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Isotopic fractionation in proteins as a measure of hydrogen bond length

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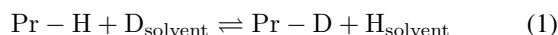
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If a deuterated molecule containing strong intramolecular hydrogen bonds is placed in a hydrogenated solvent it may preferentially exchange deuterium for hydrogen. This preference is due to the difference between the vibrational zero-point energy for hydrogen and deuterium. It is found that the associated fractionation factor Φ is correlated with the strength of the intramolecular hydrogen bonds. This correlation has been used to determine the length of the H-bonds (donor-acceptor separation) in a diverse range of enzymes and has been argued to support the existence of short low-barrier H-bonds. Starting with a potential energy surface based on a simple diabatic state model for H-bonds we calculate Φ as a function of the proton donor-acceptor distance R . For numerical results, we use a parameterization of the model for symmetric O-H \cdots O bonds [*Chem. Phys. Lett.*, **535**, 196 (2012)]. We consider the relative contributions of the O-H stretch vibration, O-H bend vibrations (both in plane and out of plane), tunneling splitting effects at finite temperature, and the secondary geometric isotope effect. We compare our total Φ as a function of R with NMR experimental results for enzymes, and in particular with an empirical parametrization $\Phi(R)$, used previously to determine bond lengths.

I. INTRODUCTION

The issue of low-barrier hydrogen bonds in proteins and whether they play any functional role, particularly in enzyme catalysis, is controversial [1–7]. Identifying such short hydrogen bonds, characterised by a donor-acceptor distance of $R \simeq 2.45 - 2.65$ Å, is not completely straightforward.[8] In protein X-ray crystallography, the standard errors in interatomic distances are about 10 to 30 per cent of the resolution. Hence, for an X-ray structure with 2.0 Å resolution, the standard errors in the distances are $\pm(0.2 - 0.6)$ Å. This uncertainty makes it difficult to distinguish between short strong bonds and the more common weak long bonds, with $R > 2.8$ Å[9]. NMR provides an alternative method of bond length determination via the ^1H chemical shift. An independent NMR “ruler” involves isotopic fractionation, where one measures how much the relevant protons (H) exchange with deuterium (D) in a solvent.



Here Pr-H denotes a protein with a proton in the relevant hydrogen bond. The fractionation ratio can also be determined from UV spectroscopy [10].

The fractionation ratio is equilibrium constant of Eq. (1):

$$\Phi \equiv \frac{[\text{Pr} - \text{D}][\text{H}_{\text{solvent}}]}{[\text{Pr} - \text{H}][\text{D}_{\text{solvent}}]} \quad (2)$$

Translated into partition functions, Φ is essentially determined by the relative zero-point energy (ZPE) of a D relative to an H in the protein. As described by Kreevoy and Liang [10], the ratio is given by

$$k_B T \ln \Phi = Z_{\text{H-Pr}} - Z_{\text{D-Pr}} + Z_{\text{D,solvent}} - Z_{\text{H,solvent}} \quad (3)$$

where T is the temperature and $Z_{\text{H-Pr}}$ denotes the zero-point energy of a proton participating in the relevant hydrogen bond in the protein. Throughout this paper we set $T = 300$ K.

Fractionation is a purely quantum effect. If the nuclear dynamics were classical, the fractionation ratio would be one. It would also be one if there were no changes in the vibrational frequencies — more correctly, zero-point energies — of both H and D when they moved from the solvent to the protein. However, the vibrational potentials *are* different in the two environments. The donor-acceptor distance, R , is typically shorter in the protein, indicating a stronger H-bond and a softer X-H stretch potential (X is the H-bond donor). Consequently, the difference between H and D zero-point energies gets larger [11], and Φ gets smaller with decreasing R . However, for very short bonds, typically when the donor and acceptor share the H or D atoms, the stretch frequencies begin to harden and Φ starts to increase. Φ would then have a non-monotonic dependence on R [12].

Mildvan and collaborators [8, 13] considered a particular parametrisation of the H-bond potential to connect the observed fractionation ratio with donor-acceptor bond lengths in a range of proteins. They generally find reasonable agreement between determinations of the length from the fractionation factor and that from the NMR chemical shift. In particular, the uncertainty is less than that deduced from X-rays.

In this paper, we systematically investigate how the fractionation factor Φ varies with the donor-acceptor distance R . Specifically, we consider the relative importance of different contributions to Φ . We find that the competing quantum effects associated with the X-H stretch and bend modes are the most significant. Non-degeneracy of the two bend modes and tunnel splitting of the stretch mode have small but noticeable effects. The only important effect of the secondary geometric isotope effect is that it enhances the contribution from the tunnel splitting, mostly for $R \sim 2.4 - 2.6$ Å. For most values of R , the value of Φ we calculate differs from the empirical relation due to Mildvan et al. [13] that has been used to determine

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bond lengths in enzymes.

II. METHOD

We calculate the H/D zero-point energies, and hence Φ , with the electronic ground state potential of a two-diabatic state model [14]. For X and Y as donor and acceptor, the two diabatic states of the model are $X-H \cdots Y$ and $X \cdots H-Y$, which are modelled as Morse oscillators. The coupling between the diabats is a function of R , the X-Y distance, as well as the H-X-Y and H-Y-X angles; it decreases exponentially with increasing R and gets weaker with larger angular excursions of the H atom. Previously, we showed that this model can give a quantitative description of the correlations observed [15] for a diverse range of chemical compounds between R and X-H bond lengths, vibrational frequencies, and isotope effects [11].

The parametrization used in the latter work and in Ref. 14 was for O-H \cdots O symmetric hydrogen bonds, i.e. the donor and acceptor have the same proton affinity (pK_a). In the present work, we retain this parametrization. This is an approximation for comparisons with H-bonds in proteins, which are generally asymmetric (donor and acceptor with different pK_a). Many H-bonds in proteins are actually N-H \cdots O bonds. However, as the H-bonds become stronger (at short R) the equal proton affinity approximation becomes more reliable. At such distances, the donor and acceptor effectively share the H atom. In the diabatic state model, the coupling element becomes large enough to strongly suppress or eliminate the barrier for the H atom transfer. Both Kreevoy and Liang [10] and Bao et al. [16] considered how an asymmetric proton transfer potential modifies the fractionation factor. Non-degeneracy smaller than 1000 cm^{-1} (or equivalently, a pK_a difference of about 2) has little effect on the proton transfer potential.

The total vibrational zero-point energy for Pr-H/D is

$$Z(R) \equiv Z_{\parallel}(R) + Z_{\perp,o}(R) + Z_{\perp,i}(R). \quad (4)$$

The three terms are the zero-point energy associated with X-H vibrations parallel to the hydrogen bond (stretch), out-of-plane bend (o), and in-plane bend (i) of $X-H \cdots Y$, respectively. (The plane typically refers to that of X-H.) The simple summation in the above equation points to our assumption that these modes are uncoupled.

The O-H/D stretch zero-point energy is calculated numerically by using the sinc-function Discrete Variable Representation (DVR) [17] to solve the one-dimensional Schrodinger equation as a function of R . This gives an essentially exact treatment for the significant anharmonic and tunnelling effects that occur for low-barrier bonds [11].

We treat zero-point energies of bend modes as half their classical harmonic frequencies as a function of R . As per the diabatic model, both bends have equal frequencies. To break the degeneracy, we use the result from the model itself that hardening of the two bend motions is similar:

$$\Omega_{\perp,o/i}(R)^2 = \omega_{\perp,o/i}^2 + 2f(R) \quad (5)$$

where $\omega_{\perp,o/i}$ is the frequency in the absence of an H-bond and the $f(R)$ is given in Eqn. (6) of Ref. 14. At least in the R range of interest, $f(R)$ is a positive function that monotonically decreases with increasing R . In general $\omega_{\perp,i} > \omega_{\perp,o}$ and so $\Omega_{\perp,i} > \Omega_{\perp,o}$. The ω parameters for the deuterium isotope are taken to be $\sqrt{2}$ smaller than for the H isotope.

Eq. (3) for Φ assumes that only the ground state energies of the species is relevant (at the temperature of interest). For a symmetric proton transfer potential, one expects a first excited state due to tunnel splitting that would be close-lying in energy to the ground state. In our model, this appears along the X-H stretch coordinate. Hence the first excited state for the H/D motion makes a further multiplicative contribution of the form

$$\Phi_{\text{tun}} = \frac{1 + \exp(-\delta E_D/k_B T)}{1 + \exp(-\delta E_H/k_B T)} \quad (6)$$

to the fractionation factor, where $\delta E_{H/D}$ is the tunnel splitting.

Another contribution comes from the secondary geometric isotope effect (SGIE) where the X-Y distance changes upon deuteration. This is a subtle effect with a non-monotonic dependence on R [11, 18, 19]. As shown in Ref. 11 and references therein, it arises because the rates of change of the zero-point energy for H and D are different. The net effect is that true minima for both H and D (R_H and R_D) are shifted relative to the classical minimum (R_o). The difference between the minima is largely under 0.04 \AA with $R_D > R_H$, but the resulting effects on frequencies are substantial. There are two consequences of SGIE for the fractionation ratio. First, the zero point energy for the H and D should be calculated at their respective minima. Second, an elastic energy associated with the stretching of the donor-acceptor distance, of the form $\frac{1}{2}K(R_{H/D} - R_o)^2$, must be included. Here, K is the elastic constant that is parametrised empirically in Ref. 11. We have included both consequences of the SGIE in our calculation.

The above details describe the calculation of $[\text{Pr-D}]/[\text{Pr-H}]$ part of Φ , in (2), as a function of R . The solvent part is taken to be the calculated model value at $R = 2.8 \text{ \AA}$, approximately the relevant length in water.

III. RESULTS AND DISCUSSION

A. Role of competing quantum effects

Figure 1 shows the computed trends of the stretch and bend zero-point energies from the model for both H and D isotopes. The solid black (H) and green (D) curves show the O-H/D stretch zero-point energies. The limiting energies at large R are those of O-H and O-D bonds, about 1800 and 1300 cm^{-1} , respectively. Of relevance to the fractionation factor Φ is the *difference* between these curves, which decreases (for the most part) with decreasing R . From Eq. (3), this leads to a drop in Φ . The black curve in Figure 2 shows the fractionation ratio with only the O-H/D stretch zero-points included.

A countervailing influence on $\Phi(R)$ comes from the bends, which harden in frequency with decreasing R . Figure 1 shows

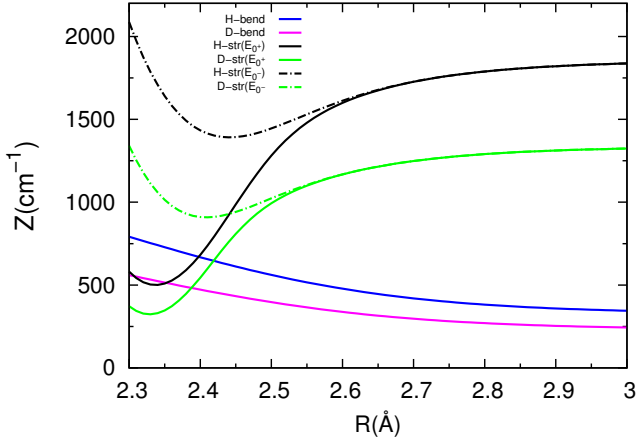


Figure 1. Competing quantum effects. The zero-point energy of the bend mode and of the two lowest stretch quantum states (due to tunnel splitting, $E_{0\pm}$) is shown as a function of the donor-acceptor distance R . The bend mode here is the out-of-plane mode that has a frequency of 650 cm^{-1} at large R . With increasing R the stretch (bend) zero-point energy increases (decreases). Curves are shown for both H and D isotopes. Note how for $R < 2.55 \text{ Å}$, the tunnel splitting of the stretch mode for the H isotope becomes observable.

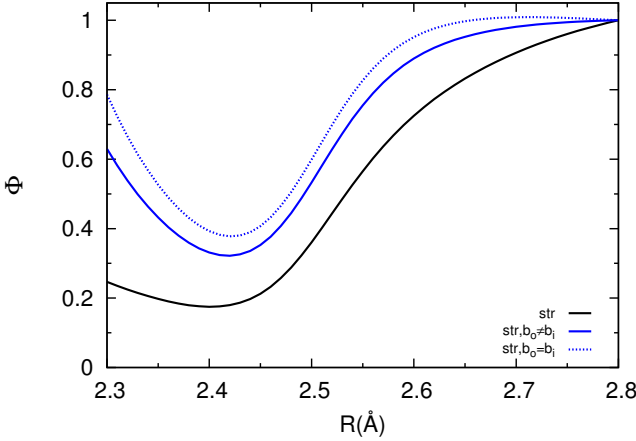


Figure 2. Effect of the bend modes on the fractionation ratio. The black curve only includes the effects of the X-H stretch vibrational mode. The blue curves include the effect of the two bending vibrational modes as well. For the upper (lower) blue curve the bend modes are degenerate (non-degenerate). For the upper blue curve, the both the out-of-plane and in-plane bends are degenerate, with the limiting frequency value at large R ($\omega_{\perp,o}$) being 650 cm^{-1} . For the lower curve, the in-plane mode's limiting frequency is raised to $\omega_{\perp,i} = 1600 \text{ cm}^{-1}$.

the zero-points only for the out-of-plane bends for the H and D cases. Their limiting values at large R are $\frac{1}{2}\omega_{H,\perp,o}$ and $\frac{1}{2\sqrt{2}}\omega_{H,\perp,o}$, respectively, where $\omega_{H,\perp,o} = 650 \text{ cm}^{-1}$. The corresponding trends for the in-plane bend (not plotted) are obtained from Eq. (5), setting $\omega_{H,\perp,i} = 1600 \text{ cm}^{-1}$. The consequences of the opposite trends for the hydrogen and deuterium bend and stretch frequencies — more compactly, competing quantum effects — has been the subject of much recent

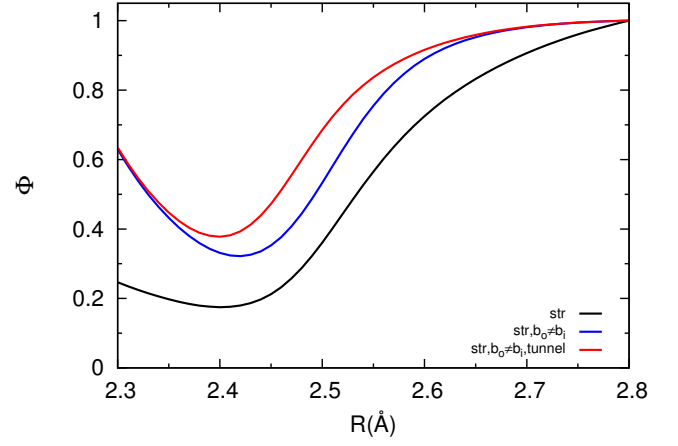


Figure 3. Effect of the tunnel splitting on the fractionation ratio. The black curve only includes the effects of the X-H stretch vibrational mode. The blue curve also includes the effect of two non-degenerate bending vibrations. The red curve includes the contribution from first excited X-H stretch state (tunnel splitting).

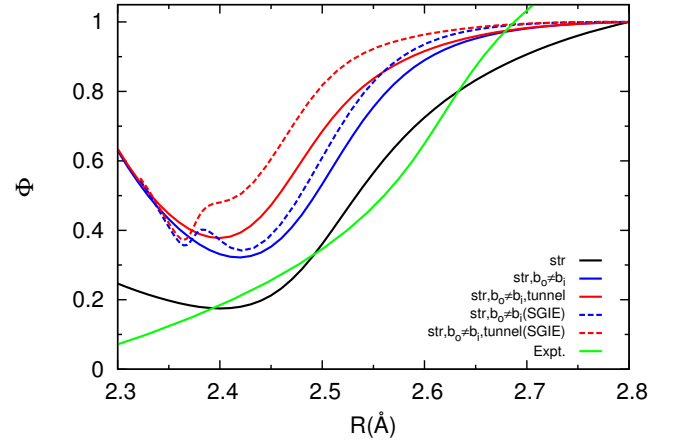


Figure 4. Corrections due to the secondary geometric isotope effect (SGIE) are shown as the dashed curves. The solid curves of the same colour are from Figure 3, which do not include the SGIE. The green curve is the empirical function, defined by Eqn. (7), and given in Ref. 13. Note that the slight undulation in the dashed curves below 2.4 Å can be traced to the very rapid change of the SGIE ($R_D - R_H$) in that region; see the lower panel of Figure 7 in Ref. 11

study.[11, 19–23].

Presently, for Φ , it is $Z_H - Z_D$ that matters, which evidently also showcases the competition between the X-H bends and the X-H stretch. The solid blue curve in Figure 2 shows that the hardening of the bend modes with decreasing R significantly increases the fractionation ratio compared to the contribution from just the stretch mode. This is one of the main results of this paper. Kreevoy and Liang [10] previously pointed out that bending modes could alter their results for the correlation of Φ and R . They gave the rough estimate that Φ could be increased by a factor of about 1.7. Edison, Weinhold, and Markley also mentioned the effect of the bend modes[24], finding values of $\Phi > 1$ for weak bonds.

B. Role of non-degeneracy of the bend modes

For the main results of this paper, the bend modes are made non-degenerate using Eq. (5) since the out-of-plane and in-plane modes are different in frequency in reality. We briefly investigate how different the fractionation factor would be if the degeneracy were retained.

The dotted blue curve in Figure 2 shows the plot of Φ with both bends having frequencies corresponding to the out-of-plane mode. Evidently, the change is relatively small, but not negligible. As per the model, the smaller the bend frequency, the faster it hardens; $\Omega_{\perp}(R)/\omega_{\perp} = \sqrt{1 + 2f(R)/\omega_{\perp}^2}$. Hence, changing one of the bends frequencies to 1600 cm^{-1} reduces $Z_H - Z_D$ relative to the degenerate case. Bend non-degeneracy can reduce the fractionation by about 10-20% compared to the degenerate case.

C. Role of the tunnel splitting

For long H-bonds, the proton transfer potential has a high barrier and the tunnel splitting of the vibrational ground state is negligible [11]. However, for $R < 2.55 \text{ \AA}$, the splitting becomes significant, as can be seen in Figure 1. A multiplicative correction Φ_{tun} (Eq. (6)) introduces the effect of the thermal population of the first low-lying excited state. This factor is always larger than one because the H tunneling splitting is larger; $\delta E_H > \delta E_D$. When the tunnel splitting is much larger than the thermal energy $k_B T$ (i.e. for $R < 2.4 \text{ \AA}$) the correction factor is extremely close to unity. When the tunnel splitting is much less than $k_B T$ the correction factor is approximately $(1 + (\delta E_H - \delta E_D)/2k_B T)$.

Figure 3 shows that the tunnel splitting has a small but non-negligible effect in the range, $R \sim 2.4 - 2.6 \text{ \AA}$. We should also clarify the nomenclature here. For sufficiently small R , the barrier is no longer present, and so there is strictly no ‘‘tunnel splitting.’’ We just have two well-separated vibrational energies instead. Note that in a solvent there will be local dynamical fluctuations of the local electric field that couple to the electric dipole moment associated with the X-H stretch and for large enough fluctuations the tunnel splitting will not appear because it will be destroyed by quantum decoherence.[25] Also, when the proton affinity of the donor and acceptor differ by more than about 500 cm^{-1} (1.5 kcal/mol) this effect may be absent.

D. Role of the secondary geometric isotope effect

The SGIE has a significant effect on the stretch mode vibrational frequencies for $R \sim 2.4 - 2.5 \text{ \AA}$, where the proton transfer barrier has effectively disappeared. Its inclusion yielded better agreement of the H/D stretch frequency ratio; compare Figure 8 in Ref. 11, where this ratio is 1 (1.15) with (without) SGIE, which is a sizeable change for strong short H-bonds.

Figure 4, however, points to a more modest influence of the SGIE on the fractionation ratio. The only significant ef-

fect is how it modifies the contribution from the tunnel splitting. Without the SGIE, the correction factor is approximately $(1 + (\delta E_H(R) - \delta E_D(R))/2k_B T)$. With the SGIE, the correction factor is approximately $(1 + (\delta E_H(R_H) - \delta E_D(R_D))/2k_B T)$. This is larger because $R_D > R_H$, and an increase in donor-acceptor distance of as little as 0.02 \AA for D relative to H can increase the energy barrier and thereby noticeably decrease $\delta E_D(R_D)$ [11].

If tunneling contributions are suppressed by, e.g., a sizeable difference in pK_a 's between the donor and acceptor, the above analysis suggests that the SGIE would have only a small influence on the fractionation factor. The key effect that appears to govern the magnitude range of $\Phi(R)$ according to our model is the competing quantum effect between the X-H stretch and X-H bends.

E. Comparison with experiment

Based on calculations from an empirical one-dimensional quartic potential [16], Mildvan et al.[13] considered a relation between the fractionation factor and donor-acceptor distance,

$$R = (2.222 + 1.1924\Phi - 1.3347\Phi^2 + 0.608\Phi^3)\text{\AA}. \quad (7)$$

This relation is plotted in Figure 2 in green. It was used together with measurements of fractionation ratios for 18 H-bonds in several different enzymes to deduce the length R . The values they obtained for R were mostly in agreement with values of R deduced from NMR chemical shifts, and from X-ray crystallography. Values of Φ ranged from 0.32 to 0.97 and the corresponding values of R were in the range 2.49 to 2.68 \AA . However, Figure 2 shows significant differences between equation (7) and our results.

Klug et al.[26] studied crystals of the dihydrated sodium salt of hydrogen bis(4-nitrophenoxide) and found a fractionation ratio of 0.63 ± 0.04 . Using the Kreevoy and Liang [10] parameterisation, they noted that this value was inconsistent with the bond length observed via X-rays, $R = 2.452 \text{ \AA}$, and with the value of $\Phi = 0.31 \pm 0.03$ deduced from UV spectroscopy for bis(4-nitrophenoxide) in acetonitrile solution. Consequently, they suggested that ‘‘the solid was not in isotopic equilibrium with the solvent from which it was precipitated.’’ However, their results are consistent with our parameterisation of Φ versus R , if tunnel splitting is not included.

Loh and Markley[27] found fractionation factors in the range 0.28 - 1.47 for the different H-bonds in the protein staphylococcal nuclease. Clearly, we cannot explain their high values.

Thakur et al.[28] have recently developed a new method for the rapid determination of H/D exchange from two-dimensional NMR spectra. Section S5 of their Supplementary material shows fractionation values for three different proteins. For 80 different amino acid residues in Tim23, the values ranged from 0.92 to 1.73 . For 58 different amino acid residues in Ubiquitin, the values ranged from 0.57 to 1.67 . For 54 different amino acid residues in Dph4, the values ranged from 0.45 to 2.04 .

Recently, an extensive study was made of mutants of the Green Fluorescent Protein with a particularly short H-bond, estimated from X-ray structures to be about $2.4 - 2.5 \text{ \AA}$ [29]. The fractionation factors found from NMR were in the range 0.6 - 0.7, consistent with our analysis.

Edison, Weinhold, and Markley performed *ab initio* calculations for a wide range of peptide clusters [24]. They observed a correlation between the fractionation ratio and the donor-acceptor distance. For $R > 2.55 \text{ \AA}$, the fractionation was larger than one, and for $R \simeq 2.45 \text{ \AA}$, $\Phi \simeq 0.6$.

IV. CONCLUSIONS

We have shown that the H/D fractionation factor is quite sensitive to the donor-acceptor distance in hydrogen bonds, and so, in principle, can be used as a “ruler” for determining bond lengths. However, caution is in order because there are a number of subtle effects that modify the exact form of the relationship between Φ and R . These include competing quantum effects between stretch and bend modes, non-degeneracy of the bend modes, tunnel splitting, the secondary geometric isotope effect, and differences between the proton affinity of

the donor and acceptor.

Our results raise questions about whether values of Φ as small as 0.3 are really possible, contrary to some measurements and previous theoretical claims. Equally, our results cannot explain Φ values that are much larger than 1. This discrepancy may be due to our assumption that the stretch and bend modes are independent. Although our model quantitatively describes many experimental results for bond lengths, vibrational frequencies, and isotope effects, for $R \sim 2.45 \text{ \AA}$, it does give stretch mode frequencies that are higher than observed. (See Figure 6 in Ref. 11 and the associated discussion.) This would also lead to a larger fractionation factor. Addressing this issue will require a systematic investigation of solutions to the vibrational Schrodinger equation for a higher-dimensional (probably four dimensional) potential energy surface. We leave this for a future study.

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