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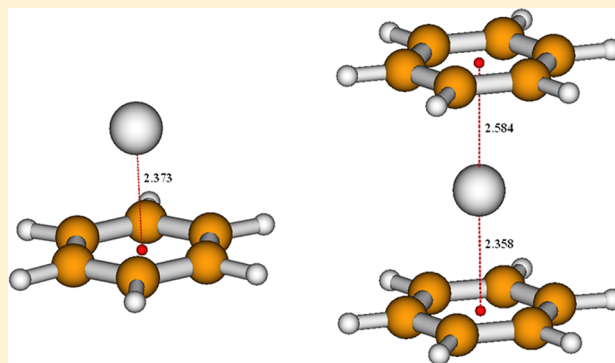
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# Dynamics of $\text{Na}^+(\text{Benzene}) + \text{Benzene}$ Association and Ensuing $\text{Na}^+(\text{Benzene})_2^*$ Dissociation

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**ABSTRACT:** Chemical dynamics simulations were used to study  $\text{Bz} + \text{Na}^+(\text{Bz}) \rightarrow \text{Na}^+(\text{Bz})_2^*$  association and the ensuing dissociation of the  $\text{Na}^+(\text{Bz})_2^*$  cluster (Bz = benzene). An interesting and unexpected reaction found from the simulations is direct displacement, for which the colliding Bz molecule displaces the Bz molecule attached to  $\text{Na}^+$ , forming  $\text{Na}^+(\text{Bz})$ . The rate constant for  $\text{Bz} + \text{Na}^+(\text{Bz})$  association was calculated at 750 and 1000 K, and found to decrease with increase in temperature. By contrast, the direct displacement rate constant increases with temperature. The cross section and rate constant for direct displacement are approximately an order of magnitude lower than those for association. The  $\text{Na}^+(\text{Bz})_2^*$  cluster, formed by association, dissociates with a biexponential probability, with the rate constant for the short-time component approximately an order of magnitude larger than that for the longer time component. The latter rate constant agrees with that of Rice–Ramsperger–Kassel–Marcus (RRKM) theory, consistent with rapid intramolecular vibrational energy redistribution (IVR) and intrinsic RRKM dynamics for the  $\text{Na}^+(\text{Bz})_2^*$  cluster. A coupled phase space model was used to analyze the biexponential dissociation probability.



## I. INTRODUCTION

The association of cations with polycyclic aromatic hydrocarbon (PAH) molecules is an interesting and important problem. The existence of PAH molecules in the interstellar medium and their possible role in forming clusters with iron atoms has been considered.<sup>1–5</sup> Many trace metals and their cations are present in hydrocarbon fuels, and they may participate in PAH coalescence, ultimately leading to soot formation.<sup>6–14</sup> From a fundamental perspective, it is important to understand the nature of cation– $\pi$  interactions in metal cation–PAH clusters.

Both experimental and theoretical/computational studies have determined properties of clusters formed by the binding of aromatic molecules to metal cations.<sup>15–33</sup> This work has provided information regarding structures of the complexes, as well as the cation–aromatic binding energy. The theoretical/computational studies have given insights regarding the relative importance of electrostatic, polarization, charge transfer, and dispersion terms for binding of aromatics to the cation.<sup>22,26–29</sup> The computational studies have given values for the cation–aromatic intermolecular frequencies and shifts.<sup>33</sup>

The dynamics and kinetics of the formation of cation–aromatic molecule clusters by bimolecular association, and of the ensuing unimolecular dissociation of the clusters, have not been studied by either experiments, theory, or computation. For the work reported here, chemical dynamics simulations were performed to determine the cross section and rate constant for  $\text{Na}^+(\text{Bz}) + \text{Bz}$  association to form the vibrationally and rotationally excited  $\text{Na}^+(\text{Bz})_2^*$  cluster, and then analyze the unimolecular dissociation dynamics of this nonrandomly excited cluster. The goal of this work is to establish an understanding of

the association and dissociation dynamics and kinetics of cation–aromatic molecule clusters. The dynamics of cations<sup>34–38</sup> and anions<sup>39–41</sup> associating with nonaromatic molecules has been investigated in previous computational studies.

## II. COMPUTATIONAL PROCEDURE

**A. Potential Energy Function.** The analytic potential energy function for the  $\text{Na}^+(\text{Bz}) + \text{Bz}$  system is written as the sum<sup>42</sup>

$$V = V_{\text{Bz}} + V_{\text{Bz,Bz}} + V_{\text{Na}^+,\text{Bz}} \quad (1)$$

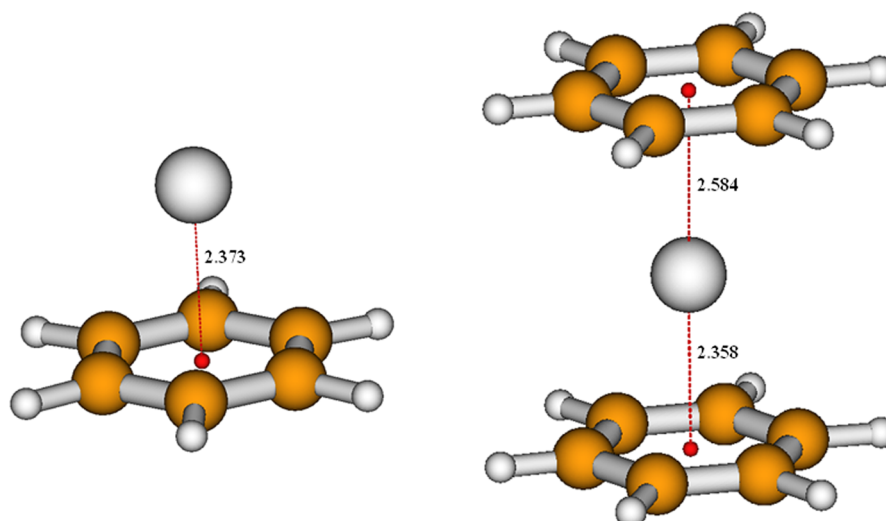
where  $V_{\text{Bz}}$  is the benzene intramolecular potential,  $V_{\text{Bz,Bz}}$  is the benzene–benzene intermolecular potential, and  $V_{\text{Na}^+,\text{Bz}}$  is the  $\text{Na}^+$ –benzene intermolecular potential.  $V_{\text{Bz}}$  is expressed in terms of Morse stretches, harmonic in-plane bends, harmonic out-of-plane wags, and torsions. The force constants for  $V_{\text{Bz}}$  are the same as those used previously.<sup>43</sup> For the Morse potentials,  $D_e$  is 125.8<sup>44,45</sup> and 116.4 kcal/mol<sup>46,47</sup> for the C–C and C–H bonds, respectively. The Morse parameter  $\beta_e$  is related to the harmonic force constant ( $f$ ) by  $\beta_e = (f/2D_e)^{1/2}$  and, respectively, is 1.95 and 1.78 Å<sup>–1</sup> for the C–C and C–H bonds.

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**Figure 1.** Equilibrium geometries of the  $\text{Na}^+(\text{Bz})$  and  $\text{Na}^+(\text{Bz})_2$  clusters for the analytic intermolecular potential as described in Section A. The distances are in angstrom.

The benzene–benzene intermolecular potential  $V_{\text{Bz},\text{Bz}}$  is represented by the OPLS model<sup>48</sup> for which the potential is written as a sum of two-body terms, each depending on  $r^{-12}$ ,  $r^{-6}$ , and  $r^{-1}$ . The parameters for the two-body terms have been given and described previously.<sup>48</sup> The OPLS global minimum for the benzene dimer has a T-shaped geometry with a 2.32 kcal/mol classical binding energy and a Bz–Bz center-of-mass separation of 4.93 Å. A similar geometry with a 4.96 Å Bz–Bz separation and a binding energy of 2.84 kcal/mol is found from a CCSD(T)/CBS calculation.<sup>49</sup> The OPLS potential is expected to give an overall good description of the benzene–benzene intermolecular potential.

The OPLS potential was developed by fitting the 298 K heat of vaporization and density for liquid benzene, and the benzene dimer's ab initio structure and binding energy.<sup>48</sup> The potential gives values for liquid benzene's C–C radial distribution function and heat capacity which are in excellent agreement with experiment. Ab initio calculations have shown that molecular mechanical (MM) potentials like OPLS often do not accurately represent high energy repulsive regions of intermolecular potentials.<sup>50,51</sup> However, these regions should not be important for the 700 and 1000 K simulations reported here. Nevertheless, in future work it would be of interest to investigate the repulsive regions of the Bz–Bz OPLS potential.

The  $\text{Na}^+\text{--Bz}$  intermolecular potential was developed in previous work<sup>42</sup> by fitting MP2/6-311+G\* calculations to two-body potentials of the form

$$V = A \exp(-Br) + \frac{C}{r^n} + \frac{D}{r^m} \quad (2)$$

to fit the  $\text{Na}^+\text{--H}$  and  $\text{Na}^+\text{--C}$  interactions. Values for the parameters  $A$ ,  $B$ ,  $C$ ,  $D$ ,  $n$ , and  $m$  for both interactions have been given previously.<sup>42</sup> MP2 potential energy curves, with both attractive and repulsive components, were calculated and fit for three  $\text{Na}^+ + \text{Bz}$  orientations; i.e., see Figure 1 of ref 42. This potential gives a  $\text{Na}^+(\text{Bz})$  binding energy of 25.5 kcal/mol compared to the MP2 value of 25.2 kcal/mol. The experimentally reported value is  $\sim 22$  kcal/mol.<sup>24,25</sup> The three  $\text{Na}^+(\text{Bz})$  intermolecular frequencies of 143, 143, 233  $\text{cm}^{-1}$  for the analytic function are in quite good agreement with the MP2 values of 134, 134, and 208  $\text{cm}^{-1}$ . The equilibrium geometries for

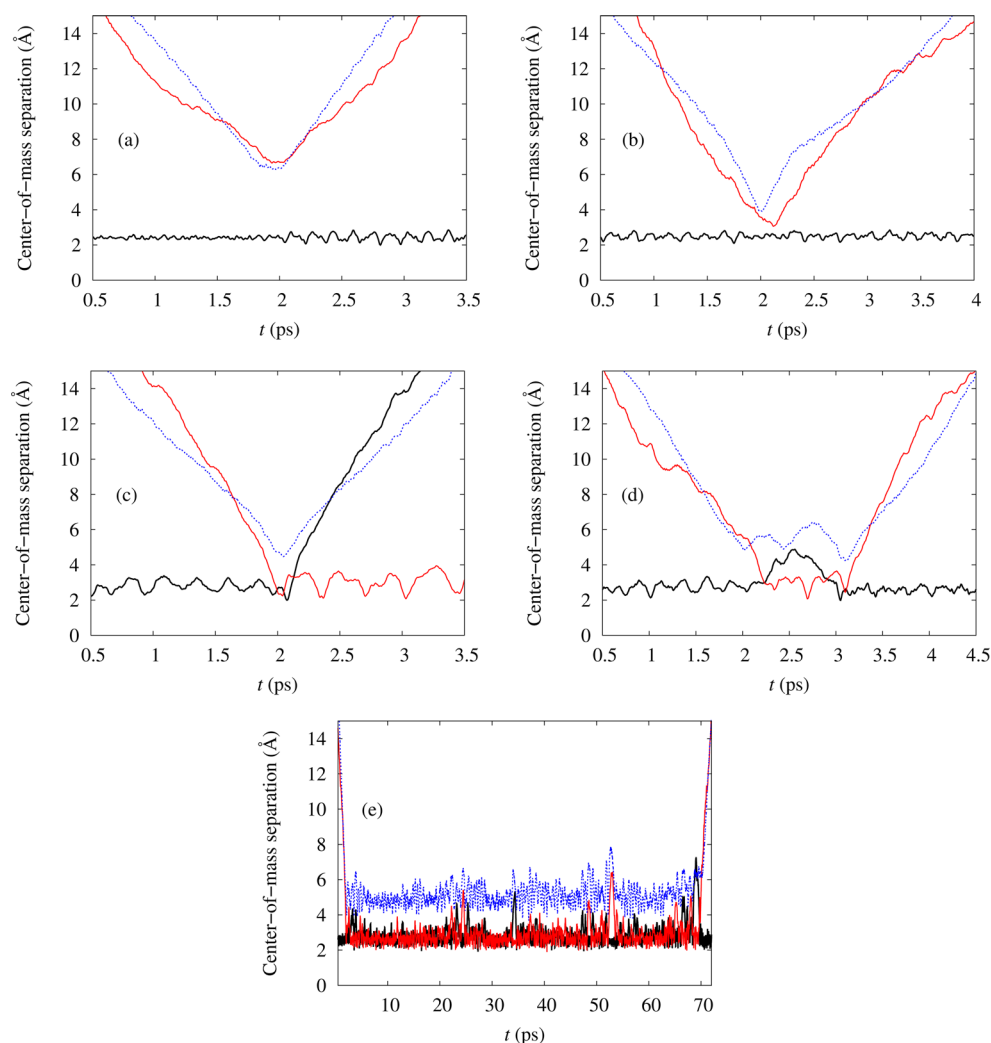
the  $\text{Na}^+(\text{Bz})$  and  $\text{Na}^+(\text{Bz})_2$  clusters as obtained from the analytic potential are presented in Figure 1.

**B. Chemical Dynamics Simulations.** Chemical dynamics simulations were performed with the VENUS computer program,<sup>52,53</sup> to study  $\text{Na}^+(\text{Bz}) + \text{Bz} \rightarrow \text{Na}^+(\text{Bz})_2$  association and the ensuing decomposition of the vibrationally and rotationally excited  $\text{Na}^+(\text{Bz})_2^*$  cluster. The simulations were performed at fixed collision impact parameters and temperatures  $T$  of 750 and 1000 K for both  $\text{Na}^+(\text{Bz})$  and Bz. Quasiclassical sampling was used to add the 750 and 1000 K Boltzmann vibrational and rotational energy distributions to an ensemble of the collision partners.<sup>54</sup> Quantum harmonic oscillator distributions were sampled for the vibrational normal modes and classical rigid rotor distributions were sampled for the external rotational degrees of freedom. Standard algorithms were used to transform the vibrational and rotational energies of  $\text{Na}^+(\text{Bz})$  and Bz to Cartesian coordinates and momenta, and then the collision partners were randomly rotated. A relative center-of-mass collision energy of  $3RT/2$  was then added to  $\text{Na}^+(\text{Bz}) + \text{Bz}$  for a fixed collision impact parameter  $b$ . This approach, for simulating the temperature dependent dynamics, was tested for the 1000 K simulations by averaging over the relative collision energy distribution for the  $\text{Na}^+(\text{Bz}) + \text{Bz}$  collisions.

For each ensemble with fixed  $b$  and  $T$ , 200 trajectories were calculated with a sixth-order symplectic integration algorithm.<sup>55</sup> The trajectories were integrated for either a maximum time of 90 ps or halted when the  $\text{Na}^+\text{--Bz}$  separation for the dissociating Bz molecule exceeded 20 Å. The integrations were performed with a time step of 0.5 fs, and energy was conserved to 1%, i.e., 0.20 kcal/mol. The properties determined from the trajectory simulations are the different types of trajectory events, the probability of forming the vibrationally and rotationally excited  $\text{Na}^+(\text{Bz})_2^*$  cluster versus impact parameter and temperature  $T$ , and the lifetime of these clusters.

### III. SIMULATION RESULTS

Before presenting and discussing the trajectory results, it is useful to review the traditional statistical model<sup>56,57</sup> for  $\text{Na}^+(\text{Bz}) + \text{Bz}$  association. It assumes  $\text{Na}^+(\text{Bz}) + \text{Bz}$  collisions form the vibrationally/rotationally excited  $\text{Na}^+(\text{Bz})_2^*$  cluster, which then dissociates in accord with the Rice–Ramsperger–Kassel–



**Figure 2.** Illustrations of the different trajectory types for  $\text{Bz}_2 + \text{Na}^+(\text{Bz}_1)$ : (a) direct scattering of  $\text{Bz}_2$ , with the  $\text{Na}^+$  and  $\text{Bz}_2$  separation remaining greater than 6 Å; (b) direct scattering with a short  $\text{Na}^+$  and  $\text{Bz}_2$  separation; (c) direct displacement of  $\text{Bz}_1$  by  $\text{Bz}_2$ , without cluster formation; (d) formation of a short-lived cluster with  $\text{Bz}_2$  dissociation; and (e) formation of a long-lived cluster with  $\text{Bz}_2$  dissociation. The black line is the  $\text{Bz}_1\text{--Na}^+$  distance, the red line the  $\text{Bz}_2\text{--Na}^+$  distance, and the dotted blue line the  $\text{Bz}_1\text{--Bz}_2$  distance.

Marcus (RRKM) theory of unimolecular kinetics. As described below, two important nonstatistical dynamical features were found from the trajectories; i.e., a direct  $\text{Na}^+(\text{Bz}) + \text{Bz}$  displacement reaction without cluster formation and a nonexponential dissociation probability for the  $\text{Na}^+(\text{Bz})_2^*$  cluster.

**A. Trajectory Types.** The trajectories were classified as either association ( $\text{Na}^+(\text{Bz})_2^*$  cluster formation), direct displacement (the two Bz molecules were interchanged) or nonreactive. For trajectories, which did not form the cluster or undergo direct displacement, the colliding Bz molecule directly scattered off  $\text{Na}^+(\text{Bz})$  without vibrating with respect to  $\text{Na}^+$ . For the majority of these trajectories, the  $\text{Na}^+\text{--Bz}$  separation for the colliding Bz remained greater than 6.0 Å, but for some Bz came very close to  $\text{Na}^+$  without forming a  $\text{Na}^+(\text{Bz})_2^*$  cluster. These two trajectory types are illustrated in Figure 2a,b.

A small fraction of noncluster forming direct reactive trajectories were also found, for which the colliding Bz molecule directly displaces the Bz attached to  $\text{Na}^+$ ; i.e.,  $\text{Bz} + \text{Na}^+(\text{Bz}) \rightarrow \text{Na}^+(\text{Bz}) + \text{Bz}$ . A representative trajectory is illustrated in Figure 2c.

The vibrationally/rotationally excited  $\text{Na}^+(\text{Bz})_2^*$  clusters, formed by  $\text{Bz} + \text{Na}^+(\text{Bz})$  association, had a range of lifetimes as shown in Figure 2d and 2e. From an analysis of  $\text{Na}^+(\text{Bz})_2^*$  dissociation, it was found that, once the dissociating Bz molecule acquired a separation of 10 Å between its center-of-mass and  $\text{Na}^+$ , it dissociated and did not reform the cluster. Thus, the time the cluster dissociated was taken as the time a  $\text{Na}^+\text{--Bz}$  separation became 10 Å. A separation of 9 Å was not sufficient to identify dissociation. For each cluster formed, its lifetime was taken as the difference in the times the dissociation and initial association had a  $\text{Na}^+\text{--Bz}$  separation of 10 Å.

**B.  $\text{Bz} + \text{Na}^+(\text{Bz}) \rightarrow \text{Na}^+(\text{Bz})_2^*$  Association Probability, Cross Section, and Rate Constant.** The association rate constant may be expressed as

$$k(T) = \int_0^\infty k(E_{\text{rel}})P(E_{\text{rel}})dE_{\text{rel}} \quad (3)$$

where  $k(E_{\text{rel}})$ , for  $\text{Na}^+(\text{Bz}) + \text{Bz}$  relative translational energy  $E_{\text{rel}}$ , is given by  $k(E_{\text{rel}}) = v(E_{\text{rel}})\sigma(E_{\text{rel}})$  and  $P(E_{\text{rel}})$  is the Boltzmann distribution for  $E_{\text{rel}}$ .  $v(E_{\text{rel}})$  and  $\sigma(E_{\text{rel}})$  are the relative velocity and association cross section, respectively. For calculating  $\sigma(E_{\text{rel}})$ ,  $\text{Na}^+(\text{Bz})$  has a Boltzmann distribution of vibrational and

rotational energies at  $T$ . Following previous work for ion–molecule association,<sup>36</sup>  $k(E_{\text{rel}})$  is expressed as

$$k(E_{\text{rel}}) = a \exp(-bE_{\text{rel}}) \quad (4)$$

Inserting eq 4 into eq 3,  $k(T)$  is analytic, i.e.,

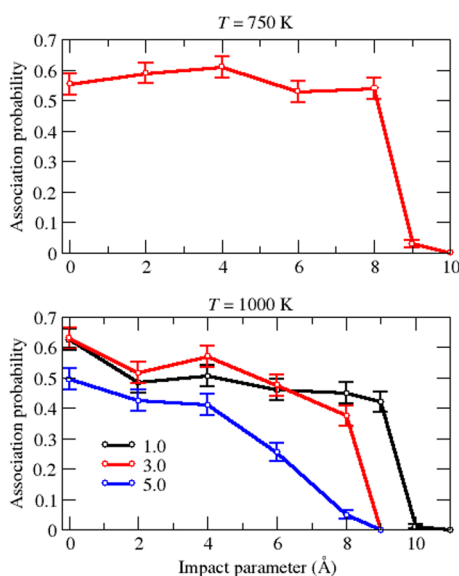
$$k(T) = \left(\frac{1}{k_B T}\right)^{3/2} a \left(b + \frac{1}{k_B T}\right)^{-3/2} \quad (5)$$

An approximate expression for  $k(T)$  is

$$k(T) \cong \nu(\bar{E}_{\text{rel}})\sigma(\bar{E}_{\text{rel}}) \quad (6)$$

where the  $\nu$  and  $\sigma$  are calculated for the average relative translational energy  $3k_B T/2$  for temperature  $T$ . For calculation of  $\sigma(E_{\text{rel}})$ ,  $\text{Na}^+(\text{Bz})$  has a Boltzmann distribution of the vibrational and rotational energies at  $T$ . The  $k(T)$  from eqs 5 and 6 are compared for the 1000 K simulations.

The probability of  $\text{Bz} + \text{Na}^+(\text{Bz}) \rightarrow \text{Na}^+(\text{Bz})_2^*$  association versus impact parameter  $b$ , i.e.,  $P_r(b)$ , was calculated to determine the association cross section. To average over  $E_{\text{rel}}$  for the 1000 K simulations,  $P_r(b)$  was calculated for  $E_{\text{rel}}$  of 1.0, 3.0, and 5.0 kcal/mol, where 3.0 kcal/mol is the average  $E_{\text{rel}}$  at 1000 K. The  $P_r(b)$  for these three  $E_{\text{rel}}$  are plotted in Figure 3. The  $P_r(b)$  for  $E_{\text{rel}}$  of 1.0



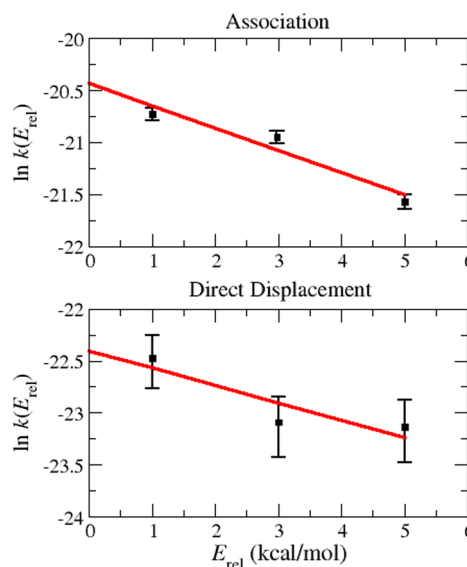
**Figure 3.** Probability of forming the  $\text{Na}^+(\text{Bz})_2$  cluster versus impact parameter  $b$ . The 1000 K simulations are performed for  $E_{\text{rel}}$  of 1.0, 3.0, and 5.0 kcal/mol, where 3.0 kcal/mol is the average  $E_{\text{rel}}$  at 1000 K. The 750 K simulations are only performed for  $E_{\text{rel}}$  of 2.2 kcal/mol, which is the average  $E_{\text{rel}}$  at this temperature.  $\text{Na}^+(\text{Bz})$  has a Boltzmann distribution of vibrational and rotational energies for both the 750 and 1000 K simulations.

and 3.0 kcal/mol are similar, but the  $P_r(b)$  are decidedly smaller for  $E_{\text{rel}}$  of 5.0 kcal/mol. For the 750 K simulations,  $P_r(b)$  was only calculated for the average  $E_{\text{rel}}$  of  $\bar{E}_{\text{rel}} = 2.2$  kcal/mol and is also plotted in Figure 3. The  $P_r(b)$  are similar for the 750 and 1000 K simulations at their  $\bar{E}_{\text{rel}}$ , except at the largest  $b$   $P_r(b)$  is somewhat larger for the lower temperature.

Integrating  $P_r(b)$  over the collision area  $2\pi b$  for each impact parameter gives the collision cross section  $\sigma$  for association; i.e.,  $\sigma = \int P_r(b)2\pi b db$ . Numerical integration gives  $\sigma$  equal to  $132 \pm 7.7$ ,  $106 \pm 6.2$ , and  $57.2 \pm 4.2 \text{ \AA}^2$  at  $E_{\text{rel}}$  of 1.0, 3.0, and 5.0 kcal/mol, respectively, for the simulations with  $T = 1000 \text{ K}$   $\text{Na}^+(\text{Bz})$

vibrational and rotational Boltzmann energy distributions. For the  $T = 750 \text{ K}$  simulation, with  $\bar{E}_{\text{rel}}$  of 2.2 kcal/mol,  $\sigma$  equals  $128 \pm 7.8 \text{ \AA}^2$ . Overall, the cross sections are precise with a standard deviation uncertainty of only  $\sim 6\text{--}7\%$ .

To determine the 1000 K  $k(T)$ , from the three  $E_{\text{rel}}$  calculations, the resulting  $k(E_{\text{rel}})$  were fit to eq 4 as shown in Figure 4. The fitting parameters are  $a = 1.34 \times 10^{-9} \text{ cm}^3/\text{molecule}\cdot\text{sec}$  and  $b = 0.213 (\text{kcal/mol})^{-1}$ . The value of  $k(T)$  from eq 5 is  $(7.85 \pm 0.47) \times 10^{-10} \text{ cm}^3/\text{molecule}\cdot\text{sec}$ .



**Figure 4.** Plots of  $\ln k(E_{\text{rel}})$  versus  $E_{\text{rel}}$  for the association and direct displacement reactions.  $\text{Na}^+(\text{Bz})$  has a 1000 K Boltzmann distribution of vibrational and rotational energies. The plots are fit to eq 4.  $k(E_{\text{rel}})$  is in units of  $\text{cm}^3/\text{molecule}\cdot\text{sec}$  for  $E_{\text{rel}}$  of 1.0, 3.0, and 5.0 kcal/mol and is, respectively,  $9.97 \times 10^{-10}$ ,  $7.98 \times 10^{-10}$ , and  $4.30 \times 10^{-10}$  for the association reaction and  $17.4 \times 10^{-11}$ ,  $9.37 \times 10^{-11}$ , and  $8.92 \times 10^{-11}$  for the displacement reaction.

The 1000 K rate constant from eq 6 is  $(7.98 \pm 0.48) \times 10^{-10} \text{ cm}^3/\text{molecule}\cdot\text{sec}$ , which agrees with that from eq 5 within statistical uncertainty. Thus, eq 6 approximate expression for  $k(T)$  gives an accurate value for the association rate constant. Equation 6 was used to determine  $k(T)$  for 750 K and the value is  $8.34 \times 10^{-10} \text{ cm}^3/\text{molecule}\cdot\text{sec}$ .

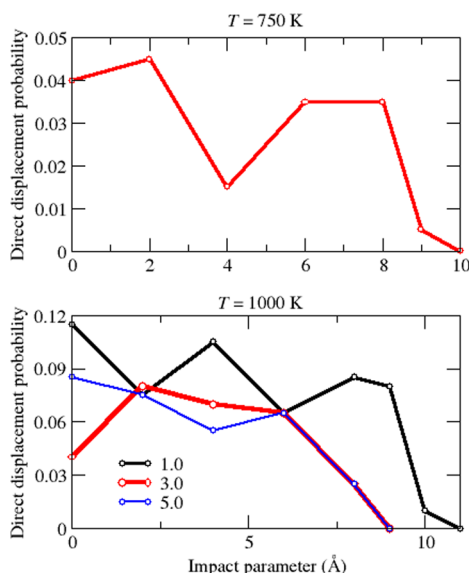
Since the association  $k(T)$  decreases with increase in  $T$ , the Arrhenius activation energy is negative. Using  $k(T)$  determined for 750 and 1000 K from eq 6, gives  $E_a = -0.26 \text{ kcal/mol}$ . The expression for  $E_a$  is analytic for  $k(T)$  in eq 5 and is given by

$$E_a(T) = -\frac{3}{2}k_B T + \frac{3}{2}\left(b + \frac{1}{k_B T}\right)^{-1} \quad (7)$$

The resulting  $E_a$  is  $-0.88 \text{ kcal/mol}$  at 1000 K, using the above parameter for  $b$ .

**C.  $\text{Bz} + \text{Na}^+(\text{Bz}) \rightarrow \text{Na}^+(\text{Bz}) + \text{Bz}$  Direct Displacement Probability, Cross Section, and Rate Constant.** The dynamics for the  $\text{Na}^+(\text{Bz}) + \text{Bz}$  direct displacement reaction were analyzed similar to the description given above for the  $\text{Na}^+(\text{Bz}) + \text{Bz}$  association reaction. The displacement probabilities versus impact parameter,  $P_r(b)$ , determined from the simulations are plotted in Figure 5. The 750 K simulation is performed at  $\bar{E}_{\text{rel}} = 2.2 \text{ kcal/mol}$ , the average relative translational energy at 750 K. Calculations are performed at  $E_{\text{rel}}$  of 1.0, 3.0, and





**Figure 5.** Same as Figure 3, but the probability of the  $\text{Bz2} + \text{Na}^+(\text{Bz1}) \rightarrow \text{Na}^+(\text{Bz2}) + \text{Bz1}$  direct displacement versus impact parameter  $b$ . The uncertainties in the displacement  $P_r(b)$  are 25–30%.

5.0 kcal for the 1000 K simulations, where 3.0 kcal/mol is  $\bar{E}_{\text{rel}}$ . The uncertainties in the  $P_r(b)$  range from 25 to 30%. Given these substantial uncertainties, the substantial structures for the  $P_r(b)$  in Figure 5 are not definitive.

Following the procedure outline above, the displacement cross section is  $7.5 \pm 2.8 \text{ \AA}^2$  for the 750 K simulation. For the 1000 K simulations at  $E_{\text{rel}}$  of 1.0, 3.0, and 5.0 kcal/mol, the respective cross sections are  $23.9 \pm 5.9$ ,  $12.4 \pm 3.6$ , and  $11.8 \pm 3.5 \text{ \AA}^2$ . An  $E_{\text{rel}}$  displacement cross section is about an order of magnitude smaller than the association cross section. For the 1000 K simulations,  $k(E_{\text{rel}})$  were calculated from the  $\sigma(E_{\text{rel}})$  and fit with eq 4, as shown in Figure 4. The fitting parameters are  $a = 1.87 \times 10^{-10} \text{ cm}^3/\text{molecule}\cdot\text{sec}$  and  $b = 0.167 \text{ (kcal/mol)}^{-1}$ .

Using eq 6,  $k(T)$  for the 750 K simulation is  $(4.8 \pm 1.8) \times 10^{-11} \text{ cm}^3/\text{molecule}\cdot\text{sec}$ . Using eq 5, and the above fitting parameters gives,  $k(T) = (12.2 \pm 3.3) \times 10^{-11} \text{ cm}^3/\text{molecule}\cdot\text{sec}$  at 1000 K. The 1000 K  $k(T)$  using eq 6 is statistically the same and  $(9.4 \pm 2.7) \times 10^{-11} \text{ cm}^3/\text{molecule}\cdot\text{sec}$ . The rate constant increases with temperature and, using the 750 and 1000 K  $k(T)$  determined from eq 6, the Arrhenius activation energy is 5.6 kcal/mol.

**D. Dynamics of  $\text{Na}^+(\text{Bz})_2^*$  Dissociation. 1. Simulation Results.** The  $\text{Na}^+(\text{Bz})_2^*$  cluster, formed by  $\text{Bz} + \text{Na}^+(\text{Bz}) \rightarrow \text{Na}^+(\text{Bz})_2^*$  association, is highly vibrationally/rotationally excited. At 1000 K its total classical energy is 209.2 kcal/mol, which is a sum of the average thermal energies of 87.9 and 93.9 for Bz and  $\text{Na}^+(\text{Bz})$ , which include their zero-point energies (ZPEs), the  $\text{Bz} + \text{Na}^+(\text{Bz})$  collision energy of 3.0 kcal/mol, and the  $\text{Bz} + \text{Na}^+(\text{Bz}) \rightarrow \text{Na}^+(\text{Bz})_2^*$  association energy of 24.4 kcal/mol. At 750 K the average  $\text{Na}^+(\text{Bz})_2^*$  energy is 186.4 kcal/mol.

Relative populations  $N(t)/N(0)$  of the  $\text{Na}^+(\text{Bz})_2^*$  clusters versus time for the different impact parameters are given in Figures 6 and 7 for the 750 and 1000 K simulations, respectively. For the 1000 K simulations, all the clusters dissociated within the 90 ps integration time and some of the dissociation involved “total dissociation” for which both Bz molecules dissociated from  $\text{Na}^+$ . However, for the 750 K simulations, some  $\text{Na}^+(\text{Bz})_2^*$  clusters remained when the trajectories were halted at 90 ps, and there were no “total dissociations”.

As shown in Figures 6 and 7, there is an initial delay in the  $N(t)/N(0)$  plots with a nondissociating component. To fit these distributions versus  $t$  it is necessary to shift the simulation  $N(t)/N(0)$  to  $t = 0$ . A nonarbitrary “shifting time” was chosen for each impact parameter by taking the “shifting time” as the average time spent by the associating Bz (i.e., Bz2) within 10 Å of  $\text{Na}^+$  for the direct displacement trajectories (Figure 2c) and the direct scattering trajectories for which Bz2 gets close to  $\text{Na}^+$  and within 6 Å (Figure 2b). As shown by the shifted  $N(t)/N(0)$  in Figures 6 and 7, this procedure identified appropriate “shifting times”.

The shifted  $N(t)/N(0)$  are excellently fit by the biexponential function

$$N(t)/N(0) = f_1 \exp(-k_1 t) + f_2 \exp(-k_2 t) \quad (8)$$

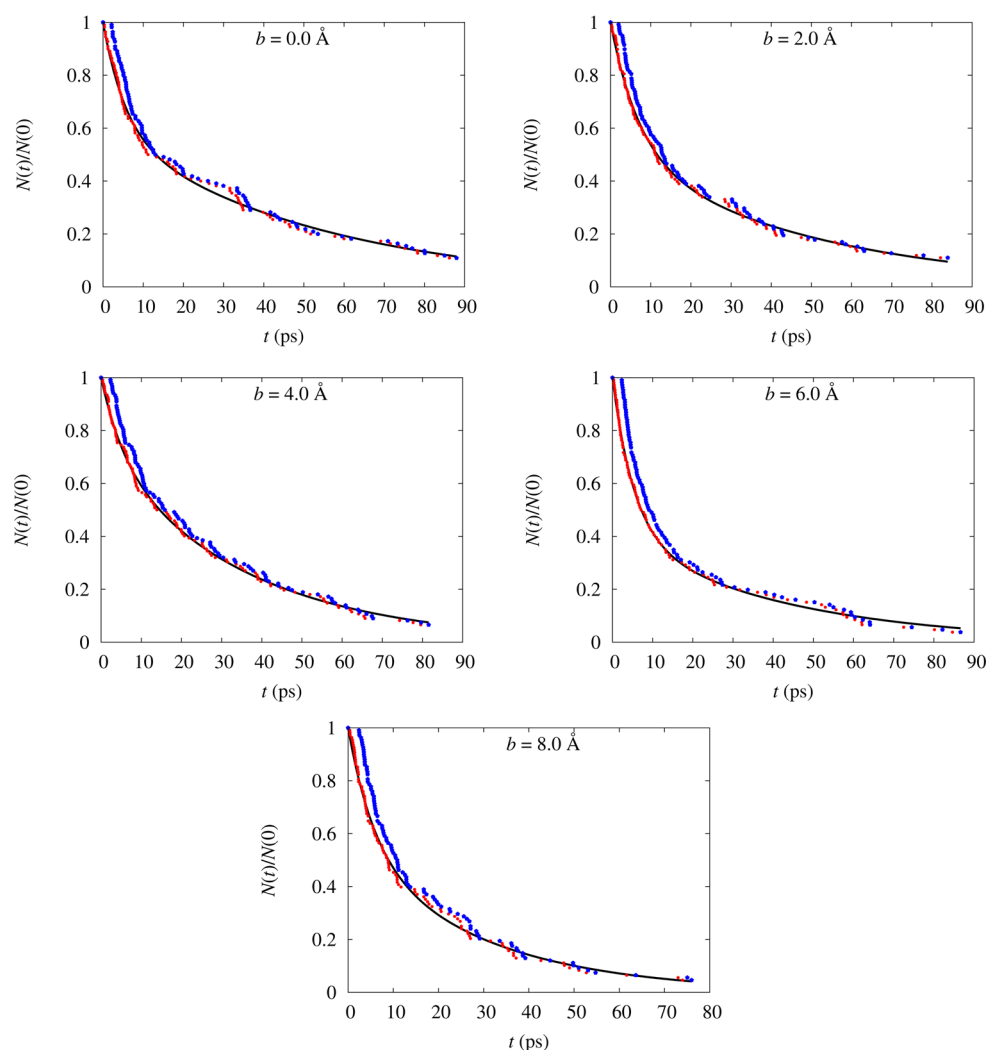
which is illustrated in Figures 6 and 7. The fit has a constraint of  $f_1 + f_2 = 1$ . The  $f$  and  $k$  fitting parameters are listed in Table 1. Overall, the  $k$  values are larger at 1000 K, but their difference with the 750 K values is not striking. At 750 K, the  $k_1$  are 5–10 times larger than the  $k_2$ . At 1000 K, the  $k_1/k_2$  ratio is similar and 5–8. The nonexponential  $N(t)/N(0)$  distributions are expected as the result of the initial nonrandom excitation of the  $\text{Na}^+(\text{Bz})_2^*$  cluster by  $\text{Bz} + \text{Na}^+(\text{Bz})$  association.<sup>54,55</sup>

As discussed above, the clusters that are formed can dissociate one or both of the Bz molecules, or remain intact when the trajectories are halted at 90 ps. Of interest is to compare the dissociation probability for the benzene molecule Bz2, which associates to form the cluster with that for Bz1 which was initially attached to  $\text{Na}^+$ , i.e., the association reaction is  $\text{Bz2} + \text{Na}^+(\text{Bz1})$ . These probabilities are given in Figures 8 and 9 for the 750 and 1000 K simulations, and for the events in which only one benzene molecule dissociates versus time. The dissociation probabilities at time  $t$  are given as the total number of dissociations of Bz1 or Bz2 at  $t$  divided by the total number of clusters formed. The difference between unity and the sum of the long-time Bz1 and Bz2 dissociation probabilities is the sum of the probability that both Bz molecules dissociate and the probability the cluster remains intact when the trajectory is halted at 90 ps.

Figures 8 and 9 show that there is not a major difference in the dissociation probabilities for the Bz1 and Bz2 molecules. Since energy is released into the  $\text{Na}^+\text{-Bz2}$  bond when Bz2 associates, it might be expected that Bz2 would have the higher dissociation probability. However, this is not the case. For the 750 K simulations, with impact parameters of 0 and 6 Å, it is Bz1 that has the significantly higher dissociation probability. Bz2 does not have a significantly higher dissociation probability at short times for any of the simulations.

**2. Comparison with Previous Simulations of Randomly Excited  $\text{Na}^+(\text{Bz})_2^*$  Clusters.** In a previous chemical dynamics simulation,<sup>42</sup> the classical unimolecular dynamics of randomly excited  $\text{Na}^+(\text{Bz})_2^*$  was studied. With random initial conditions, the cluster dissociated with an exponential probability versus time, in accord with RRKM theory. The total  $\text{Na}^+(\text{Bz})_2^*$  energies considered in these simulations are 164.5, 191.9, 219.4, and 246.8 kcal/mol, for which the respective microcanonical rate constants for the exponential decomposition are 0.013, 0.030, 0.063, and  $0.105 \text{ ps}^{-1}$ . For the current study,  $\text{Na}^+(\text{Bz})_2^*$  is nonrandomly excited at total energies of 186.4 and 209.2 kcal/mol by  $\text{Na}^+(\text{Bz}) + \text{Bz}$  association. Interpolating the above energies and rate constants from the previous study yields microcanonical rate constants of 0.027 and  $0.051 \text{ ps}^{-1}$  for the energies of 186.4 and 209.2 kcal/mol.

As discussed above, the dissociation probabilities  $N(t)/N(0)$ , for the nonrandomly excited  $\text{Na}^+(\text{Bz})_2^*$  clusters in the current

$T = 750 \text{ K}$ 

**Figure 6.** Relative population,  $N(t)/N(0)$ , of  $\text{Na}^+(\text{Bz})_2^*$  clusters versus time for the 750 K simulations at different collision impact parameters. The blue and red points are the simulation and shifted  $N(t)/N(0)$ , respectively. The black curve is the fit to the shifted  $N(t)/N(0)$  with the biexponential function in eq 8.  $\text{Na}^+(\text{Bz})$  has a 750 K Boltzmann distribution of vibrational and rotational energies for  $\text{Na}^+(\text{Bz}) + \text{Bz} \rightarrow \text{Na}^+(\text{Bz})_2^*$  association.  $E_{\text{rel}}$  is 2.2 kcal/mol for the association simulation, which is the average  $E_{\text{rel}}$  at 750 K.

study are well fit by a biexponential function with the  $k_2$  rate constant  $\sim 10$  times smaller than  $k_1$ ; see Table 1. It is of interest to see whether  $k_2$ , for the long-time component of  $N(t)/N(0)$ , agrees with the above interpolated microcanonical rate constant. For the current 750 K simulation, with total energy of 186.4 kcal/mol, the fraction of the long-time component for the different impact parameters varies from 0.41–0.72 and  $k_2$  varies from 0.018–0.034  $\text{ps}^{-1}$ . The interpolated microcanonical rate constant of 0.027  $\text{ps}^{-1}$  is consistent with this range of values. Similarly, the  $k_2$  values for the 1000 K simulations (total energy of 209.2 kcal/mol) are consistent with the interpolated microcanonical rate constant of 0.051  $\text{ps}^{-1}$ . For the impact parameters with a long-time component of 0.23 and longer,  $k_2$  varies from 0.028–0.057.

The above analysis indicates that, though the nonrandomly excited  $\text{Na}^+(\text{Bz})_2^*$  clusters initially dissociate with a rate constant larger than the RRKM microcanonical value, at long times the rate constant agrees with the RRKM prediction. Such dynamics occur when the initial nonrandom ensemble of  $\text{Na}^+(\text{Bz})_2^*$  clusters undergoes intramolecular vibrational energy redistrib-

ution (IVR) to form a microcanonical ensemble.<sup>58–60</sup> The relaxation time for IVR is then expected to be shorter than the RRKM lifetime which ranges from 20–37 ps. That the long-time dissociation of nonrandomly excited  $\text{Na}^+(\text{Bz})_2^*$  agrees with RRKM theory is consistent with the previous simulation study, for which a microcanonical ensemble of  $\text{Na}^+(\text{Bz})_2^*$  has intrinsic RRKM dynamics<sup>58</sup> and dissociates exponentially with the RRKM rate constant.

**3. Coupled Phase Space Model for Nonexponential Dissociation.** In previous work, Marcus et al.<sup>61</sup> presented a coupled phase space model for describing the type of nonstatistical unimolecular dynamics found here. The model was recently considered for a  $\text{S}_{\text{N}}2$  ion–molecule intermediate.<sup>62</sup> It consists of two phase space regions 1 and 2 with state densities of  $N_1$  and  $N_2$ . Region 1 is populated by the excitation step, which is  $\text{Na}^+(\text{Bz}) + \text{Bz} \rightarrow \text{Na}^+(\text{Bz})_2^*$  association for the current study. The intramolecular relaxation and unimolecular dissociation processes are



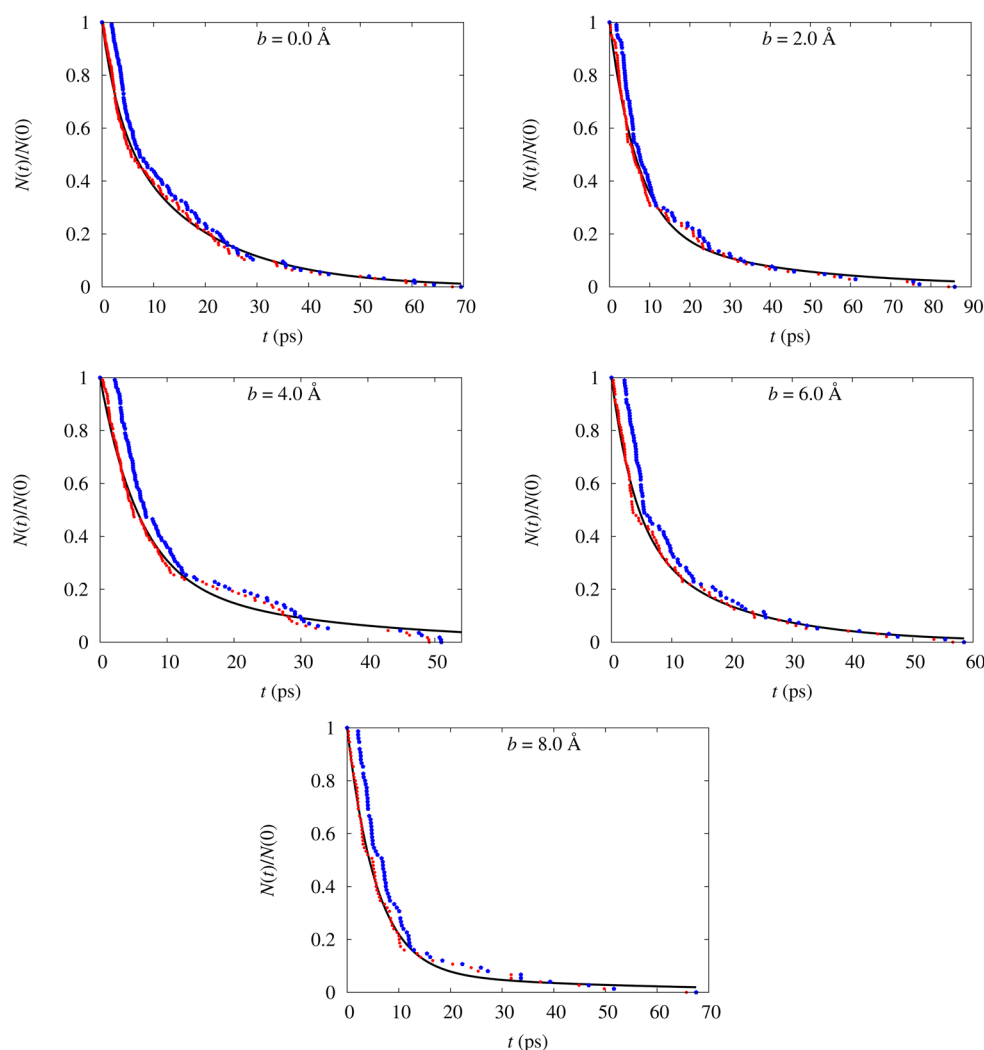
$T = 1000 \text{ K}$ 

Figure 7. Same as Figure 6, but for the 1000 K simulations.  $E_{\text{rel}}$  is 3.0 kcal/mol.

Table 1. Parameters for Fits to the  $N(t)/N(0)$  Distributions<sup>a</sup>

$b^c$	fitting parameters <sup>b</sup>			
	$f_1$	$f_2$	$k_1$	$k_2$
750 K				
0	0.41	0.59	0.181	0.018
2	0.49	0.51	0.141	0.020
4	0.28	0.72	0.180	0.028
6	0.59	0.41	0.187	0.024
8	0.45	0.55	0.174	0.034
1000 K				
0	0.36	0.64	0.301	0.057
2	0.77	0.23	0.145	0.028
4	0.75	0.25	0.173	0.035
6	0.58	0.42	0.258	0.057
8	0.92	0.08	0.178	0.021

<sup>a</sup>The collision energy is  $3RT/2$ . <sup>b</sup>The rate constants  $k$  are in the units of  $\text{ps}^{-1}$ . <sup>c</sup>The impact parameter  $b$  is in the unit of angstroms.



where  $k_b$  and  $k_c$  are IVR rate constants. The  $t = 0$  initial populations of the two phase space regions are  $N_1(0) = N(0)$  and  $N_2(0) = 0$ . The total number of excited molecules versus time is  $N(t) = N_1(t) + N_2(t)$ , and is biexponential and given by

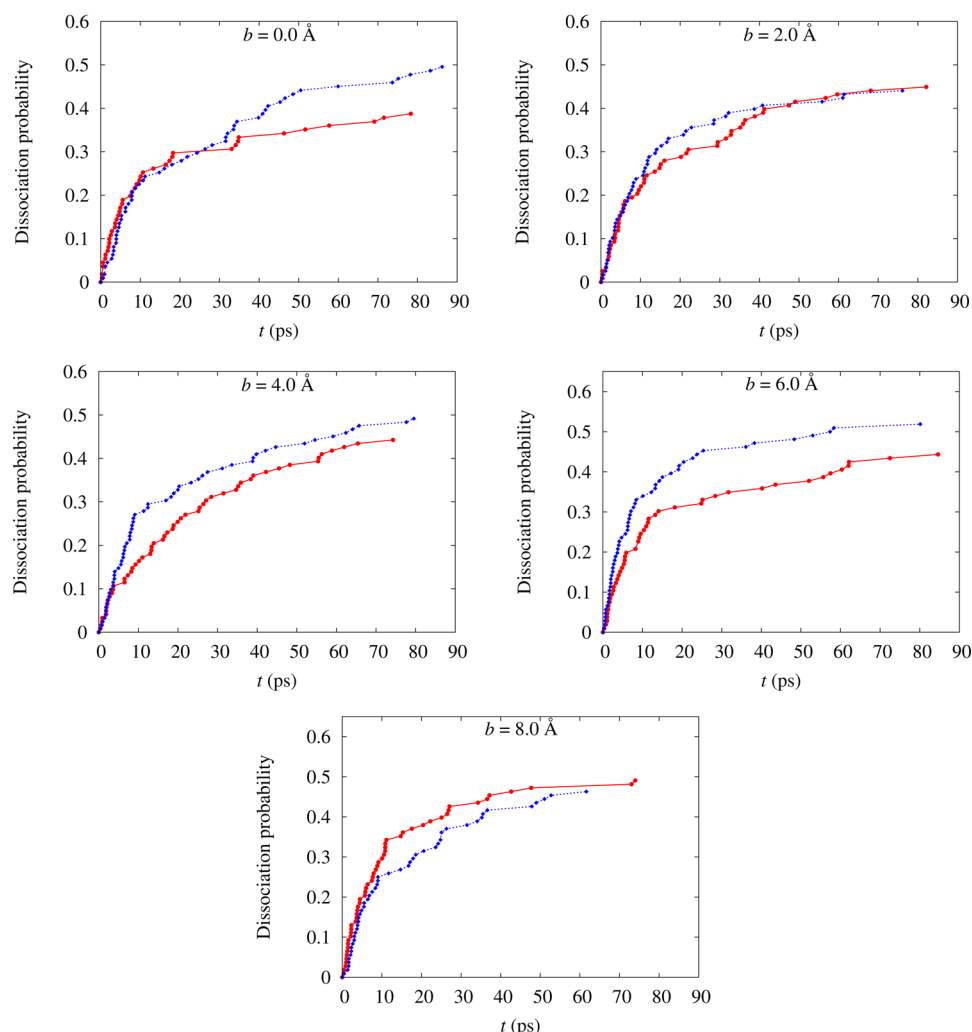
$$N(t)/N(0) = [(k_a - \lambda_2)e^{-\lambda_1 t} - (k_a - \lambda_1)e^{-\lambda_2 t}]/(\lambda_1 - \lambda_2) \quad (10)$$

where  $\lambda_1$  and  $\lambda_2$  are the eigenvalues for the linear system in eqs 9b and 9c, and satisfy

$$\lambda_1 + \lambda_2 = k_a + k_b + k_c \quad \lambda_1 \lambda_2 = k_a k_c \quad (11)$$

The parameters for the biexponential in eq 10 are related to  $f_1$ ,  $f_2$ ,  $k_1$ , and  $k_2$  in eq 8, i.e.,  $\lambda_1 = k_1$ ,  $\lambda_2 = k_2$ , and  $f_1 = (k_a - k_2)/(k_1 - k_2)$ . Using the parameters in Table 1, two representative sets of  $k_a$ ,  $k_b$ , and  $k_c$  in  $\text{ps}^{-1}$  are those for the 1000 K simulations with  $b$  of 4 and 8 Å: i.e.,  $b = 4 \text{ Å}$ ,  $k_a = 0.139$ ,  $k_b = 0.026$ , and  $k_c = 0.044$ ; and  $b = 8 \text{ Å}$ ,  $k_a = 0.165$ ,  $k_b = 0.011$ , and  $k_c = 0.023$ . For all five 1000 K simulations in Table 1,  $k_a$  ranges from 0.118 to 0.174,  $k_b$  from 0.011 to 0.095, and  $k_c$  from 0.022 to 0.118; and for the 750 K simulations, these ranges are  $k_a$  from 0.071 to 0.120,  $k_b$  from 0.046 to 0.076, and  $k_c$  from 0.036 to 0.071. Given the



$T = 750 \text{ K}$ 

**Figure 8.** Total dissociation probability versus time for dissociating Bz1 and Bz2 from the  $\text{Na}^+(\text{Bz})_2^*$  cluster. Bz2 associates with  $\text{Na}^+(\text{Bz}1)$  to form the cluster. Red points are for Bz2 dissociation and blue points are for Bz1 dissociation. The lines connect the points and are not fits. Simulations are for 750 K.  $\text{Na}^+(\text{Bz})$  has a 750 K Boltzmann distribution of vibrational and rotational energies for  $\text{Na}^+(\text{Bz}) + \text{Bz} \rightarrow \text{Na}^+(\text{Bz})_2^*$  association.  $E_{\text{rel}}$  is 2.2 kcal/mol for the association simulation, which is the average  $E_{\text{rel}}$  at 750 K.

nonexponential dissociation,  $k_a$  larger than  $k_b$  and  $k_c$  is expected.<sup>61</sup> The IVR times for  $k_b$ , i.e.,  $1/k_b$ , range from 10 to 91 ps and those for  $k_c$  range from 8 to 45 ps. These IVR times are similar to, but some are larger than, the RRKM lifetimes of 37 and 20 ps for the respective 750 and 1000 K simulations, given above in Section 2.

The microcanonical RRKM rate constant for the above model is<sup>61</sup>

$$k_{\text{RRKM}} = k_a k_c / (k_b + k_c) \quad (12)$$

For the five sets of 750 K simulation parameters in Table 1, values for this  $k_{\text{RRKM}}$  range from 0.028 to 0.053  $\text{ps}^{-1}$  and for the five 1000 K sets of parameters they range from 0.074 to 0.111  $\text{ps}^{-1}$ . These  $k_{\text{RRKM}}$  range from the same as and only two times larger than the microcanonical unimolecular rate constants determined from the simulations and given above. Their values are 0.027 and 0.051  $\text{ps}^{-1}$  for the 750 and 1000 K simulations, respectively.

In assessing the coupled phase space model in eqs 9, its significant feature is that it gives the biexponential  $\text{Na}^+(\text{Bz})_2^*$  dissociation probability found from the simulation. However, it gives IVR times that seem to be somewhat too large as compared

to the intrinsic RRKM dynamics and RRKM, microcanonical rate constant for  $\text{Na}^+(\text{Bz})_2^*$  dissociation. However, the model's estimate of the microcanonical rate constant is at most only a factor of 2 to large. Although the model has some shortcomings, overall it gives a good description of the simulation dynamics.

#### IV. COMPARISON OF CHEMICAL DYNAMICS SIMULATIONS OF ION–MOLECULE ASSOCIATION RATE CONSTANTS

In Table 2, the rate constants calculated for  $\text{Na}^+(\text{Bz}) + \text{Bz}$  association are compared with those for other ion–molecule associations, determined from previous chemical dynamics simulations. For these previous studies, the rate constant decreases with increase in temperature as found here for  $\text{Na}^+(\text{Bz}) + \text{Bz}$  association. Overall, the rate constants for the different associations are similar, but they increase as the strength of the ion–molecule attractive potential increases; e.g., at 300 K the  $\text{Li}^+ + \text{H}_2\text{O}$  rate constant is about 2.5 times larger than that for  $\text{K}^+ + \text{H}_2\text{O}$ . The association rate constants for  $\text{Na}^+(\text{Bz}) + \text{Bz}$  at 750 and 1000 K are similar to that for  $\text{Cl}^- + \text{CH}_3\text{Cl}$  at 1000 K.

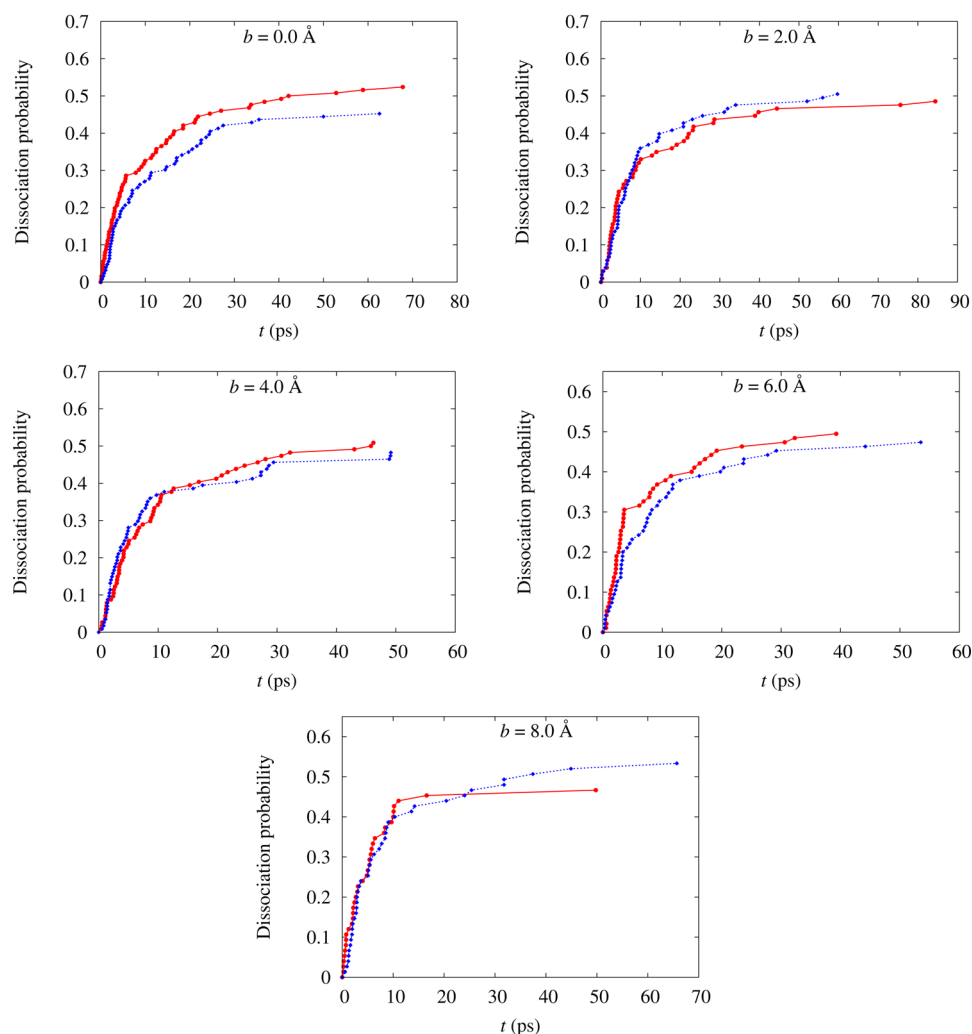
$T = 1000 \text{ K}$ 

Figure 9. Same as Figure 8, , but for the 1000 K simulations.  $E_{\text{rel}}$  is 3.0 kcal/mol.

Table 2. Ion–Molecule Association Rate Constants from Chemical Dynamics Simulations

association	$T$ (K)	rate constant <sup>a</sup>	ref.
$\text{K}^+ + \text{H}_2\text{O}$	300	$1.3 \times 10^{-9}$	36
$\text{Li}^+ + \text{H}_2\text{O}$	300	$3.1 \times 10^{-9}$	36
$\text{Li}^+(\text{H}_2\text{O}) + \text{H}_2\text{O}$	300	$4.2 \times 10^{-9}$	36
$\text{Li}^+ + (\text{CH}_3)_2\text{O}$	200	$12.0 \times 10^{-9}$	37
	300	$8.0 \times 10^{-9}$	37 <sup>b</sup>
	1000	$4.8 \times 10^{-9}$	37
$\text{Cl}^- + \text{CH}_3\text{Cl}$	200	$2.2 \times 10^{-9}$	39
	300	$1.7 \times 10^{-9}$	39
	500	$1.2 \times 10^{-9}$	39
	1000	$7.0 \times 10^{-10}$	39
$\text{Na}^+(\text{Bz}) + \text{Bz}$	750	$8.3 \times 10^{-10}$	This work
	1000	$8.0 \times 10^{-10}$	This work

<sup>a</sup>Rate constant is in units of  $\text{cm}^3/\text{molecule}\cdot\text{sec}$ . <sup>b</sup>In an earlier study (ref 36), a rate constant of  $5.2 \times 10^{-9} \text{ cm}^3/\text{molecule}\cdot\text{sec}$  was reported for  $\text{Li}^+ + (\text{CH}_3)_2\text{O}$  at 300 K.

The  $\text{Li}^+ + (\text{CH}_3)_2\text{O}$  association rate constant at 1000 K is six times larger than that for  $\text{Na}^+(\text{Bz}) + \text{Bz}$ .

## V. SUMMARY

Chemical dynamics simulations were performed to study  $\text{Na}^+(\text{Bz}) + \text{Bz}$  association at 750 and 1000 K to form the vibrationally/rotationally excited  $\text{Na}^+(\text{Bz})_2^*$  cluster. The ensuing unimolecular dissociation of this cluster was also investigated. Four trajectory types were found in the simulations, and for two, the colliding Bz molecule directly scattered off  $\text{Na}^+(\text{Bz})$  without forming a  $\text{Na}^+(\text{Bz})_2^*$  cluster. For most of these trajectories, the  $\text{Na}^+-\text{Bz}$  separation for the colliding Bz molecule remained greater than 6.0 Å, without a strong  $\text{Na}^+-\text{Bz}$  interaction. However, for some, the separation became quite small, and the  $\text{Na}^+-\text{Bz}$  interaction was strong. However, the reactant collision energy was not transferred to vibration and/or rotation energy of the  $\text{Na}^+(\text{Bz}) + \text{Bz}$  system and a  $\text{Na}^+(\text{Bz})_2^*$  cluster was not formed.<sup>36–41,63</sup> The third and fourth trajectory types are formation of the  $\text{Na}^+(\text{Bz})_2^*$  cluster and a direct noncluster displacement reaction, for which the colliding Bz molecule directly displaces Bz attached to  $\text{Na}^+$ ; i.e.,  $\text{Bz} + \text{Na}^+(\text{Bz}) \rightarrow \text{Na}^+(\text{Bz}) + \text{Bz}$ .

Cross sections and rate constants were calculated for the  $\text{Bz} + \text{Na}^+(\text{Bz}) \rightarrow \text{Na}^+(\text{Bz})_2^*$  association and  $\text{Bz} + \text{Na}^+(\text{Bz}) \rightarrow \text{Na}^+(\text{Bz}) + \text{Bz}$  direct displacement reactions. For the association reaction, both the cross section and rate constant decreased as the

temperature was increased from 750 to 1000 K. However, the cross section and rate constant increased for the direct displacement reaction with this increase in temperature. At 750 K the cross section for direct displacement is  $\sim 20$  times smaller than that for association, while this factor is  $\sim 10$  at 1000 K. The uncertainty in the calculated association cross section is small and only 6–7%. For the displacement cross section, the uncertainty is larger and 25–30%. However, since the displacement reaction makes only a small contribution to the total reaction, its rather large uncertainty does not appreciably affect the uncertainty for the overall reaction rate. The rate constant for  $\text{Bz} + \text{Na}^+(\text{Bz}) \rightarrow \text{Na}^+(\text{Bz})_2^*$  association is consistent with chemical dynamics simulations of rate constants for other ion–molecule associations.<sup>34–41</sup> The  $\text{Bz} + \text{Na}^+(\text{Bz})$  association rate constant at 1000 K is similar to that determined for  $\text{Cl}^- + \text{CH}_3\text{Cl}$  association at the same temperature.<sup>39</sup> In a simulation of  $\text{H}_2\text{O} + \text{Li}^+(\text{H}_2\text{O})$  a direct displacement reaction was found as found here for  $\text{Bz} + \text{Na}^+(\text{Bz})$ .<sup>36</sup>

The dissociation probability  $N(t)/N(0)$  of the energized  $\text{Na}^+(\text{Bz})_2^*$  clusters, prepared by  $\text{Bz} + \text{Na}^+(\text{Bz})$  association, is biexponential. The fractions for the two components in the biexponential are similar in size, with the rate constant for the short-time component approximately an order of magnitude larger than that for longer times. This nonexponential dissociation is a result of the nonrandom excitation of the  $\text{Na}^+(\text{Bz})_2^*$  clusters by  $\text{Bz} + \text{Na}^+(\text{Bz})$  association.<sup>58,59</sup> The rate constant for the long-time component agrees with that of RRKM theory, consistent with rapid IVR<sup>60</sup> and intrinsic RRKM<sup>58</sup> unimolecular dynamics. The Bz molecules of the  $\text{Na}^+(\text{Bz})_2^*$  cluster have nearly equal dissociation probabilities.

Ion–molecule association is expected to initially preferentially and nonrandomly excite the intermolecular modes of the ion–molecule complex. Vibrational energy will then transfer from the intermolecular to intramolecular modes. For  $\text{Na}^+(\text{Bz})_2^*$  this IVR is sufficiently rapid that, if the molecule is excited randomly, its dissociation probability is exponential and in accord with RRKM theory.<sup>42</sup> However, not all ion–molecule complexes have such intrinsic RRKM dynamics. An illustrative example is the  $\text{Cl}^- - \text{CH}_3\text{Cl}$  ion–dipole complex for the  $\text{Cl}^- + \text{CH}_3\text{Cl}$   $\text{S}_\text{N}2$  nucleophilic substitution reaction.<sup>39</sup> For this system there is weak coupling between the intermolecular and intramolecular modes, and, though not quantified, IVR is slow.

The different IVR dynamics for  $\text{Na}^+(\text{Bz})_2^*$  and  $\text{Cl}^- - \text{CH}_3\text{Cl}$  may be understood by considering their intermolecular and intramolecular vibrational frequencies  $\nu$ . IVR occurs via resonance pathways and when the number of these pathways and their couplings increase IVR is enhanced.<sup>64</sup> The intermolecular  $\nu$  values for  $\text{Na}^+(\text{Bz})_2^*$  range from 40 to 271  $\text{cm}^{-1}$ , while the Bz intramolecular  $\nu$  values are as low as 400 and 613  $\text{cm}^{-1}$ . Thus, there are low-order resonance conditions for IVR in  $\text{Na}^+(\text{Bz})_2^*$ . By contrast, there are no low-order resonance conditions for IVR in  $\text{Cl}^- - \text{CH}_3\text{Cl}$ . The three intermolecular frequencies are 71(2) and 101  $\text{cm}^{-1}$  and the lowest  $\text{CH}_3\text{Cl}$  intramolecular frequency is the 783  $\text{cm}^{-1}$  C–Cl stretch.<sup>39</sup> Thus, IVR for ion–molecule complexes may be qualitatively understood by considering resonance conditions between the intermolecular and intramolecular modes of the complex.

## AUTHOR INFORMATION

### Notes

The authors declare no competing financial interest.

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