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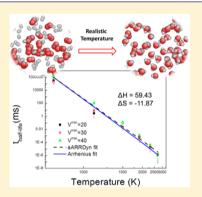


# Adaptive Accelerated ReaxFF Reactive Dynamics with Validation from Simulating Hydrogen Combustion

Tao Cheng,†,‡ Andrés Jaramillo-Botero,\*,‡ William A Goddard, III,\*,‡ and Huai Sun\*,†

Supporting Information

ABSTRACT: We develop here the methodology for dramatically accelerating the ReaxFF reactive force field based reactive molecular dynamics (RMD) simulations through use of the bond boost concept (BB), which we validate here for describing hydrogen combustion. The bond order, undercoordination, and overcoordination concepts of ReaxFF ensure that the BB correctly adapts to the instantaneous configurations in the reactive system to automatically identify the reactions appropriate to receive the bond boost. We refer to this as adaptive Accelerated ReaxFF Reactive Dynamics or aARRDyn. To validate the aARRDyn methodology, we determined the detailed sequence of reactions for hydrogen combustion with and without the BB. We validate that the kinetics and reaction mechanisms (that is the detailed sequences of reactive intermediates and their subsequent transformation to others) for H<sub>2</sub> oxidation obtained from aARRDyn agrees well with the brute force reactive molecular dynamics (BF-RMD) at 2498 K. Using aARRDyn, we then extend our simulations to the whole range of combustion temperatures from ignition (798



K) to flame temperature (2998K), and demonstrate that, over this full temperature range, the reaction rates predicted by aARRDyn agree well with the BF-RMD values, extrapolated to lower temperatures. For the aARRDyn simulation at 798 K we find that the time period for half the H<sub>2</sub> to form H<sub>2</sub>O product is ~538 s, whereas the computational cost was just 1289 ps, a speed increase of ~0.42 trillion (1012) over BF-RMD. In carrying out these RMD simulations we found that the ReaxFF-COH2008 version of the ReaxFF force field was not accurate for such intermediates as H<sub>3</sub>O. Consequently we reoptimized the fit to a quantum mechanics (QM) level, leading to the ReaxFF-OH2014 force field that was used in the simulations.

#### 1. INTRODUCTION

Most chemical processes involve a complex system of interacting molecules and atoms in which collisions can energize molecules sufficiently to break existing bonds and form new ones. Determining the reaction mechanisms, that is the sequences of reaction steps and product distributions and how they depend on temperature, pressure, and concentrations is very difficult because of multiple collisions of energized molecules. The exception is the case of very dilute low-pressure low temperature reactions, where bimolecular and unimolecular processes dominate the reactive events. In such cases, an excellent understanding of the details for many processes has been obtained by combining theory and experiment to provide an exquisite description of even subtle processes involving coupling of vibrational, rotational, and electronic excitations. Our goal is to extend this level of mechanistic understanding to high pressure, high temperature, nonequilibrium systems relevant for such chemical processes as chemical vapor deposition (CVD), atomic layer deposition (ALD), shock induced decompositions and reactions, combustion, and propulsion. We report here what we consider to be a dramatic step forward in accomplishing this.

The problem with molecular dynamics (MD) simulations of reactions is that most of the time the atoms are vibrating and bouncing around with no reactions, then very occasionally part

of the system is sufficiently energized that a reactive step occurs. Following the RMD for a billion dynamics steps using a 1 fs time step (a microsecond) to finally observe each rare reaction event is impractical. To tackle this rare-event problem, transition state focused methods of accelerated dynamics have been developed to identify transition pathways between known initial and final states. Example implementations include targeted molecular dynamics,<sup>2</sup> transition path sampling,<sup>3</sup> and essential molecular dynamics.<sup>4</sup> However, these approaches assume that the reaction steps are already known. In contrast hyperdynamics techniques explore the potential energy surfaces (PES) without requiring prior knowledge of reaction pathways, by efficiently identifying regions of phase space that dominate the reaction steps. These hyperdynamics methods include replica exchange MD<sup>5,6</sup> metadynamics, hyperdynamics, temperature accelerated dynamics, kappa dynamics, tappa bond boost (BB), <sup>13–20</sup> and accelerated molecular dynamics (AMD) methods. <sup>21–36</sup>

Hyperdynamics methods<sup>8,9</sup> can produce information on both kinetics and thermodynamics, but calculations to determine transition states are too demanding. The BB variation 13,14 of hyperdynamics employs simple rules based on bond lengths to

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identify the transition state and then applies a boost potential based on these bond lengths. This decreases computational costs, making it applicable to realistic systems. Successful results using BB have been reported on surface diffusion, desorption, and film growth. Although the concepts of accelerated dynamics developed over the past decade have been applied to a number of hyperdynamics processes, these techniques have not yet been applied to realistic chemical reaction processes.

We describe here how to combine Reactive Molecular Dynamics (RMD) based on the ReaxFF reactive force field with accelerated dynamics concepts to simulate long-term realistic chemical reaction processes. Our formulation is patterned after the bond boost (BB) method developed to work with classical force fields, but modified to use the bond order concepts present in ReaxFF. We refer to this approach as adaptive Accelerated ReaxFF Reaction Dynamics or aARRDyn.

To validate the aARRDyn methodology we consider the combustion of H<sub>2</sub>/O<sub>2</sub> mixtures. In this case, it is well-known that there are just a few important intermediates (HO<sub>2</sub>, H, HO, O), with only two stable initial products (HOH and HOOH). Despite the simplicity, BF-RMD takes too long in real time to convert the reactants all the way to HOH at, say, the ignition temperatures, requiring the RMD to be done at high temperature. For example, at the ignition temperature for H<sub>2</sub> oxidation (798 K), we estimate that it takes 1000 s for half the H<sub>2</sub> to form H<sub>2</sub>O product based on an Arrhenius fit from the calculated reaction barrier from BF-RMD, which would require  $\sim$ 4 quintillion (10<sup>18</sup>) times steps for BF-RMD. Doing this 4 quintillion (10<sup>18</sup>) time steps for good statistics, makes the BF-RMD approach quite impractical. In contrast, we find that with aARRDyn, this will reduce to ~4000 thousand time steps, for which the computational cost is equivalent to 1000 ps of BF-RMD, a speed up by a factor of 1 trillion  $(10^{12})$ .

To validate aARRDyn against BF-RMD, we carried out BF-RMD at a sufficiently high temperature, 2498 K for  $\rm H_2$  oxidation for 19 independent ReaxFF simulations (requiring  $\sim \! 10$  ns each) to follow the production of intermediates and products. Then we validate that the aARRDyn (again for 19 cases) dramatically decreases the simulation time while producing the same sequence of reaction intermediates and the same kinetics parameters (after converting the times in aARRDyn from MD time to hypertime).

In addition to validating aARRDyn, reactions involving the combustion of H<sub>2</sub> at higher pressures and lower temperatures have not been fully elucidated, making the detailed study of mechanistic steps very important. The combustion of H2 is exoergic, making H2 one of the highest energy fuels for rocket science and transportation (new generation fuel cells).<sup>37</sup> Also, H<sub>2</sub> is a green energy resource, since it does not produce unwanted emissions during combustion. Yet, in order to improve the design of combustion system for hydrogen, details on the mechanism of H<sub>2</sub> combustion under high pressure, low temperature, and nonequilibrium conditions need further elucidation. Here, ReaxFF-based RMD allows one to simulate the combustion mechanisms at atomic scales.<sup>38–41</sup> Previously, no such realistic combustion simulations at realistic temperatures have been reported, because BF-RMD simulations cannot yet reach the millisecond time scale needed to directly simulate the combustion reactions at the most interesting

In this paper we outline the implementation of the aARRDyn method into the ReaxFF/PuReMD software suite<sup>42</sup> and we

compare the results of simulating hydrogen combustion using aARRDyn to standard BF-RMD to provide validation. We benchmark the reaction kinetics and reaction mechanisms from aARRDyn against BF-RMD using exactly the same ReaxFF field for 19 independent simulations to increase the statistical accuracy of our comparisons (Supporting Information, Figure S1 shows one case of the statistics). Furthermore, we demonstrate the validity of aARRDyn over the broad temperature range of H<sub>2</sub> combustion temperatures, from ignition (798 K) to flaming (2998 K).

In carrying out these RMD simulations we found that the ReaxFF-COH2008 version of the ReaxFF force field was not accurate for such intermediates as  $H_3O$ . Consequently we reoptimized the fit from quantum mechanics (QM) results at the level of  $B3LYP/6-311G^{**}$ , leading to the ReaxFF-OH2014 force field that was used in the simulations, and which is reported in the Supporting Information.

## 2. THEORY AND METHOD

**2.1. Theory.** In the original BB method, <sup>13,14</sup> the tagged bonds depend solely on the bond length. This is a good approximation for dynamics of nonreactive systems, but for chemically reacting system, it is not sufficiently accurate. Here, the connectivity between atoms depends not just on the pairwise distance, but also on the valence and bonding states of the atoms involved. To address this issue we use the ReaxFF reactive force field framework to provide the essential information. Thus, at each step of the dynamics we use the bond order (BO) concept of ReaxFF to identify bonds weak enough to be approaching a transition state, but we refrain from selecting species whose bond may have already broken (radicals) so as to not interfere with their dynamics which might select between various intermediate or product states.

As described below aARRDyn uses concepts of bond order, overcoordination, and undercoordination that are already calculated as part of the ReaxFF force evaluations, so that aARRDyn does not introduce new computational overhead, making its introduction into ReaxFF RMD framework simple and efficient.

In ReaxFF, the bond order expression contains contributions from sigma, pi, and double pi type bonds, with the form:

$$BO'_{ij} = BO'_{ij} + BO'_{ij} + BO'_{ij} + BO'_{ij}^{\pi\pi}$$

$$= \exp\left[p_{bo1}\left(\frac{r_{ij}}{r_0^{\sigma}}\right)^{p_{bo2}}\right] + \exp\left[p_{bo3}\left(\frac{r_{ij}}{r_0^{\pi}}\right)^{p_{bo4}}\right]$$

$$+ \exp\left[p_{bo5}\left(\frac{r_{ij}}{r_0^{\pi\pi}}\right)^{p_{bo6}}\right]$$
(1)

Given the bond orders of an atom to all its neighbors, ReaxFF then makes corrections based on whether the sum of bond orders is larger than the valence of the atom (overcoordinated) or smaller than the valence (undercoordinated). The uncorrected overcoordination,  $\Delta_i{}',$  was originally defined as the difference between the total bond order around an atom and the number of its bonding electrons (Val $_i$ ),

$$\Delta' = -\text{Val}_i + \sum_{j=1}^{\text{neighbors}(i)} \text{BO}'_{ij}$$
(2)

but was later modified by a second order coordination term,  $\Delta_i^{\text{boc}}$  to soften the correction for atoms bearing lone electron pairs,

$$\Delta_{i}^{\prime \text{boc}} = -\text{Val}_{i}^{\text{boc}} + \sum_{j=1}^{\text{neighbors}(i)} \text{BO}_{ij}^{\prime}$$
(3)

as described by Chenoweth et al.<sup>39</sup> (reproduced here in the Supporting Information). A corrected over coordination is then

derived from the corrected bond orders, which are in turn used to calculate the dependence of the bond energies on distance,

$$\begin{split} E_{\rm bond} &= -D_{e}^{\sigma} B O_{ij}^{\sigma} \exp[p_{\rm bel} (1 - (B O_{ij}^{\sigma})^{p_{\rm be2}})] \\ &- D_{e}^{\pi} B O_{ij}^{\pi} - D_{e}^{\pi\pi} D_{ij}^{\pi\pi} \end{split} \tag{4}$$

The corrected bond orders are critical to obtain accurate condensed phase properties, because bonded atoms and nonbonded neighbor atoms may have similar interaction distances. In this work, we use  $BO_{cut} = 0.3$  to determine the bonds to tag for a bond boost.

The original BB method has been described in detail elsewhere. <sup>13,14</sup> The basic concept behind BB is simply to introduce a boost potential that reduces the time to overcome potential barriers. The boost potential is expressed as a function of bond lengths, and given by

$$\Delta V\{x_1, x_2...x_N\} \equiv \Delta V\{r_1, r_2...r_{N_b}\}$$
(5)

where, N is the total number of atoms,  $N_{\rm b}$  is the total number of bonds in the simulation system, and  $r_{\rm i}$  is the length of each bond. Furthermore, a fractional change  $(\varepsilon_{\rm i})$  in bond length from the equilibrium bond length  $(r_{\rm i}^{\rm eq})$  is defined as follows:

$$\varepsilon_i = \frac{r_i - r_i^{\text{eq}}}{r_i^{\text{eq}}} \tag{6}$$

Then, the boost potential becomes a function of bond fractional changes,  $\varepsilon_{\nu}$ , as

$$\Delta V\{x_1, x_2...x_N\} \equiv \Delta V\{\varepsilon_1, \varepsilon_2...\varepsilon_{N_L}\}$$
(7)

An empirical threshold parameter, q, was defined to ensure that the boost energy is not applied to transition states. In this paper we apply BB only when both BO > BOcut = 0.3 and  $\varepsilon_i$  < q = 0.5.

The boost potential,  $\Delta V$ , consists of an "envelope function", and a boost potential applied to each bond,  $\delta V(\varepsilon_i)$ , as follows:

$$\Delta V\{\varepsilon_{1}, \, \varepsilon_{2}...\varepsilon_{N_{b}}\} = A\{\varepsilon_{1}, \, \varepsilon_{2}...\varepsilon_{N_{b}}\} \sum_{i=1}^{N_{b}} \delta V(\varepsilon_{i})$$
(8)

The boost potential applied to each bond is defined as follows:

$$\delta V\{\varepsilon_i\} = \frac{\Delta V^{\text{max}}}{N_{\text{b}}} \left[ 1 - \left( \frac{\varepsilon_i}{q} \right)^2 \right] \tag{9}$$

where  $\Delta V^{\rm max}$  controls the amplitude of the boost potential. The idea of an "envelope function",  $A\{\varepsilon_{\rm l},\,\varepsilon_{\rm 2},\,...,\,\varepsilon_{\rm Nb}\}$ , is to channel energy into the bond that is closest to reacting. The bond change is determined by  $\varepsilon_{\rm i}$ . The bond with the largest  $\varepsilon$  ( $\varepsilon^{\rm max}$ ) is considered to be the one closest to breaking. The envelope function is defined as

$$A\{\varepsilon_{1}, \, \varepsilon_{2} \dots \varepsilon_{N_{b}}\} = A\{\varepsilon^{\max}\} = \left[1 - \left(\frac{\varepsilon^{\max}}{q}\right)^{2}\right] \frac{1 - (\varepsilon^{\max}/q)^{2}}{1 - P_{1}^{2} \left(\frac{\varepsilon^{\max}}{q}\right)^{2}}$$

$$(10)$$

Here,  $P_1$  is a parameter to control the curvature near the boundary. The effect of the envelope function is clearer from the force calculation:

$$\delta F_{i} = -\frac{\mathrm{d}}{\mathrm{d}r_{i}} \Delta V$$

$$= \begin{cases}
-A(\varepsilon^{\max}) \frac{\mathrm{d}}{\mathrm{d}r_{i}} \delta V(\varepsilon_{i}), & \text{if } \varepsilon_{i} < \varepsilon^{\max} \\
-A(\varepsilon^{\max}) \frac{\mathrm{d}}{\mathrm{d}r_{i}} \delta V(\varepsilon^{\max}) - \frac{dA(\varepsilon^{\max})}{dr_{i}} \sum_{j=1}^{N_{b}} \delta V(\varepsilon^{\max}), \\
& \text{if } \varepsilon_{i} = \varepsilon^{\max}
\end{cases}$$
(11)

To clarify how these equations work, consider two  $H_2$ , one with  $\varepsilon_1=0.44$  and the other with  $\varepsilon_2=0.45$  ( $\varepsilon^{max}$ ). Assume q=0.5 and  $\Delta V^{max}=30$  kcal/mol. Then, the boost force added to the first  $H_2$  would be eq 11 case 1, which leads to a boost force of 22.89 kcal·mol<sup>-1</sup>·Å<sup>-1</sup>. However, the boost force added to the second  $H_2$  would be case 2, 23.41 + 30.17, which leads to 53.58 kcal·mol<sup>-1</sup>·Å<sup>-1</sup>. The extra term (30.17) arises because the excess energy in the first  $H_2$  flows into the reactive bond. This formulation provides an unequal treatment for small changes for a normal bond, but large changes in the most reactive bond.

A key issue in accelerated dynamics is how to convert accelerated time scale to physical time (hypertime). The original form of time reweighing is  $^8$ 

$$t_{\text{hyper}} = \sum_{i=1}^{N_{\text{tot}}} \Delta t_{\text{sim}} \exp(\Delta V^{i}/k_{\text{B}}T)$$
(12)

where  $N_{\rm tot}$  is the number of integration steps, and  $\Delta t_{\rm sim}$  is the time step of MD simulation. To achieve good statistics, the simulation should be sufficiently long to sample enough boost regions. This means that large numbers of transitions should be included to reduce the relative error. Recently, Kim et al. proposed a modified reweighing method: 43

$$t_{\text{hyper}} = \sum_{i=1}^{N_{\text{tot}}} \Delta t_{\text{sim}} \frac{\rho_{V_b}(r)}{\rho(r)} \exp(\Delta V^i / k_{\text{B}} T)$$
(13)

where  $\rho(r)$  is the probability distribution of bond length in the original potential and  $\rho_{\rm Vb}(r)$  is the probability distribution in the biased simulation. The probability distributions of bond length can be obtained easily from separate short MD simulations. Once we have this information, the accuracy of reweighting can be improved, even when the transition times between reactions are short, which is often the case in simulating chemical reactions.

**2.2. aARRDyn Parameters.** For ReaxFF the  $r^{\rm eq}$  parameters are the equilibrium bond lengths of the bonded atoms, which are 0.750 Å (H–H), 0.950 Å (O–H) and 1.250 Å (O–O).  $P_1$  was introduced to adjust the stiffness of the boost potential at the boundary of the boosted region of phase space. If  $P_1$  is small,  $\Delta V$  increases more slowly at the boundary between the boosted and unboosted regions of phase space making it less likely to create a steep wall or peak.

Thus, the parameters in aARRDyn are (i) q, the maximum bond fluctuation to be considered for a BB, which we take as q=0.5. (Note that this is not the BO limit; rather it is the maximum ratio of the current bond distance to the equilibrium  $r^{\rm eq}$ . We use 0.5 here because the H–H bond is very short.) (ii)  $P_1$ , the bond boost stiffness, which we take as  $P_1=0.98$  as the original BB paper. (iii)  $\Delta V^{\rm max}$ , the bond boost that adjusts during the dynamics to control the boost amplitude.

**2.3. Determining the Radicals.** A problem inherent to rare-event simulation methods is that some reaction steps may already have small barriers that we do NOT want to accelerate. For hydrogen combustion, the small-barrier events are the radical recombination reactions, such as  $H + O \rightarrow OH$ ,  $H + OH \rightarrow H_2O$ , and  $HO + HO \rightarrow HOOH$ . These have very small barriers and do not need a bond boost. Thus, for aARRDyn we track how many radicals there are at every simulation step. Only when no radicals exist, is the boost turned on to accelerate the system. Otherwise, the boost is off.

A general approach to detect radicals was devised using the undercoordination and overcoordination terms from ReaxFF, which compares the calculated sum of bond orders (Sum(BO)) to an atom with the valence of the atom (e.g., 4 for C, 1 for H, and 2 for O). Thus, we consider an H atom to be an H radical, if the undercoordination number is -1, which means no bonds at all. Taking into account fluctuations in the dynamics, we consider that H is under coordinated (a radical) if BO  $_{\rm sum} < 0.3$ , leading to undercoordination < -0.7.

For a molecule containing O atoms, we use both undercoordination and overcoordination to assess whether the molecule is a radical. Thus, both O atom and OH radical are under coordinated. But for HO<sub>2</sub>, the bond order of the HO bond order is 1 while the bond order of the OO bond is 1.5, so that the central oxygen atom is over coordinated by 0.5 while the outer O is under-coordinated by -0.5. Thus, we consider an oxygen atom to be a radical, if either  $BO_{sum}$  < 0.3 or  $BO_{sum}$  > 2.4, which corresponds to under coordination  $\leftarrow$ 0.7 or over coordination > +0.4. These under/over coordination numbers are already calculated at every step for ReaxFF.

- 2.4. Bond Boost in ReaxFF. The general procedure for performing aARRDyn using ReaxFF is as follows:
- (1) Start with the new geometry predicted from a previous step of RMD and calculate forces using ReaxFF.
- (2) Perform the radical analysis using ReaxFF under/overcoordination data. If the number radicals are less than 2, go to step 3 to perform bond boost acceleration; otherwise, (no bond boost) go to step 5.
- (3) Tag each atom having a corrected bond order  $BO_i \leq BO_{max} =$
- 0.3, Denote this number as  $N_{\text{tag}}$ .

  (4) Determine  $\varepsilon^{\text{max}}$ . If  $\varepsilon^{\text{max}} < q$  (q = 0.5), then calculate the boost force; otherwise, (no bond boost) go to step 5. Thus, we calculate a BB only when a particular bond has BO > BO<sub>cut</sub> = 0.3 and simultaneously the extension of this bond beyond equilibrium is not more than 50%. For example, a bond with BO = 1 and  $r = r^{eq}$  would be considered for a BB. Thus, the majority of bonds are considered for a BB. However, for bonds having a small  $\varepsilon$ , the extra energy is small. We then sum up these extra incremental energies for all the bonds considered for the BB, and focus this energy on the bonds with the higher  $\varepsilon$ . In this way only bonds near the threshold of  $\varepsilon$  get the most boost. Of course changing just the energy does not lead to a force that would modify the dynamics. This bond boost is converted into a force by eq 11.
- (5) Use modified forces to predict changes in velocities and coordinates and go to step 1 for the next dynamics iteration.
- **2.5. Simulation Details.** In carrying out these RMD simulations we found that the ReaxFF-COH2008 version of the ReaxFF force field was not accurate for such intermediates as H<sub>3</sub>O. Consequently we reoptimized the fit to QM, leading to the ReaxFF-OH2014 force field that was used in the simulations. The parameters and validation of ReaxFF-OH2014 are reported in the Supporting Information.

The simulations of hydrogen combustion were carried out using the set of OH ReaxFF parameters (ReaxFF-OH2014), which are summarized in the Supporting Information. NVT MD simulations were performed with a time step of 0.25 fs, using the Nose-Hoover thermostat<sup>44</sup> to control temperature. The in-house revised version of PuReMD software was used in all simulations.<sup>42</sup>

The cubic simulation box was fixed at sides of 2.5 nm and initially contained 66 H<sub>2</sub> and 33 O<sub>2</sub> molecules. The H<sub>2</sub> and O<sub>2</sub> molecules were inserted into the box randomly using Packmol<sup>45</sup> and equilibrated with ReaxFF at 298 K for 100 ps at 298 K, which leads to a pressure of

We then heated the system to the target temperatures (798, 1098, 1498, 1898, 2298, 2498, 2698, and 2998 K) at a rate of 10 K/ps. This leads to initial pressures at these temperatures ranging from 673.23 to 2788.71 atm. We built 19 boxes independently to provide statistical analysis. For each of the simulation boxes, we carried out 2 to 20 ns of NVT simulations. At the end of the BF-RMD calculations, the final average pressures ranged from 450.23 to 862.45 atm.

#### 3. RESULTS AND DISCUSSION

3.1. Combustion at 2498 K. We chose to compare the simulation results between BF-RMD and aARRDyn at a temperature of 2498 K. This is reasonable, given it lies between the ignition temperature (798 K) and the combustion temperature (2998 K) of hydrogen. More importantly the reaction rate at 2498 K is sufficiently fast that it only takes 10 ns for BF-RMD simulation to provide sufficient reaction data. The reaction rates and reaction mechanisms produced in BF-RMD serve as a reference for validating the accuracy of aARRDyn. We expect that aARRDyn should reproduce both the kinetics and the reaction mechanisms (within statistical errors).

In aARRDyn simulations, the only adjustable parameter is  $\Delta V^{
m max}$ . Larger  $\Delta V^{
m max}$  produces larger boost potentials,

increasing the pace of the reactions. Thus, increased  $\Delta V^{max}$ decreases computational time, but too large a  $\Delta V^{\text{max}}$  might modify the kinetics. Thus, if the boost potential is too large, it could make the potential energy surface too flat, leading to a random walk among excited species, which would not reflect the true reaction kinetics. This might reduce the kinetic differences between favorable and unfavorable reaction steps that might allow unrealistic chemical reactions. Moreover, the calculation of hypertime depends exponentially on  $\Delta V^{\text{max}}$  (eq 12 and 13)), so that too large a value might lead to uncertainties in assessing hypertime. A good boost potential should provide both efficiency and accuracy.

Our choices for  $\Delta V^{\text{max}}$  were based on the bond energy. In ReaxFF the strength of the H-H bond is 108.72 kcal/mol while the strength of the O-O bond is 125.93 kcal/mol. Thus, we choose  $\Delta V^{\max}$  to be less than  $^1/_2$  of these values or 54 kcal/ mol. We considered three values, 20, 30, and 40 kcal/mol, all of which we consider to provide kinetics and mechanism the same as for BF-RMD. Figure 1 compares with BF-RMD the rate of water generation for these different values of  $\Delta V^{\rm max}$ . (We also extended our simulation to larger  $\Delta V^{\text{max}}$ . The results are shown in Supporting Information, Figure S2). For aARRDyn, the simulation time is 0.5 ns for  $\Delta V^{\text{max}} = 20$  and 40 but 1.0 ns for  $\Delta V^{\text{max}}$  = 30. For BF-RMD, we extended the simulation to 10 ns

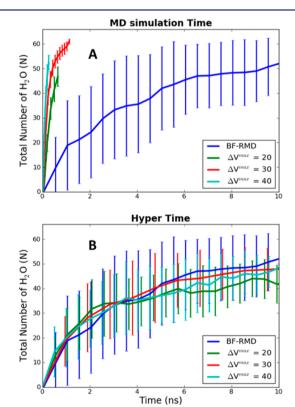


Figure 1. Comparison between BF-RMD and aARRDyn of H<sub>2</sub>O products generated from combustion of H2 at 2498 K as a function of (A) the MD simulation time and (B) hypertime. Here we considered  $\Delta V^{\text{max}} = 20$ , 30, and 40 kcal/mol. For BF-RMD, the physical time is the simulation time. For aARRDyn, the physical time is converted to hypertime by reweighing the simulation time using eq 13 as shown in Table 1. The colors are as follows: BF-RMD, blue; aARRDyn, with  $\Delta V^{\text{max}}$  =20 kcal/mol, green = 30 kcal/mol, red and = 40 kcal/mol cyan. The colors of the error bars are the same as the lines. The H<sub>2</sub> loss curve and H2O2 formation curve are shown in the Supporting Information (Figures S5 and S6).

Table 1. Comparison of the Simulation Times  $(t_{\text{sim}})$  and Hypertimes  $(t_{\text{hyper}})$  for 50% H<sub>2</sub> Loss  $(t_{\text{reactant}})$  and for Forming 50% of the H<sub>2</sub>O Products  $(t_{\text{production}})$  at 2498 K<sup>a</sup>

		t <sub>reactant</sub> (ns)		$t_{production}$ (ns)		
simulation	$\Delta V^{ m max}$	$t^{ m sim}$	$t^{ m hyper}$	$t^{ m sim}$	thyper	boost factor
aARRDyn	40	0.13 (0.07)	4.01(2.37)	0.14(0.04)	4.28(3.42)	30.57
aARRDyn	30	0.18(0.06)	2.74(1.24)	0.20(0.06)	2.97(2.44)	14.85
aARRDyn	20	0.37(0.07)	3.62(2.74)	0.41(0.06)	3.88(3.90)	9.46
BF-RMD		3.30(2.19)	3.30(2.19)	3.51(2.32)	3.51(2.32)	1.0

"We consider the BF-RMD simulation along with three cases of aARRDyn, with  $\Delta V^{\rm max} = 20$ , 30, and 40 kcal/mol. All data in the Table are averaged from 19 independent simulations, with the uncertainties (in parentheses) estimated from this sampling. The boost factors (the ratio of hypertime and simulation time) are calculated based on  $t_{\rm production}$ . The excellent agreement of the hypertime for both loss of reactant and for formation of the validates the aARRDyn methodology.

in order to observe sufficient reactions. In every case, the water generation curve is averaged from 19 independent simulations.

To obtain a quantitative reaction rate, we can compare the time to make  $^1/_2$  the products, that is the time to form 33 water molecules. This is not a real reaction rate since a number of reaction processes are convoluted. Table 1 compares  $\rm t_{product}$  for both simulation time and hyper-time for aARRDyn and BF-RMD simulations. After reweighting to hyper-time, all simulations show similar  $\rm t_{product}$ . Thus, for aARRDyn with  $\Delta V^{\rm max}=40$ , 30 and 20,  $\rm t_{product}=4.28\pm3.42$ , 2.97  $\pm$  2.44, and 3.88  $\pm$  3.90 ns compared with 3.51  $\pm$  2.32 ns for BF-RMD. Thus, within the error bars, all aARRDyn simulations converge to the BF-RMD simulation after time reweighting, which is one criterion for establishing that the kinetics in aARRDyn simulation are correct.

The efficiency of the BB simulations can be expressed as the ratio of hypertime and simulation time, the boost factor. For  $\Delta V^{\rm max} = 20$ , 30, and 40, the boost factors are 9.46, 14.85, and 30.57.

A second measure to compare is the rate of reactant disappearance. Here a useful metric is the half-life reaction time  $(t_{\rm reactant})$ , which is the time for 50% of the fuel reactants to react, that is, for 33 H<sub>2</sub> to disappear. This is also compared in Table 1, where we see that  $t_{\rm reactant}$  is about 0.21 ns (210 ps) shorter than  $t_{\rm production}$  in all the cases. These 210 ps include also the time for the H<sub>2</sub>O<sub>2</sub> formed during the early reaction times to finally convert to the final HOH product (~150 ps). In aARRDyn simulations, the H<sub>2</sub>O<sub>2</sub> decomposition is also accelerated, taking 30, 15, and 10 ps in aARRDyn with  $\Delta V^{\rm max} = 20$ , 30 and 40, respectively. When converted to hypertime, the differences between  $t_{\rm reactant}$  and  $t_{\rm production}$  are 140 ps, 187 ps, and 205 ps, consistent with the BF-RMD simulation (150 ps) and within the corresponding statistical error (Table 1).

**3.2. Reaction Mechanism.** Of course the most important reason for atomistic level simulations of chemical reaction systems is to determine the reaction mechanism, that is, the sequence of steps and rates that convert reactants to products. To validate aARRDyn, we must determine how well it reproduces the reaction mechanism found with BF-RMD. Here we used ensemble-averaged trajectories to analyze the reaction mechanisms. To perform a complete comparison, we averaged all 19 simulations for BF-RMD simulations and compared the results with those obtained by aARRDyn simulations, starting with the same initial configuration and velocities.

Figure 2 shows the major species generated during the simulation, which include two stable products,  $H_2O$  and HOOH, and three active species  $HO_2$ , HO, and H. The production of O atoms was too small to be significant.

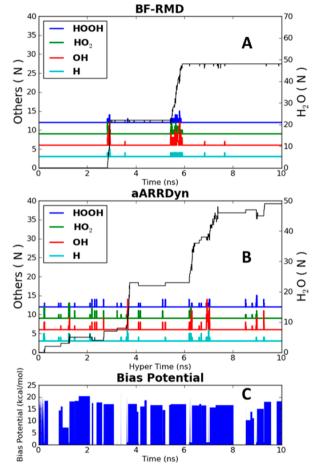


Figure 2. Comparison of the numbers of intermediate species generated by (A) BF-RMD and (B) aARRDyn simulations ( $\Delta V^{\max} = 30 \text{ kcal/mol}$ ) at 2498 K and (C) the corresponding bias potential. Both simulations were carried out starting from exactly the same initial configurations and velocities. The simulation times are 10 ns for BF-RMD and 1 ns for aARRDyn. The time shown for aARRDyn is the hypertime. The populations of H<sub>2</sub>O are shown in the right *y*-axis; the others are shown in the left *y*-axis. For clarity, the data on H, OH, HO<sub>2</sub>, and HOOH are shifted by 3, 6, 9, and 12, respectively. The production of O atoms was too small to show here. The bias potential along with the simulation time are shown in (C) for  $\Delta V^{\max} = 30 \text{ kcal/mol}$ . The other two cases ( $\Delta V^{\max} = 20 \text{ and } 40 \text{ kcal/mol}$ ) are in Supporting Information (Figures S7 and S8).

The first intermediate formed was  $\mathrm{HO}_2$  along with H. This came from the reaction

$$H_2 + O_2 \rightarrow H + HO_2 \tag{r1}$$

Table 2. Analysis of the Reaction Frequencies for the Final Step of H<sub>2</sub>O Production<sup>a</sup>

		aARRDyn (%)			
	reactions	40	30	20	BF-RMD (%)
r5	$H_2 + OH = H + H_2O$	62(6)	59(7)	60(9)	62(12)
r6	$H + OH = H_2O$	17(5)	19(6)	20(7)	16(8)
r7	$OH + HO_2 = H_2O + O_2$	9(3)	9(4)	5(4)	8(4)
r4	$H + HOOH = OH + H_2O$	4(3)	5(5)	6(5)	6(6)
r3	$H_2 + HO_2 = H_2O + OH$	4(2)	4(3)	4(3)	5(4)
r8	$H + HO_2 = H_2O + O$	3(4)	3(3)	4(3)	2(4)
r9	$HO_2 + HOOH = OH + H_2O + O_2$	1(3)	1(3)	1(3)	1(3)

<sup>&</sup>quot;Listed here are the percentages of those reactions producing water molecules at 2498 K. The data are obtained from 19 independent simulations by BF-RMD and aARRDyn with  $\Delta V^{\text{max}}$  =20, 30, and 40 kcal/mol. The root mean square (RMS) differences are shown in parentheses. The close correspondence between BF-RMD and the three aARRDyn cases validates the aARRDyn methodology.

Table 3. Analysis of the Reaction Frequencies for HOOH Generation and Loss during the Simulation<sup>a</sup>

		aARRDyn (%)			
	reactions	40	30	20	BF-RMD (%)
		HOOH Generation	on		
r3	$H_2 + HO_2 = HOOH + H$	42(11)	44(19)	43(12)	44(17)
r10	$H + HO_2 = HOOH$	29(13)	28(16)	39(16)	34(18)
r11	$HO_2 + HO_2 = HOOH + O_2$	23(9)	19(8)	14(11)	17(8)
r12	OH + OH = HOOH	5(9)	8(11)	3(8)	4(8)
r13	$H_2O + HO_2 = HOOH + OH$	1(13)	1(13)	1(12)	1(14)
		HOOH Loss			
r14	HOOH = OH + OH	68(19)	66(16)	67(17)	72(16)
r4	$H + HOOH = H_2O + OH$	31(6)	33(11)	32(11)	27(12)
r15	$HOOH + O = OH + HO_2$	1(6)	1(7)	1(6)	1(10)

<sup>&</sup>quot;Listed here are the percentages of generation reactions that produce HOOH molecules and four HOOH loss reactions (at 2498 K). The data are obtained from 19 independent simulations by BF-RMD and aARRDyn with  $\Delta V^{\rm max} = 20$ , 30, and 40 kcal/mol. The RMS differences are shown in parentheses. The close correspondence between BF-RMD and the three aARRDyn cases validates the aARRDyn methodology.

in which either or both of the  $H_2$  and  $O_2$  had been energized from previous collisions. We find that this H radical reacts quickly with another  $O_2$  to form a second  $HO_2$ ,

$$H + O_2 \rightarrow HO_2 \tag{r2}$$

so that the combination of these two steps can be considered as  $H_2 + 2O_2 \rightarrow 2HO_2$ .

We find that HO<sub>2</sub> induces a sequence of radical reactions:

$$HO_2 + H_2 \rightarrow H + HOOH$$
 (r3)

$$H + HOOH \rightarrow H_2O + OH$$
 (r4)

$$H_2 + OH \rightarrow H + H_2O \tag{r5}$$

which continue to produce water and HOOH. After these reactive radicals are fully consumed by termination reactions (forming  $\rm H_2O$  or HOOH), the system returns to a nonreactive period waiting for the next radical induction event. This is illustrated in Figure 2, which shows the actual bond boosts. When radicals appear, the boost is turned off (no signal in the figure). After the radicals are fully consumed, the boost is turned on again. In this case,  $\Delta V^{\rm max} = 30$  kcal/mol, the maximum boost in the simulations was 22.31 kcal/mol. The average boost potential energy was 17.71 kcal/mol (averaging only the cases with nonzero boost).

We show in Table 2 all reactions generating water. Here reaction r5 is a radical propagation reaction, in which the radical

(OH) reacts with a reactant  $(H_2)$  to produce a second radical (H) plus  $H_2O$ . We expect this to be fast and indeed reaction r5 accounts for 62% of  $H_2O$  generation. Reaction r6 is a radical termination reaction, and accounts for 16% of the  $H_2O$  generation.

$$H + OH \rightarrow H_2O$$
 (r6)

The remaining reactions are as follows:

• r7, a radical termination reaction, accounts for 8% of H<sub>2</sub>O production. This is

$$OH + HO_2 \rightarrow H_2O + O_2 \tag{r7}$$

- r4, a radical propagation reaction accounts for 6% of H<sub>2</sub>O production
- r3, a radical propagation reaction, accounts for 5% of H<sub>2</sub>O production
- r8 a radical propagation reaction accounts for 2% of H<sub>2</sub>O production

$$H + HO_2 \rightarrow H_2O + O \tag{r8}$$

r9 a radical termination reaction accounts for 1% of H<sub>2</sub>O production,

$$HO_2 + HOOH \rightarrow OH + H_2O + O_2$$
 (r9)

Thus, aARRDyn leads to the same reaction steps as BF-RMD and with the same percentages (within statistical fluctuations), indicating that aARRDyn captures the atomistic reaction mechanism.

Table 3 shows reactions related to the other stable product molecule, HOOH, in r3 and which forms during the combustion, but finally reacts to form water. Here we list both reactions related to the generation and to loss of HOOH.

The most important reactions generating HOOH are r3 and radical recombination r10:

$$H + HO_2 \rightarrow HOOH$$
 (r10)

These two reactions account for 78% of the HOOH production. The remaining reactions are

• r11, a radical termination reaction, accounts for 17% of HOOH production:

$$HO_2 + HO_2 \rightarrow HOOH + O_2$$
 (r11)

• r12, also a radical termination reaction, accounts for 4% of HOOH production:

$$OH + OH \rightarrow HOOH$$
 (r12)

• r13 a radical propagation reaction, accounts for 1% of HOOH production:

$$H_2O + HO_2 \rightarrow OH + HOOH$$
 (r13)

The most important reactions for the subsequent destruction are r14 and r4, which account for 99%. In r14 the HOOH decomposes into 2OH radicals (energized by collisions with other molecules). When no radicals are present, this mechanism eventually occurs but it needs an induction time, which we find to be about 150 ps at 2498 K for BF-RMD. aARRDyn accelerates this reaction, requiring 30, 15, and 10 ps for  $\Delta V^{\rm max} = 20$ , 30, and 40 kcal/mol. Converted to hypertime, the induction times for r14 are 140, 187, and 205 ps, which are consistent with the BF-RMD values (150 ps). The remaining reaction r15 generates only trace amount of HOOH, accounting for 1% of the HOOH loss.

As shown in Table 3, aARRDyn reproduces well the relative ratios of both the generation and loss of HOOH. These results are in excellent agreement with the reaction distributions and serve to validate that aARRDyn reproduces the correct reaction mechanisms.

3.3. Kinetics over the Temperature Range from Ignition to Combustion. To explore the capabilities of the aARRDyn method to describe the lower temperature processes that are completely impractical with BF-RMD, we extended our simulation to the full temperature range of H<sub>2</sub> combustion, from ignition temperature (798 K) to flame temperature (2698 K). At low temperatures, BF-RMD is too slow to produce enough data for validation. Thus, for validating aARRDyn, we used the BF-RMD NVT simulations ranging from 2498 K to 2998 K to estimate the apparent activation energy and preexponential terms and then used these to predict the BF-RMD kinetics at lower temperatures. Figure 3 shows the results which lead to  $\Delta H^{\rm act} = 59.01$  kcal/mol and  $A = (kT/h) \exp(\Delta S^{\rm act}/R)$ where  $\Delta S^{\text{ac t}} = -4.97 \text{ J} \cdot \text{K}^{-1} \cdot \text{mol}^{-1}$ . This  $\Delta H^{\text{act}}$  is  $\sim 1/2$  the bond energy of the weakest bond (108.72 kcal/mol for H<sub>2</sub>), which is consistent with the dominant process involving formation of an H<sub>2</sub>-O<sub>2</sub> complex which is activated by collision of a third particle to form effectively two H radicals.

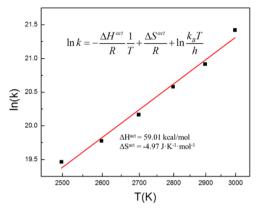


Figure 3. Arrhenius analysis for the overall rate constant of  $\rm H_2O$  production derived from BF-RMD NVT simulations at 2498, 2598, 2698, 2798, 2898, and 2998 K. X-axis is in reciprocal scale. The solid line is the least-squares fit. The optimum kinetic parameter  $\Delta H^{\rm act}$  = 59.01 kcal/mol, which can be compared to half the ReaxFF bond enthalpy of  $\rm H_2$ , at a high temperature of 109.56/2 + 2R = 58.74, suggesting that  $\rm H_2$  dissociation dominates the rate. The pre-exponential factor from transition state theory is A = ( $k_{\rm B}T/h$ ) exp( $\Delta \rm S^{act}/R$ ) leading to  $\Delta \rm S^{act}$  = -4.55 J·K<sup>-1</sup>·mol<sup>-1</sup>. The entropy of  $\rm H_2$  and  $\rm O_2$  at 2000 K are 187.10 and 258.70 J·K<sup>-1</sup>·mol<sup>-1</sup>, and the entropy of H and HO<sub>2</sub> are 154.17 and 312.72 J·K<sup>-1</sup>·mol<sup>-1</sup> at 2498 K. This  $\Delta \rm S^{act}$  is consistent with the rate-determining step involving  $\rm H_2$  and  $\rm O_2$  forming a weakly bound cluster that is subsequently activated by a collision with another  $\rm H_2$  or  $\rm O_2$  to form an H atom and an HO<sub>2</sub>. Then, the H reacts with  $\rm O_2$  to form another HO<sub>2</sub>.

For aARRDyn simulations, we used boost potentials of  $\Delta V^{\rm max} = 20$ , 30, and 40 kcal/mol ranging from 798 K to 2698 K. The reaction kinetics ( $t_{\rm half-life}$  of production) at these three temperatures together with previous 2498 K data are shown in Figure 4 and Table 4.

On the basis of the kinetic parameters for BF-RMD, we find that the hypertimes for the aARRDyn simulations at 798 K

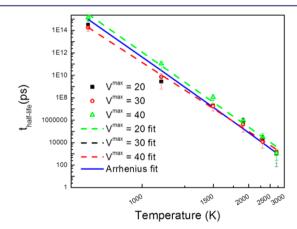


Figure 4. Half-time for product formation  $t_{\rm product}$  in hypertime for aARRDyn at temperatures from 798 K to 2698 K. This is compared with the Arrhenius fit (solid line) to BF-RMD at temperatures from 2498 to 2998 shown in Figure 3. Fitting the Arrhenius rate expression instead to the aARRDyn hypertimes over the full temperature range from 798 K to 2698 K leads to the dashed lines. The average of these three aARRDyn simulations leads to  $\Delta H^{\rm act} = 57.97$  kcal/mol and  $\Delta S^{\rm act} = -13.557$  J·K $^{-1}$ ·mol $^{-1}$ . This more negative value of  $\Delta S^{\rm act}$  is consistent with formation of the  $H_2$  plus  $O_2$ , which would be sampled more often at the lower temperatures. The x-axis uses reciprocal scaling, while a log scale is used for the y-axis.

Table 4. Temperature Dependence (from 798 K to 2698 K) of the Simulation Times (ps) and Hypertime (ps) for Forming 50% of the  $H_2O$  Products for aARRDyn with  $\Delta V^{\text{max}} = 20$ , 30, and 40 kcal/mol<sup>a</sup>

		$H_2O$		
temp (K)	$\Delta V^{ ext{max}}$	$t_{ m half-life}^{ m sim}$	$t_{ m half-life}^{ m hyper}$	boost factor
798	40	$7.67 \times 10^{2}$	$1.41 \times 10^{15}$	$1.83 \times 10^{12}$
	30	$1.25 \times 10^{3}$	$1.77 \times 10^{14}$	$1.41 \times 10^{11}$
	20	$1.85 \times 10^{3}$	$3.25 \times 10^{14}$	$1.75 \times 10^{11}$
1098	(BF-RMD)		$9.73 \times 10^{14}$	
	40	$6.56 \times 10^{2}$	$1.07 \times 10^{11}$	$1.63 \times 10^{8}$
	30	$7.71 \times 10^{2}$	$7.42 \times 10^9$	$0.96 \times 10^{7}$
	20	$1.14 \times 10^{3}$	$2.80 \times 10^{9}$	$2.45 \times 10^{6}$
	(BF-RMD)		$2.72 \times 10^{10}$	
1498	40	$4.01 \times 10^{2}$	$1.12 \times 10^{8}$	$2.79 \times 10^{5}$
	30	$4.70 \times 10^{2}$	$1.79 \times 10^{7}$	$3.80 \times 10^{4}$
	20	$6.48 \times 10^{2}$	$2.12 \times 10^{7}$	$3.27 \times 10^{4}$
	(BF-RMD)		$1.46 \times 10^{7}$	
1898	40	$2.69 \times 10^{2}$	$9.95 \times 10^5$	$3.70 \times 10^{3}$
	30	$2.99 \times 10^{2}$	$4.38 \times 10^{5}$	$1.46 \times 10^{3}$
	20	$5.01 \times 10^{2}$	$6.37 \times 10^5$	$1.27 \times 10^{3}$
	(BF-RMD)		$1.76 \times 10^{5}$	
2298	40	$1.54 \times 10^{2}$	$3.20 \times 10^4$	$2.08 \times 10^{2}$
	30	$2.31 \times 10^{2}$	$1.22 \times 10^4$	$0.53 \times 10^{2}$
	20	$4.44 \times 10^{2}$	$2.07 \times 10^4$	$0.47 \times 10^{2}$
	(BF-RMD)		$9,57 \times 10^{3}$	
2698	40	$1.13 \times 10^{2}$	$1.15 \times 10^{3}$	10.18
	30	$1.31 \times 10^{2}$	$1.47 \times 10^{3}$	11.22
	20	$2.46 \times 10^{2}$	$1.07 \times 10^{3}$	4.33
	(BF-RMD)		$1.20 \times 10^{3}$	

"This is compared with the BF-RMD results extrapolated from higher temperature BF-RMD (from Figure 3). All data in this Table are averaged from 19 independent simulations, with the uncertainties quoted in parentheses. The boost factors are calculated based on the ratio of hypertime and simulation time. The RMS differences are shown in parentheses. Note that the BF-RMD\* denotes the extrapolated values.

range from 177 to 1410 s with an average of 538 s ( $5.38 \times 10^{14}$  ps) at a computational cost from 767 to 1850 ps with average of 1289 ps. This shows the power of aARRDyn, leading to reasonable descriptions near ignition at 798 K with a boost factor of  $0.42 \times 10^{12}$ . Figure 4 shows the comparison of the  $t_{\rm half-life}$  time between aARRDyn for various BB and the theoretical value estimated from BF-RMD, where we find good agreement.

Fitting the rates from aARRDyn simulations over the full temperature range of 798 to 2698 K to K =  $(k_{\rm B}T/h)$  exp $(\Delta S^{\rm act}/R)$  exp $(-\Delta H^{\rm act}/RT)$ , leads to  $\Delta H$  = 56.40 kcal/mol and  $\Delta S^{\rm act}$  = -14.52 J·K<sup>-1</sup>·mol<sup>-1</sup> for  $\Delta V^{\rm max}$  = 20,  $\Delta H$  = 56.30 kcal/mol and  $\Delta S^{\rm act}$  = -14.28 J·K<sup>-1</sup>·mol<sup>-1</sup> for  $\Delta V^{\rm max}$  = 30 and  $\Delta H$  = 61.21 kcal/mol and  $\Delta S^{\rm act}$  = -11.874 J·K<sup>-1</sup>·mol<sup>-1</sup> for  $\Delta V^{\rm max}$  = 40. The average of three aARRDyn simulations is  $\Delta H^{\rm act}$  = 57.97 kcal/mol and  $\Delta S^{\rm act}$  = -13.557 J·K<sup>-1</sup>·mol<sup>-1</sup> which can be compared to  $\Delta H^{\rm act}$  = 59.01 kcal/mol and  $\Delta S^{\rm act}$  = -4.55 J·K<sup>-1</sup>·mol<sup>-1</sup> from BF-RMD done over the range of 2498 K to 2998 K. This more negative value of  $\Delta S^{\rm act}$  aARRDyn is consistent with formation of the  $H_2$  plus  $O_2$ , which would be more stable at the lower temperatures. Thus, we consider that the aARRDyn results are more reliable, in which a larger temperature range can be explored.

We could not find experimental data for a direct comparison to our calculations. However, flow reactor experiments <sup>46</sup> for a  $\rm H_2/O_2/N_2$  mixture with  $\rm H_2/O_2=0.3$  and a total pressure or 6.5 atm at 884 K led to  $\rm \Delta H=61.3~kcal/mol$  and  $\rm \Delta S=-32.14~J~mol^{-1}~K^{-1}$ .

#### 4. CONCLUSION

This paper extends ReaxFF technology to address the remaining issue in first-principles-based simulations of reaction dynamics of complex systems by reducing the computational cost of such a long-term reaction process to a practical level.

Combining aARRDyn with ReaxFF provides the means for first-principles-based simulations to accurately describe the reaction rates and mechanism for large-scale complex reactions (assuming an accurate ReaxFF potential). Here, we demonstrated an example, showing that aARRDyn leads to the correct reaction kinetics of  $\rm H_2$  combustion while reducing the cost at the reaction initiation temperature by a factor of a trillion compared to BF-RMD. We found that the adaptive boost potential in aARRDyn did not alter the underlying reaction mechanisms, and we found that the hypertime estimation (acceleration) is accurate against BF-RMD. We expect that the kinetics parameters developed here, including the percentages for the steps of  $\rm H_2$  and HOOH loss and formation that provide relative rates, may be used to analyze the results of shock tube and combustion studies of hydrogen oxidation.

We expect that the aARRDyn methodology may be particularly valuable for describing biological processes where the temperatures must be  $<\!100~^\circ\text{C}$  and the kinetics time scales may be microseconds and longer.

One might find a way to accelerate QM-based RMD to address some of these problems on small systems (up to a few hundred atoms). However, aARRDyn makes direct use of concepts like bond order, overcoordination, and undercoordination that are not defined in QM. Thus, aARRDyn provides a unique solution to this problem, while enabling significantly larger system length and time scales, and retaining the underlying physical insight.

### ASSOCIATED CONTENT

#### S Supporting Information

 $H_2O$  generation curves of all 19 samples,  $H_2O$  generation curves of  $\Delta V^{max} = 50$ , 60, 70 and 80, potential energy and force curves,  $H_2$  loss curve at 2498 K,  $H_2O_2$  generation curve at 2498 K, species generated in aARRDyn simulations with  $\Delta V^{max} = 20$  and 40 kcal at 2498 K; the new ReaxFF-OH2014 force field parameters plus some of the validations against QM; results for the Arrhenius analysis, reaction mechanisms and kinetics from the older ReaxFF-CHO2008 force field, the force field file, and the plot script. This material is available free of charge via the Internet at http://pubs.acs.org.

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#### Notes

The authors declare no competing financial interest.

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