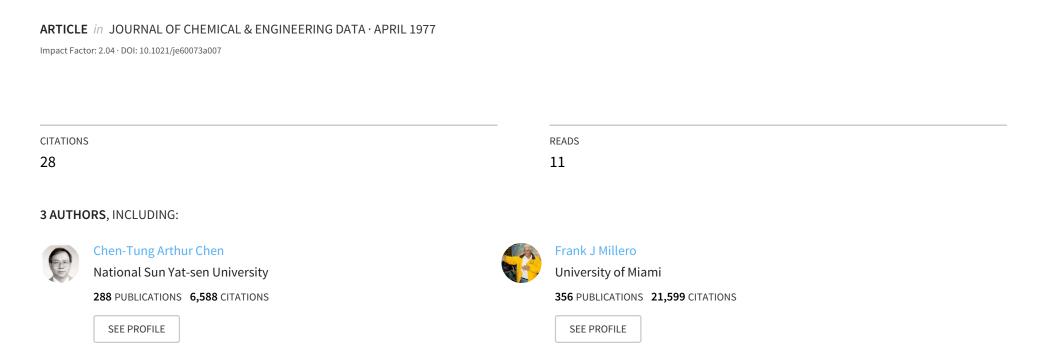
The apparent molal volumes of aqueous solutions of sodium chloride, potassium chloride, magnesium chloride, sodium sulfate, and magnesium sulfate from 0 to 1000 bars at 0, 25, and...



The Apparent Molal Volumes of Aqueous Solutions of NaCl, KCl, MgCl₂, Na₂SO₄, and MgSO₄ from 0 to 1000 Bars at 0, 25, and 50 °C[†]

Chen-Tung Chen, Robert T. Emmet, and Frank J. Millero*

Contribution from the Rosenstiel School of Marine and Atmospheric Science, University of Miami, Miami, Florida 33149

The densities of aqueous solutions of NaCl, KCl, MgCl₂, Na₂SO₄, and MgSO₄ have been measured with a high pressure magnetic float densimeter from 0 to 1000 bars, 0.01 to 1.0 m ionic strength, and at 0, 25, and 50 °C. The relative apparent molal volumes, $\phi_V(P) - \phi_V(0)$, of these solutions have been fitted to an equation of the form $\phi_V(P) - \phi_V(0) = \phi_V^0(P) - \phi_V^0(0) + Sm^{1/2}$ where the relative infinite dilution partial molal volumes, $\phi_V^0(P) - \phi_V^0(0)$, and the slopes S are functions of applied pressure and temperature. The pressure, temperature, and concentration dependence of the apparent molal volumes are briefly discussed.

Although there are reliable density and apparent molal volume data for many electrolytes at 1 atm (9, 11), little reliable data are available at high pressures. In our recent studies of the volume properties of multicomponent electrolyte solutions (13, 15) we have been examining the use of Young's rule (18) in predicting the properties of seawater. In order to predict the apparent molal volumes of seawater at elevated pressures (3), we had a need for reliable volume data on sea salts (NaCl, KCl, MgCl₂, Na₂SO₄, and MgSO₄). The present paper contains results on the apparent molal volumes of these salts from 0 to 1000 bars applied pressure, 0.01 to 1.0 ionic strength (to 2.0 ionic strength for NaCl), and 0, 25, and 50 °C.

Experimental Section

The high pressure magnetic float densimeter used in this study is described in detail elsewhere (12). The high pressure densimeter consists essentially of a 1 atm densimeter (8) enclosed

† Taken in part from the dissertation submitted by Robert T. Emmet in partial fulfillment of the requirements for the degree of Doctor of Philosophy, University of Miami.

in a nonmagnetic bomb with optical ports to observe the motion of the float. The apparatus consists of a pressure bomb, a magnetic float, and auxiliary measuring and control systems.

The pressure bomb used in this study was machined from beryllium copper. The cylindrical bomb contains two plugs seated with O rings to form a vessel of 170 cm³. The magnetic float is made of thick-wall (0.4 cm) Pyrex glass and contains an Alnico-5 bar magnet. The volume of the float is 58.7672 cm³ at 0 °C and 1 atm.

The pressure bomb was completely immersed in a 30-L constant temperature bath controlled to ± 0.001 °C with a Hallikainen Thermotrol. The temperature of the bath was set to ± 0.005 °C with a platinum resistance thermometer (calibrated by the National Bureau of Standards, 1968 temperature scale). A 2800-bar Enerpac hand pump was used to generate pressure. A 1400-bar Heise Bourdon tube gauge was used to set the pressure. The Heise gauge was calibrated with a Harwood Engineering deadweight tester. The pressures were found to be reproducible to ± 0.5 bars from 0 to 1000 bars and are thought to be accurate to 1.4 bars.

lon-exchanged (18 M Ω) water (Millipore-Super Q system) was used in the calibration runs and in the preparation of the solutions. Reagent grade salts were used, without further purification, for preparation of the solutions. The solutions of NaCl, KCl, Na₂SO₄, and MgSO₄ were analyzed by evaporation to dryness. The MgCl₂ solutions were analyzed gravimetrically with AgNO₃.

The calibration of the densimeter (2, 3) was made with ion-exchanged water using the densities of water from the sound-derived equation of state (4). The calibration results (2) indicate that the precision of the densities is ± 3 ppm at a given temperature and ± 8 ppm over the entire temperature range. The accuracy of the densities is thought to be $\sim \!\! 30$ ppm at 1000 bars applied pressure. An error of ± 30 ppm in density is equivalent to an error of ± 0.3 cm³ mol⁻¹ at 0.1 m and ± 0.03 cm³ mol⁻¹ at 1.0 m in ϕ_V for 1–1 electrolytes.

Table I. The Apparent Molal Volumes of Aqueous Salt Solutions as a Function of Concentration and Pressure at 0 °C

				$\phi_{V}(NaCI)$		•		
P, bar	m = 0.03027	m = 0.1299	$m = 0.250^{\circ}$		m = 0.7766	m = 0.9630	m = 1.307	m = 2.008
0.00 <i>a</i>	13.209	13.607	13.952	14.279	15.089	15.436	16.040	17.182
99.90	14.998	14.871	15.149	14.899	15.796	16.049	10.040	17.680
199.80	15.70 6	14.07 1	15.818		15.790		17 101	
		45.000		15.324	40.007	16.632	17.121	18.159
300.20	16.697	15.929	16.450	15.768	16.827			_
401.00	17.281	16.375	16.954	16.009	17.335	17.713	18.096	19.044
501.10		16.738	17.464	_	17.880	18.202	18.531	
601.00	17.530	17.203	17.996		18.230	18.664	19.935 .	19.829
701.60	18.176	17.635	18.438		18.647	19.101	19.353	20.185
802.00	18.246	17.970	18.935	_	19.032	19.510	19.728	20.528
901.70	18.579	18.244	19.250		19.420	19.877	20.066	20.840
1001.20	18.878	10.244	19.655	_	19.757	13.077	20.406	21.136
	10.070	-	19.033		19.737		20.400	21.130
				$\phi_{V}(KCI)$				
P, bar	m=0.	.1655 <i>n</i>	n = 0.3331	m = 0.5009	m=0.6	693 m =	= 0.8360	m = 1.0040
0.00ª	24.4	07	24.853	25.244	25.60	9 2	5.949	26.280
196.62		-	26.280	26.573	26.85		6.976	27.267
396.29	27.3	26	27.275	27.538	27.80		7.871	28.123
595.29 595.97	27.6 27.6		28.129	28.369	28.60		8.651	28.873
	27.0	.00						
795.65		-	28.857	29.086	29.30	ક 2	9.331	29.536
895.49 995.33	29.3 —	880 -	 29.498	<u> </u>	 29.89	7 2	— 9.930	_
				20.110	20.00	<u>-</u>	0.000	
				$\phi_{V}(MgCl_2)$				
<i>P</i> , bar	m = 0.0	00876 m =	0.03505 r	n = 0.07877	m = 0.07937	m = 0.1395	m = 0.2184	m = 0.3150
0.00 <i>ª</i>	11.1	74 1 ⁻	1.914	12.638	12.646	13.343	14.041	14.726
99.90	12.5		3.305	13.937	14.010	15.786	15.326	16.024
199.80	12.5		4.598	15.059		16.890	16.425	
				15.059			10.425	17.132
300.20	15.7		5.980		16.776	17.890		18.208
401.00	15.3		6.980	17.545	17.905	17.983	18.520	19.192
501.10	15.80	00 . 17	7.433	18.349	18.162	18.875	19.274	20.059
601.00	18.4	24 18	8.822	19.296	19.649		20.215	20.969
701.60			9.999	20.189	20.658	20.780	21.114	21.804
802.00	20.5			21.332	21.677	21.730	21.799	
901.70	20.0	•		22.336	22.580	22.580	22.652	23.322
1001.20		•	_	22.955	22.973	23.446	23.336	
0.1		0 0000	•	$\phi_{V}(Na_{2}SO_{4})$			2040	0 0005
P, bar		m = 0.00899	9 <i>m</i>	= 0.0832	m = 0.1480	m = 0	.2312	m = 0.3335
0.00	a	3.227		5.809	7.467	9.3	371	11.536
99.90)	5.110		8.214	9.898	11.6	699	13.440
199.80				9.692	11.740	13.4	139	15.083
300.20				11.641		15.		16.698
401.00				13.022	15.254	16.7		18.175
		11.005						
501.10		11.805		14.365	16.626	18.1		19.576
601.00		13.933		15.781	18.103	19.4		20.960
701.60		14.391		17.068	19.474	20.9		22.219
802.00	•	16.562		18.291	20.853	22.	128	23.471
901.70		18.219		19.517	22.177	23.2	218	24.652
1001.20			· .		23.255	24.4		25.676
D h		o = 0.01985	- n	$\phi_{ extsf{V}}(extsf{MgSO}_{ extsf{4}})$	m = 0.1029	m=0.1	1603	m = 0.2503
P, bar				·		11 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		
0.00ª		-9.081	-7 .	. 159	-5.568	-4.1 7	72	-2.881
196.62	,	-2.095	_	-	_			_
296.95		·	· -	_				·
396.29		1.140	2	.000	2.686	3.4	32	3.447
496.13			_					
		3 500		755	 E E01	<u> </u>	82	6.054
595.97		3.599	/	.755	5.501	6.0	UZ	0.034
695.81			-			_		
795.65		6.455	7	.755	8.208	8.50	07	8.444
895.49			_	<u> </u>	_			

 $[^]a$ The values of $\phi_{
m V}$ have been normalized to the best available literature values calculated from eq 3.

Table II. The Apparent Molal Volumes of Aqueous Salt Solutions as a Function of Concentration and Pressure at 25 $^{\circ}$ C

0.1	.		$\phi_{ m V}$ (Na	•			
P, bar	m = 0.1299	m = 0.2507	m = 0.3852	m = 0.7766	m = 0.9630	m = 1.3070	m=2.00
0.00 <i>a</i>	17.289	17.547	17.765	18.237	18.416	18.705	19.189
99.90	18.493	18.536	18.446	18.583	18.738	19.044	19.536
199.80	18.764	18.898	18.820	10.000	19.104	19.374	19.853
300.20	19.294	19.332	19.171		19.451		
401.00				10.505		19.700	20.145
	19.517	19.681	19.478	19.565	19.799	20.009	20.439
501.10	19.757	19.988	19.785	19.844		20.284	20.704
601.00	20.157	20.294	20.083	20.135	20.417	20.566	- 20.956
701.60		20.625	20.373	20.434	20.695	20.827	21.195
802.00	20.693	20.847	20.641	20.714	20.972	21.066	21.428
901.70	20.938	_	20.877	20.953	21.233	21.304	21.645
1001.20	31.133		21.131		21.462	21.524	
			$\phi_{f ee}$ (K	(CI)			
P, bar	m = 0.333	1 <i>m</i>	$\rho = 0.5009$	m = 0.6693	m = 0.8	3360	m = 1.0040
0.00 a	27.935		28.193	28.415	28.61	10	28.791
196.62	28.873		29.104	29.258	29.24		29.467
396.29	29.470		29.670	29.867	29.80		30.000
595.97	29.985		30.189	30.319	30.28		30.465
795.65	30.434		30.628	30.752	30.71		30.896
995.33	30.789		31.015	31.137	31.08	10	31.257
			φ _V (M g	rCla)			
<i>P</i> , bar		m = 0.00876		= 0.03505	m = 0.2184		m = 0.3150
0.00 a		15.172		15.781	17.162		17.477
99.90		15.970		16.596	18.058		18.476
199.80				17.140	18.825		19.250
300.20		16.460		18.454	19.587		19.967
401.00		16.664		18.812	21.199		20.692
501.10				19.484	20.839		21.324
601.00		•		19.806	21.537		21.977
701.60		19.437		20.239			22.587
802.00		21.241		21.693			23.129
901.70		21.241			22.640		
1001.20				22.446 22.385	23.241 23.704		24.157
<i>P</i> , bar		m = 0.0832	$\phi_{ m V}$ (Na $_{ m 2}$	2SO ₄) = 0.1480	m = 0.2312		m = 0.3335
				16 005			
0.00 <i>a</i>		14.963		16.095	17.234		18.388
99.90		16.508		17.711	19.130		20.352
99.90 199.80		16.508 17.767					
99.90		16.508		17.711	19.130		20.352
99.90 199.80		16.508 17.767		17.711	19.130 20.311		20.352 21.454
99.90 199.80 300.20		16.508 17.767 18.994		17.711 18.902	19.130 20.311 21.481		20.352 21.454 22.564
99.90 199.80 300.20 401.00		16.508 17.767 18.994 20.150 21.328	· ·	17.711 18.902 — 21.232 22.218	19.130 20.311 21.481 22.544 23.558		20.352 21.454 22.564 23.569 24.553
99.90 199.80 300.20 401.00 501.10 601.00		16.508 17.767 18.994 20.150 21.328 22.412	:	17.711 18.902 — 21.232 22.218 23.311	19.130 20.311 21.481 22.544 23.558 24.568		20.352 21.454 22.564 23.569
99.90 199.80 300.20 401.00 501.10 601.00 701.60		16.508 17.767 18.994 20.150 21.328 22.412 23.435		17.711 18.902 —— 21.232 22.218 23.311 24.299	19.130 20.311 21.481 22.544 23.558 24.568 25.560		20.352 21.454 22.564 23.569 24.553 25.548
99.90 199.80 300.20 401.00 501.10 601.00 701.60 802.00		16.508 17.767 18.994 20.150 21.328 22.412		17.711 18.902 	19.130 20.311 21.481 22.544 23.558 24.568 25.560 26.494		20.352 21.454 22.564 23.569 24.553
99.90 199.80 300.20 401.00 501.10 601.00 701.60		16.508 17.767 18.994 20.150 21.328 22.412 23.435		17.711 18.902 —— 21.232 22.218 23.311 24.299	19.130 20.311 21.481 22.544 23.558 24.568 25.560		20.352 21.454 22.564 23.569 24.553 25.548
99.90 199.80 300.20 401.00 501.10 601.00 701.60 802.00 901.70		16.508 17.767 18.994 20.150 21.328 22.412 23.435		17.711 18.902 ————————————————————————————————————	19.130 20.311 21.481 22.544 23.558 24.568 25.560 26.494 27.415		20.352 21.454 22.564 23.569 24.553 25.548 — 27.394
99.90 199.80 300.20 401.00 501.10 601.00 701.60 802.00 901.70	m = 0.0198	16.508 17.767 18.994 20.150 21.328 22.412 23.435 24.569		17.711 18.902 ————————————————————————————————————	19.130 20.311 21.481 22.544 23.558 24.568 25.560 26.494 27.415	1693	20.352 21.454 22.564 23.569 24.553 25.548 — 27.394
99.90 199.80 300.20 401.00 501.10 601.00 701.60 802.00 901.70 1001.20	m = 0.0198 -3.402	16.508 17.767 18.994 20.150 21.328 22.412 23.435 24.569	φ _∨ (M g	17.711 18.902 — 21.232 22.218 23.311 24.299 25.332 26.255 27.268	19.130 20.311 21.481 22.544 23.558 24.568 25.560 26.494 27.415 28.318		20.352 21.454 22.564 23.569 24.553 25.548 — 27.394 — 29.121
99.90 199.80 300.20 401.00 501.10 601.00 701.60 802.00 901.70 1001.20 P, bar	-3.402 	16.508 17.767 18.994 20.150 21.328 22.412 23.435 24.569	$\phi_{\text{V}}(\text{Mg})$ $\eta = 0.05328$	17.711 18.902 21.232 22.218 23.311 24.299 25.332 26.255 27.268 SO ₄) m = 0.1029	19.130 20.311 21.481 22.544 23.558 24.568 25.560 26.494 27.415 28.318		20.352 21.454 22.564 23.569 24.553 25.548 — 27.394 — 29.121
99.90 199.80 300.20 401.00 501.10 601.00 701.60 802.00 901.70 1001.20		16.508 17.767 18.994 20.150 21.328 22.412 23.435 24.569	$\phi_{\text{V}}(\text{Mg})$ $\eta = 0.05328$	17.711 18.902 21.232 22.218 23.311 24.299 25.332 26.255 27.268 SO ₄) m = 0.1029	19.130 20.311 21.481 22.544 23.558 24.568 25.560 26.494 27.415 28.318	46	20.352 21.454 22.564 23.569 24.553 25.548 — 27.394 — 29.121
99.90 199.80 300.20 401.00 501.10 601.00 701.60 802.00 901.70 1001.20 P, bar	-3.402 	16.508 17.767 18.994 20.150 21.328 22.412 23.435 24.569	$\phi_{V}(Mg)$ $h = 0.05328$ -1.833	17.711 18.902 21.232 22.218 23.311 24.299 25.332 26.255 27.268 SO ₄) m = 0.1029 -0.660	19.130 20.311 21.481 22.544 23.558 24.568 25.560 26.494 27.415 28.318 m = 0.4	46	20.352 21.454 22.564 23.569 24.553 25.548 — 27.394 — 29.121 m = 0.2503
99.90 199.80 300.20 401.00 501.10 601.00 701.60 802.00 901.70 1001.20 P, bar 0.00 ^a 96.79 196.62 296.45	-3.402 1.861 	16.508 17.767 18.994 20.150 21.328 22.412 23.435 24.569	$\phi_{V}(Mg)$ $h = 0.05328$ -1.833 -1.833 -1.839 -1.839	17.711 18.902 21.232 22.218 23.311 24.299 25.332 26.255 27.268 SO ₄) m = 0.1029 -0.660	19.130 20.311 21.481 22.544 23.558 24.568 25.560 26.494 27.415 28.318 m = 0.1	46 98	20.352 21.454 22.564 23.569 24.553 25.548 — 27.394 — 29.121 m = 0.2503 1.375 — 4.351
99.90 199.80 300.20 401.00 501.10 601.00 701.60 802.00 901.70 1001.20 P, bar 0.00 ^a 96.79 196.62 296.45 396.29	-3.402 	16.508 17.767 18.994 20.150 21.328 22.412 23.435 24.569	$\phi_{V}(Mg)$ $h = 0.05328$ -1.833	17.711 18.902 21.232 22.218 23.311 24.299 25.332 26.255 27.268 SO ₄) m = 0.1029 -0.660	19.130 20.311 21.481 22.544 23.558 24.568 25.560 26.494 27.415 28.318 m = 0.4	46 98	20.352 21.454 22.564 23.569 24.553 25.548 — 27.394 — 29.121 m = 0.2503
99.90 199.80 300.20 401.00 501.10 601.00 701.60 802.00 901.70 1001.20 P, bar 0.00 a 96.79 196.62 296.45 396.29 496.13	-3.402 1.861 4.569	16.508 17.767 18.994 20.150 21.328 22.412 23.435 24.569	$\phi_{V}(Mg)$ $a = 0.05328$ -1.833 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839	17.711 18.902 —21.232 22.218 23.311 24.299 25.332 26.255 27.268 SO ₄) m = 0.1029 —0.660 —3.653 —————	19.130 20.311 21.481 22.544 23.558 24.568 25.560 26.494 27.415 28.318	46 98 74	20.352 21.454 22.564 23.569 24.553 25.548 — 27.394 — 29.121 m = 0.2503 1.375 — 4.351 — 6.443
99.90 199.80 300.20 401.00 501.10 601.00 701.60 802.00 901.70 1001.20 P, bar 0.00 ^a 96.79 196.62 296.45 396.29 496.13 595.97	-3.402 1.861 	16.508 17.767 18.994 20.150 21.328 22.412 23.435 24.569	$\phi_{V}(Mg)$ $h = 0.05328$ -1.833 -1.833 -1.839 -1.839	17.711 18.902 21.232 22.218 23.311 24.299 25.332 26.255 27.268 SO ₄) m = 0.1029 -0.660	19.130 20.311 21.481 22.544 23.558 24.568 25.560 26.494 27.415 28.318 m = 0.1	46 98 74	20.352 21.454 22.564 23.569 24.553 25.548 — 27.394 — 29.121 m = 0.2503 1.375 — 4.351
99.90 199.80 300.20 401.00 501.10 601.00 701.60 802.00 901.70 1001.20 P, bar 0.00 96.79 196.62 296.45 396.29 496.13 595.97 695.81	-3.402 1.861 4.569 6.614	16.508 17.767 18.994 20.150 21.328 22.412 23.435 24.569	$\phi_{V}(Mg)$ $a = 0.05328$ -1.833 -1.833 -1.839 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8400 -1.8389	17.711 18.902 — 21.232 22.218 23.311 24.299 25.332 26.255 27.268 SO ₄) $m = 0.1029$ — 0.660 — 3.653 — — 8.008 —	19.130 20.311 21.481 22.544 23.558 24.568 25.560 26.494 27.415 28.318	46 98 74 77	20.352 21.454 22.564 23.569 24.553 25.548 27.394 29.121 m = 0.2503 1.375 4.351 6.443 8.395 8.395
99.90 199.80 300.20 401.00 501.10 601.00 701.60 802.00 901.70 1001.20 P, bar 0.00 ^a 96.79 196.62 296.45 396.29 496.13 595.97 695.81 795.65	-3.402 1.861 4.569	16.508 17.767 18.994 20.150 21.328 22.412 23.435 24.569	$\phi_{V}(Mg)$ $a = 0.05328$ -1.833 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839 -1.839	17.711 18.902 —21.232 22.218 23.311 24.299 25.332 26.255 27.268 SO ₄) m = 0.1029 —0.660 —3.653 —————	19.130 20.311 21.481 22.544 23.558 24.568 25.560 26.494 27.415 28.318	46 98 74 77	20.352 21.454 22.564 23.569 24.553 25.548 — 27.394 — 29.121 m = 0.2503 1.375 — 4.351 — 6.443
99.90 199.80 300.20 401.00 501.10 601.00 701.60 802.00 901.70 1001.20 P, bar 0.00 96.79 196.62 296.45 396.29 496.13 595.97 695.81	-3.402 1.861 4.569 6.614	16.508 17.767 18.994 20.150 21.328 22.412 23.435 24.569	$\phi_{V}(Mg)$ $a = 0.05328$ -1.833 -1.833 -1.839 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8389 -1.8400 -1.8389	17.711 18.902 — 21.232 22.218 23.311 24.299 25.332 26.255 27.268 SO ₄) $m = 0.1029$ — 0.660 — 3.653 — — 8.008 —	19.130 20.311 21.481 22.544 23.558 24.568 25.560 26.494 27.415 28.318	46 98 74 77	20.352 21.454 22.564 23.569 24.553 25.548 — 27.394 — 29.121 m = 0.2503 1.375 — 4.351 — 6.443 — 8.395

Table III. The Apparent Molal Volumes of Aqueous Salt Solutions as a Function of Concentration and Pressure at 50 °C

<i>P</i> , bar	m = 0.1299	m = 0.2507	$\phi_{V}(NaCl)$ $m = 0.385$	m = 0.7766	m = 0.9630	m = 1.307
0.00 <i>a</i>	18.610	18.865	19.060	19.416	19.527	19.677
99.90	19.718		19.648	19.917	19.838	19.954
		19.545				
199.80	20.090	_	19.942	20.203	20.137	20.232
300.20	20.438	20.125	20.242		20.422	20.492
401.00	20.698	20.393	20.533	20.731	20.705	20.950
501.10	20.858	20.686	20.793	20.987	20.971	
601.00	21.154	21.029	21.048	21.205	21.224	· 21.223
701.60	21.339	21.348	21.306	21.448	21.470	21.442
802.00	21.607	21.601	21.612	21.699		21.666
901.70	21.742	21.964	21.881	21.893	_	21.868
1001.20	21.938	22.253	22.114	22.126		_
			4 (KCI)			
P, bar	m = 0.3331	m = 0.5009	$\phi_{V}(KCI)$	= 0.6693	m = 0.8360	m = 1.0040
0.00 a	28.869	29.134		29.350	29.533	29.694
196.62	29.757	29.968		30.125	30.110	30.303
396.29	30.235	30.432		30.585	30.547	30.735
595.97	_	30.849		30.988	30.939	31.123
795.65	31.046	_		31.350	31.281	31.464
995.33	31.350	31.580		31.661	31.595	31.770
			d. (MaCL.)			
<i>P</i> , bar	m = 0.0	7937	$\phi_{V}(MgCl_2)$ $m = 0.1395$	<i>m</i> =	0.2184	m = 0.3150
0.002	45.04		10,000	16	700	17.295
0.00 <i>ª</i>	15.62		16.229		.792	
99.90	16.63		17.619		.023	18.317
199.80	17.23	38	18.261	18	.717	19.028
300.20	18.10)5	18.974	19	.454	19.747
401.00	18.5		19.546	20	.118	20.353
					.709	21.010
501.10	19.18		20.206			
601.00	19.9 ⁻		20.645		.356	21.602
701.60	20.54	14	21.246	21	.917	
802.00	20.84	14	21.755	22	.531	22.705
<i>P</i> , bar	m = 0.00899	m = 0.0367	$\phi_{V}(Na_{2}SO_{4})$ $m = 0.0832$	m = 0.1480	m = 0.2312	m = 0.3335
0.00 <i>a</i>	15.256	16.428	17.584	18.714	19.826	20.925
99.90		16.478	18.726	19.787	20.905	21.982
	46.074				21.904	22.975
199.80	16.371	17.563	19.717	20.849		
300.20	18.017	Autoridan	20.918	21.810	22.910	23.912
401.00	19.114	19.650		22.679	23.847	24.779
501.10	_	20.563	22.703	23.630	24.705	25.624
601.00	_	21.341	23.567	24.487	25.516	26.440
	20 250	22.503	24.323	25.329	26.365	27.230
701.60 802.00	22.358 22.799	22.997	27.323	26.129	27.075	28.008
002.00	22.133	££.331		20.123	27.070	20.000
<i>P</i> , bar	m = 0.01985	m = 0.0533	φ _∨ (MgSO₄) 28	m = 0.1029	m = 0.1693	m = 0.2503
. ,	0.0		-			
0.00 <i>ª</i>	-2.861	-1.053		0.073	0.973	2.068
196.62	2.783	4.211		4.564	5.191	5.025
396.29	6.012	6.784		6.764	7.185	6.933
496.13				***************************************	engramme.	
	0.045	0.700		9 500	Ω Ω7Ω	8.643
595.97	8.345	8.730		8.500	8.979	0.043
695.81				_	_	_
795.65	9.496	10.229		9.904	10.515	10.140
				_	_	_
895.49						
895.49 995.33	9.979			11.420	11.777	11.535

Results and Discussion

The densities of aqueous solutions of NaCl, KCl, MgCl₂, Na₂SO₄, and MgSO₄ have been measured (2) from 0.01 to 1.0 ionic strength with a high pressure densimeter. The measurements were made from 0 to 1000 bars (in 100 bar increments)

and at 0, 25, and 50 °C. The apparent molal volumes have been determined from these densities (d) by using the equation

$$\phi_{V} = \frac{1000(d^{0} - d)}{dd^{0}m} + \frac{M}{d}$$
 (1)

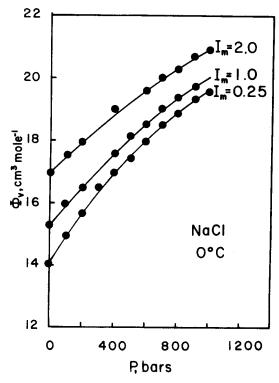


Figure 1. Apparent molal volumes of NaCl as functions of pressure at various concentrations and 0 °C.

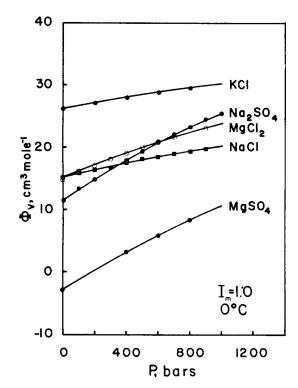


Figure 2. Apparent molal volumes of NaCl, KCl, MgCl₂, Na₂SO₄, and MgSO₄ as functions of pressure at $I_m = 1$ and 0 °C.

where d^0 is the density of water (4), m is the molality of the solution, and M is the molecular weight of the salt. The values of ϕ_V determined from eq 1 are given in Tables I, II, and III for various solutions. Since the ϕ_V 's for NaCl solutions have been obtained over the largest concentration range (0.03 to 2 m), we have examined the pressure and concentration dependence in Figure 1. The values of ϕ_V for NaCl at various molal ionic strengths, I_m , are plotted vs. pressure. The ϕ_V 's increase with increasing pressure over the entire concentration range studied. At low molalities the ϕ_V 's show a nonlinear pressure dependence, while at higher molalities the ϕ_V 's have a near linear pressure dependence. This behavior is similar at each temperature for all of the electrolytes studied (see Figure 2).

Although the concentration dependences for some of the electrolytes studied are not linear functions of $m^{1/2}$ at a given pressure (Figure 3), the relative apparent molal volumes, $\phi_V(P) - \phi_V(0)$, are linear functions of $m^{1/2}$ (see Figure 4). Since the high pressure magnetic float system was designed to study the pressure effect on the densities or apparent molal volumes, we examined the relative apparent molal volumes as a function of applied pressure P (at P=0, the absolute pressure is 1 atm), temperature (°C), and concentration (m, mol/kg of H₂O) by using the linear equation

$$\phi_{V}(P) - \phi_{V}(0) = \phi_{V}^{0}(P) - \phi_{V}^{0}(0) + Sm^{1/2}$$
 (2)

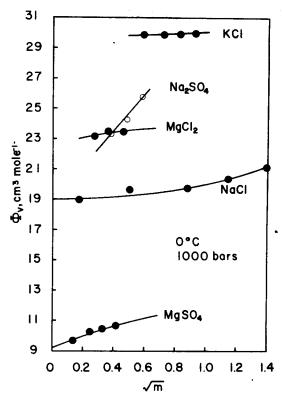


Figure 3. Apparent molal volumes of NaCl, KCl, MgCl₂, Na₂SO₄, and MgSO₄ as functions of $m^{1/2}$ at 0 °C and 1000 bars.

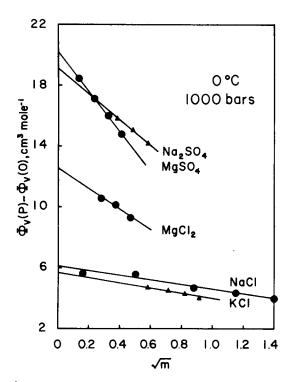


Figure 4. Relative apparent molal volumes, $\phi_V(P) - \phi_V(0)$, for NaCl, KCl, MgCl₂, Na₂SO₄, and MgSO₄ as functions of $m^{1/2}$ at 0 °C and 1000 bars.

where $\phi_V(P)$ and $\phi_V(0)$ are the apparent molal volumes at applied pressure, P and 0; the superscript zero is used to denote infinite dilution; and S is an empirical parameter that varies with pressure and temperature. The relative infinite dilution apparent molal volumes and the parameter S were fitted by using a least-squares method to equations of the form

$$\phi_{V}^{0}(P) - \phi_{V}^{0}(0) = \sum_{i,j}^{n} a_{i,j} P^{i} t^{j}$$
 (2a)

$$S = \sum_{i,j}^{n} b_{i,j} P^{i} t^{j}$$
 (2b)

The coefficients needed for eq 2a and 2b were arrived at by fitting the data on an UNIVAC 1106 computer. These coefficients are given in Table IV along with the standard deviations.

In order to calculate the ϕ_V at a given P, t, and m from these equations, it is necessary to have reliable ϕ_V data at 1 atm or P=0. The "best" available literature values for the 1 atm apparent molal volumes have been selected (1, 5–7, 10, 14, 17) and were fitted to the equation

$$\phi_{V}(0) = \phi_{V}^{0}(0) + Am^{1/2} + Bm + Cm^{3/2}$$
 (3)

where $\phi_V^0(0)$, A, B, and C are all temperature dependent parameters

Table IV. Coefficients for Equation 2^a

Variables	NaCl	KCI	MgCl ₂	Na ₂ SO ₄	MgSO ₄
ρ	1.542 (E - 2)	1.228 (E - 2)	1,566 (E = 2)	2.285 (E - 2)	4.076 (E -2)
Pt	-1.099 (E 4)	-1.589 (E -4)	-3,150 (E - 4)	-3.141 (E - 4)	-2.901 (E - 4
Pt ²	9.68 (E - 7)	1.79 7 (E — 6)	3.911 (E + 6)	2.125 (E - 6)	5.888 (E - 6
Pm1/2	-7.62 (E - 3)	-6.964 (E - 3)	-2.269 (E - 3)	-1.576 (E - 3)	-3.867 (E - 2
Ptm ^{1/2}	3.05 (E - 6)	7.060 (E 5)	2.611 (E - 4)	1.257 (E - 4)	3,066 (E - 4
Pt ² m ^{1/2}	0	-9.849 (E - 7)	-3.115 (E - 6)	-1.597 (E - 6)	-9.099 (E - 6
p 2	-2.439 (E - 5)	-1.261 (E - 5)	-1.202 (E - 5)	-1.250 (E - 5)	-3.593 (E - 5
P ² !	1.81 (E 8)	1.19 (E - 8)	1.19 (E - 8)	6.92 (E - 8)	-1.273 (E 7
$P^2m^{1/2}$	1.415 (E - 5)	1.089 (E 5)	-3.14 (E 6)	-3.11 (E - 6)	4.239 (E - 5
P ² Im ^{1/2}	o ·	0	0	0	2.261 (E 7
p 3	2.158 (E → 8)	6.50 (E - 9)	1.496 (E - 8)	9.82 (E - 9)	1.567 (E - 6
P ³ m ^{1/2}	-8.11 (E - 9)	-6.26 (E - 9)	-5.3 (E - 11)	0	-1.662 (E - 8
ρı	-6.48 (E - 12)	0	-6.54 (E - 12)	-3.08 (E - 12)	0
Std dev	0.23	80.0	0.18	0.24	0.28

^{*} The terms (E = a), given for each variable, mean the coefficient is times 10^{-a}.

Table V. Coefficients for Equation 3*

Variables	NaCl	KCI	MgCl ₂	Na ₂ SO ₄	MgSO₄
φ _V ⁰ , _{1 alm} 0 °C	12.90	23.63	10.42	2.33	-13.06
t	0.1990	0.1788	0.2660	0.508	0.3720
t ²	-2.008 (E - 3)	-2.000 (E - 3)	-4.128 (E - 3)	-5.456 (E - 3)	-5.472 (E - 3)
$m^{1/2}$	1.5992	1.407	8.132	8, 188	33.3710
tm1/2	5.388 (E - 3)	1.118 (E — 2)	-0.0498	0.1777	-0.2963
$t^2m^{1/2}$	2.194 (E - 4)	1.848 (E - 4)	1,277 (E - 3)	-1.8704 (E - 3)	1,314 (E - 2)
m	1.004	1.235	-0.820	13.427	-40.4948
tm	-4.951 (E 2)	-5.714 (E -2)	-0.2202	-0.7505	-4.843 (E - 2)
t ² m	3.082 (E - 4)	5.256 (E - 4)	3.382 (E - 3)	9.2568 (E 3)	-2.821 (E - 2)
m ^{3/2}	0	0	0	0	28.8998
tm ^{3/2}	o	0	0	0	0.2388
$t^2 m^{3/2}$	0	0	0	0	2.482 (E - 2)
Av dev	0.05	0.010	0.033	0.04,	0.02 ₈

The terms (E = a), given for each variable, mean the coefficient is times 10^{-a}.

$$\phi_{\mathsf{V}}{}^{\mathsf{O}}(0) = \sum_{i}^{n} \phi_{i} t^{i} \tag{3a}$$

$$A = \sum_{i}^{n} A_{i}t^{i}$$
 (3b)

$$B = \sum_{i}^{n} B_{i} t^{i} \tag{3c}$$

$$C = \sum_{i}^{n} C_{i} t^{i}$$
 (3d)

The coefficients for eq 3 are given in Table V along with the standard deviations.

The temperature effect on the apparent molal volumes at 1000 bars and $I_{\rm m}=1$ is shown in Figure 5. The values of $\phi_{\rm V}$ for NaCl and KCl increase with temperature, the values of ϕ_V for MgCl $_2$ have small temperature effects, while $\phi_{\rm V}$'s for Na $_2$ SO $_4$ increase rapidly at temperatures between 0 and 30 °C, then start to level off and have a tendency to decrease at temperatures above 40 °C. The values of ϕ_V for MgSO₄ actually show a maximum at 30 °C.

The smoothed apparent motal volumes of these electrolytes calculated from eq 2 and 3 can be used to calculate the densities by using the equation

$$d = d^0(1000 + mM)/(d^0m\phi_V + 1000) \tag{4}$$

The average errors in ϕ_V for NaCl at 1000 bars are approximately ± 0.1 (at $I_{\rm m}=1.0$) and ± 0.2 (at $I_{\rm m}=0.1$) cm³ mol⁻¹, which correspond to density errors of ± 100 and ± 20 g cm⁻³, respectively. The density errors for other salts are smaller.

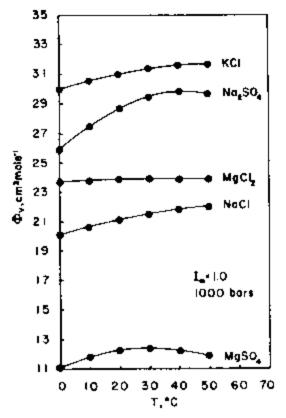


Figure 5. Apparent moial volumes of NaCl, KCl, MgCl₂, Na₂SO₄, and MgSO₄ as functions of temperature at $I_m = 1$ and 1000 bars.

The apparent motal compressibilities can be calculated by differentiating eq 1 with respect to pressure

$$\phi_{\mathsf{K}} = -\partial \phi_{\mathsf{V}} / \partial P \tag{5}$$

The values of $\phi_{\rm K}$ for NaCl, MgCl₂, and Na₂SO₄ calculated at $I_{\rm m}$ = 1.0, 0 °C, and 1 atm agree reasonably with the data of Millero

Table VI. Comparisons of $\phi_{\rm K}$ Obtained in this Study and the Data of Millero et al. at $I_{\rm m}=$ 1.0, 0 °C, and 1 Atm

Salt	$-10^4\phi_{ m K}$ (ours)	−10 ⁴ φ _K ^a (Millero et al.)
NaCl	78 ± 28	60.4
MgCl ₂	143 ± 22	121.2
Na ₂ SO ₄	219 ± 29	171.4
MgSO ₄	213 ± 24	156.4
Millero et al. (16).	. ea 10.	

et al. (16) (Table VI). The result of MgSO₄ is higher than the data of Millero et al.

Currently, the atmospherical densities and heat capacities of the major sea salts are being measured over a wide temperature range in our laboratory. Also the high pressure sound speed in the aqueous solutions of the major sea salts is being measured; these new results will be combined with the atmospherical densities and heat capacities to give precise equations of state for the major sea salts. The apparent molal volumes and compressibilities calculated from the sound-derived equations of state will be compared with the results of this study.

Literature Cited

- (1) Dunn, L. A., Trans. Faraday Soc., 64, 1898, 2951 (1968); 62, 2348 (1966).
- (2) Emmet, R. T., Ph.D. Dissertation, University of Miami, Miami, Florida, 1973.
- (3) Emmet, R. T., Millero, F. J., J. Geophys. Res., 79, 3463 (1974).
- (4) Fine, R. A., Millero, F. J., J. Chem. Phys., 59, 5529 (1973).
- (5) Franks, F., Smith, H. T., Trans. Faraday Soc., 63, 2586 (1967).
 (6) Geffcken, W., Price, D., Z. Phys. Chem., Abt. B, 26, 81 (1934).
- (7) Lee, S., Ph.D. Dissertation, Yale University, New Haven, Conn.; University Microfilm, Ann Arbor, Mich., Ord. No. 66-4906; Diss. Abstr. Int. B, 27, 131 (1966).
- (8) Millero, F. J., Rev. Sci. Instrum., 38, 1441 (1967).
- (9) Millero, F. J., Chem. Rev., 70, 147 (1970).
- (10) Millero, F. J., J. Phys. Chem., 74, 356 (1970).
- (11) Millero, F. J., "Water and Aqueous Solutions", R. A. Horne, Ed., Wiley, New York, N.Y., 1972, Chapter 15.
- (12) Millero, F. J., Knox, J. H., Emmet, R. T., J. Soln. Chem., 1, 173 (1972).
- (13) Millero, F. J., J. Soln. Chem., 2, 1 (1973).
- (14) Millero, F. J., Knox, J. H., J. Chem. Eng. Data, 18, 407 (1973).
- (15) Millero, F. J., "The Sea", Vol. 5, E. D. Goldberg, Ed., Wiley, New York, N.Y., 1974, Chapter 1.
- (16) Millero, F. J., Ward, G. K., Lepple, F. K., Hoff, E. V., J. Phys. Chem., 78, 1636 (1974).
- (17) Vaslow, F., J. Phys. Chem., 70, 2286 (1966).
- (18) Young, T. F., Smith, M. B., J. Phys. Chem., 58, 716 (1954).

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