

XII.—*Researches on Atomic Volume and Specific Gravity*, by JAMES P. JOULE, ESQ. *Corresponding Member of the Royal Academy of Sciences, Turin*, and LYON PLAYFAIR, F.R.S. *of the Museum of Practical Geology*.

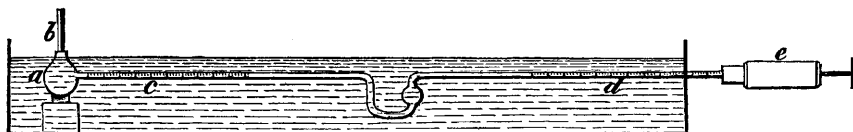
SERIES IV.—EXPANSION BY HEAT OF SALTS IN THE SOLID STATE.

In pursuing our researches on atomic volume and specific gravity, we have thought it desirable, as has been already intimated in a previous memoir, to ascertain the expansion of the salts by heat, as well as their volume at a given temperature. In this way we hope to arrive ultimately at the solution of the apparent discrepancies between theory and experiment. We are not aware that any experiments of this kind have hitherto been made. Brunner has indeed determined the expansion of ice, and we are led to expect that Pierre, who has already given valuable results on the expansion of liquids, will extend his labours to solid salts. We hope, therefore, that our own results, as detailed in the present memoir, will be speedily confirmed. The expansion of solids by heat is a subject which although little cultivated hitherto, is of very great importance to science, and will require, in all probability, the labours of many experimenters for its complete development. It will not, therefore, be expected that we shall be able to include the expansions of the whole range of known inorganic salts in one memoir; our object being simply to examine a sufficient number of them, in order to throw light on the causes

which produce variations in the sp. gr. of bodies, and thus enable us to confirm or correct our views on atomic volumes.

It was only after much consideration and some preliminary trials, that we were enabled to select what appeared to us an unexceptionable method of conducting the experiments. The first form of apparatus which suggested itself to us, consisted of a glass volumometer, Fig. 1, in which *a* is a bulb, of two and a half cubic inches capacity, having a neck fitted with a perforated glass stopper *b*. A graduated tube *c d*, of small diameter, was attached to this bulb,

FIG 1.

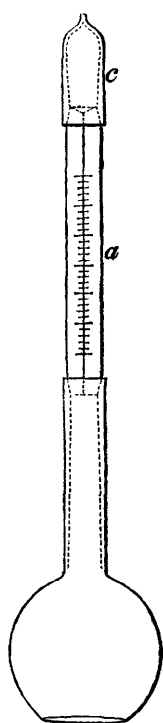


having at the centre a smaller bulb, of one cubic inch capacity. A syringe was attached tightly to the extremity, and the whole was immersed in a large vessel containing water. The method of experimenting with this apparatus was as follows :—The bulb *a* was filled with turpentine or any liquid incapable of dissolving the salt, and the exact quantity was noted on the graduated stem at *c*. The piston of the syringe was then gradually withdrawn, so as to draw the liquid nearly to the end of the tube *d*, entirely filling the intermediate bulb. A known quantity of the salt was then thrown into the bulb *a*, and the stopper being re-adjusted, the liquid was driven back by the syringe till it ascended into the perforation of the stopper. By examining the position of the liquid in the graduated tube, the space occupied by the salt was rendered evident. By conducting experiments with a salt in the above manner, at different temperatures, its expansion could be made evident, regard being of course paid to the expansion of the glass tube.

Several trials were made with the above-described apparatus, the use of which appeared to offer a great advantage in not requiring an acquaintance with the expansion of the liquid employed. However, it was speedily found that there were grave inconveniences attending it, in consequence of the difficulty of drying the tube thoroughly after each experiment, as well as the danger of losing a portion of the salt whilst introducing it through the narrow neck of the bulb. But these objections might have given way to time and patience. Our chief, and with this apparatus, insurmountable difficulty, arose from the fact, that a quantity of air always remained attached to the

salt after immersion. Since, therefore, it was highly probable that the quantity of adhering air varied with the temperature, the apparatus appeared liable to error, and was consequently abandoned.

FIG. 2.



After some other attempts, we at last fixed upon a plan, which appeared to combine the advantages of accuracy with great practical facility. We procured four sp. gravity bottles, made of the same sample of glass. Two of them, marked No. 1 and No. 3, were capable of containing somewhat more than 500 grs. of water, whilst the other two, No. 2 and No. 4, had a capacity for about 270 grs. of water, the latter being destined for ascertaining the volumes and expansions of weighty articles in small quantities. We have given a half-size representation of one of the larger bulbs in Fig. 2, where *a* is a stopper formed from a piece of thermometer tube of narrow bore, terminated at the upper end by a small conical cavity, over which a cap *c* is accurately fitted by grinding, so that any liquid which may have ascended through the capillary, is confined in the cap without loss. There is a fine capillary perforation at the summit of the cap, for allowing the egress of the air displaced by the liquid.

In order to ascertain the expansion of the glass of these volumenometers, the capillary tubes which served for their stoppers were carefully calibrated and graduated. They were then filled with distilled water and immersed for half an hour in a bath containing a large quantity of water, kept constantly at $38^{\circ}92$ (F). The exact height of the water in the capillary tube being then noted, the water in the bath was from time to time increased in temperature. At every successive increase, the position of the water in the stem was observed. It first descended and then of course ascended, until at the temperature of $45^{\circ}82$, the water stood at exactly the same point as at $38^{\circ}92$. Hence it was evident that the glass had expanded exactly as much as the water, through the interval between $38^{\circ}92$ and $45^{\circ}82$. According to the table given by Despretz, it appears that the expansion of water through this interval is 0.0001069; so that, supposing the expansion of glass to go on at the same rate through 180° , the expansion of the bulbs of the volumenometers will be 0.002788 between the freezing and boiling points of water.

Another experiment of the same kind showed that the expansions of the glass and water were the same through the interval between $38^{\circ}478$ and $46^{\circ}218$, which placed the expansion of the volumometers at 0.002798 .

The expansion of the glass bulbs being thus known, it was easy to see how they might be employed in ascertaining the expansion of turpentine and salts. For by weighing them filled with turpentine, at different temperatures, we could obtain the expansion of that fluid. And then by weighing the bulbs filled with turpentine, and a given weight of salt at different temperatures, we could readily obtain the volume and expansion of the salt.

It need hardly be observed, that experiments of this nature require to be performed with very great accuracy. We therefore employed an excellent calibrated thermometer, in which each division was equal to $\frac{1}{12 \cdot 192}$ of a degree, of Fahrenheit's scale, and the freezing point, which had remained nearly stationary, for half a year stood at 16.1 divisions. It was easy to read off temperatures to within $\frac{1}{150}$ th of a degree by this instrument. We also employed a very sensible balance by Dancer, which would turn well with the addition of $\frac{1}{1000}$ th of a grain, when each scale was loaded with 1000 grs. The barometric pressure was always noted, in order to correct the observed weights, and before weighing, the bulbs were reduced nearly to the temperature of the apartment, to prevent the inaccuracy arising from the currents of air they would otherwise occasion in the balance case. In taking temperatures, regard was had to the temperature of that part of the stem not immersed in the bath; and, whenever necessary, the rule of the committee of the Royal Society was employed in order to supply the requisite correction.

In the first place the weights of the bulbs, both empty and filled with water, were ascertained, in order to find their exact capacity. The water employed for this purpose was distilled, and had been recently boiled. The stoppers were placed in the necks of the bulbs, causing the water to ascend through the capillary tubes into the small cavities at the tops of the stoppers. A noose of string was now placed on the neck of each of the bulbs, which were then immersed to within an inch of the tops of the stoppers in the bath of water. The thermometer in the bath stood at the 113 th division, and kept as nearly as possible at that point for about three quarters of an hour, during the whole of which time the water was repeatedly agitated by a stirrer. Experience had already shown that three quarters of an hour was more than sufficient to reduce the temperature of the bulbs to the exact tempera-

ture of the bath ; the water remaining in the cavities at the tops of the stoppers was therefore now removed by means of bibulous paper, and the caps were placed upon them. The bulbs were then removed in succession from the bath, reduced to the temperature of the room, dried with a soft silk handkerchief, and weighed. The results corrected for barometrical pressure were as follows :

	No. 1. Volumenometer.	No. 2. Volumenometer.	No. 3. Volumenometer.
Bulbs and water at 113	623·572	882·042	922·522
Bulbs alone	349·546	377·036	397·649
Capacity in grs. of water at 113	274·026	505·006	524·873

The bulbs being now thoroughly dried, were filled with the turpentine destined for the experiments. The range of temperature fixed upon was between about 100 and 750 of the thermometer, corresponding to about 38°·5 and 88°·8 Fahr. The low temperature was attained by dissolving carbonate of soda in the water of the bath, adding a small quantity from time to time, to keep the temperature uniform. The high temperature was maintained by a lamp, burning underneath the bath. When, after half an hour's immersion, the turpentine had attained the exact temperature of the bath, the bulbs were successively weighed, as in the case of the trial with water already described. The bulbs were then again immersed in the bath for half an hour, and re-weighed, in order to preclude the possibility of an accidental error.

Volumenometer.	Temp.	Weight.	Mean temp.	Mean weight.	Weight of empty bulbs.	Weight of turpentine only			
No. 1	120	589·648	123·5	589·616	349·546	240·070			
	127	589·584							
	745·2	583·854	747·8				583·828	349·546	234·282
	750·4	583·802							
No. 2	107·6	819·779	111·8	819·710	377·036	442·674			
	116·0	819·640							
	744·5	808·874	747·45				808·831	377·036	431·795
	750·4	808·788							
No. 3	106	857·852	110·5	857·773	397·649	460·124			
	115	857·694							
	744·9	846·456	747·55				846·411	397·649	448·762
	750·2	846·366							

The above results were obtained on the 11th of August, 1846, and immediately afterwards the experiments on the expansion of salts were commenced, and continued until the 26th of August, when the

turpentine (which was kept in a large glass bottle, holding about a gallon) was again tested, in order to ascertain whether any change had taken place in its density. Such was found to have happened, in consequence of the absorption of atmospheric air, as will be seen by the results given below.

	Volumenometer.	Temp.	Weight.	Mean temp.	Mean weight.	Weight of empty bulb.	Weight of turpentine alone.
No. 1		93	590.052	93.5	590.052	349.546	240.506
		94	590.052				
		399.9	587.214	399.7	587.220	349.546	237.674
		399.5	587.227				
		754.4	583.906	752.5	583.926	349.546	234.380
		750.6	583.946				
No. 2		93.9	820.271	95.1	820.255	377.036	443.219
		96.4	820.239				
		399.6	815.044	399.3	815.050	377.036	438.014
		399	815.056				
		752.8	808.934	751.3	808.962	377.036	431.926
		749.9	808.991				
No. 3		93.8	858.358	94.2	858.353	397.649	460.704
		94.7	858.349				
		399.9	852.905	399.7	852.907	397.649	455.258
		399.5	852.909				
		753.5	846.554	751.8	846.582	397.649	448.933
		750.2	846.610				

In the above table we have recorded observations taken at a temperature intermediate between the two extremes. The same was done in the case of a large proportion of the salts tried, with a view to ascertain whether their expansion was uniform. Such appeared to be invariably the case; at least if any discrepancy occurred, it was within the limits of experimental errors. We have not, however, thought it right to extend our paper, already too voluminous, by these details. It will be seen from the observations on the volume of turpentine at the three temperatures above given, that that fluid is remarkably uniform in its expansion, a circumstance which eminently adapts it for experiments on the expansion of salts.

Owing to the slight change which had occurred in the density of the turpentine, we calculated the expansion of the salts first tried by the first table of results on the expansion of turpentine, and that of the salts last tried by the last table, employing the mean of the two tables for the intermediate experiments.

In trying a salt, the bulb, partially filled with turpentine, was accurately weighed. A quantity of salt having been then introduced,

the bulb was again weighed, the increase of weight giving the exact quantity of salt, attention being paid to the correction for barometrical pressure. The bulb was then placed under the exhausted receiver of an air-pump, until the air adhering to the salt was entirely boiled away. This done, the vacant space in the bulb was filled up with turpentine, and the stopper inserted. The weights of the volumenometers and their contents at different temperatures were then ascertained, as in the case of the experiments with turpentine alone, already described. We may mention in this place that, for convenience sake, two or three bulbs containing different salts were always tried at the same time.

Exp^t. 1.—634·200 grs. of Powdered Red Oxide of Mercury, in No. 3 Volumenometer.

Temp.	Weight.	Mean Temp.	Mean Weight.
108	1442·086	109	1442·072
110	1442·058		
747·9	1431·882	748·5	1431·863
749·2	1431·844		

In calculating the volume and expansion of the red oxide of mercury from the above results, we proceeded as follows. From our first table of results for the expansion of turpentine, it appears that the weights of No. 3 volumenometer, filled with turpentine at the temperatures 110·5 and 747·55, are respectively 857·773 and 846·411. Hence, at the temperatures of the above experiment (109 and 748·5), the weights would have been 857·800 and 846·394. Subtracting the weight of oxide from the weights of the volumenometer at the two temperatures, we have $1442·072 - 634·200 = 807·872$ and $1431·863 - 634·200 = 797·663$. These numbers being subtracted from 857·800 and 846·394, leave 49·928 and 48·731 as the quantities of turpentine displaced by the oxide at the respective temperatures. But from the first table of the expansion of turpentine, it appears that 48·731 grs. at 748·5 are equivalent to 50·008 grs. at 109, regard being had to the expansion of glass. The expansion of the oxide for the interval of temperature between 109 and 748·5 is therefore 0·001596, which gives 0·005802 as the expansion for an interval of 2325 divisions of the thermometer corresponding to 180° Fahrenheit.

It appears also that the volume of 634·200 grs. of the oxide is equal to the volume of 49·928 grs. of turpentine at 109. But from the relative weights of the volumenometer containing water and turpentine, already given, we find that the sp. gravity of turpentine at 109 is to that of water at 107·7 as 0·87669 is to 1. Hence we

readily find that the sp. gravity of the oxide at $107\cdot7$, the point of maximum density of water, is $11\cdot136$.

Exp^t. II.—540·940 grs. of Sulphuret of Lead in powder in No. 2 Volumenometer :

Temperature.	Weight.	Mean Temp.	Mean Weight.
108·2	1292·228	111·3	1292·172
114·4	1292·116		
748·2	1282·824	748·9	1282·807
749·6	1282·791		

Therefore expansion for $180^0 = 0\cdot01045$. Sp. gr. at $39^0\cdot1 = 6\cdot9238$.

Exp^t. III.—585·500 grs. of Bichromate of Potash in small crystals in No. 3 Volumenometer :

111·2	1252·440	112·7	1252·421
114·2	1252·402		
749·8	1245·290	749·3	1245·297
748·9	1245·303		

Therefore expansion for $180^0 = 0\cdot0122$. Sp. gr. at $39^0\cdot1 = 2\cdot692$.

Exp^t. IV.—146·355 grs. of pounded Muriate of Ammonia in No. 2 Volumenometer :

111·8	882·348	113·8	882·329
115·8	882·310		
750	873·149	749·5	873·149
748·8	873·150		

Therefore expansion for $180^0 = 0\cdot0191$. Sp. gr. at $39^0\cdot1 = 1\cdot5333$.

Exp^t. V.—376·520 grs. of Peroxide of Tin in powder. No. 1 Volumenometer :

109·2	917·088	111·1	917·073
113	917·058		
750	912·379	749·5	912·381
749	912·383		

Therefore expansion for $180^0 = 0\cdot00172$. Sp. gr. at $39^0\cdot1 = 6\cdot7122$.

Exp^t. VI.—405·131 grs. of Sulphate of Iron, prepared by pounding, and pressing between bibulous paper, in No. 3 Volumenometer :

104	1074·826	107·5	1074·792
111	1074·758		
749·4	1077·586	750	1077·576
750·6	1077·567		

Therefore expansion for $180^0 = 0\cdot01153$. Sp. gr. at $39^0\cdot1 = 1\cdot8889$.

Exp^t. VII.—426·672 grs. of Sulphate of Copper, prepared by pressing the pounded salt between folds of bibulous paper. No. 2 Volumenometer :

Temperature.	Weight.	Mean Temp.	Mean Weight.
104·5	1083·046 }	108·2	1083·004
112	1082·963 }		
749·6	1075·777 }	750	1075·776
750·4	1075·775 }		

Therefore expansion for $180^0 = 0·009525$. Sp. gr. at $39^0·1 = 2·2901$.

Exp^t. VIII.—552·605 grs. of Protoxide of Lead in powder in No. 1 Volumenometer :

103·5	1090·670 }	106·4	1090·649
109·4	1090·629 }		
749·6	1085·902 }	750	1085·900
750·4	1085·898 }		

Therefore expansion for $180^0 = 0·00795$. Sp. gr. at $39^0·1 = 9·3634$.

Exp^t. IX.—327·760 grs. of Sulphate of Magnesia, prepared by pressing the pounded salt between folds of bibulous paper. No. 3 Volumenometer :

90	1014·948 }	93·3	1014·913
96·6	1014·879 }		
750	1007·181 }	749·5	1007·182
749	1007·182 }		

Therefore expansion for $180^0 = 0·01019$. Sp. gr. at $39^0·1 = 1·6829$.

Exp^t. X.—417·706 grs. of Nitrate of Potash in No. 2 Volumenometer :

89·4	1063·822 }	93·4	1063·776
97·4	1063·731 }		
750·3	1056·109 }	749·4	1056·114
748·6	1056·119 }		

Therefore expansion for $180^0 = 0·01967$. Sp. gr. at $39^0·1 = 2·1078$.

Exp^t. XI.—287·080 grs. of Copper, prepared from the oxide by passing hydrogen over it at a red heat, in No. 1 Volumenometer :

89	846·962 }	92·3	846·932
95·6	846·903 }		
401·2	844·420 }	400·6	844·426
400	844·432 }		

Therefore expansion for $180^0 = 0·0055$. Sp. gr. at $39^0·1 = 8·367$.

Exp^t. XII.—621·528 grs. of Yellow Chromate of Potash in No. 3 Volumenometer :

91·4	1278·445 }	95·2	1278·402
99	1278·360 }		
752·5	1271·323 }	752·8	1271·304
753·2	1271·285 }		

Therefore expansion for $180^0 = 0·01134$. Sp. gr. at $39^0·1 = 2·7110$.

Exp^t. XIII.—531·794 grs. of Nitrate of Soda in No. 2 Volumeno-
meter :

Temperature.	Weight.	Mean Temp.	Mean Weight.
92	1145·372	95·8	1145·323
99·6	1145·274		
752·4	1138·724	752·7	1138·720
753	1138·715		

Therefore expansion for $180^{\circ}=0\cdot0128$. Sp. gr. at $39^{\circ}\cdot1=2\cdot2606$.

Exp^t. XIV.—133·131 grs. of Red Oxide of Manganese in No. 1
Volumenometer :

91·2	696·149	94·6	696·113
98	696·077		
753·4	690·654	753·2	690·660
753	690·666		

Therefore expansion for $180^{\circ}=0\cdot00522$. Sp. gr. at $39^{\circ}\cdot1=4\cdot325$.

Exp^t. XV.—424·298 grs. of Sugar Candy, coarsely pounded.
No. 3 Volumenometer :

102·6	1048·504	107·0	1048·472
111·5	1048·440		
752·6	1042·251	753·8	1042·244
755	1042·238		

Therefore expansion for $180^{\circ}=0\cdot01116$. Sp. gr. at $39^{\circ}\cdot1=1\cdot5927$.

Exp^t. XVI.—546·662 grs. of Nitrate of Lead in No. 1 Volumeno-
meter :

99·4	1029·299	104·1	1029·280
108·8	1029·261		
753·4	1025·773	753·9	1025·772
754·4	1025·771		

Therefore expansion for $180^{\circ}=0\cdot00839$. Sp. gr. at $39^{\circ}\cdot1=4\cdot472$.

The above experiments were, as we have already stated, completed before the commencement of September 1846, and a variety of circumstances prevented our resumption of the research before March in the succeeding year. However, previously to the commencement of the new series, we provided ourselves with a large quantity of turpentine, which after having been well mixed, was decanted into small bottles and preserved over mercury. In this way the turpentine was kept without material change, as will be seen from the following series of results obtained with it before the commencement of the experiments, and after their completion.

SERIES I. *Experiments on the Expansion of Turpentine, on
March 20, 1847.*

Volumeno- meter.	Tempe- rature.	Weight.	Mean Tempe- rature.	Mean Weight.	Weight of Bulb.	Weight of Turpentine alone.
No. 1.	89·5	590·119	88·2	590·127	349·546	240·581
	87·0	590·136				
	747·6	584·024	747·6	584·024	349·546	234·478
No. 2.	89·4	820·472	88·2	820·492	377·036	443·456
	87·0	820·512				
	746·6	809·169	746·6	809·169	377·036	432·133
No. 3.	89	858·553	88	858·568	397·649	460·918
	87	858·584				
	734·1	847·030	739·9	846·918	397·649	449·269
	745·7	846·806				

SERIES II. *Experiments on the Expansion of Turpentine, on
January 21, 1848.*

Volumeno- meter.	Tempe- rature.	Weight.	Mean Tempe- rature.	Mean Weight.	Weight of Bulb.	Weight of Turpentine alone.
No. 2.	73	820·752	71·5	820·778	377·036	443·742
	70	820·805				
	754·6	809·031	754·6	809·031	377·036	431·995
	754·6	809·032				
No. 3.	70·8	858·871	71·4	858·863	397·649	461·214
	73·2	858·831				
	70·2	858·886	754·6	846·644	397·649	448·995
	754·6	846·645				
	754·6	846·641	754·6	846·644	397·649	448·995
	754·6	846·647				

In calculating the expansion of the salts, the mean of the above two series was employed, viz. :

Volumenometer.	Temperature.	Weight.	Weight of Volumenometer alone.	Weight of Turpentine alone.
No. 1.	88·2	590·127	349·546	240·581
	747·6	584·024	349·546	234·478
No. 2.	79·85	820·635	377·036	443·599
	750·6	809·100	377·036	432·064
No. 3.	79·7	858·715	397·649	461·066
	747·25	846·781	397·649	449·132

Exp^t. XVII.—466·202 grs. of Nitrate of Potash in large crystals.
No. 3 Volumenometer :

Temperature.	Weight.	Mean Temp.	Mean Weight.
75	1129·601	76·5	1129·589
78	1129·578		
739·3	1121·954	742·9	1121·937
746·5	1121·920		

Therefore expansion for $180^0 = 0·017237$. Sp. gr. at $39^0·1 = 2·09584$.

Expt. XVIII.—654·992 grs. of Sulphate of Potash in small crystals.
No. 2 Volumenometer :

74·6	1259·066	76·3	1259·060
78·0	1259·054		
738·4	1252·752	742·5	1252·721
746·6	1252·690		

Therefore expansion for $180^0 = 0·010697$. Sp. gr. at $39^0·1 = 2·65606$.

Expt. XIX.—302·609 grs. of Copper prepared from the oxide by passing hydrogen gas over it at a red heat. No. 1 Volumenometer :

74	861·271	75·9	861·263
77·8	861·256		
740	855·884	743·7	855·850
747·4	855·816		

Therefore expansion for $180^0 = 0·00767$. Sp. gr. at $39^0·1 = 8·41613$.

Expt. XX.—501·286 grs. of Nitrate of Potash, pounded small.
No. 3 Volumenometer :

60	1151·237	61·4	1151·217
62·8	1151·197		
736·6	1143·634	739·8	1143·596
743	1143·558		

Therefore expansion for $180^0 = 0·019487$. Sp. gr. at $39^0·1 = 2·10657$.

Expt. XXI.—427·790 grs. of Sulphate of Copper and Ammonia, in large crystals. No. 2 Volumenometer :

60·8	1050·197	62	1050·182
63·2	1050·167		
736	1043·559	739·5	1043·529
743	1043·499		

Therefore expansion for $180^0 = 0·0066113$. Sp. gr. at $39^0·1 = 1·89378$.

Expt. XXII.—429·784 grs. of Sulphate of Magnesia and Ammonia, in good crystals. No. 3 Volumenometer :

76·0	1068·645	76·6	1068·644
77·2	1068·643		
739·0	1062·177	737·3	1062·202
735·6	1062·227		

Therefore expansion for $180^0 = 0·007161$. Sp. gr. at $39^0·1 = 1·71686$.

Exp^t. XXIII.—507·958 grs. of Sulphate of Potash and Zinc, in good crystals. No. 2 Volumenometer :

Temperature.	Weight.	Mean Temp.	Mean Weight.
75·0	1129·497 }	75·8	1129·480
76·6	1129·463 }		
738·7	1122·899 }	736·6	1122·920
734·5	1122·941 }		

Therefore expansion for $180^0 = 0·008235$. Sp. gr. at $39^0·1 = 2·24034$.

Exp^t. XXIV.—444·494 grs. of Sulphate of Magnesia and Potash, in good crystals. No. 3 Volumenometer :

75·0	1113·108 }	75·4	1113·101
75·8	1113·095 }		
747·9	1105·678 }	748·0	1105·683
748·1	1105·688 }		

Therefore expansion for $180^0 = 0·009372$. Sp. gr. at $39^0·1 = 2·05319$.

Exp^t. XXV.—456·314 grs. of Sulphate of Copper and Potash, in good crystals. No. 2 Volumenometer :

74·9	1091·772 }	75·4	1091·761
75·9	1091·750 }		
748·3	1084·695 }	748·0	1084·698
747·7	1084·701 }		

Therefore expansion for $180^0 = 0·009043$. Sp. gr. at $39^0·1 = 2·16376$.

Exp^t. XXVI.—449·535 grs. of Sulphate of Copper, in small crystals, prepared by stirring the cupreous solution while cooling. This specimen contained 5·112 equivalents of water, or an excess, due to a mechanical admixture of water. No. 3 Volumenometer.

83·7	1132·089 }	83·9	1132·094
84·1	1132·099 }		
746·2	1124·632 }	746·2	1124·653
746·2	1124·674 }		

Therefore expansion for $180^0 = 0·005315$. Sp. gr. at $39^0·1 = 2·2422$.

Exp^t. XXVII.—320·027 grs. of Sulphate of Ammonia, in fine small crystals. No. 3 Volumenometer :

89·4	1019·9 }	85·3	1019·095
81·2	1019·141 }		
746·2	1011·018 }	746·1	1011·011
746·0	1011·005 }		

Therefore expansion for $180^0 = 0·010934$. Sp. gr. at $39^0·1 = 1·76147$.

Exp^t. XXVIII.—377·686 grs. of Sulphate of Chromium and Potash, in good crystals. No. 2 Volumenometer :

Temperature.	Weight.	Mean Temp.	Mean Weight.
89·0	1019·481	85·1	1019·526
81·2	1019·571		
746·2	1012·614	746·2	1012·617
746·2	1012·620		

Therefore expansion for $180^{\circ}=0\cdot005242$. Sp. gr. at $39^{\circ}\cdot1=1\cdot85609$.

Exp^t. XXIX.—517·725 grs. of Sulphate of Copper, pounded and well pressed between folds of bibulous paper. No. 3 Volumenometer :

86·0	1176·752	87·0	1176·743
88·0	1176·734		
745·3	1169·776	743·7	1169·794
742·1	1169·812		

Therefore expansion for $180^{\circ}=0\cdot00812$. Sp. gr. at $39^{\circ}\cdot1=2\cdot2781$.

Exp^t. XXX.—600·594 grs. of Yellow Chromate of Potash, in fine small crystals. No. 2 Volumenometer :

86·0	1227·440	87·0	1227·433
88·0	1227·427		
745·3	1220·612	743·8	1220·634
742·3	1220·656		

Therefore expansion for $180^{\circ}=0\cdot011005$. Sp. gr. at $39^{\circ}\cdot1=2\cdot72309$.

Exp^t. XXXI.—467·184 grs. of Potash Alum, in good crystals. No. 2 Volumenometer :

80·0	1053·484	80·0	1053·482
80·0	1053·480		
748·0	1047·995	746·4	1048·018
744·8	1048·042		

Therefore expansion for $180^{\circ}=0\cdot003682$. Sp. gr. at $39^{\circ}\cdot1=1\cdot75125$.

Exp^t. XXXII.—402·116 grs. of Binocalate of Potash, in good crystals. No. 3 Volumenometer :

80·0	1088·032	80·0	1088·033
80·0	1088·034		
748·2	1080·146	746·6	1080·170
745·0	1080·194		

Therefore expansion for $180^{\circ}=0\cdot011338$. Sp. gr. at $39^{\circ}\cdot1=2\cdot04401$.

Exp^t. XXXIII.—447·312 grs. of Oxalate of Potash, in good crystals. No. 2 Volumenometer :

61·6	1083·389	63·3	1083·374
65·0	1083·359		
752·2	1075·978	751·6	1075·996
751·0	1076·014		

Therefore expansion for $180^{\circ}=0\cdot01162$. Sp. gr. at $39^{\circ}\cdot1=2\cdot12657$.

Temperature.	Weight.	Mean Temp.	Mean Weight.
Exp ^t . XXXIV.—406·552 grs. of Chloride of Potassium, coarsely pounded. No. 3 Volumenometer :			
60.8	1084·916	63·2	1084·886
65·6	1084·856		
752·5	1076·959	751·9	1076·970
751·3	1076·981		

Therefore expansion for $180^{\circ}=0\cdot010944$. Sp. gr. at $39^{\circ}\cdot1=1\cdot97756$.

Exp ^t . XXXV.—292·039 grs. of Oxalate of Ammonia, in fine small crystals. No. 3 Volumenometer :			
79·2	979·728	80·8	979·713
82·4	979·698		
752·0	971·874	750·9	971·890
749·8	971·907		

Therefore expansion for $180^{\circ}=0\cdot00876$. Sp. gr. at $39^{\circ}\cdot1=1\cdot49985$.

Exp ^t . XXXVI.—621·193 grs. of Nitrate of Barytes, in small crystals. No. 2 Volumenometer :			
85·8	1269·101	87·9	1269·085
90·0	1269·069		
745·8	1262·089	746·4	1262·086
747·0	1262·083		

Therefore expansion for $180^{\circ}=0\cdot004523$. Sp. gr. at $39^{\circ}\cdot1=3\cdot16052$.

Exp ^t . XXXVII.—450·560 grs. of Bisulphate of Potash, pounded. No. 3 Volumenometer :			
86·9	1149·461	88·5	1149·445
90·1	1149·429		
746·0	1141·345	746·5	1141·339
747·0	1141·333		

Therefore expansion for $180^{\circ}=0\cdot012387$. Sp. gr. at $39^{\circ}\cdot1=2\cdot47767$.

Exp ^t . XXXVIII.—373·783 grs. of Oxalic Acid, in good crystals. No. 2 Volumenometer :			
89·2	994·334	87·8	994·346
86·4	994·359		
744·9	986·783	744·8	986·784
744·7	986·785		

Therefore expansion for $180^{\circ}=0\cdot027476$. Sp. gr. at $39^{\circ}\cdot1=1\cdot64138$.

Exp ^t . XXXIX.—393·044 grs. of Chlorate of Potash, in small crystals. No. 3 Volumenometer :			
89·2	1103·259	87·9	1103·269
86·6	1103·279		
744·7	1094·718	744·7	1094·722
744·7	1094·726		

Therefore expansion for $180^{\circ}=0\cdot017112$. Sp. gr. at $39^{\circ}\cdot1=2\cdot32643$.

Exp^t. XL.—541·833 grs. of Chloride of Barium, in small crystals. No. 2 Volumenometer:

Temperature.	Weight.	Mean Temp.	Mean Weight.
64·8	1206·826	67·1	1206·800
69·4	1206·774		
755·4	1198·800	755·8	1198·797
756·2	1198·794		

Therefore expansion for $180^{\circ}=0\cdot009873$. Sp. gr. at $39^{\circ}\cdot1=3\cdot05435$.

Exp^t. XLI.—326·462 grs. of Sugar of Milk, pounded. No. 3 Volumenometer:

65·0	998·393	67·2	998·383
69·4	998·373		
755·6	990·721	755·9	990·720
756·2	990·719		

Therefore expansion for $180^{\circ}=0\cdot009111$. Sp. gr. at $39^{\circ}\cdot1=1\cdot53398$.

Exp^t. XLII.—307·866 grs. of Binocalate of Ammonia in good crystals. No. 2 Volumenometer:

81·8	960·874	83·6	960·862
85·4	960·850		
750·8	953·203	750·9	953·210
751·0	953·217		

Therefore expansion for $180^{\circ}=0\cdot013718$ sp. gr. at $39^{\circ}\cdot1=1\cdot61341$.

Exp^t. XLIII.—234·865 grs. of Bichromate of Chloride of Potassium in good crystals. No. 3 Volumenometer:

81·6	1010·939	83·4	1010·914
85·2	1010·889		
750·7	1000·808	750·9	1000·816
751·1	1000·824		

Therefore expansion for $180^{\circ}=0\cdot015902$. Sp. gr. at $39^{\circ}\cdot1=2\cdot49702$.

Exp^t. XLIV.—392·901 grs. of Quadroxalate of Potash in good crystals. No. 2 Volumenometer:

74·5	1026·945	75·3	1026·940
76·1	1026·935		
751·0	1019·509	752·2	1019·502
753·4	1019·494		

Therefore expansion for $180^{\circ}=0\cdot015916$. Sp. gr. at $39^{\circ}\cdot1=1\cdot84883$.

Exp^t. XLV.—396·646 grs. of Quadroxalate of Ammonia in good crystals. No. 3 Volumenometer:

74·9	1044·521	75·6	1044·518
76·3	1044·515		
751·0	1037·270	752·2	1037·263
753·4	1037·256		

Therefore expansion for $180^{\circ}=0\cdot014347$. Sp. gr. at $39^{\circ}\cdot1=1\cdot65194$.

The foregoing results are collated in the following Table:

No. of Exp.	Name of Salt.	Formula.	Atomic weight.	Expansion for 180°.	Sp. gravity at 39°-1.	Atomic Volume.	Atomic Volume, divided by 1.225.
11	Copper	Cu	31.66	0.0055	8.367	3.7839	3.0889
19	Ditto	ditto	ditto	0.00767	8.41613	3.7618	3.0709
1	Red Oxide of Mercury	HgO	108.07	0.005802	11.136	9.7046	7.9221
8	Protioxide of Lead	PbO	111.56	0.00795	9.3634	11.887	9.7037
14	Red Oxide of Manganese	Mn ₃ O ₄	115.0	0.00522	4.325	26.590	21.706
5	Peroxide of Tin	SnO ₂	74.82	0.00172	6.7122	11.147	9.0995
2	Sulphuret of Lead	PbS	119.56	0.01045	6.9238	17.268	14.096
34	Chloride of Potassium	KCl	74.5	0.010944	1.97756	37.673	30.753
40	Chloride of Barium	BaCl + 2HO	122.14	0.009873	3.05435	39.989	32.644
4	Chloride of Ammonium	NH ₄ Cl	53.5	0.0191	1.5333	34.892	28.483
13	Nitrate of Soda	NaO, NO ₅	85.0	0.0128	2.2606	37.601	30.694
10	Nitrate of Potash	KO, NO ₅	101.0	0.01967	2.1078	47.917	39.116
17	Ditto	ditto	ditto	0.017237	2.09584	48.191	39.339
20	Ditto	ditto	ditto	0.019487	2.10657	47.945	39.139
16	Nitrate of Lead	PbO, NO ₅	165.56	0.00839	4.472	37.021	30.222
36	Nitrate of Barytes	BaO, NO ₅	130.64	0.004523	3.16052	41.335	33.743
39	Chlorate of Potash	KO, ClO ₃	122.5	0.017112	2.32643	52.656	42.984
12	Chromate of Potash	KO, Cr O ₃	99.15	0.01134	2.711	36.573	29.856
30	Ditto	ditto	ditto	0.011005	2.72309	36.411	29.723
3	Bichromate of Potash	KO, 2Cr O ₃	151.3	0.0122	2.692	56.204	45.880
43	Bichromate of Chloride of Potassium	K Cl + 2Cr O ₃	178.8	0.015902	2.49702	71.605	58.453
38	Oxalic Acid	HO, C ₂ O ₃ + 2HO	63.0	0.027476	1.64138	38.382	31.332
33	Oxalate of Potash	KO, C ₂ O ₃ + HO	92.0	0.01162	2.12657	43.262	35.316

No. of Exp.	Name of Salt.	Formula.	Atomic weight.	Expansion for 180°	Sp. gravity at 39°-1.	Atomic Volume	Atomic Volume, divided by 1.225.
32	Binoxalate of Potash . . .	KO, 2C ₂ O ₃ + 3HO	146.0	0.011338	2.04401	71.428	58.309
44	Quadroxalate of Potash . . .	KO, 4C ₂ O ₃ + 7HO	254.0	0.015916	1.84883	137.384	112.150
35	Oxalate of Ammonia . . .	NH ₄ O, C ₂ O ₃ + HO	71.0	0.00876	1.49985	47.338	38.643
42	Binoxalate of Ammonia . . .	NH ₄ O, 2C ₂ O ₃ + 3HO	125.0	0.013718	1.61341	77.476	63.245
45	Quadroxalate of Ammonia . . .	NH ₄ O, 4C ₂ O ₃ + 7HO	233.0	0.014347	1.65194	141.046	115.140
18	Sulphate of Potash . . .	KO, SO ₃	87.0	0.010697	2.65606	32.755	26.739
37	Bisulphate of Potash . . .	KO, SO ₃ + HO, SO ₃	136.0	0.012287	2.47767	32.755	26.739
27	Sulphate of Ammonia . . .	NH ₄ O, SO ₃ + HO	75.0	0.010934	1.76147	42.578	34.758
7	Sulphate of Copper . . .	CuO, SO ₃ + 5HO	124.66	0.009325	2.2901	54.434	44.436
26	Ditto . . .	ditto	ditto	0.005315	2.2422	55.597	45.385
29	Ditto . . .	ditto	ditto	0.00812	2.2781	54.721	44.670
6	Sulphate of Iron . . .	FeO, SO ₃ + 7HO	139.0	0.01153	1.8889	73.588	60.072
9	Sulphate of Magnesia . . .	MgO, SO ₃ + 7HO	123.67	0.01019	1.6829	73.486	59.989
21	Sulphate of Copper and Ammonia . . .	CuO, SO ₃ + NH ₄ O, SO ₃ + 6HO	199.66	0.0066113	1.89378	105.430	86.065
25	Sulphate of Copper and Potash . . .	CuO, SO ₃ + KO, SO ₃ + 6HO	220.66	0.009043	2.16376	101.980	83.249
24	Sulphate of Magnesia and Potash . . .	MgO, SO ₃ + KO, SO ₃ + 6HO	201.67	0.009372	2.05319	98.223	80.182
28	Sulphate of Chromium and Potash . . .	Cr ₂ O ₃ , 3SO ₃ + KO, SO ₃ + 24HO	503.3	0.005242	1.85609	271.161	221.356
31	Potash Alum . . .	Al ₂ O ₃ , 3SO ₃ + KO, SO ₃ + 24HO	476.38	0.003682	1.75125	272.023	222.060
23	Sulphate of Potash and Zinc . . .	ZnO, SO ₃ + KO, SO ₃ + 6HO	221.0	0.008235	2.24034	98.646	80.527
22	Sulphate of Magnesia and Ammonia . . .	MgO, SO ₃ + NH ₄ O, SO ₃ + 6HO	180.67	0.007161	1.71686	105.233	85.904
15	Cane Sugar . . .	C ₁₂ H ₂₂ O ₁₁	171.0	0.011160	1.5927	107.365	87.645
41	Sugar of Milk . . .	C ₁₂ H ₂₂ O ₁₂	180.0	0.009111	1.53398	117.342	95.789

On a cursory inspection of the above table, it will be observed that considerable discrepancy occurs in the results obtained with salts of the same name. This must not throw doubt on the accuracy of the experiments, as it arose from the state in which the salts were tried. The specific gravity of copper in the 19th experiment is somewhat greater than that in the 11th experiment; the reason for which is, that the copper in the former case was exposed to hydrogen at a red heat for a considerable time after the oxygen had been removed from the oxide. In the case of nitrate of potash, the 17th experiment was made with large crystals, averaging $\frac{3}{16}$ of an inch in diameter, whilst in experiment 20 we employed another portion of the same salt pounded very small, so as to free it from mechanical water, and in experiment 10 a different specimen was used in small crystals. It will be observed, that a very considerable difference exists between the results of the three trials. The large crystals were lighter and in a more coerced state, as shown by their smaller expansion. Of the three specimens of sulphate of copper tried, that employed in experiment 26 had, as we have stated, a larger quantity of water than 5 equivalents attached to it, and hence we observe a great difference in its expansion and specific gravity, the decrease of gravity being, as before, accompanied by a decrease of expansion. With regard to the expansions, we may call attention to the close approximation of the highly hydrated salts to 0.01125, or the expansion of ice as determined by Brunner. The expansion of oxalic acid is remarkable as being greater, and that of peroxide of tin as being less than those of any solid bodies on record. In all cases of hydrated salts, it is extremely difficult to obtain them in their exact normal state of hydration, and therefore the results of experiment with different specimens are subject to variation.
