

Structure and Bonding of $\text{Sr}_3\text{In}_{11}$: How Size and Electronic Effects Determine Structural Stability of Polar Intermetallic Compounds

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Received June 3, 2003

The binary compound $\text{Sr}_3\text{In}_{11}$ ($\text{SrIn}_{3.667}$) was synthesized and structurally characterized by X-ray diffraction experiments. It crystallizes in the orthorhombic $\text{La}_3\text{Al}_{11}$ structure type (space group $Immm$, $Z = 2$; $a = 4.9257(6)$, $b = 14.247(2)$, $c = 11.212(2)$ Å). The crystal structure of $\text{Sr}_3\text{In}_{11}$ bears features of the monoclinic EuIn_4 structure, which is adopted by SrIn_4 , and the prominent tetragonal BaAl_4 structure. $\text{Sr}_3\text{In}_{11}$ is stable until 550 °C. At higher temperatures it decomposes peritectically into SrIn_2 and In . Structural stability and bonding properties of $\text{Sr}_3\text{In}_{11}$ were investigated by first principles calculations and compared to SrIn_4 in the monoclinic EuIn_4 and the tetragonal BaAl_4 structure. All three structures consist of a three-dimensional, polyanionic, network formed by In atoms and Sr cations encapsulated in cages. For the BaAl_4 -type SrIn_4 , In – In network bonding is perfectly optimized. In contrast, the networks of EuIn_4 -type SrIn_4 and $\text{Sr}_3\text{In}_{11}$ appear hypo- and hyperelectronic, respectively. The formation of $\text{Sr}_3\text{In}_{11}$ with a composition close to 1:4 and the nonexistence of BaAl_4 -type SrIn_4 is explained by a delicate interplay of size and electronic factors governing structural stability in the In -rich part of the Sr – In system.

1. Introduction

Polar intermetallic compounds represent the link between metallic and nonmetallic s–p-bonded materials. They form between active metals (alkali, alkaline earth, or rare earth metals) with the metallic elements from the triel (Al , Ga , In , Tl) and tetrel groups (Sn , Pb), and their systematic exploration in recent years revealed a wealth of novel and peculiar structures.^{1–6} The p-elements are formally reduced by the electropositive component and form polyanionic clusters or networks with localized multicenter bonding patterns. Thus, bonding in polar intermetallics is intermediate to that of semiconducting Zintl phases with two-center localized bonding within polyanionic entities and s–p-bonded metallic systems without notable internal charge transfer displaying completely delocalized bonding. As a consequence, structural stability of polar intermetallics is not

easily rationalized. The intermediate situation between two bonding types involves a complicated interplay between electronic factors and size and packing effects.

Corbett et al. elaborated on this complex question by exploring binary alkaline earth–triel systems with three-dimensional polyanionic networks. In particular, the Sr – In system afforded two new and interesting case examples. Sr_3In_5 ⁷ and SrIn_4 ⁸ both exhibit electron-deficient In networks. The deviation from optimum electron count for In – In network bonding was suggested to be a consequence of optimizing size and packing effects between counteranions and their hosting cavities provided by the In network.^{7,8} In that respect SrIn_4 is especially remarkable. This compound crystallizes in the rarely adopted monoclinic EuIn_4 structure type, whereas the large majority of 1:4 alkaline earth–triel compounds realize the simple tetragonal BaAl_4 structure type. In this work we report on the new Sr – In compound $\text{Sr}_3\text{In}_{11}$ with a composition close to 1:4. The structure of this compound bears features of both tetragonal BaAl_4 and the monoclinic EuIn_4 structures. A stability and bonding analysis of $\text{Sr}_3\text{In}_{11}$ performed on the basis of first principles calculations strongly corroborates the ideas developed by Corbett. Thus, the Sr – In system appears especially susceptible for

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principal studies concerning structural and phase stability in polar intermetallic compounds.

2. Experimental Section

2.1. Synthesis. The title compound was obtained in an attempt to prepare a high-temperature form of SrIn₄ with the tetragonal BaAl₄ structure. All materials were handled in an Ar-filled glovebox that had moisture and oxygen levels below 1 ppm. Samples were prepared with an excess of In. Under this condition the solid indide is in equilibrium with an In-rich melt (self-flux condition), which is very favorable for crystal growth. Mixtures of Sr (ABCR, 99.9%) and In (ABCR, 99.999%) with an atomic ratio of 1:8 were loaded into specially prepared stainless steel ampules as described by Boström.⁹ These ampules contained the reaction mixture at the bottom and a layer of coarsely crushed quartz glass fixed by a plug of quartz wool at the top. Sealed ampules were put into a quartz wool insulated reaction container made of stainless steel, which was subsequently placed into a furnace. The reaction mixture was first heated to 700 °C for 12 h to ensure complete melting and mixing of the metals. After that, temperature was lowered to a reaction temperature between 300 and 450 °C. According to the reported Sr–In phase diagram,¹⁰ in this temperature range a composition 1:8 corresponds to an equilibrium between melt and the In-rich compound. After a reaction time of 48 h the reaction container was turned upside down into a centrifuge which was operated at 3000 rpm for 3 min. The ampule was opened, and the crystalline product was collected from the top of the quartz wool plug. It displayed a silvery luster and was characterized by powder X-ray diffraction patterns taken on a Guinier powder camera with Cu Kα₁ radiation ($\lambda = 1.540\,562\text{ Å}$) and by compositional analysis with the EDX (energy-disperse X-ray) method in a JEOL 820 scanning electron microscope. The average composition of five crystallites was 21.9(5) at. % Sr and 78.1(5) at. % In. Sr₃In₁₁ is very sensitive to moisture and decomposes rapidly in air.

2.2. Structure Determination. The lattice parameters of Sr₃In₁₁ were obtained from a least-squares refinement of 17 measured and indexed lines in the Guinier powder pattern (Si standard).¹¹ To ensure proper assignment of the indices the observed lines were compared with the calculated ones¹² using the positional parameters resulting from the structure refinements. A needle-shaped Sr₃In₁₁ crystal was picked from the 450 °C synthesis sample and sealed in a capillary. Intensity data was collected at 170 K on a STOE IPDS diffractometer with monochromatic Mo Kα radiation ($\lambda = 0.710\,73\text{ Å}$). All data sets were corrected for Lorentz and polarizations effects. Absorption correction was performed by the program X-shape as included in the STOE IPDS software.¹³ The space group *Immm* was assigned on the basis of the systematic absences and the statistical analysis of the intensity distributions. Structure determination (direct methods) and refinement (full-matrix least squares on F^2) of Sr₃In₁₁ was performed with the program SHELX-97 and revealed two and four fully occupied Sr and In positions, respectively.¹⁴ Some details of the single-crystal data collections and refinements are listed in Table 1. Atomic position parameters

Table 1. X-ray Single-Crystal Refinement Data for Sr₃In₁₁^a

| | |
|--|---|
| chem formula | Sr ₃ In ₁₁ |
| lattice params (Å) | $a = 4.9257(6)$ $b = 14.247(2)$ $c = 11.212(2)$ |
| $V (\text{Å}^3)$ | 786.86(19) |
| space group, Z | <i>Immm</i> , 2 |
| T (K) | 170 |
| fw | 1525.9 |
| λ (Å) | 0.710 73 |
| ρ_{calcd} (g/cm ³) | 6.51 |
| μ (mm ⁻¹) | 26.08 |
| R_1, wR_2 | 0.0224, 0.0564 |

^a $R_1 = \sum |F_o| - |F_c| / \sum |F_o|$. $wR_2 = (\sum [w(F_o^2 - F_c^2)^2]) / (\sum [w(F_o^2)^2])$, $w = 1/[\sigma^2(F_o^2) + (aP)^2 + bP]$ and $P = (F_o^2 + 2F_c^2)/3$ ($a = 0.031$, $b = 0$). The lattice parameters are obtained from Guinier X-ray powder data (Cu Kα₁, 23 °C, 17 indexed lines).

Table 2. Atomic Coordinates and Isotropic-Equivalent Thermal Displacement Parameters for Sr₃In₁₁

| | site | x | y | z | U_{eq}^a |
|-----|------|-----|-----------|-----------|-------------------|
| Sr1 | 2a | 0 | 0 | 0 | 0.0072(3) |
| Sr2 | 4g | 0 | 0.3102(1) | 0 | 0.0077(2) |
| In1 | 2c | 1/2 | 1/2 | 0 | 0.0127(3) |
| In2 | 4j | 1/2 | 0 | 0.6954(1) | 0.0108(2) |
| In3 | 8l | 0 | 0.3426(1) | 0.3726(1) | 0.0088(2) |
| In4 | 8l | 0 | 0.1475(1) | 0.2753(1) | 0.0094(2) |

^a U_{eq} is defined as one-third of the trace of the orthogonalized U_{ij} tensor.

Table 3. Selected Bond Lengths in Sr₃In₁₁^a

| | | | | | |
|---------|-------|----|---------|-------|----|
| In1–In4 | 3.281 | ×4 | In4–In3 | 2.973 | ×2 |
| In1–In2 | 3.297 | ×4 | In4–In3 | 2.985 | |
| | | | In4–In2 | 3.254 | ×2 |
| In2–In3 | 2.996 | ×2 | In4–In1 | 3.281 | |
| In2–In4 | 3.254 | ×4 | | | |
| In2–In1 | 3.297 | ×2 | Sr1–In3 | 3.624 | ×8 |
| | | | Sr1–In4 | 3.735 | ×4 |
| In3–In3 | 2.856 | | | | |
| In3–In4 | 2.973 | ×2 | Sr2–In2 | 3.481 | ×2 |
| In3–In4 | 2.985 | | Sr2–In4 | 3.574 | ×4 |
| In3–In2 | 2.996 | | Sr2–In3 | 3.583 | ×4 |
| | | | Sr2–In1 | 3.658 | ×2 |
| | | | Sr2–In1 | 3.860 | ×2 |

^a Standard deviations are equal or less than 0.001 Å.

and selected interatomic distances are given in Tables 2 and 3. Further details of the crystal structure investigation may be obtained as Supporting Information.

2.3. Electronic Structure Calculations. Total energy calculations for SrIn₄ (BaAl₄- and EuIn₄-types) and Sr₃In₁₁ were performed in the framework of the frozen core all-electron projected augmented wave (PAW) method¹⁵ (as implemented in the program VASP¹⁶). For all systems atomic position parameters and lattice parameters were relaxed for a set of constant volumes until forces had converged to less than 0.01 eV/Å. In a second step, we extracted the equilibrium volume V_0 and its corresponding energy E_0 by fitting the E vs V values to a Birch–Murnaghan equation of state. The exchange and correlation energy was assessed by the generalized gradient approximation (GGA).¹⁷ Convergency of the calculations was checked with respect to the plane wave cutoff and the number of k points used in the summation over the Brillouin zone. Concerning the plane wave cutoff a energy value of 300 eV was

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chosen for all systems. k points were generated by the Monkhorst–Pack method¹⁸ and sampled on grids of $10 \times 10 \times 10$ ($\text{Sr}_3\text{In}_{11}$), $11 \times 11 \times 11$ (SrIn_4 (BaAl_4)), and $8 \times 8 \times 8$ (SrIn_4 (EuIn_4)). The integration over the Brillouin zone was performed with a Gaussian smearing of 20 mRy. Total energies were converged to better than 1 meV/atom.

The TB-LMTO method in the atomic sphere approximation¹⁹ was employed to calculate In–In crystal orbital Hamilton populations (COHP)²⁰ for the three systems. A COHP analysis provides a measure of the bonding character and strength of atomic contacts. The TB-LMTO calculations were performed on the basis of the VASP–PAW relaxed structures. The electronic density of states (DOS) produced by both methods were found to be in good agreement.

3. Results and Discussion

3.1. Comments on the In-Rich Part of the Sr–In Phase Diagram. For the In-rich part of the Sr–In phase diagram the phases SrIn_5 , SrIn_3 , Sr_2In_5 , and SrIn_2 are reported.¹⁰ The former three phases decompose peritectically at 420, 540, and 620 °C, respectively, whereas SrIn_2 melts congruently at 930 °C. The applied melt–centrifugation synthesis method presents an excellent tool for screening particular temperature ranges for thermodynamic stable compounds. We obtained monoclinic SrIn_4 ⁸ from the 1:8 Sr–In reaction mixtures in a temperature interval between 200 and 425 °C. At 450 °C this reaction mixture yielded $\text{Sr}_3\text{In}_{11}$. Thus, it can be safely stated that SrIn_4 is the most In-rich compound in the binary system Sr–In. It is stable until $425 + \delta$ °C ($\delta < 25$ K). We proceeded to investigate the In-rich part of the Sr–In phase diagram at higher temperatures. To keep the reaction mixture below the liquidus curve the Sr:In ratio was successively decreased. Reaction mixtures with a composition 1:6 were employed between 450 and 550 °C, mixtures 1:5 between 550 and 600 °C, mixtures 1:4 between 600 and 700 °C, and mixtures 1:3 between 700 and 800 °C. $\text{Sr}_3\text{In}_{11}$ was found to be stable until $550 + \delta$ °C ($\delta < 25$ K). At higher temperatures this compound is succeeded by SrIn_2 (CaIn_2 structure type),²¹ which was formed at temperatures between 575 and 800 °C. Importantly, there was no indication of the intermediate phases SrIn_3 and Sr_2In_5 . The temperatures of the peritectic decompositions of SrIn_5 and SrIn_3 are close to those of SrIn_4 and $\text{Sr}_3\text{In}_{11}$. Therefore, it is likely that SrIn_5 corresponds to SrIn_4 and SrIn_3 to $\text{Sr}_3\text{In}_{11}$.

3.2. Crystal Structure Relationships. $\text{Sr}_3\text{In}_{11}$ is the first compound with the $\text{La}_3\text{Al}_{11}$ structure²² exclusively formed by main group metals. There are about 75 representatives for the $\text{La}_3\text{Al}_{11}$ type, most of them ternary compounds consisting of a rare earth metal, a transition metal, and either Ga or Al.²³ Binary compounds exist in rare-earth aluminum and rare-earth zinc systems. The structure of $\text{Sr}_3\text{In}_{11}$ resembles strongly that of tetragonal BaAl_4 but also bears

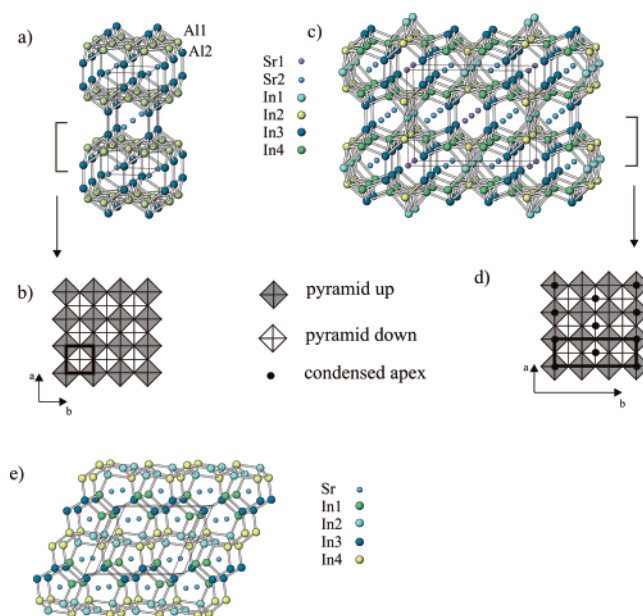


Figure 1. Comparison of the crystal structures of tetragonal BaAl_4 (a), orthorhombic $\text{Sr}_3\text{In}_{11}$ ($\text{La}_3\text{Al}_{11}$ -type) (c), and monoclinic SrIn_4 (EuIn_4 -type) (e). BaAl_4 and $\text{Sr}_3\text{In}_{11}$ consist of layers of square pyramids. These layers and their connection are shown in (b) and (d), respectively.

features of monoclinic SrIn_4 (EuIn_4 type). These structural relationships are discussed in the following (Figure 1).

In body-centered tetragonal BaAl_4 (space group $I4/mmm$) Ba atoms occupy corner and center positions and the Al atoms form a ${}^3[\text{Al}_4]^{2-}$ network (Figure 1a). This network contains two independent sites: the basal Al (Al1) atoms occupy the Wyckoff site 4d and form two-dimensional square nets which are alternately capped above and below the plane by the apical atoms (Al2) on Wyckoff site 4e. The resulting layers of square pyramids (Figure 1b) are connected between Al2 atoms to yield the final network. Orthorhombic body-centered $\text{Sr}_3\text{In}_{11}$ (Figure 1c) can be considered as a ordered defect variant of BaAl_4 .^{24,25} The unit cell is three times larger and contains 28 atoms (6 Sr and 22 In). Two of the apical–apical connections have been condensed to single atoms (In1, Figure 1d), which accounts for the deviation from the composition 1:4 (6:24). In $\text{Sr}_3\text{In}_{11}$ the ratio between apical–apical connections and condensations (defects) is 2:1.²⁶ The introduction of apical atom defects leads to a disruption of the square nets (i.e. the bases of the square pyramids) which change into ribbons along the b axis. These apical atom defects in $\text{Sr}_3\text{In}_{11}$ have also important consequences for the counteranion coordination. In BaAl_4 the coordination polyhedron of Ba corresponds to an 18-vertex space-filling Fedorov polyhedron composed of six- and four-membered rings. In $\text{La}_3\text{Al}_{11}$ -type $\text{Sr}_3\text{In}_{11}$ Sr1 has a comparable coordina-

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(26) The recently discovered compound $\text{Rb}_5\text{Hg}_{19}$ realizes another defect variant of the BaAl_4 -type with an apical–apical connection-to-defect ratio of 4:1.²⁵

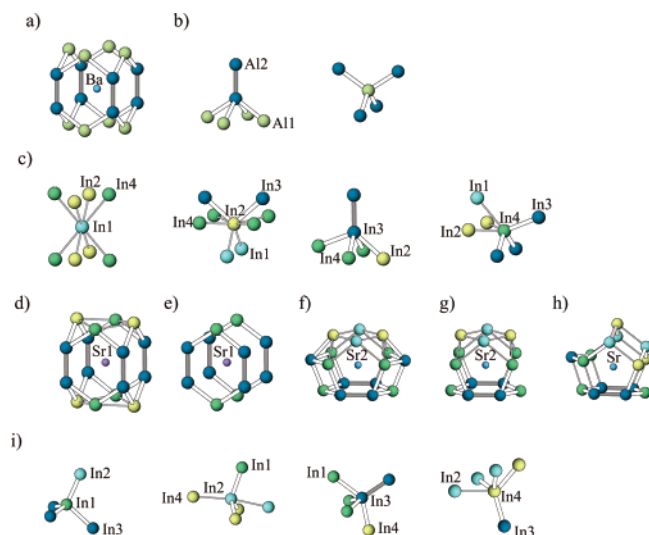


Figure 2. Coordination environment of atoms in the structures of BaAl_4 , $\text{Sr}_3\text{In}_{11}$, and SrIn_4 : (a) Ba and (b) Al coordination in BaAl_4 ; (c) In coordination in $\text{Sr}_3\text{In}_{11}$; (d) extended and (e) actual ($<4 \text{ \AA}$) coordination of Sr1 in $\text{Sr}_3\text{In}_{11}$; (f) extended and (g) actual ($<4 \text{ \AA}$) coordination of Sr2 in $\text{Sr}_3\text{In}_{11}$; (h) Sr coordination in SrIn_4 ; (i) In coordination in SrIn_4 . The three sets of In–In network distances are indicated: gray bold lines, white bold lines, and thin lines represent short, medium, and long distances, respectively.

tion polyhedron, whereas that of Sr2 features five-membered rings. The Sr2 coordination by In is very similar to that of Sr in monoclinic SrIn_4 (Figure 1e).

In the next step we deepen the comparison between the three structures by examining in more detail the local coordination of the network forming atoms and the countercations (Figure 2). We first note that in BaAl_4 Ba is rather 16 coordinated by 8 Al1 and 8 Al2 atoms (Figure 2a), since two additional Al2 atoms are distinctly farther away from the center of the Fedorov polyhedron (cf. Figure 1a). Al1 is nearly tetrahedrally surrounded by four Al2 atoms, Al2 is surrounded by four Al1, and one Al2 in a square pyramidal fashion (Figure 2b). According to the bonding description of Zheng and Hoffmann²⁷ and Burdett and Miller,²⁸ Al2–Al2 two-center two-electron (2c2e) bonds connect neighboring sheets of square pyramids. The second bonding contact in this network is the distance between Al1 and Al2 atoms yielding localized multicenter (5c6e) bonding in the pyramids Al_2Al_1_4 . The distance between two Al1 atoms in the square net is long and considered to be nonbonding. The condensation of apexes in $\text{Sr}_3\text{In}_{11}$ leads to a square prismatic coordination of In1 by four In2 and four In4 atoms (Figure 2c). The distances of In1 to its nearest neighbors (cf. Table 3) compare to those in elemental bct-In ($3.25 \text{ \AA} \times 4$ and $3.38 \text{ \AA} \times 8$).²⁹ In3 corresponds to apical Al2 in the BaAl_4 structure. Its 1 + 4 coordination is clearly recognizable. In2 and In4 correspond to the basal Al1 atoms. However, their local coordination is increased to 2 + 6 and 3 + 3, respectively. The shorter distances (of about 3.0 \AA) involve formally apical In3 atoms, and the longer ones (of about 3.3 \AA) involve further In2 and In4 atoms. The latter distances

are in the range of nearest neighbor distances in elemental In. This is an important difference to the network of the BaAl_4 structure. For all alkaline earth–trial compounds, the interbasal distance (i.e. the distance of the square net) is considerably longer than nearest neighbor distances in the elemental structures of the constituting triels metals. Remarkably, the In–In distances in the $\text{Sr}_3\text{In}_{11}$ network are distinctively split into three sets (Table 3). The shortest distance of 2.86 \AA occurs between two In3 atoms. This is the formally apical–apical connection, which might be associated with a 2c2e bond. The next set of distances (In3–In2, In3–In4) is in the narrow range between 2.97 and 3.0 \AA and might be associated with localized multicenter bonding. The third set (In1–In4, In1–In2, In2–In4) between 3.25 and 3.3 \AA corresponds to formally interbasal distances. Their distance distribution compares well with that of the nearest-neighbor distances in elemental In and, thus, indicates metallic bonding interaction between the involved atoms.

Next we turn to the countercation coordinations. Sr1 in $\text{Sr}_3\text{In}_{11}$ corresponds to Ba in BaAl_4 , which has a 16 atom coordination (Figure 2d). This number, however, appears reduced to 12 atoms ($8 \times \text{In3}$ and $4 \times \text{In4}$) for Sr1 (Figure 2e). Figure 2f shows an extended coordination environment for Sr2. Sr2 is sandwiched between two pentagon rings which are connected by a ring of 6 more In atoms which forms a plane with Sr2. Of this 16 atoms only 14 (or rather $12 + 2$) can be considered as nearest neighbor coordination for Sr2 (Figure 2g). Interestingly, the Sr2 coordination in $\text{Sr}_3\text{In}_{11}$ greatly resembles the Sr coordination in monoclinic SrIn_4 . There, the two In pentagon rings sandwiching Sr are connected by a ring of 5 additional In atoms, which, however, has a quite irregular shape (Figure 2h). Also, the local coordination of the In atoms in SrIn_4 bears similarities to $\text{Sr}_3\text{In}_{11}$ (Figure 2i). In3 can be identified as an apical, 1 + 4 coordinated atom, and In1, as a basal, tetrahedrally coordinated atom. The distances in the In network of SrIn_4 show a similar, although not so pronounced, splitting in three sets as in $\text{Sr}_3\text{In}_{11}$. The shortest In–In distance (between two In 3 atoms) is 2.85 \AA , the next group of distances is in a range of 2.91 to 3.08 \AA , and the third set is between 3.28 and 3.32 \AA (see ref 8 and the discussion in the next section).

The comparison of the crystal structures of $\text{Sr}_3\text{In}_{11}$, SrIn_4 , and BaAl_4 allows some conclusions. In the BaAl_4 structure, which has the highest symmetry, network forming atoms and countercations have low and high coordination numbers, respectively. For SrIn_4 the BaAl_4 structure leads to a size mismatch between the volumes of the countercation and its coordination polyhedron (cage) provided by the In network. This was already stressed by Corbett.⁸ However, there is a strong driving force to form a 1:4 compound in the Sr–In system, and there appear two solutions to this dilemma. Instead of realizing the tetragonal BaAl_4 structure, SrIn_4 adopts the monoclinic EuIn_4 structure and, additionally, a slightly In-deficient compound ($\text{SrIn}_{3.667}$) with a structure closely related to BaAl_4 is formed. Compared to BaAl_4 , in the structures of SrIn_4 and $\text{Sr}_3\text{In}_{11}$ the coordination number of the Sr atoms is lowered (i.e. the size of their coordination polyhedra is decreased) and in turn the coordination number

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Table 4. Calculated Lattice Parameters and Formation Enthalpies ($\Delta H_f = E(\text{Sr}_m\text{In}_n) - (m \times E(\text{Sr}) + n \times E(\text{In}))$) for SrIn_4 (BaAl₄- and EuIn₄-Types) and $\text{Sr}_3\text{In}_{11}$ ^a

| | SrIn_4 (BaAl ₄): tetragonal | $\text{Sr}_3\text{In}_{11}$: orthorhombic | SrIn_4 (EuIn ₄): monoclinic |
|------------------------|---|---|---|
| V (Å ³) | 298.25 | 815.86 786.82 | 582.18 557.2 |
| a (Å) | 4.9393 | 4.9688 4.9257 | 12.1265 12.079 |
| b (Å) | | 14.4068 14.247 | 5.2787 5.1245 |
| c (Å) | 12.2251 | 11.3971 11.212 | 10.0346 9.920 |
| β (deg) | | | 114.99 114.85 |
| ΔH_f (eV/atom) | −0.291 | −0.328 | −0.306 |

^a Experimental values are given in italics (SrIn_4 (EuIn₄), ref 8).**Table 5.** Selected Calculated Distances (Å) in SrIn_4 (BaAl₄- and EuIn₄-Types) and $\text{Sr}_3\text{In}_{11}$ ($d < 4$ Å)^a

| SrIn_4 (BaAl ₄) | | $\text{Sr}_3\text{In}_{11}$ | | SrIn_4 (EuIn ₄) | |
|--------------------------------------|-----------------|-----------------------------|--------------------------|--------------------------------------|--------------------------|
| In1–In2 | 2.98×4 | In1–In4 | 3.32 (3.28) $\times 4$ | In1–In2 | 2.98 (2.93) |
| In1–In1 | 3.51×4 | In1–In2 | 3.33 (3.30) $\times 4$ | In1–In3 | 2.99 (2.93) $\times 2$ |
| | | | | In1–In3 | 3.10 (3.08) |
| In2–In2 | 2.80 | In2–In3 | 3.05 (3.00) $\times 2$ | | |
| In2–In1 | 2.98×4 | In2–In4 | 3.28 (3.25) $\times 4$ | In2–In1 | 2.98 (2.93) |
| | | In2–In1 | 3.33 (3.30) $\times 2$ | In2–In4 | 3.00 (2.94) $\times 2$ |
| Sr–In2 | 3.77×8 | | | In2–In4 | 3.27 (3.28) |
| Sr–In1 | 3.94×8 | In3–In3 | 2.90 (2.86) | In2–In2 | 3.35 (3.32) |
| | | In3–In4 | 3.01 (2.97) $\times 2$ | | |
| | | In3–In4 | 3.03 (2.99) | In3–In3 | 2.89 (2.85) |
| | | In3–In2 | 3.05 (3.00) | In3–In4 | 2.96 (2.91) |
| | | | | In3–In1 | 2.99 (2.93) |
| | | In4–In3 | 3.01 (2.97) $\times 2$ | In3–In1 | 3.10 (3.08) |
| | | In4–In3 | 3.03 (2.99) | | |
| | | In4–In2 | 3.28 (3.25) $\times 2$ | In4–In3 | 2.96 (2.91) |
| | | In4–In1 | 3.32 (3.28) | In4–In2 | 3.00 (2.94) $\times 2$ |
| | | | | In4–In4 | 3.05 (3.00) |
| | | Sr1–In3 | 3.66 (3.62) $\times 8$ | In4–In2 | 3.27 (3.28) |
| | | Sr1–In4 | 3.79 (3.74) $\times 4$ | | |
| | | | | Sr–In2 | 3.52 (3.50) |
| | | Sr2–In2 | 3.52 (3.48) $\times 2$ | Sr–In1 | 3.55 (3.51) |
| | | Sr2–In4 | 3.62 (3.57) $\times 4$ | Sr–In2 | 3.63 (3.56) $\times 2$ |
| | | Sr2–In3 | 3.62 (3.58) $\times 4$ | Sr–In1 | 3.64 (3.57) $\times 2$ |
| | | Sr2–In1 | 3.69 (3.66) $\times 2$ | Sr–In3 | 3.66 (3.64) $\times 2$ |
| | | Sr2–In4 | 3.93 (3.86) $\times 2$ | Sr–In1 | 3.71 (3.66) |
| | | | | Sr–In3 | 3.75 (3.68) $\times 2$ |
| | | | | Sr–In4 | 3.76 (3.68) $\times 2$ |
| | | | | Sr–In3 | 3.86 (3.86) |
| | | | | Sr–In4 | 3.90 (3.89) |

^a Experimental values are given in parentheses (SrIn_4 (EuIn₄), ref 8).

of the In atoms is increased. This introduces new, longer, In–In network distances, which compare to those in elemental In. In the following, we attempt to put these considerations on a more quantitative basis.

3.3. Electronic Structure and Bonding Relationships.

We performed first principles density functional calculations to investigate structure and phase competition in the In-rich part of the Sr–In system and to analyze electronic structure and bonding properties of the compounds SrIn_4 and $\text{Sr}_3\text{In}_{11}$. The results of the computational structure optimization are summarized in Tables 4 and 5. An additional table is given as Supporting Information. For $\text{Sr}_3\text{In}_{11}$ the experimental structural parameters are well reproduced, and for SrIn_4 the deviations are somewhat larger. The theoretical equilibrium volume for both compounds is overestimated by about 4%. The overestimation of ground state volumes is frequently

observed when using GGA for assessing exchange and correlation energy. For $\text{Sr}_3\text{In}_{11}$ the calculated energy of formation (enthalpy of formation at 0 K) is by 0.022 eV/atom larger than that for EuIn₄-type SrIn_4 . This difference is also reflected in the higher thermal stability of the former compound. The energy difference between SrIn_4 in the monoclinic EuIn₄ and in the hypothetical tetragonal BaAl₄ structure is 0.075 eV/Z or 7.5 kJ/mol. For the reaction $3 \times \text{SrIn}_4$ (BaAl₄) $\rightarrow \text{Sr}_3\text{In}_{11} + \text{In}$ we obtain a negative enthalpy (referring to 0 K). Thus, in accord with our experimental results, SrIn_4 does not realize a high-temperature form with the higher symmetry BaAl₄ structure. Instead, the formation of slightly In-deficient $\text{Sr}_3\text{In}_{11}$ is preferred. The volume/formula unit of SrIn_4 is by 2.5% larger in the BaAl₄ than in the EuIn₄ structure. This strongly supports the idea that structure selection depends on size effects, because in the more condensed EuIn₄ structure Sr should be more effectively coordinated.

First principles calculation allow one to study compounds in hypothetical structures. It is instructive to have a closer look at SrIn_4 with the important BaAl₄-type structure. In Table 5 we compare interatomic distances in SrIn_4 (BaAl₄ and EuIn₄ structures) and in $\text{Sr}_3\text{In}_{11}$. Calculated interatomic distances deviate by 1–2% from the experimental ones for $\text{Sr}_3\text{In}_{11}$ - and EuIn₄-type SrIn_4 . In BaAl₄-type SrIn_4 the short apical–apical contact in the In network, which is associated with a 2c2e bond, is 2.8 Å. The apical–basal (In2–In1) distance within the multicenter-bonded pyramids is 2.98 Å. The interbasal distance (In1–In1) within the square nets is 3.51 Å and thus considerably longer than the nearest-neighbor distances in elemental In (3.25 Å $\times 4$ and 3.38 Å $\times 8$). The apical–apical and apical–basal distances in SrIn_4 with the hypothetical BaAl₄ structure are important indicators for the other structures since they are connected with a well-understood bonding picture developed for this structure type.^{27,28} Indeed, as already discussed, distances in EuIn₄-type SrIn_4 and $\text{Sr}_3\text{In}_{11}$ group around 2.85, 3.0, and 3.3 Å. The In–In distance distribution in BaAl₄-type SrIn_4 justifies the assignment of localized 2c2e and multicenter bonding for the first and second set of distances, respectively, in EuIn₄-type SrIn_4 and $\text{Sr}_3\text{In}_{11}$; i.e., both compounds bear bonding features of the BaAl₄ type. In BaAl₄-type SrIn_4 Sr is coordinated by 16 In atoms at distances between 3.8 and 3.9 Å. In the two lower symmetry structures Sr is coordinated by fewer In atoms and Sr–In distances are significantly shorter.

The electronic density of states (DOS) of the three Sr–In compounds are assembled in Figure 3. Most conspicuously, the DOS of BaAl₄-type SrIn_4 exhibits a pronounced pseudogap at the Fermi level. The features of this pseudogap are considerably diminished for $\text{Sr}_3\text{In}_{11}$ - and EuIn₄-type SrIn_4 . The contribution of Sr states is rather low below the Fermi level and drastically increasing above. This behavior is typical for polar intermetallic compounds and Zintl phases, which formally are composed of an oxidized electropositive component (the active metal) and a polyanionic (reduced) network. Although the overall shape of the DOS curves is

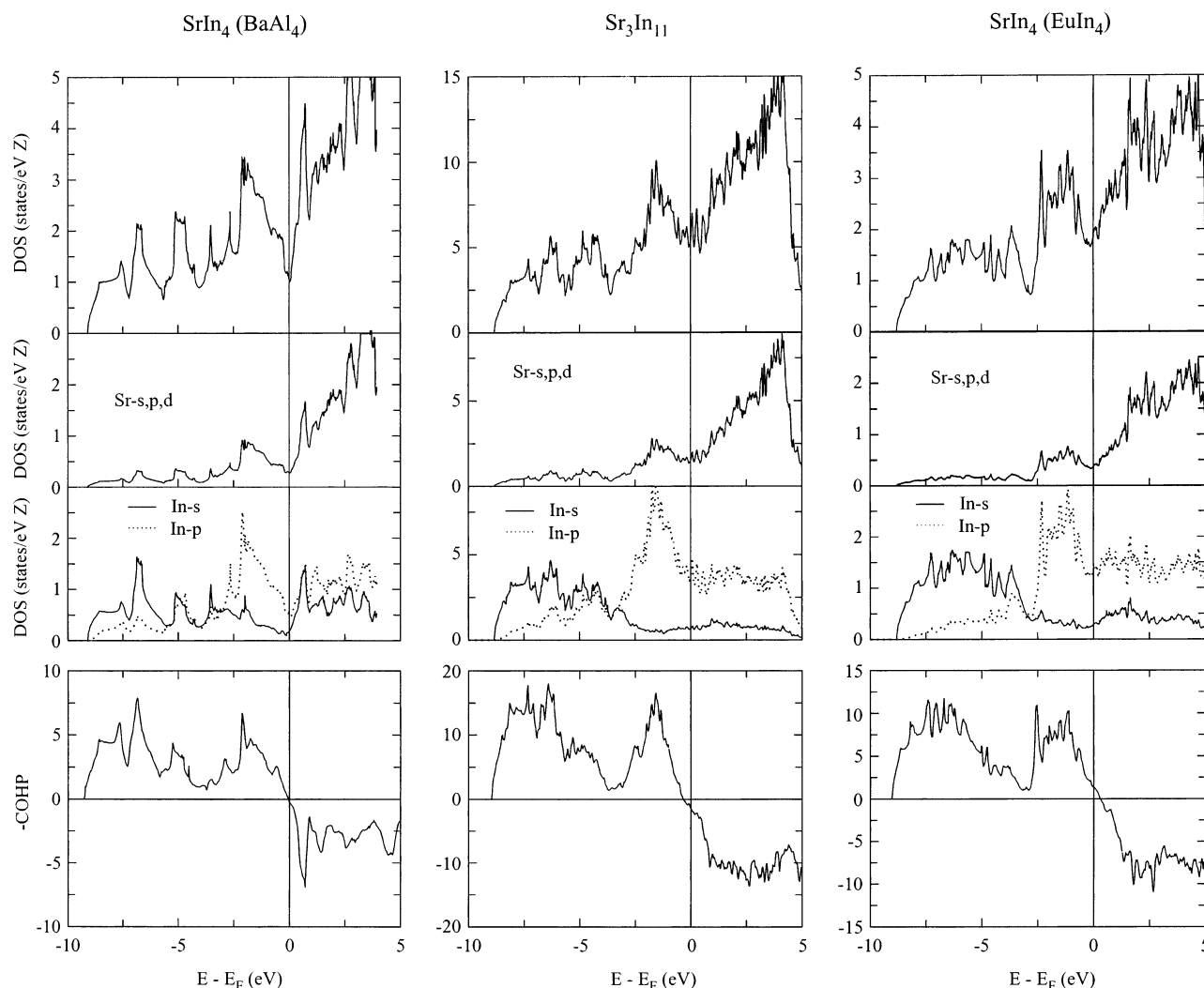


Figure 3. Total DOS (top panel) and partial DOS (middle panels) of the Sr and In sites for the systems SrIn_4 (BaAl_4), $\text{Sr}_3\text{In}_{11}$, and SrIn_4 (EuIn_4) calculated at the theoretical equilibrium volume. The In states are divided into s- and p-orbital contributions. The bottom panel shows $-\text{COHP}$ summed for all In–In network contacts in the unit cell below 4 Å for each system. Positive values of $-\text{COHP}$ indicate bonding and negative antibonding character. The Fermi level E_F is set to zero.

similar, the distribution of s- and p-based In bands is different for the three compounds. For BaAl_4 -type SrIn_4 we observe a pronounced s–p mixing, whereas for EuIn_4 -type SrIn_4 s and p bands are markedly separated. For $\text{Sr}_3\text{In}_{11}$ the situation is intermediate. The analysis of the COHP reveals that the Fermi level (and thus the pseudogap) in BaAl_4 -type SrIn_4 sharply and exactly separates In–In bonding from antibonding states. Thus, In–In bonding in this network appears most effectively optimized. In contrast, the In networks in EuIn_4 -type SrIn_4 and $\text{Sr}_3\text{In}_{11}$ are hypo- and hyperelectronic, respectively. As already pointed out by Corbett, the optimum electron count for EuIn_4 -type SrIn_4 to fill all In–In bonding levels would be 15 electrons/formula unit (i.e. one electron more than in SrIn_4).⁸ For $\text{La}_3\text{Al}_{11}$ -type $\text{Sr}_3\text{In}_{11}$ the electron count for optimum In–In bonding would be 38 electrons/formula unit (i.e. one electron less than in $\text{Sr}_3\text{In}_{11}$). According to Nordell and Miller, this optimum electron count is achieved in ternary derivatives of the $\text{La}_3\text{Al}_{11}$ type (e.g. $\text{Dy}_3\text{Au}_2\text{Al}_9$).²⁴ Conclusively, structural stability of compounds in the In-rich part of the Sr–In system is not exclusively determined by optimizing In–In network

bonding. The requirement of size match between Sr and the cavities provided by the In network leads to small deviations from optimum electron count for In–In network bonding in SrIn_4 , $\text{Sr}_3\text{In}_{11}$, and Sr_3In_5 .

We conclude this section by inspecting the integrated COHP (ICOHP) values for the In–In contacts occurring in the computationally relaxed structures of SrIn_4 and $\text{Sr}_3\text{In}_{11}$. This is shown in Figure 4. In the distance range of 2.8–3.4 Å ICOHP values vary approximately linearly. When using the apical–apical (2c2e bonded) distance of 2.8 Å in BaAl_4 -type SrIn_4 as a reference, a bond order scale for In–In distances can be established. According to this scale, the shortest In–In contacts in EuIn_4 -type SrIn_4 and $\text{Sr}_3\text{In}_{11}$ obtain bond orders of 0.85–0.9. Multicenter bonded and metallic bonded In–In contacts obtain bond orders around 0.6 and 0.35, respectively. These two types of contacts are well separated in EuIn_4 -type SrIn_4 and $\text{Sr}_3\text{In}_{11}$ by about 0.2 Å. The ICOHP (and bond order) values of the In–In nearest neighbor contacts in elemental bct-In coincide with those of the long In network distances in EuIn_4 -type SrIn_4 and $\text{Sr}_3\text{In}_{11}$.

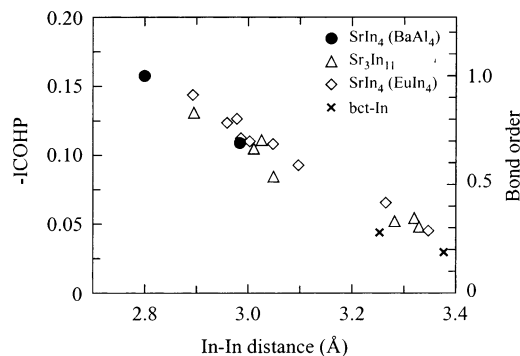


Figure 4. Distribution of the energy-integrated $-ICOHP$ values for the In–In network contacts below 3.5 Å occurring in the structures of $BaAl_4$ -type $SrIn_4$ (black circles), Sr_3In_{11} (triangles), $EuAl_4$ -type $SrIn_4$ (diamonds), and elemental In (crosses). The right-hand side of the graph shows an In–In bond order scale based on the shortest network distance as a reference.

4. Conclusions

We reported on the new polar intermetallic compound Sr_3In_{11} which is the first representative of the La_3Al_{11} structure exclusively formed by main group metals. The crystal structure of Sr_3In_{11} resembles that of the $BaAl_4$ and $EuIn_4$ structure types with a three-dimensional polyanionic In network encapsulating Sr counterions. As in Sr_3In_5 ⁷ and $SrIn_4$,⁸ In–In network bonding in Sr_3In_{11} is not completely optimized. From the results of first principles calculations we conclude that the formation of Sr_3In_{11} stems from the strong endeavor of the Sr–In system to form a 1:4 compound. The great majority of alkaline earth–trial systems

display such a compound with the $BaAl_4$ structure. In this structure triel–trial network bonding is perfectly optimized. On the other side, the rather rigid high-symmetry $BaAl_4$ structure implies a size mismatch between the Sr and the cavities provided by the surrounding In network. This size mismatch is countered flexibly by the Sr–In system with the realization of the lower symmetry $EuIn_4$ structure for $SrIn_4$ and the formation of Sr_3In_{11} crystallizing with a defect variant of the $BaAl_4$ structure.

Acknowledgment. This work was supported by the Swedish Research Council (VR).

Note Added in Proof. Recently, we became aware of a work by J.-G. Mao and A. M. Guloy who also reported on the crystal structure and bonding properties of Sr_3In_{11} .³⁰ Their result of the crystal structure determination is virtually identical to ours. For assessing the electronic structure of Sr_3In_{11} Mao and Guloy used semiempirical extended-Hückel band structure calculations while we employed a first principles method. We arrive at a somewhat different conclusion concerning the bonding properties of this compound.

Supporting Information Available: One X-ray crystallographic file in CIF format and one table containing the computationally obtained positional parameters of $SrIn_4$ ($BaAl_4$ - and $EuIn_4$ -types) and Sr_3In_{11} . This material is available free of charge via the Internet at <http://pubs.acs.org>.

IC0301829

(30) Mao, J.-G.; Guloy, A. M. *J. Alloys Compds.* **2003**, in press.