} - 7O_{3c}$ | -100.8/-93.5 | NI |
| | O_{3c} -Li _{3c} | -35.2/-39.3 | NI |
| | O_{3c} -Mg _{3c} | Not bound | |
| | $O7_{3c}$ -Mg _{3c} | Not bound | |
| (MgO) ₆ ª | O_{3c} -Mg _{3c} | -34.3/-16.6 | NI |
| | $O_{3c}-Mg_{4c}$ | 1.8/14.3 | NI |
| | $O_{4c}-Mg_{3c}$ | -4.0/9.5 | NI |
| LiMg ₅ O ₆ | $O2_{3c}-O6_{4c}$ | -89.6/-90.5 | NTF |

^{*}From Ref. 15.

coordinate magnesium atom Mg_{3c} , or a four-coordinate magnesium atom Mg_{4c} . The ground electronic state for a cluster in which Mg_{3c} was replaced by Li was $^2A'$ (C_s symmetry), and it was found to be 61.6 kcal/mol more

stable than the C_{2v} structure obtained by substituting Li for Mg_{4c} . Although it is not unreasonable to expect Li substitution at four-coordinate sites, we have limited this study to the more stable situation in which Li is three coordinate. For the $^2A'$ state of this cluster, the hole was located at the four-centered oxygen site [O6 in Fig. 2(b); charge =-0.96] and $\langle S^2 \rangle$ was equal to 0.755.

For all chemisorption energies reported in this paper, the bare clusters are assumed to be in the lowest energy electronic state that transform as the completely symmetric irreducible representation of that cluster's point group. In every case except for LiMg_3O_4 , this corresponds to the ground state. An ambiguity that exists in using cluster methods in theoretical chemistry resides in the choice of the electronic state of the bare cluster that best represents the electronic environment on the surface of the infinite solid. Both the 2A_1 and symmetry broken $^2A'$ states are symmetry allowed with respect to chemisorption of an S state atom at any of the available three-coordinate sites. However, the choice of 2A_1 state yielded chemisorption energies that were consistent with surface experiments and were also comparable to results obtained on the larger

TABLE II. Optimized geometries for H₂ chemisorption products, transition states, and physisorbed products on (MgO)₄, LiMg₃O₄, and LiMg₅O₆. The dihedral angle atom1-atom2-atom3-atom4 is the angle between the plane defined by atom1, atom2, and atom3 and the plane defined by atom2, atom3, and atom4.

| Cluster and symmetry | Adsorbates and site | R _{site H} (Å) | Bond angle | Dihedral angle |
|--|------------------------|-------------------------|------------------|-----------------------|
| Symmetry | and site | A _{site} H (A) | Bond angle | Dinedial angle |
| $(MgO)_4 C_{2v}$ | O2-H | 0.97 | O4-O2-H=148.4 | Mg6-O4-O2-H=180.0 |
| | O4–H | 0.97 | O2-O4-H=148.4 | Mg8-O2-O4-H=180.0 |
| $(MgO)_4 C_s$ | Mg1-H- | 1.79 | O2-Mg1-H=100.6 | Mg8-O2-Mg1-H=180.0 |
| | O2-H+ | 0.97 | Mg1-O2-H=107.7 | O7-Mg1-O2-H=180.0 |
| $(MgO)_4 C_s^{a,c}$ | Mg1-H1 | 2.13 | O2-Mg1-H=66.5 | Mg8-O2-Mg1-H=180.0 |
| | O2-H2 | 1.57 | Mg1-O2-H=654 | O7-Mg1-O2-H=180.0 |
| $(MgO)_4 C_{2v}^c$ | O2-H1 | 1.39 | O4-O2-H1 = 58.1 | Mg6-O2-O4-H1=180.0 |
| | O4-H2 | 1.39 | O2-O4-H2=58.1 | Mg8-O2-O4-H2=180.0 |
| $LiMg_3O_4C_s$ | O2-H | 0.96 | O4-O2-H=136.4 | Mg8-O4-O2-H=177.42 |
| | O4H | 0.96 | O2-O4-H=136.4 | Mg6-O2-O4-H = -177.42 |
| $LiMg_3O_4C_1$ | O5-H | 0.96 | Li1-O5-H=123.1 | Mg3-Li1-O5-H=176.4 |
| | O7-H | 0.97 | Mg3-O7-H=132.1 | Li-Mg3-O7-H=174.3 |
| $LiMg_3O_4C_s$ | Li1-H- | 2.68 | O2-Li1-H=128.2 | Mg8-O2-Li1-H=180.0 |
| | O2~H+ | 0.97 | Li1-O2-H=114.2 | Mg8-Li1-O2-H=180.0 |
| LiMg ₃ O ₄ C ₅ ^b | O2-H1 | 1.19 | Li1-O2-H1=123.3 | Mg6-O2-Li1-H1=180.0 |
| | O2-H2 | 2.11 | Li1-O2-H2=123.3 | Mg6-O2-Li1-H2=180.0 |
| LiMg ₃ O ₄ C ₅ ^b | O2-H1 | 2.61 | Li1-O2-H=126.9 | Mg6-O2-Li1-H1=180.0 |
| | O2-H2 | 3.34 | Li1-O2-H=127.8 | Mg6-O2-Li1-H2=180.0 |
| $(MgO)_6 C_1^c$ | $Mgl_{3c}-H^-$ | 1.78 | O6-Mg1-H=103.3 | O7-O6-Mg1-H=137.4 |
| | O5 _{3c} -H+ | 0.96 | Mg1-O6-H=110.1 | Mg12-Mg1-O6-H=137.4 |
| $(MgO)_6 C_s^c$ | $Mgl_{3c}-H^-$ | 1.81 | O2-Mg1-H=83.5 | Mg12-O2-Mg1-H=180.0 |
| | O2 _{4c} -H+ | 0.99 | Mg1-O2-H=72.1 | Mg12-Mg1-O2-H=180.0 |
| $(MgO)_6 C_s^c$ | O4 _{3c} -H+ | 0.97 | Mg5-O4-H=89.6 | Mg8-Mg5-O4-H=180.0 |
| | Mg5 _{4c} -H- | 1.94 | $O4-Mg_5-H=74.3$ | Mg8-O4-Mg5-H=180.0 |
| LiMg ₅ O ₆ C ₁ | O2 _{4c} -H | 0.97 | Li1-O2-H=137.2 | O11-Li1-O2-H=181.8 |
| | O6 _{3c} -H | 0.96 | Li1-O6-H=117.8 | O11-Li1-O6-H=182.2 |
| LiMg ₅ O ₆ C ₁ ^a | O6-H1 | 1.20 | Li1-O6-H1=125.2 | Mg12-O6-Li1-H1=178.2 |
| | O6H2 | 2.11 | Li1-O6-H2=125.8 | Mg12-O6-Li1-H2=182.4 |
| LiMg ₅ O ₆ C ₁ ^b | O6-H1 | 2.60 | Li1-O6-H1=119.0 | Mg12-O6-Li1-H1=171.4 |
| | O6-H2 | 3.34 | Li1-O6-H2=119.0 | Mg12-O6-Li1-H1=171.4 |
| LiMg ₅ O ₆ C ₁ * | O2-H1 | 1.20 | Li1-O2-H1=73.3 | O11-O2-Li1-H1=180.0 |
| | O2-H2 | 2.12 | Li1-O2-H1=73.7 | O11-O2-Li1-H2=180.0 |

^{*}Transition state.

^bPhysisorbed state.

From Ref. 15.

LiMg₅O₆ cluster for which only the $^2A'$ state was symmetry allowed.³⁸ (In addition, we carried out cursory calculations on a still larger Li-doped cluster LiMg₇O₈ and the results were again consistent with the two smaller Li-doped clusters 2A_1 LiMg₃O₄ and $^2A'$ LiMg₅O₆.)

The explanation we give for this behavior is that from the NPA, we observe that for the ${}^{2}A'$ state, the electron hole created by the Li dopant resides on one of the symmetry equivalent, three-coordinate, neighboring oxygens this being the site which we will use to study chemisorption and abstraction of H from H2 and CH4. However, for LiMg₅O₆ (and for LiMg₇O₈ mentioned parenthetically above), the three-coordinate oxygen sites neighboring Li are filled, and it is the four-coordinate neighboring oxygen which is one electron deficient. To get proper convergence in the calculated chemisorption energies, it is necessary that the state chosen to represent the bare cluster be such that the electronic structure in the environment near the adsorption site be similar as the size of the cluster is increased. This point has been more thoroughly discussed by Panas et al. in a recent paper on the evaluation of chemisorption energies from cluster models.³⁹

B. Chemisorption of H₂

1. (MgO)4

The reaction

$$H_2+(MgO)_4\rightarrow H_2(MgO)_4$$

has been studied extensively by other workers. 15-17 We recapitulate many of their findings below, as we will later compare them to the Li-doped systems.

In Table I, the chemisorptions energies for H_2 onto $(MgO)_4$ and other clusters incorporated in this study are given. By chemisorption energy, we mean the calculated energies of products minus reactants as, e.g., in the equation shown above. In Table II, data are given specifying the UHF optimized geometries of these systems.

For chemisorption of H_2 onto $(MgO)_4$, it was found that the most exothermic process is one in which H_2 homolytically dissociates onto neighboring oxygen sites across a face of the $(MgO)_4$ cube O_{3c} — O_{3c} . Also exothermic, but 3.1/8.7 kcal/mol less stable, was heterolytically chemisorbed H_2 at neighboring oxygen and magnesium sites along an edge of the cube Mg_{3c} — O_{3c} .

However, it was also discovered that the transition state energy to homolytic dissociation at O_{3c} – O_{3c} was 59.5/71.7 kcal/mol, but the transition state barrier to heterolytic dissociation at Mg_{3c} – O_{3c} was only 4.2/2.4 kcal/mol, so it is predicted that undoped MgO dissociation of H_2 occurs primarily heterolytically. Figures 3(a) and 3(b) depict the geometries of the abovementioned transition states.

2. LiMg₃O₄

We turn our attention to the study of the reaction

$$H_2 + LiMg_3O_4 \rightarrow H_2LiMg_3O_4$$
.

We shall see that the mechanism of H_2 dissociation is dramatically changed upon lithium doping.

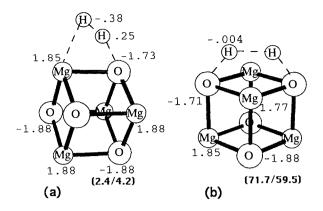


FIG. 3. (a) The transition state for heterolytic dissociation of H_2 and neighboring O_{3c} Mg_{3c} sites. (b) Transition state homolytic dissociation of H_2 at two O_{3c} sites. The numbers in parentheses are the SCF/MP2 energies relative to free H_2 and the bare cluster expressed in kilocalories per mole. The other numbers give the natural populations of symmetry inequivalent atoms. Geometries of these states are given in Table II.

As was the case for $(MgO)_4$, the most stable product occurs when H_2 is homolytically adsorbed at two neighboring oxygen sites on a face of the cluster. However, H_2 was not found to chemisorb at all on neighboring magnesium and oxygen sites. Interestingly, our attempt to force H_2 to chemisorb on an edge of the $LiMg_3O_4$ cube was initiated at the optimized geometry for H_2 adsorbed on the edge of $(MgO)_4$, but the optimization algorithm followed the gradient of the energy downhill to the O_{3c} - O_{3c} product.

For LiMg₃O₄, there are two symmetry inequivalent faces on which H₂ may adsorb on neighboring oxygen sites. Adsorption at the O2–O4 pair site was found to be 13.4/5.0 kcal/mol more stable than adsorption at the O2–O7 pair site [see Fig. 1(b) for the numbering scheme]. We have included the results for adsorption at the O2–O7 mainly for completeness. If we consider the LiMg₃O₄ as a model for an island on the Li/MgO surface with the lithium atom situated at a three-coordinate site, then the hydrogen atom optimized at O7 would lie in the subsurface, and this is not a system of interest for this study.

For (MgO)₄, we found that there was a large barrier to chemisorption at neighboring oxygen sites. So the question naturally arises: If LiMg₃O₄ can no longer support heterolytic dissociation, is there also a large barrier to homolytic dissociation as observed in the undoped (MgO)₄ analog? We found that H₂ can dissociate homolytically on the Li-doped cluster without a barrier. A discussion on this finding is given below.

We began the search for a transition state to O_{3c} - O_{3c} adsorption by positioning the H_2 molecule at various distances above a face of the LiMg₃O₄ cluster with the H_2 bond stretched so that the oxygen-to-hydrogen distance was about 0.97 Å. No *a priori* symmetry was assumed (i.e., the calculations were carried out using C_1 symmetry). When the transition state search was begun with the H_2 center of mass far from the face of the cluster (e.g., greater than 1 Å), the center of mass of the molecule moved further away from the cluster at every optimization step. When the search was begun close to the surface of the

TABLE III. The energy of abstraction of $H \cdot H^+$, and H^- from H_2 and CH_4 onto various sites of $(MgO)_4$, $LiMg_3O_4$, and $LiMg_5O_6$. The binding energy is obtained by subtracting D_e for homolytic or heterolytic dissociation of H_2 from the abstraction energy.

| | | Adsorption | Abstraction ener | Binding | | |
|----------------------------------|----------------|------------------|------------------|-----------------|-------------------|--|
| Cluster | Adsorbate | site | H ₂ | CH ₄ | energy (kcal/mol) | |
| (MgO) ₄ | Н· | O _{3c} | 79.4/90.1 | 85.6/100.2 | -0.8/-1.0 | |
| | H+ | O _{3c} | 127.5/146.4 | 186.1/204.8 | -272.8/-256.0 | |
| | H- | Mg_{3c} | 337.4/334.1 | 240.0/247.4 | -62.9/-68.3 | |
| LiMg ₃ O ₄ | Η· | O _{3c} | -34.6/-38.5 | -28.4/-28.4 | -114.8/-129.6 | |
| 0, 4 | H· | O7 _{3c} | -8.9/-23.1 | -2.7/-12.9 | -89.1/-114.2 | |
| | Н٠ | Li _{3c} | | Not bound | | |
| | H+ | O_{3c} | 106.2/113.8 | 164.7/172.2 | -294.1/-288.6 | |
| | H | Mg_{3c} | 314.4/321.2 | 217.9/234.4 | -85.9/-81.2 | |
| | \mathbf{H}^- | Li _{3c} | 350.9/359.4 | 254.4/272.7 | -49.4/-43.0 | |
| LiMg ₅ O ₆ | H· | O6 _{3c} | -42.0/-55.1 | -35.8/-44.9 | -122.2/-146.2 | |
| | Η· | $O2_{4c}$ | -6.0/-21.3 | 0.1/-11.6 | -86.2/-112.4 | |

cluster, the H_2 molecule was absorbed into the interior. In the former case, the transition state search led to the energy of dissociated H_2 unperturbed by MgO, and in the latter case, the transition state search led to the absorption barrier of H_2 through the surface of the cluster. No transition state connecting free H_2 to the homolytic adsorption product was found.

Next, we attempted a search for a local minimum on the potential surface. This time the H_2 bond length was started at the experimental value of 0.741 Å, and the center of mass of the H_2 molecule was placed 1 Å above the surface of the cluster. Again the orientation of H_2 was chosen so as to possess only C_1 symmetry. A geometry optimization, following the gradient of the energy downhill via the Berney optimization algorithm, ⁴⁰ led directly to the O_{3c} – O_{3c} adsorption state discussed above. Hence, we conclude that H_2 may dissociate homolytically on LiMg₃O₄ without a barrier.

3. (MgO)₆

The study of H_2 chemisorption presented here is taken directly from the work of Sawabe¹⁵ and is reproduced here so that the results may be compared to chemisorption of H_2 on $LiMg_5O_6$ in the next section.

From Table I, it can be seen that the difference in the calculated chemisorption energy of H_2 at the O_{3c} - Mg_{3c} site going from the $(MgO)_4$ to $(MgO)_6$ cluster is 3.9/2.8 kcal/mol. This represents a 11%/17% change in the calculated energies and gives us some feeling for the magnitude of the cluster size effect.

Also from Table I, we see that when one of the hydrogens is adsorbed at a four-coordinate site, the calculated chemisorption energy is reduced. Compared to chemisorption in which both hydrogens are bonded to three-coordinate sites, chemisorption in which one of the hydrogens is bonded at a four-coordinate site is from 23 to 31 kcal/mol less stable. In fact, this type of chemisorption is predicted to be endothermic except in the case of the SCF evaluation of the chemisorption energy of H_2 at a Mg_{3c} – O_{4c} site

A study of homolytic dissociation of H₂ onto neighboring O_{3c}-O_{4c} sites was not carried out, since even if a stable product were found, it is expected that there would be a large energy of activation. This result is anticipated since, as we have already seen, there exists a large barrier to dissociation on neighboring oxygen sites on (MgO)₄, and the increase in coordination of one of the oxygens is unlikely to reduce this barrier. Therefore, our conclusion that MgO supports mainly heterolytic dissociation at neighboring Mg and O sites remains the same.

4. LiMg₅O₆

In LiMg₅O₆, it was found that chemisorption involving the O_{4c} site reduces the chemisorption energy compared to chemisorption involving only three-coordinate sites by 24.6/8.0 kcal/mol (see Table I). However, in contrast to the results found for the undoped (MgO)₆ cluster, there is still a strongly exothermic chemisorbed product (-89.6/-90.5 kcal/mol) with hydrogens adsorbed at neighboring O_{3c} and O_{4c} sites.

We were neither able to find a transition state connecting free H₂ and the bare cluster to the chemisorbed product at the O_{3c}-O_{4c} site, nor did it appear that H₂ could dissociate without a barrier onto this site. Specifically, we began by using the Berny optimization algorithm to search for a transition state to the chemisorption of H₂ to neighboring three-coordinate and four-coordinate oxygen sites. The hydrogen was placed at varying distances away from the cluster with the ends directed towards the three- and fourcoordinate oxygen. Likewise, we attempted optimization runs starting from similar initial starting points to determine if simultaneous chemisorption at three- and fourcoordinate sites could be obtained without a barrier. These geometry searches led to states involving the abstraction of a single hydrogen from H₂ at either the three- or fourcoordinated oxygen site, but not to states connecting free H₂ to a chemisorbed product in which both hydrogens were adsorbed to the surface. Further discussion on hydrogen atom abstraction from H2 onto the Li-doped clusters will be given in Sec. IV.

Cluster and Adsorbates R_{site H} (Å) Dihedral angle and site Bond angle symmetry . . . $(MgO)_4 C_{3v}$ O2-H 2.62 . . . O2-H.+ 0.97 Mg1-H 1.84 LiMg₃O₄ C₅ O2-H 0.97 Li1-O2-H=114.2O7-Li1-O2-H = 180.0LiMg₃O₄ C_{3v} O7-H 0.97 O7-Li-O2-H=180.00.98 LiMg₃O₄ C_s O2-H+ Li-O2-H=116.0LiMg₃O₄ C_{3v} Li1-H-2.84 LiMg₃O₄ C_s Mg3-H-1.85 O7-Mg3-H=121.6Li1-O7-Mg3-H=180.0LiMg₅O₆ C₁ $O6_{3c}$ 0.96 Li1-O6-H=116.3O11-Li1-O6-H=181.8LiMg₅O₆ C_s 0.97 Li1-O2-H=69.9O7-Li1-O2-H = 180.0 $O2_{4c}$

TABLE IV. Optimized geometries for H^+ , H^+ , and H^- on various sites of $(MgO)_4$, $LiMg_3O_4$, and $LiMg_5O_6$. For complexes with C_{3v} symmetry, the bond is collinear with the C_3 axis.

C. Abstraction of H., H⁺, and H⁻ from H₂ and CH₄

1. (MgO)4

In this section, we present a study of the abstraction of hydrogen by MgO from either H_2 or CH_4 . Specifically, we will look at the energetics of reactions of the type

$$XH + (MgO)_4 \rightarrow X \cdot + H(MgO)_4$$
(adsorbed at the O site)

(homolytic dissociation),

$$XH + (MgO)_4 \rightarrow X^- + H(MgO)_4^+$$
(adsorbed at the O site)

(heterolytic dissociation),

and

$$XH + (MgO)_4 \rightarrow X^+ + H(MgO)_4^-$$
(adsorbed at the Mg site)

(heterolytic dissociation),

where $X = CH_3$ or H.

In Table III, results are presented for the abstraction energy (the energy of the products minus the reactants for the equations displayed above) of $H \cdot$, H^+ , and H^- from both H_2 and CH_4 . The UHF optimized geometries and natural populations for these systems are given in Tables IV and V, respectively.

To evaluate the binding energy of the hydrogen atom adsorbate, one should subtract D_e for homolytic dissociation of H_2 (80.2/91.1 kcal/mol) from the H^+ abstraction energy given in column four of Table III. Likewise, to estimate the binding energy of either the H^+ or H^- adsorbate, one should subtract D_e for the heterolytic dissociation of H_2 (400.3/402.4 kcal/mol) from either the H^+ or H^- abstraction energy given in the same table and column. (A negative binding energy is indicative of a bound state of the adsorbate.)

As can be seen from the positive values for the energies listed in Table III for $(MgO)_4$, the energy given back to the formation of a single adsorbate to cluster atom bond does not compensate for the energy required to homolytically or heterolytically break either the H-H or C-H bond. However, after subtraction of D_e , we observe that the binding energies for all the species shown in Table III are negative, and the bond strengths follow the order

$$H^+ > H^- > H \cdot$$
.

At the MP2 level, the binding energies are -256.0 kcal/mol (O-H⁺), -68.3 kcal/mol (Mg-H⁻), and -1.0 kcal/mol (O-H).

From Table V, we may observe that this trend in the binding energies varies directly as the amount of electron density donated from the hydrogen species to the cluster.

TABLE V. Natural populations for systems in which $H \cdot H^+$, and H^- are adsorbed onto various sites of $(MgO)_4$ and $LiMg_3O_4$.

| | Adsorption sites for H, H ⁺ , and H ⁻ | | | | | | | |
|-----|---|-------|-------|----------------------------------|-------|-------|-------|--------|
| | (MgO) ₄ | | | LiMg ₃ O ₄ | | | | |
| | O2-H | O2-H+ | Mg1-H | O2-H | O7-H | O2-H+ | Mg3-H | Lil-H |
| Lil | ••• | • • • | ••• | 0.97 | 0.97 | 0.94 | 0.96 | 0.97 |
| Mgl | 1.88 | 1.75 | 1.75 | ••• | | ••• | | ••• |
| 02 | -1.88 | -1.35 | 1.86 | -1.45 | -1.82 | -1.47 | -1.82 | 1.86 |
| Mg3 | 1.88 | 1.76 | 1.85 | 1.84 | 1.82 | 1.89 | 1.76 | 1.84 |
| 04 | -1.88 | 1.70 | -1.86 | -1.85 | -1.82 | -1.36 | -1.81 | 1.86 |
| O5 | -1.88 | 1.70 | -1.86 | -1.85 | -1.82 | -1.36 | -0.97 | -1.86 |
| Mg6 | 1.88 | 1.76 | 1.85 | 1.84 | 1.82 | 1.89 | 1.78 | 1.84 |
| 07 | -1.88 | -1.78 | -1.89 | —1.87 | -1.46 | -1.86 | -1.84 | - 1.89 |
| Mg8 | 1.88 | 1.78 | 1.85 | 1.88 | 1.82 | 1.82 | 1.78 | 1.84 |
| н | -0.006 | 0.42 | -0.83 | 0.49 | 0.50 | 0.52 | -0.84 | 0.002 |

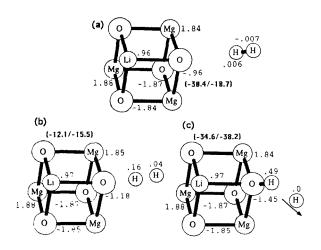


FIG. 4. (a) Physisorbed and (b) transition states of H_2 . (c) H atom abstracted from H_2 and adsorbed at O_{3c} . The numbers in parentheses are the SCF/MP2 energies relative to free H_2 and the bare cluster expressed in kilocalories per mole. Other numbers give the the natural populations of symmetry inequivalent atoms. Geometries of these states are given in Table II.

This quantity is given by the difference in the formal charge of the hydrogen species (viz., +1, -1, and 0) from the population of the adsorbed hydrogen species. For (MgO)₄, the amount of electron density donated is 0.58, 0.17, and -0.006 for H⁺, H⁻, and H·, respectively.

2. LiMg3O4

We next consider the hydrogen abstraction reactions for a Li-doped system

$$XH + LiMg_3O_4 \rightarrow X \cdot + HLiMg_3O_4$$
(adsorbed at O or Li)

(homolytic dissociation),

$$XH + LiMg_3O_4 \rightarrow X^- + HLiMg_3O_4^+$$

(heterolytic dissociation),

and

$$XH + LiMg_3O_4 \rightarrow X^+ + HLiMg_3O_4^-$$
(adsorbed at Mg or Li site)

(heterolytic dissociation)

where $X = CH_3$ or H.

From Table III, we observe that for the abstraction of $H \cdot \text{from } H_2$ or CH_4 and subsequent adsorption of $H \cdot \text{at}$ O_{3c} that the reaction energy is negative. That is, even given the highly reactive hydrogen atom or methyl radical byproduct, these calculations predict that these reactions proceed exothermically.

A search for a transition state to this process was carried out. For the hydrogen molecule, it was discovered that the molecule is first physisorbed at 2.61 Å away from the O_{3c} site with an energy of -30.4/-18.7 kcal/mol. A transition state at -12.1/-15.5 kcal/mol was found in which the shortest distance from the H_2 to the O_{3c} site was reduced to 1.19 Å and the H-H bond length was stretched to 0.92 Å. A diagram of this process is shown in Fig. 4. The

barrier to abstraction is given by the difference in energy of the physisorbed state from the transition state (i.e., 18.3/3.2 kcal/mol).

As noted in Table III, the hydrogen atom is not bound to the Li_{3c} site, but the hydride ion is bound. The binding energy of this hydride is -49.4/-43.0 kcal/mol. However, the population analysis shown in Table V indicates that the charge on the "hydride" is only 0.002. That is, the excess charge initially carried by the hydride ion is completely donated to the LiMg_3O_4 cluster.

Table III also indicates that chemisorbed states are possible for H^+ bound to O_{3c} and H^- bound to Mg_{3c} or Li_{3c} . However, as with $(MgO)_4$, although the binding energy is positive—294.1/288.6 kcal/mol for H^+ – O_{3c} , 85.9/81.2 kcal/mol for H^- – Mg_{3c} , and 49.4/43.0 kcal/mol for H^- – Li_{3c} —the processes of heterolytic abstraction of a single hydrogen ion from H_2 or CH_4 is a highly endothermic process.

3. LiMg₅O₆

Table III shows that on LiMg₅O₆, a hydrogen atom can be abstracted from $\rm H_2$ or CH₄ exothermically at either an O6_{3c} or O2_{4c} site. At the SCF level, the CH bond was found to be nearly equal in strength to the H-O_{4c}2 bond. At the MP2 level, the H-O_{4c}2 bond was somewhat stronger by 11.6 kcal/mol. Transition states for abstraction at both the O_{3c} and O_{4c} sites were located and are discussed below.

It was found that the process of hydrogen atom abstraction onto an O_{3c} site of LiMg₅O₆ was very similar to the same process for LiMg₃O₄ depicted in Fig. 4. A bound state of H_2 at a long distance (2.60 Å) from an O_{3c} site was discovered with an adsorption energy of -37.1/-34.3kcal/mol. The geometry optimization of this state was computationally very expensive. In addition to the fact that 158 basis functions were employed, the geometry of this state carried only C_1 symmetry and the potential energy surface for the nuclear coordinates in the region of the energy minimum was relatively flat, so that small steps had to be taken to find the optimized structure. In order to make the problem computationally tractable, it was necessary to only partially optimize the H₂ coordinates. That is, the H₂ center of mass coordinates were optimized, but the H₂ internal coordinates were set equal to those obtained from the optimization of H_2 relative to the O_{3c} site in LiMg₃O₄ discussed above. Specifically, the H-H distance was set to 0.746 Å and the internal, angular coordinates were fixed so that the line of the H₂ molecule was pointed directly at the $O_{3c}6$ site.

A transition state was located with an energy of -19.2/-31.3 kcal/mol in which the shortest distance from the hydrogen to the O_{3c} was 1.20 Å and the H-H distance was stretched to 0.92 Å. The barrier to hydrogen abstraction at an O_{3c} site is given by the difference in energy of the physisorbed state discussed in the preceding paragraph and this transition state (i.e., 17.9/3.0 kcal/mol). This is in close agreement to the same barrier determined using LiMg₃O₄ discussed in Sec. III O 2 (viz. 18.3/3.2 kcal/mol).

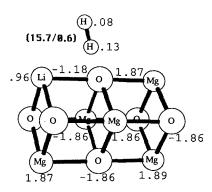


FIG. 5. The transition state for the abstraction of hydrogen from H_2 onto an O_{4c} site. The numbers in parentheses are the SCF/MP2 energies relative to free H_2 and the bare cluster expressed in kilocalories per mole. Other numbers give the natural populations of the symmetry inequivalent atoms. The geometry of this state is given in Table II.

At the O_{4c} site, the transition state was such that the distance between the O_{4c} site and the hydrogen was 1.20 Å, the H-H distance was 0.92 Å, and the barrier height was 15.7/0.6 kcal/mol. No physisorbed state near O_{4c} was found, so that this energy directly gives the barrier to hydrogen atom abstraction from H_2 at an O_{4c} site. A diagram of this transition state is shown in Fig. 5.

IV. DISCUSSION

The chemistry of the MgO catalyst is markedly different from the Li/MgO catalyst. On MgO, we have seen that H_2 dissociates heterolytically on neighboring three-coordinate Mg and O sites, and possibly undergoes heterolytic dissociation at O_{3c} -Mg_{4c} or O_{4c} -Mg_{3c} sites. In contrast, no heterolytic dissociation at neighboring oxygen and magnesium sites was observed in Li/MgO. Instead, we found that the H-H bond could be cleaved without a barrier at proximal O_{3c} - O_{3c} sites and that a hydrogen atom could be abstracted from H_2 or CH_4 at either an O_{3c} or O_{4c} site.

At the end of Sec. III B 4, we noted that no transition state was found for the direct dissociation and subsequent chemisorption of H_2 at an O_{3c} – O_{4c} site. Nor did we find that H_2 chemidissociated onto these sites without a barrier. That is, the following reaction does not appear to be possible in a single step

$$H_2 + O_{3c} + O_{4c} \rightarrow HO_{3c} + HO_{4c}$$
.

From our study of the transition state to abstraction of $H \cdot \text{from } H_2 \text{ or } CH_4$, it appears that the pathway to the product found in Sec. III B 4 could result from two separate abstraction events at O_{3c} and O_{4c} . That is,

$$H_2 + O_{3c} + O_{4c} \rightarrow HO_{3c} + O_{4c} + H$$
,

$$H_2 + O_{3c} + O_{4c} + H \rightarrow HO_{3c} + HO_{4c} + 2H \cdot .$$

Another plausible mechanism is that hydrogen atoms generated as products abstraction could migrate to other three- or four-coordinated sites and be adsorbed. For example,

$$H_2+O_{3c}+O_{4c}\to HO_{3c}+O_{4c}+H\cdot,$$

 $HO_{3c}+O_{4c}+H\cdot\to HO_{3c}+HO_{4c}.$

The increase of the catalytic activity of MgO upon Li doping does not appear to be a consequence of lowering the transition state barrier to C-H or H-H bond breaking, as has been previously suggested. In fact, it was found that the transition barrier to heterolytic dissociation at O_{3c} -Mg_{3c} was negligibly low at 2.4/4.2 kcal/mol.

We observed that MgO does not support a pathway to hydrogen atom abstraction for either H₂ or CH₄. Additionally, Ito et al., using theoretical methods similar to the ones presented in this work, concluded that CH₄ dissociates heterolytically on clean MgO with CH₃ bound to Mg and H⁺ bound to O.¹⁸ A possible mechanism for the formation of higher order alkanes from methane passed over a clean MgO catalyst that is not in disagreement with either of these observations is one in which adsorbed CH₃ groups combine on the surface and deadsorb in the gas phase as C₂H₆. For Li/MgO systems, methyl radicals or hydrogen atoms are generated directly into the gas phase via hydrogen atom abstraction and may combine with other radicals so generated. Such a difference in the mechanisms of reaction could account for the observed difference in the activity of Li/MgO relative to MgO.

In our study, we assumed that the Li dopant was located at a three coordinate site. Let us suppose for the moment that the ability of the Li/MgO cluster would still be able to support an abstraction mechanism at O_{3c} and O_{4c} sites even if Li were situated at a more highly coordinated position. (This is not an unreasonable supposition since the primary function of the Li dopant is to provide reactive Li⁺O⁻ centers—a function that it should be able to carry out regardless of its coordination.)

If this is the case, we also note that Li/MgO provides many more sites, whereby the H-H or C-H bond may be cleaved. In MgO, two neighboring sites on the surface had to fulfill the condition that they be triply or quadruply coordinated in order for the site to be active. Whereas for Li/MgO, if a Li atom is proximal, dissociation may occur at an O_{3c} or O_{4c} site regardless of the coordination of the neighboring atoms. This, then is a second way in which Li doping may increase the catalytic activity of MgO.

ACKNOWLEDGMENTS

We would like to thank Dr. K. Sawabe and Dr. N. Koga for very helpful discussions and comments. JLA would like to acknowledge the Japan Society for the Promotion of Science for his postdoctoral fellowship. The present research is in part supported by a grant in aid from the Ministry of Education, Science and Culture, Japan. Some of the calculations were carried out at the Computer Center for the Institute for Molecular Science. ACH wishes to thank the Advanced Industrial Concepts Division of the Office of Conservation and Renewable Energies (Contract No. 16697) for its support of this study. The Division of Chemical Sciences Office of Basic Energy Research, U.S. Department of Energy is acknowledged for

access to computational facilities. We also wish to acknowledge Pacific Northwest Laboratory for the funding of proposal LDRD 90001.

- ¹M. Boudart, A Delbouille, E. G. Derouane, V. Indovina, and A. B. Walters, J. Am. Chem. Soc. 94, 6622 (1972).
- ²D. C. Foyt and J. M. White, J. Catal. 47, 260 (1977).
- ³S. H. C. Liang and I. D. Gay, J. Catal. 101, 293 (1986).
- ⁴Y. Tanaka, Y. Imizu, and K. Tanabe, Proceedings of the 7th International Congress on Catalysis, Kodansha, Tokyo, 1254, 1981.
- ⁵T. Shido, K. Asakura, and Yasuhiro Iwasawa, J. Catal. 122, 55 (1990).
- ⁶J. L. Lemberton, G. Perot, and M. Guisnet, J. Catal. 89, 69 (1984).
- ⁷J. L. Limberton, G. Perot, and M. Guisnet, J. Catal. 117, 416 (1989).
- ⁸T. Ito and J. H. Lunsford, Nature 314, 721 (1985).
- ⁹T. Ito, J.-X. Wang, and J. H. Lunsford, J. Am. Chem. Soc. 107, 5062 (1985).
- ¹⁰P. F. Nelson and N. W. Cant, J. Phys. Chem. 94, 3756 (1990).
- ¹¹E. A. Colbourn and W. C. Mackrodt, Surf. Sci. 117, 571 (1982).
- ¹²T. Ito, M. Kuramoto, M. Yoshioka, and T. Tokuda, J. Phys. Chem. 87, 4411 (1983).
- ¹³S. Coluccia, F. Boccuzzi, G. Ghiotti, and C. Mirra, Z. Phys. Chem. N. F. 121, 141 (1980).
- ¹⁴S. Coluccia, F. Boccuzzi, and C. Morterra, J. Chem. Soc., Faraday Trans. 1 78, 2111 (1982).
- ¹⁵Kyoichi Sawabe, Ph.D. thesis, University of Tokyo, 1990.
- ¹⁶H. Kobayashi and M. Yamaguchi, J. Phys. Chem. 94, 7206 (1990).
- ¹⁷ K. Sawabe, N. Koga, K. Morokuma, and Y. Iwasawa, J. Chem. Phys. 97, 6871 (1992).
- ¹⁸ T. Ito, T. Tashiro, M. Kawasaki, K. Toi, T. Watanabe, and K. Kobayashi, J. Phys. Chem. 95, 4476 (1991).
- ¹⁹T. Ito, T. Tashiro, T. Watanabe, K. Toi, and I. Ikemoto, Chem. Lett. 9, 1723 (1987).
- ²⁰D. J. Driscoll, W. Martir, J. Wang, and Jack Lunsford, J. Am. Chem. Soc. 107, 58 (1985).
- ²¹ J. Rodriguez, Y. Aray, and F. Ruette, J. Mol. Struct. 210, 323 (1990).
- ²²S. P. Mehandru, A. B. Anderson, and J. F. Brazdil, J. Am. Chem. Soc. 110, 1715 (1988).

- ²³R. W. G. Wyckoff, *The Structure of Crystals* (American Chemical Society, New York, 1931).
- ²⁴E. A. Colbourn and W. C. Mackrodt, Solid State Ion. 8, 221 (1983).
- ²⁵ M. Causà, R. Dovesi, C. Pisani, and C. Roetti, Surf. Sci. 175, 551 (1986).
- ²⁶M. R. Welton-Cook and W. Berndt, J. Phys. C 15, 5691 (1982).
- ²⁷T. Urano, T. Kanaji, and M. Kaburagi, Surf. Sci. 134, 109 (1983).
- ²⁸P. A. Maksym, Surf. Sci. 149, 157 (1985).
- ²⁹ A. Ayuela and A. B. Kunz, J. Chem. Phys. 98, 4783 (1993).
- ³⁰Jun Zuo and Ravinda Pandey, Phys. Rev. B 44, 7187 (1991).
- ³¹ K. P. Huber and G. Herzberg, Molecular Spectra and Molecular Structure IV. Constants of Diatomic Molecules (Van Nostrand-Reinhold, New York, 1979).
- ³² D. G. Leopold, K. K. Murray, A. E. S. Miller, and W. C. Lineberger, J. Chem. Phys. 83, 4861 (1985).
- ³³ W. J. Hehre, L. Radom, R. v. R. Schleyer, and J. A. Pople, Ab Initio Molecular Orbital Theory (Wiley, New York, 1986).
- ³⁴T. H. Dunning, Jr. and P. J. Hay, in *Modern Theoretical Chemistry*, edited by H. F. Schaefer III (Plenum, New York, 1977), Vol. 3, Chap.
- ³⁵ M. J. Frisch, M. Head-Gordon, G. W. Trucks, J. B. Foresman, H. B. Schlegel, K. Raghavachari, M. Robb, J. S. Binkley, C. Gonzalez, D. J. Defrees, D. J. Fox, R. A. Whiteside, R. Seeger, C. F. Melius, J. Baker, R. L. Martin, L. R. Kahn, J. J. P. Stewart, S. Topiol, and J. A. Pople, GAUSSIAN 90, Gaussian, Inc., Pittsburgh PA, 1990, revision 1.
- ³⁶ A. E. Reed, R. B. Weinstock, and F. A. Weinhold, J. Chem. Phys. 83, 735 (1985).
- ³⁷J. B. Collins and A. Streitweiser, J. Comput. Chem. 1, 81 (1980).
- ³⁸ For example, using the $^2A'$ state as a reference yields chemisorption energies indicating that the four-coordinate oxygen is more active than the three-coordinate site. The converse is found if we use the 2A_1 state as a reference—a result which is in agreement with previous theoretical and experimental findings.
- ³⁹ I. Panas, J. Schüle, P. Siegbahn, and U. Wahlgren, Chem. Phys. Lett. 149, 265 (1988).
- ⁴⁰H. B. Schlegel, J. Comput. Chem. 3, 214 (1982).