

Density Functional Theory Study of Nitrous Oxide Decomposition over Fe- and Co-ZSM-5

Jason A. Ryder,[†] Arup K. Chakraborty,^{‡,§,†} and Alexis T. Bell^{*,||,†}*Chemical and Materials Sciences Divisions, Lawrence Berkeley National Laboratory and Departments of Chemistry and Chemical Engineering, University of California, Berkeley, California 94720-1462**Received: December 31, 2001; In Final Form: May 8, 2002*

Iron- and cobalt-exchanged ZSM-5 are active catalysts for the dissociation of nitrous oxide. In this study, density functional theory was used to assess a possible reaction pathway for the catalytic dissociation of N₂O. The active center was taken to be mononuclear [FeO]⁺ or [CoO]⁺, and the surrounding portion of the zeolite was represented by a 24-atom cluster. The first step of N₂O decomposition involves the formation of [FeO₂]⁺ or [CoO₂]⁺ and the release of N₂. The metal-oxo species produced in this step then reacts with N₂O again, to release N₂ and O₂. The apparent activation energies for N₂O dissociation in Fe-ZSM-5 and Co-ZSM-5 are 39.4 and 34.6 kcal/mol, respectively. The preexponential factor for the apparent first-order rate coefficient is estimated to be of the order 10⁷ s⁻¹ Pa⁻¹. Although the calculated activation energy for Fe-ZSM-5 is in good agreement with that measured experimentally, the value of the preexponential factor is an order of magnitude smaller than that observed. The calculated activation energy for Co-ZSM-5 is higher than that reported experimentally. However, consistent with experiment, the rate of N₂O decomposition on Co-ZSM-5 is predicted to be significantly higher than that on Fe-ZSM-5.

Introduction

Transition metals cation-exchanged into ZSM-5 have been shown to catalyze the dissociation of nitrous oxide to oxygen and nitrogen.^{1–7} The activity of such catalysts depends on the identity of the exchanged transition metal cation and decreases in the order Rh, Ru > Pd > Cu > Co > Fe > Pt > Ni > Mn.^{1–3} Studies of nitrous oxide dissociation over Cu-, Co-, and Fe-ZSM-5 show that the reaction is first order in N₂O and in the case of Cu-ZSM-5 is inhibited by O₂.^{1,5,6,8} It has also been reported that isotopically labeled oxygen scrambles into the products of nitrous oxide dissociation in the case of Cu-ZSM-5 but not in the case of either Co- or Fe-ZSM-5. This suggests that the mechanisms of N₂O dissociation are similar on Co- and Fe-ZSM-5, and that the mechanism for Cu-ZSM-5 may be different.

Much effort has been devoted to the characterization of Fe in Fe-ZSM-5.^{9–19} Work by Lobree et al. suggests that up to an Fe/Al ratio of 0.56, Fe³⁺ cations substitute, as [Fe(OH)₂]⁺, on a one for one basis with Brønsted acid protons.⁹ Similar conclusions have been reported by Sachtler and co-workers.¹⁰ However, other authors have demonstrated that iron may be present as binuclear oxo cations and as small particles of iron oxide.^{11–15} The extent to which iron cations can exchange as such species has been estimated by Rice et al.¹⁶ These authors showed that for a Si/Al ratio of 25 if all pairs of cation exchange sites capable of accommodating species such as [Fe(OH)OFe(OH)]²⁺ were filled, the corresponding value of Fe/Al would be 0.50, assuming that the distance between Al atoms in the cation-exchange sites is < 7.5 Å. As the Si/Al ratio increases the value of Fe/Al rapidly decreases. Similar conclusions about

the accommodation of oxo metal cations have been reported by Goodman et al.^{17,18} Fe³⁺ cations can also be accommodated as [Fe(OH)]²⁺ in five- and six-membered rings containing two Al atoms. For such species the value of Fe/Al is 0.07 if the Si/Al ratio of the zeolite is 25. Here too, the value of Fe/Al decreases with increasing Si/Al ratio. By contrast, there are no constraints on the Fe/Al ratio for cations such as [Fe(OH)₂]⁺ or [FeO]⁺, since only isolated charge-exchange sites are required to accommodate these species. Thus, it is reasonable to conclude that a significant fraction of the Fe³⁺ cations exchanged into ZSM-5 (Si/Al ≥ 25) would be present as isolated cations associated with a single charge-exchange site. It is also notable that in the case of Co-ZSM-5, an even more active catalyst to N₂O decomposition than Fe-ZSM-5, there is no evidence for binuclear Co species.²⁰

Attempts to characterize the energetics of N₂O decomposition on Fe-ZSM-5 via quantum chemical calculations have been reported by several authors.^{21–24} Yoshizawa et al. have proposed a model for the dissociation of nitrous oxide in Fe-ZSM-5 based on an isolated 3T-atom zeolite model.^{21,22} Although they demonstrate that N₂O decomposition could occur on such a site, their proposed reaction mechanism assumes that O₂ desorbs via the process, Z-[Fe(O)₂]⁺ → Z-Fe⁺ + O₂ (g). This step seems unrealistic because the experimental evidence does not support the existence of Fe⁺ cations in ZSM-5.^{9,19} Yakovlev and co-workers have also carried out quantum calculations of N₂O decomposition. In the first of their studies, the active sites was modeled as M(OH)₃(H₂O)₂ (M = Fe, Co, Rh).²³ The energies of intermediates and transition states were computed and it was determined that Co and Rh sites are more active than Fe. In the second study, the energetics of N₂O decomposition were investigated for binuclear Fe complexes in Fe-ZSM-5.²⁴ The zeolite was modeled by a pair of 5T rings sharing an edge and the Fe complex was represented as either [(HO)FeOFe(OH)]²⁺ or [FeOFe]²⁺. Although only stable states for active sites and intermediates along the reaction path were considered, the

* To whom correspondence should be addressed.

[†] Department of Chemical Engineering, University of California, Berkeley.

[‡] Materials Sciences Divisions, Lawrence Berkeley National Laboratory.

[§] Department of Chemistry, University of California, Berkeley.

^{||} Chemical Sciences Divisions, Lawrence Berkeley National Laboratory.

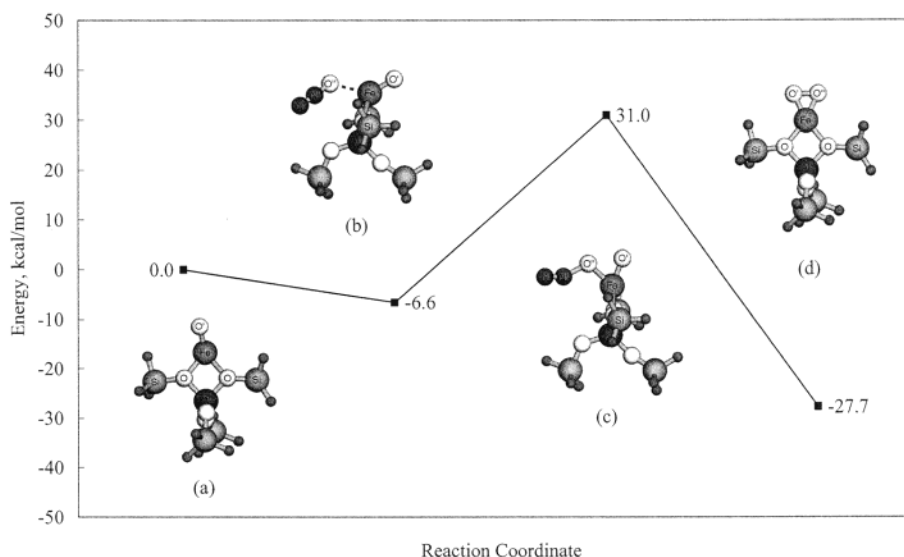


Figure 1. Energy versus reaction coordinate for nitrous oxide decomposition over $Z^-[\text{FeO}]^+$.

authors did show that oxo-metal cations could serve as active sites for N_2O decomposition.

In this study, we report an investigation of the mechanisms of nitrous oxide dissociation in Co- and Fe-ZSM-5 using density functional theory. We proceed by postulating a mechanism for the dissociation process, computing the energetics for each elementary step, and developing a rate expression for the overall rate of reaction. The apparent rate parameters (activation energy and preexponential factor) are then compared with experiments to evaluate the plausibility of the proposed mechanism.

Theoretical Methods

The catalytically active center and a portion of the zeolite framework are represented by a 24-atom cluster. As shown in Figure 1, the portion of the cluster describing the zeolite contains an Al atom in the T12 site of the framework surrounded by shells of O and Si atoms. The terminal Si-atoms are fixed in their crystallographic positions as reported by Olson et al.²⁵ Dangling bonds are terminated by H-atoms located 1.5 Å from each terminal Si atom oriented in the direction of the next T (tetrahedral) site. The anionic cluster is charge-compensated by a metal-oxo species, $[\text{FeO}]^+$ or $[\text{CoO}]^+$, placed between two of the four O atoms surrounding the Al atom.

The choice of $[\text{FeO}]^+$ or $[\text{CoO}]^+$ as the active center is guided by the following experimental observations.⁹ Dry exchange of H-ZSM-5 with FeCl_3 results in the release of HCl and the replacement of each Bronsted acid proton by $[\text{FeCl}_2]^+$. The Cl atoms associated with iron are removed by washing in water, with the results that the charge-exchange positions in Fe-ZSM-5 are now occupied by $[\text{Fe}(\text{OH})_2]^+$. Upon heating, the water is liberated and the charge compensating unit becomes $[\text{FeO}]^+$. As noted in the Introduction, $[\text{Fe}(\text{OH})_2]^+$ and $[\text{FeO}]^+$ are expected to be the predominant forms of in which Fe^{3+} cations are present in ZSM-5 with Si/Al ratio of 25 or greater.

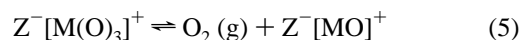
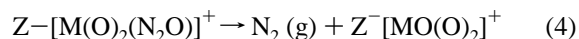
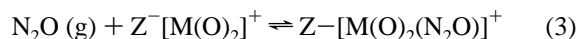
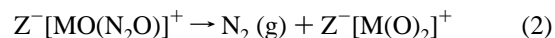
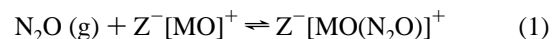
Quantum chemical calculations of the geometry and energies of ground states and transition-state structures were performed using nonlocal, gradient-corrected density-functional theory (DFT).²⁶ To represent the effects of exchange and correlation, Becke's 3-parameter exchange with correlation functionals of Lee, Yang, and Parr (B3LYP) were used.^{27,28} Basis sets at the 6-31G or double- ζ level were used for all atoms, with the exception of Fe. To describe Fe, the energy-consistent pseudo-

potentials of Stuttgart and Bonn were used in the small-core approximation.²⁹ Polarization functions were added to all atoms, with the exception of terminal H groups. No corrections were made for basis-set superposition error. All calculations were carried out using the Jaguar 4.0 suite of programs (Schrödinger, Inc.) and Gaussian 98.^{30,31} During these calculations, all of the atoms of the cluster were allowed to relax with the exception of the terminal Si atoms, as noted above.

Overall equilibrium constants and reaction rate constants were computed using standard statistical mechanics and absolute rate theory.³² We use the harmonic approximation, and include contributions of the translational, rotational, and vibrational partition functions of all gaseous species participating in the reaction and the vibrational contribution due to the zeolite cluster. Because the zeolite cluster is part of a solid, translational and rotational partition functions for the zeolite were assumed to be equal in the reactant and transition-state. All molecular structures were assumed to be in the ground-state electronic configuration.

Results and Discussion

The dissociation of N_2O at a single metal center can be envisioned to proceed via the following sequence of steps



In this sequence, M represents either Fe or Co. Reactions 1 and 3 involve the adsorption of gas-phase N_2O , assumed to be reversible, to the catalytically active site. Reactions 2 and 4 describe the dissociation of each of the adsorbed N_2O species to give two equivalents of gas-phase N_2 and two surface oxygen species. Reaction 5 represents the desorption of O_2 molecules, which is also assumed to be reversible. The sum of these five

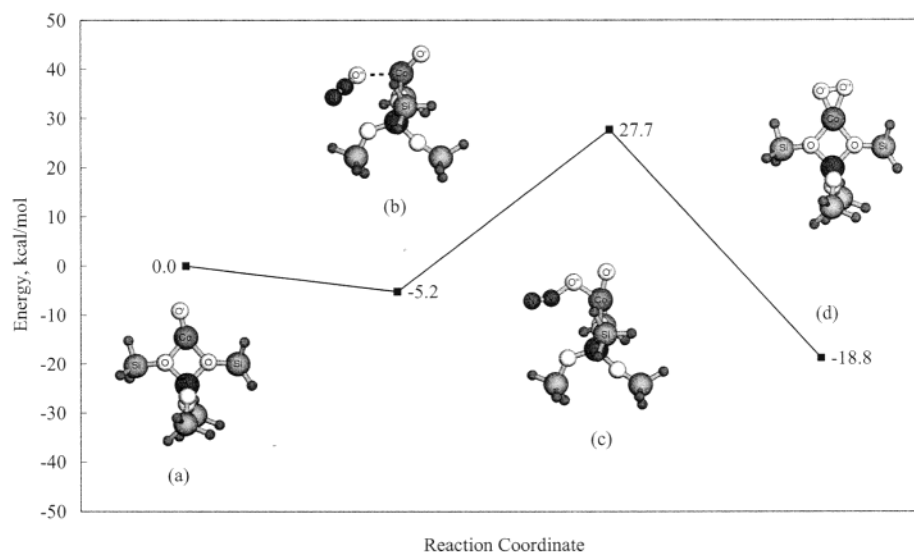


Figure 2. Energy versus reaction coordinate for nitrous oxide decomposition over $Z^{-}[\text{CoO}]^{+}$.

TABLE 1: Computed Frequency Shifts for N_2O Adsorbed on $Z^{-}[\text{MO}]^{+}$

mode ^a	$Z^{-}[\text{FeO}]^{+}$ (ONN)	$Z^{-}[\text{FeO}]^{+}$ (NNO)	$Z^{-}[\text{CoO}]^{+}$ (ONN)	$Z^{-}[\text{CoO}]^{+}$ (NNO)
$\Delta\nu(\text{N}-\text{N})$ (cm^{-1})	15	48	15	39
$\Delta\nu(\text{N}-\text{O})$ (cm^{-1})	-47	45	-19	46

^a Calculated frequency shift relative to gas-phase N_2O .

steps constitutes a complete catalytic cycle. In what follows, we present the calculations on the energetics for reactions 1 and 2 first, and then reactions 3 and 4. The desorption of O_2 via reaction 5 is examined separately, as well as the possibility of desorbing O_2 from $Z^{-}[\text{M}(\text{O})_2]^{+}$. It should be noted that while the proposed mechanism leads to a rate expression that is consistent with experimental observations, other mechanisms are also possible.

Figure 1 shows the calculated energy profile for reactions 1 and 2 occurring over Fe-ZSM-5. The corresponding calculations for Co-ZSM-5 are shown in Figure 2. In both figures, structures (a), (b), and (d) correspond to local minima on the potential energy surface, whereas structure (c) represents the transition-state for nitrous oxide dissociation. At each point along the reaction coordinate, the sextet (total spin 5/2) potential energy surface lies below those of the doublet (total spin 1/2) and quartet (total spin 3/2) for Fe. In the case of Co, the lowest energy is for the quintet (total spin 2). For this reason, we report results only for the sextet spin-state in the case of Fe and for the quintet spin state for Co.

The energy of nitrous oxide adsorption, ΔE_{ads} , is defined as the difference in energy between structures (a) and (b). For Fe-ZSM-5 this value is -6.6 kcal/mol and the corresponding value of the enthalpy of adsorption, ΔH_{ads} , is -7.2 kcal/mol at 298 K. The calculated value of ΔH_{ads} is smaller than that measured experimentally by Wood et al., $\Delta H_{\text{ads}} = -15$ kcal/mol.³³ Failure to achieve agreement is perhaps not surprising because the accuracy of DFT is particularly poor for weakly adsorbing species.³⁴ For Co-ZSM-5, the values of ΔE_{ads} and ΔH_{ads} are -5.2 kcal/mol and -5.8 kcal/mol, respectively.

The calculated frequency shifts for N_2O adsorbed on $Z^{-}[\text{FeO}]^{+}$ and $Z^{-}[\text{CoO}]^{+}$ are presented in Table 1. Results are given for adsorption through both the oxygen and the nitrogen end of the molecule. Our calculations show a red-shift of the symmetric mode and a blue-shift of the asymmetric mode of N_2O with respect to gas-phase molecule when N_2O is adsorbed through

the oxygen end of the molecule. Similar calculations for nitrous oxide adsorbed through the nitrogen end of the molecule show a blue shift for both modes. These trends are identical for Fe- and Co-ZSM-5 and are consistent with previous theoretical calculations of the interactions of N_2O with other cations.³⁵ Recently reported infrared spectra of N_2O adsorbed on Fe-ZSM-5 at 298 K indicate a blue shift for both vibrational modes of N_2O , suggesting a preference for adsorption through the nitrogen end of the molecule.³³

The activation energy for nitrous oxide dissociation, E_{act} , is defined as the difference in energy between the adsorbed structure (b) and the transition-state (c). This value, corrected for zero-point energy, is 37.6 kcal/mol for Fe-ZSM-5. The imaginary frequency associated with the transition-state is $726i$ cm^{-1} . The major difference between the transition state and the adsorbed state is the bending of the N-N'-O" bond angle from 180° in the adsorbed state to 150.6° at the transition-state. The activation energy for nitrous oxide dissociation, corrected for zero-point energy, is 32.9 kcal/mol for Co-ZSM-5. The imaginary frequency associated with the transition-state is $756i$ cm^{-1} . Here too, the major difference between the transition state and the adsorbed state is the bending of the N-N'-O" bond angle from 180° in the adsorbed state to 151.3° in the transition-state.

The product of reaction 2 is $Z^{-}[\text{MO}_2]^{+}$. The calculated distance between the two O atoms is 0.137 nm in the case of Fe and 0.133 nm in the case of Co. The corresponding M-O bond distances are 0.175 and 0.177 nm for Fe and 0.186 and 0.170 nm for Co. Spectroscopic observations made on Fe-ZSM-5 confirm the presence of a stable form of diatomic oxygen associated with Fe. Based on ESR studies of Fe-ZSM-5 (Si/Al = 14, Fe/Al = 1), Chen et al. suggest the presence of superoxide ions, O_2^{-} , at 77 K.³⁶ Diatomic oxygen surface species have also been observed in Fe-ZSM-5 by Gao et al. using in situ UV-Raman spectroscopy.³⁷ In the presence of gas-phase O_2 , Gao et al. observe a distinct band at 730 cm^{-1} , which they assign to a peroxide anion, O_2^{2-} . The band disappears upon purging with He, but reappears after subsequent exposure to O_2 . The band vanishes at 540 K, indicating weak adsorption to the surface.

The calculated vibrational modes associated with O_2 in $Z^{-}[\text{Fe}(\text{O})_2]^{+}$ are 501, 652, and 986 cm^{-1} . We attribute the frequencies at 501 and 652 cm^{-1} to the bending modes of $[\text{Fe}-(\text{O})_2]^{+}$. These modes are similar to those observed for ferrous

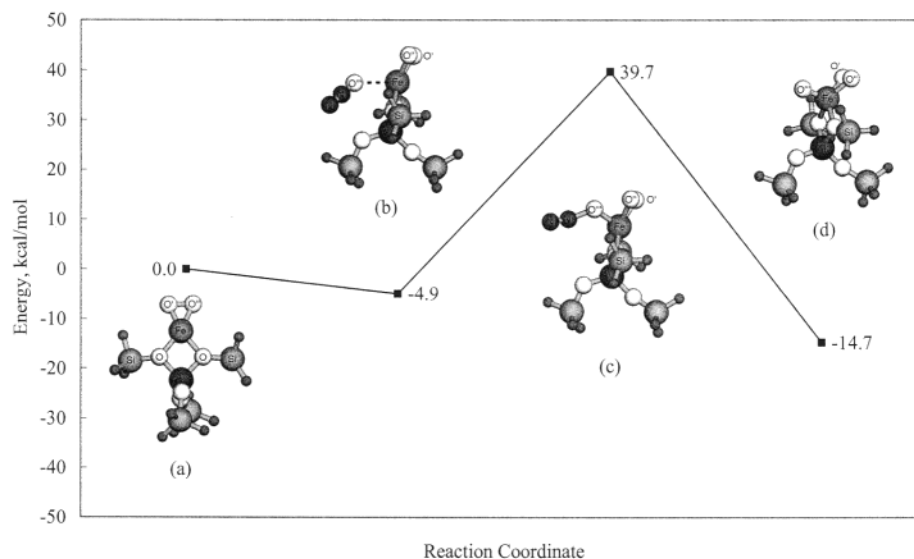


Figure 3. Energy versus reaction coordinate for nitrous oxide decomposition over $Z^-[\text{FeO}_2]^+$.

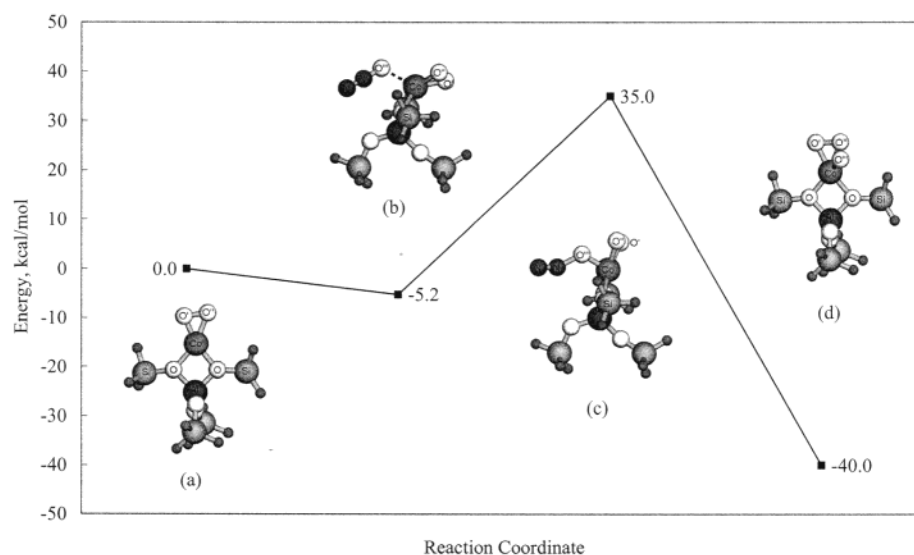
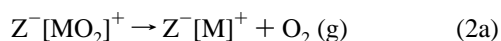


Figure 4. Energy versus reaction coordinate for nitrous oxide decomposition over $Z^-[\text{CoO}_2]^+$.

cytochrome P450cam, which occur at 402 and 540 cm^{-1} reported by MacDonald et al.³⁸ As noted above, Gao et al.³⁵ have observed a band at 730 cm^{-1} for adsorbed O_2 but do not assign this band to a specific mode. The vibrational frequency at 986 cm^{-1} is assigned to vibrations of the O–O bond and lies in a range characteristic of both peroxide and superoxide species. Peroxides on various metal oxides exhibit bands in the region of 640–970 cm^{-1} , whereas superoxide complexes exhibit bands in the range of 1015–1180 cm^{-1} .^{39,40} The observed frequency of for O–O vibrations in cytochrome P450cam is 1139 cm^{-1} .³⁸

The possibility that O_2 desorption could occur via the process



was considered. Because our model is based on an isolated cationic site, the occurrence of reaction 2a would require the metal cation to adopt a formal charge of +1. As noted in the Introduction, this state of Fe or Co seems unlikely, since ESR studies by Kucherov et al. on Fe–ZSM-5 and magnetic susceptibility studies by Armor et al. on Co–ZM-5 show no evidence for Fe^+ or Co^+ .^{4,19} Our calculations of the energetics for reaction 2a further support the unlikelihood of the occurrence

of this process. The calculated values of for the heat of energy change upon desorption, ΔE_{des} , are 94.9 and 85.6 kcal/mol for Fe and Co, respectively. This energetic penalty is compensated by an entropic gain of approximately of $T\Delta S^\circ = +25$ kcal/mol at 723 K, but even so the overall energetics for reaction 2a are prohibitive.

Figures 3 and 4 show the reaction profiles for reactions 3 and 4 occurring on Fe–ZSM-5 and Co–ZSM-5, respectively. The energy of nitrous oxide adsorption, ΔE_{ads} , is -4.9 and -5.2 kcal/mol for Fe–ZSM-5 and Co–ZSM-5, respectively. The corresponding values of enthalpy of adsorption, ΔH_{ads} , are -5.5 and -5.8 kcal/mol at 298 K. These values are comparable to those reported for reaction 1. The activation energy for N_2O dissociation, E_{act} , corrected for zero-point energy, is 44.6 kcal/mol for Fe–ZSM-5 and 40.2 kcal/mol for Co–ZSM-5.

The desorption of O_2 from $Z^-[\text{MO}(\text{O}_2)]^+$ occurs via reaction 5. The energy of reaction for this process of is 51.9 kcal/mol for $Z^-[\text{FeO}(\text{O}_2)]^+$ and 52.8 kcal/mol for $Z^-[\text{CoO}(\text{O}_2)]^+$ – roughly half that computed for reaction 2a. When one takes in to account the entropy gained upon the desorption of O_2 , the contribution of entropy to the free energy of desorption is $T\Delta S^\circ = +25$ kcal/mol at 723 K. As a consequence, the free energy

change for reaction 5 lies in a range, which makes it a plausible candidate for the release of O₂.

In the preceding discussion, a valence of -1 has been assigned to the zeolite framework and a valence of $+1$ to the charge-compensating group, e.g., [FeO]⁺, [FeO₂]⁺. Such use of valence is merely a convenience because it is known that zeolites are soft bases and that covalent as well as ionic bonding is involved in the binding of the charge-compensating cation. For example, when protons are the charge-compensating cation, the charge on the Brønsted acid proton has been estimated to be $+0.3$, rather than $+1$. In the present study, we have performed a Mulliken Population Analysis for the structures given in Figures 1(a), 1(d), and 3(a).⁴¹ The Mulliken Charges associated with [FeO_x] are $+0.27$, $+0.29$, and $+0.22$ for $x = 1, 2$, and 3 , respectively. The corresponding charges on Fe were computed to be $+0.68$, $+0.75$, and $+0.98$ for $x = 1, 2$, and 3 , respectively. These results indicate that the charge on Fe increases with increasing number of O ligands, but does not reach or exceed the maximum valence of Fe, $+3$.

The apparent rate coefficient for nitrous oxide dissociation can be determined from the sequence of reactions 1–5. The overall rate of N₂O dissociation is given by the sum of the rates of reactions 2 and 4

$$-r_{\text{N}_2\text{O}} = r_{\text{N}_2} = k_2[\text{Z}^-\text{[MO]}^+(\text{N}_2\text{O})] + k_4[\text{Z}^-\text{[MO}_2\text{]}^+(\text{N}_2\text{O})] \quad (6)$$

If we assume steps 1 and 3 are quasi-equilibrated because of the weak binding of N₂O, we can write

$$[\text{Z}^-\text{[MO]}^+(\text{N}_2\text{O})] = K_1[\text{N}_2\text{O}][\text{Z}^-\text{[MO]}^+] \quad (7)$$

$$[\text{Z}^-\text{[MO}_2\text{]}^+(\text{N}_2\text{O})] = K_3[\text{Z}^-\text{[MO}_2\text{]}^+][\text{N}_2\text{O}] \quad (8)$$

$$r_{\text{N}_2} = k_2K_1[\text{Z}^-\text{[MO]}^+][\text{N}_2\text{O}] + k_4K_3[\text{Z}^-\text{[MO}_2\text{]}^+][\text{N}_2\text{O}] \quad (9)$$

The site balance on the active centers is given by

$$[\text{Z}^-\text{[MO]}^+]_0 = [\text{Z}^-\text{[MO]}^+] + [\text{Z}^-\text{[MO}_2\text{]}^+] + [\text{Z}^-\text{[MO(O}_2\text{)]}^+] \quad (10)$$

If we assume that $\text{Z}^-\text{[MO]}^+$ and $\text{Z}^-\text{[MO}_2\text{]}^+$ are the most abundant surface species, the site balance can be rewritten in terms of surface coverage

$$1 = \theta_{\text{MO}} + \theta_{\text{MO}_2} \quad (11)$$

where $\theta_{\text{MO}} = [\text{Z}^-\text{[MO]}^+]/[\text{Z}^-\text{[MO]}^+]_0$ and $\theta_{\text{MO}_2} = [\text{Z}^-\text{[MO}_2\text{]}^+]/[\text{Z}^-\text{[MO]}^+]_0$. Because reaction 4 has the higher activation energy, we assume that it is rate-limiting

$$r_2 = r_4 \quad (12)$$

$$k_2[\text{Z}^-\text{[MO]}^+(\text{N}_2\text{O})] = k_4[\text{Z}^-\text{[MO}_2\text{]}^+(\text{N}_2\text{O})]$$

$$k_2K_1[\text{Z}^-\text{[MO]}^+] = k_4K_3[\text{Z}^-\text{[MO}_2\text{]}^+]$$

Rewriting our expression in terms of the surface coverage

$$k_2K_1\theta_{\text{MO}} = k_4K_3(1 - \theta_{\text{MO}}) \quad (13)$$

$$\theta_{\text{MO}} = K'/(1 + K') \quad (14)$$

where $K' = k_4K_3/(k_2K_1)$. Because $E_2 < E_4$ we assert that $k_2 \gg$

TABLE 2: Calculated Rate Parameters for N₂O Dissociation over M-ZSM-5

sample [ref]	Fe/Al (Si/Al)	Fe wt %	E_{app} , kcal/mol	k_0 , s ⁻¹ (Pa N ₂ O) ⁻¹
Fe-ZSM-5			39.4	4×10^7
Co-ZSM-5			34.6	7×10^7
Fe-ZSM-5 [32]	0.01 (25)	0.17	42.4	8.1×10^7
Fe-ZSM-5 [32]	0.17 (25)	0.57	42.1	1.8×10^8
Fe-ZSM-5 [32]	0.33 (25)	1.11	42.3	3.0×10^9
Fe-ZSM-5 [5]	0.033 (50)	0.056	35 ± 4	3.1×10^7
Fe-ZSM-5 [5]	0.21 (50)	0.35	37 ± 1.5	1.0×10^8

k_4 and $K_3 \approx K_4$. Hence, $K' \ll 1$ and

$$\theta_{\text{MO}} = 0 \quad (15)$$

Thus, the overall rate of nitrous oxide dissociation can be written as

$$-r_{\text{N}_2\text{O}} = 2k_4K_3[\text{Z}^-\text{[MO}_2\text{]}^+][\text{N}_2\text{O}]$$

$$-r_{\text{N}_2\text{O}} = k_{\text{app}}[\text{N}_2\text{O}] \quad (16)$$

where $k_{\text{app}} = 2k_4K_3[\text{Z}^-\text{[MO}_2\text{]}^+]$. The form of this rate expression is in good agreement with that found experimentally for Fe-ZSM-5.³³

On the basis of the proposed mechanism, the experimental result that can be compared to the apparent activation energy, E_{app} , defined in two limiting cases

$$E_{\text{app}} = E_2 + \Delta H_1, \text{ if } \theta_{\text{MO}} \approx 1 \quad (17)$$

$$E_{\text{app}} = E_4 + \Delta H_3, \text{ if } \theta_{\text{MO}} \approx 0 \quad (18)$$

Given the very high heat of desorption for O₂ from $\text{Z}^-\text{[Fe(O)}_2\text{]}^+$, it can reasonably be assumed that $\theta_{\text{MO}} = 0$. From these considerations, $E_{\text{app}} = 39.4$ kcal/mol for Fe-ZSM-5 and $E_{\text{app}} = 34.6$ kcal/mol.

Table 2 compares the calculated value of the apparent activation energy for N₂O decomposition over Fe-ZSM-5 with those measured experimentally. Very good agreement is observed with the values of E_{app} reported recently by Wood et al.³³ The values of E_{app} reported by Panov and co-workers are somewhat lower.⁵ In the case of Co-ZSM-5, the calculated value of E_{app} is significantly higher than the value of 26.4 kcal/mol reported experimentally by Kapteijn et al.¹ However, in agreement with experimental observation the apparent activation energy is lower for Co-ZSM-5 than for Fe-ZSM-5.

The magnitude of the preexponential factor for the decomposition of N₂O was estimated, assuming that the transition state for reaction 4 involves a species that is mobile in two dimensions and has one degree of rotational freedom.⁴² For this calculation the concentration of Fe atoms on the surface of the zeolite pores is estimated in the following manner. The area occupied by an O atom in the pore is taken as 0.04 nm², which leads to an O-atom concentration of 2.5×10^{15} O/cm². The ratio of Fe to O can be determined from the values of the ratios of Si/Al, O/Si, and Fe/Al, which are taken to be 25, 2, and 0.1–0.5, respectively. Thus, Fe/O is 2×10^{-3} – 10^{-2} and the surface concentration of active sites is 5×10^{12} – 2.5×10^{13} Fe/cm². The contributions of vibrations to the partition functions in the reactant and transition states for reaction 4 were determined from our quantum calculations. As seen in Table 2, the apparent first-order rate coefficient is estimated to be 4×10^7 s⁻¹ Pa⁻¹ for an assumed Fe/Al ratio of 0.5. Similar calculations for Co-ZSM-5 give a value of 7×10^7 s⁻¹ Pa⁻¹. Variations in the computed

modes between Fe— and Co—ZSM-5 account for the difference in the two values. Table 2 also shows that the preexponential factor calculated for Fe—ZSM-5 is one to two orders of magnitude smaller than that determined from experimentally.

Upon the basis of the results presented in Table 2, the activity of Co—ZSM-5 is expected to be higher than that of Fe—ZSM-5 because the preexponential factor for Co—ZSM-5 is higher and the activation factor for this catalyst is lower. At a temperature of 723 K, which is typical of N₂O decomposition over both catalysts, the ratio of activities predicted is 33. This figure can be compared with the experimentally observed value of 88.⁴

Conclusions

An analysis of the reaction pathway for N₂O decomposition on Fe—ZSM-5 and Co—ZSM-5 suggests that metal oxo cations ([FeO]⁺ and [CoO]⁺) can serve as active centers. For both metals, the active center is transformed into [MO₂]⁺, a species that has characteristics intermediate between those of a metal superoxo and peroxo species. The apparent activation energy for N₂O decomposition is calculated to be 39.4 kcal/mol for Fe—ZSM-5, which agrees well with experimental measurements. The apparent activation energy for Co—ZSM-5 is 34.6 kcal/mol. This figure is higher than that reported experimentally. The preexponential factor for the apparent first-order rate coefficient for N₂O decomposition is estimated to be $4 \times 10^7 \text{ s}^{-1} \text{ Pa}^{-1}$ for Fe—ZSM-5 and $7 \times 10^7 \text{ s}^{-1} \text{ Pa}^{-1}$ for Co—ZSM-5. In both cases, M/Al = 0.5. Consistent with experimental observation, the rate of N₂O decomposition is predicted to be more rapid on Co—ZSM-5 than Fe—ZSM-5. This conclusion is a direct consequence of the lower activation energy and higher preexponential factor for N₂O decomposition over Co—ZSM-5.

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