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## Hydration of Kr(aq) in Dilute and Concentrated Solutions

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Molecular dynamics simulations of water with both multi-Kr and single Kr atomic solutes are carried out to implement quasi-chemical theory evaluation of the hydration free energy of Kr(aq). This approach obtains free energy differences reflecting Kr-Kr interactions at higher concentrations. Those differences are negative changes in hydration free energies with increasing concentrations at constant pressure. The changes are due to a slight reduction of packing contributions in the higher concentration case. The observed Kr-Kr distributions, analyzed with the extrapolation procedure of Krüger, et al., yield a modestly attractive osmotic second virial coefficient,  $B_2 \approx -60 \text{ cm}^3/\text{mol}$ . The thermodynamic analysis interconnecting these two approaches shows that they are closely consistent with each other, providing support for both approaches.

Keywords: hydrophobic interactions, quasi-chemical theory, osmotic second virial coefficient

## I. INTRODUCTION

#### II. COMPUTATIONAL METHODS

Here we analyze the hydration of the classic hydrophobic solute krypton (Kr) in liquid water solution, including at elevated concentrations that permit Kr-Kr encounters to be assessed. Kr(aq) is specifically interesting for several reasons. Firstly, Kr is isoelectronic with Rb<sup>+</sup>, which has been analyzed in detail.<sup>1</sup> Secondly, Kr(aq) has been a target of sophisticated experimental structural work.<sup>2,3</sup> Finally, Kr(aq) has been the focus of intense theoretical attention,<sup>4–7</sup> but the statistical mechanical theory has become much more sophisticated in recent years.<sup>8</sup>

Here, we use molecular dynamics simulations to study Kr(aq) solutes utilizing quasi-chemical theory.  $^{9-11}$  This theory rigorously decomposes the free energy of hydration into packing, outer-shell and chemical components, is independent of van der Waals assumptions, and thus physically clarifies the hydrophobic solubility of Kr in water. Recent theoretical work has returned to the basic problem of evaluating the osmotic second virial coefficients,  $B_2$ , for simple hydrophobic solutes in water.  $^{12,13}$  We use the new statistical thermodynamic results here to reanalyze that important problem.

The next section specifies the technical data for the simulations carried out here. Succeeding sections lay out the quasi-chemical theory employed, then present results and discussion.

The structural properties of interest are computed using the GROMACS molecular dynamics simulation package. <sup>14</sup> Simulations were carried out in the isothermal-isobaric (NpT) ensemble at T=300 K and p=1 atm. The simulation cell was a cube, and standard periodic boundary conditions were used to mimic bulk solution.

A single Kr atom and 16 Kr in water were simulated separately to study the effects of solute concentration. The mole fraction of 1 Kr in 1000 water molecules is comparable to concentrations used in experimental hydration free energy studies;<sup>5</sup> the higher concentration case is likely a supersaturated solution, but that did not lead to problematic behavior. After energy minimization and 1 ns of volume equilibration, the simulations were extended to 20 ns of production run. Bonds involving hydrogens were fixed by the LINCS algorithm. <sup>15</sup> The equations of motions were integrated using a time step of 1 fs. Temperature and pressure were maintained using a Nose-Hoover<sup>16</sup> thermostat and a Parinello-Rahman<sup>17</sup> barostat. Interactions between water molecules were described by the SPC/E model. 18 The Kr atoms were treated as Lennard-Jones (LJ) spheres with parameters  $\sigma_{\rm KrKr} = 3.935 \text{ Å} \text{ and } \epsilon_{\rm KrKr} = 0.4342 \text{ kcal/mol.}^{19} \text{ For}$ KrO interactions, the mixing rules of the OPLS forcefield were followed. 14 Configurations were sampled every

## III. THEORY

The hydration free energy of Kr(aq) was computed using quasi-chemical theory (QCT), 20,21

$$\beta \mu_{\mathrm{Kr}}^{(\mathrm{ex})} \left( \rho_{\mathrm{Kr}}, p, T \right) = -\ln p^{(0)} (n_{\lambda} = 0)$$
$$+ \ln \langle e^{\beta \varepsilon} \mid n_{\lambda} = 0 \rangle + \ln p(n_{\lambda} = 0) . \quad (1)$$

This equation involves packing, outer-shell and chemical contributions on the right-hand side. Those contributions are discussed further below. Eq. (1) has been used to study hydration free energies of water,  $^{22-24}$  CH<sub>4</sub>,  $^{25}$  CF<sub>4</sub>/C(CH<sub>3</sub>)<sub>4</sub>,  $^8$ , hydrogen  $^{26}$  and carbon dioxide.  $^{27}$  We evaluate the free energy contributions numerically by analyzing simulation trajectories.

Recognizing  $p^{(0)}(n_{\lambda}=0)$  as the probability of finding an empty inner shell at an arbitrary point in the fluid, the term  $-\ln p^{(0)}(n_{\lambda}=0)$  assesses the free energy required to form the corresponding cavity. This packing contribution was estimated by random placement of 30,000 spheres of radius  $\lambda$ , scoring the fraction of those placements conforming to the 'vacant' event.

The middle term represents interactions of outer-shell solvent molecules with a solute in a vacant inner shell. This outer-shell contribution is approximated as

$$\begin{split} \ln \langle e^{\beta \varepsilon} \mid n_{\lambda} = 0 \rangle &\approx \beta \langle \varepsilon \mid n_{\lambda} = 0 \rangle \\ &+ \beta^2 \langle \delta \varepsilon^2 \mid n_{\lambda} = 0 \rangle / 2 \; . \end{split} \tag{2}$$

This is the important simplification of quasi-chemical theory that the construction of Eq. (1) is designed to achieve. With this ingredient, quasi-chemical theory is seen to be a generalization of the van der Waals picture of liquids.<sup>21,28</sup> This gaussian approximation has been well-tested for the substantial list of applications noted,<sup>8,22–27</sup> and including electrolyte solutions.<sup>29</sup>

The right-most term of Eq. (1) is the 'chemical' contribution to the hydration free energy. It can also be recognized as the free energy regained with relaxation of the constraint associated with the successful formation of a cavity at the initial step.<sup>21</sup> This contribution is estimated directly by observing Kr atoms present in the simulation.

The individual contributions of Eq. (1) depend on  $\lambda$ , which sets the boundary between inner- and outer-shell solvent molecules. The excess chemical potential,  $\mu_{\rm Kr}^{(\rm ex)}$ , should be independent of that boundary. Here, we evaluate  $\mu_{\rm Kr}^{(\rm ex)}$  for a range of  $\lambda$  covering as much structural data as statistically feasible.

## IV. RESULTS AND DISCUSSION

Characterizing the solution structure around the Kr atoms, FIG. 1 shows several radial distribution functions. Both KrO and KrH distributions display a principal maximum at about 3.7 Å. The water structure,  $g_{\rm OO}\left(r\right)$  (not

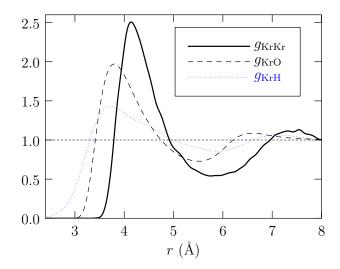


FIG. 1: Radial distribution functions observed for the aqueous Kr solution at elevated concentration,  $n_{\rm Kr}=16$ . The water structure,  $g_{\rm OO}\left(r\right)$  (not shown), is closely similar to that of bulk water.

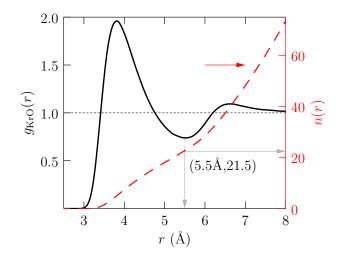


FIG. 2: Higher detail for  $g_{\rm KrO}(r)$  around Kr atoms (for the  $n_{\rm Kr}=16$  case). The red dashed line is the running coordination number n(r), indicating an average O-occupancy of 21.5 for the sphere within the first minimum defined by a first inner-shell radius of  $\lambda=5.5$  Å. The principal minimum is not unusually deep, and outside the principal maximum, the fluid is only weakly structured.

shown), is largely unaffected by the Kr for these calculations. A more exclusive view of the hydration structure (FIG. 2) shows that the average O-occupancy of the sphere within the first minimum for first inner-shell boundary of 5.5 Å is 21.5. The principal minimum is not unusually deep, and outside the principal maximum the fluid is only weakly structured. Neighborship decomposition (FIG. 3) shows that the principal maximum of  $g_{\rm KrO}(r)$  is saturated by fewer than 10 nearest neighbors.

For solutes of van der Waals type generically, the nat-

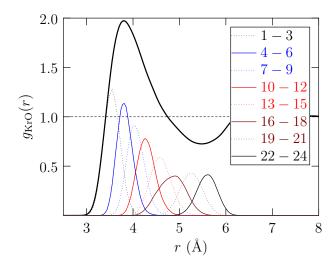


FIG. 3: Neighborship decomposition of the radial distribution  $g_{\rm KrO}(r)$ , from the  $n_{\rm Kr}=1$  case. The maximum is located at  $r\approx 3.8 {\rm \AA}$ . Note that the principal maximum of  $g_{\rm KrO}(r)$  is saturated by fewer than 10 nearest neighbors. See also FIG. 2. Outside the principal maximum, the fluid is only weakly structured.

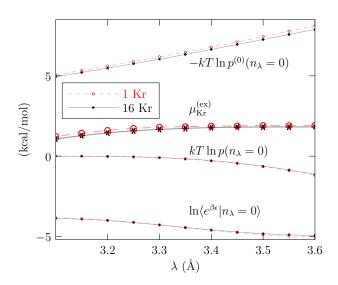


FIG. 4: Packing, chemical and outer-shell contributions to the hydration free energy of Kr were calculated numerically for a range of  $\lambda$ .

ural physical idea is to identify  $\lambda$  with the van der Waals distance of closest approach.<sup>8,25</sup> The individual contributions (FIG. 4) lead to free energies (FIG. 5) that are substantially independent of  $\lambda$ , provided  $\lambda > 3.4$ Å. This displacement is less than the position of the principal

maximum of  $g_{KrO}(r)$  and involves fewer than six (6) water molecules (FIG. 3).

Substituting these directly calculated numerical values for the various QCT contributions into Eq.1, we obtain a net Kr hydration free energy of  $\mu_{\rm Kr}^{ex}=1.8-1.9$  kcal/mol,

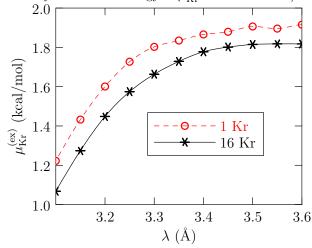


FIG. 5: Evaluations of hydration free energies on the basis of quasi-chemical theory for a range of inner-shell boundaries (3.1Å<  $\lambda$  < 3.6Å) for the two Kr concentrations.  $\mu_{\rm Kr}^{\rm (ex)}$  becomes insensitive to  $\lambda$  for 3.4Å<  $\lambda$  <3.6Å. The experimental value is 1.66 kcal/mol.  $^{30}$ 

in reasonable agreement with the experimental value of  $1.66~\rm kcal/mol.^{30}$  Results for the two simulations, single Kr and multi-Kr, track each other. The multi-Kr results are distinctly lower (FIG. 5). The significant difference derives from the packing contribution.

The correlation function,  $h_{KrKr}(r) = g_{KrKr}(r) - 1$ , observed in the multi-Kr simulation (FIG. 6) provides access to the osmotic second virial coefficient,

$$B_2 = -\frac{1}{2} \lim_{\rho_{\mathrm{Kr} \to 0}} \int h_{\mathrm{KrKr}}(r) \,\mathrm{d}^3 r \ . \tag{3}$$

On the basis of the McMillan-Mayer theory, <sup>29</sup> the integral can be identified thermodynamically as

$$2B_2 = \lim_{\rho_{Kr \to 0}} \left( \frac{\partial \beta \mu_{Kr}^{(ex)}}{\partial \rho_{Kr}} \right)_{T, \mu_W} . \tag{4}$$

The partial derivative requires constancy of the water chemical potential,  $\mu_{\rm W}$ , but the calculations were done at constant pressure. The appropriate thermodynamic consideration of this distinction is

$$2B_2 = \lim_{\rho_{\mathrm{Kr}\to 0}} \left[ \left( \frac{\partial \beta \mu_{\mathrm{Kr}}^{(\mathrm{ex})}}{\partial \rho_{\mathrm{Kr}}} \right)_{T,p} + \left( \frac{\partial \beta \mu_{\mathrm{Kr}}^{(\mathrm{ex})}}{\partial p} \right)_{T,\rho_{\mathrm{Kr}}} \left( \frac{\partial p}{\partial \rho_{\mathrm{Kr}}} \right)_{T,\mu_{\mathrm{W}}} \right] . \tag{5}$$

We note that

$$\lim_{\rho_{\mathrm{Kr}\to 0}} \left( \frac{\partial \beta p}{\partial \rho_{\mathrm{Kr}}} \right)_{T,\mu_{\mathrm{W}}} = \lim_{\rho_{\mathrm{Kr}\to 0}} \left( \frac{\partial}{\partial \rho_{\mathrm{Kr}}} \left[ \beta p_{\mathrm{W}} \left( T, \mu_{\mathrm{W}} \right) + \rho_{\mathrm{Kr}} + O \left( \rho_{\mathrm{Kr}}^2 \right) \right] \right)_{T,\mu_{\mathrm{W}}} = 1 , \tag{6}$$

reflecting ideal osmotic pressure at low concentration. Referring again to Eq. (5), we use the notation

$$v_{\rm Kr}^{\rm (ex)} = \lim_{\rho_{\rm Kr} \to 0} \left( \frac{\partial \mu_{\rm Kr}^{\rm (ex)}}{\partial p} \right)_{T, \rho_{\rm Kr}} \tag{7}$$

for the excess contribution to the partial molar volume of the solute. Combining, we obtain

$$2B_2 = \lim_{\rho_{\mathrm{Kr}\to 0}} \left( \frac{\partial \beta \mu_{\mathrm{Kr}}^{(\mathrm{ex})}}{\partial \rho_{\mathrm{Kr}}} \right)_{T,p} + v_{\mathrm{Kr}}^{(\mathrm{ex})}$$
 (8)

in the infinite dilution limit. For water,  $^{31}$  the ideal contribution to these partial molar volumes is about 1 cm³/mol. For noble gases in water, the partial molar volumes are positive, and  $v_{\rm Kr}^{\rm (ex)}$  is about 33 cm³/mol - 1 cm³/mol = 32 cm³/mol.  $^{32}$  The present simulation results yield a value of  $v_{\rm Kr}^{\rm (ex)} \approx 39~{\rm cm}^{3}/{\rm mol}$ , obtained by direct differencing of average volumes of simulation (at constant pressure) with/without a single Kr atom. Similarly, the leading term on the right-side of Eq. (8) is roughly estimated as  $-160~{\rm cm}^{3}/{\rm mol}$ , using  $\Delta\beta\mu_{\rm Kr}\approx-0.13$  (FIG. 5) and the observed  $\Delta\rho_{\rm Kr}\approx 4.8\times 10^{-4}{\rm \AA}^{-3}$ . The combined right-side of Eq. (8) is then about  $-120~{\rm cm}^{3}/{\rm mol}$ .

Our direct analysis of the correlation function integral (FIG. 7) utilizes the extrapolation procedure advocated by Krüger, et al.  $^{33,34}$  That approach evaluates the mean and variance of Kr occupancy  $(n_{\rm Kr})$  of a sphere of radius R, which is a sub-volume of the simulation cell. That sphere is the basis of a grand canonical ensemble with variable  $n_{\rm Kr}$ . Being tied to a grand canonical construction, the data analysis then corresponds directly to the McMillan-Mayer theory theoretical development, which proceeds through a grand ensemble.  $^{29}$  The formulae derived on that basis

$$-2B_2 = \lim_{R \to \infty} 4\pi \int_0^{2R} h_{KrKr}(r) w(r/2R) r^2 dr , \quad (9)$$

with

$$w(x) = 1 - \left(\frac{3}{2}\right)x + \left(\frac{1}{2}\right)x^3$$
, (10)

are easy to use with conventionally available distribution functions. The 1/2R=0 extrapolated value (FIG. 7)

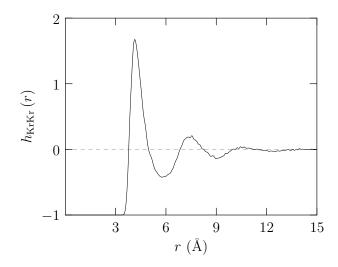


FIG. 6: For the multi-Kr simulation, the Kr-Kr correlation function,  $h_{\rm KrKr}(r) = g_{\rm KrKr}(r) - 1$ , as in FIG. 1, but viewed more globally. Note the accessible r-range. The second- and third-shell structures are distinct, but quantitatively much less structured than the results of Watanabe and Andersen.<sup>4</sup>

agrees precisely with Eq. (8) to the significant figures given there, the net value being  $B_2 \approx -60 \text{ cm}^3/\text{mol}$ . In contrast, we found that direct integration of the distribution functions, or the  $k \to 0$  extrapolation of the spatial Fourier transform, did not provide practical evaluations of  $B_2$ .

## V. CONCLUSION

Though Rb<sup>+</sup> is isoelectronic with Kr, the solution structure is vastly different, and convincing inter-relation of these cases requires serious statistical mechanical theory.<sup>1</sup> Nevertheless,<sup>20</sup> the quasi-chemical approach evaluates the hydration free energy of Kr(aq) successfully, and in physical terms. This approach also obtains free energy differences reflecting Kr-Kr interactions at higher concentrations (FIG. 5). Those differences are negative changes in hydration free energies with increasing concentrations at constant pressure. The changes are due to a slight reduction of unfavorable packing contributions

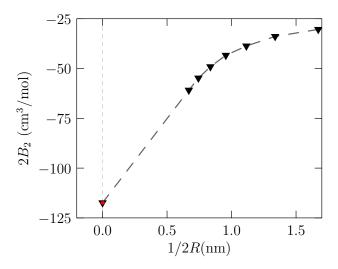


FIG. 7: Extrapolation (Eq. (9)) following Krüger, et al.<sup>33,34</sup> Computed values for 1/2R > 0 were utilized to obtain a least-squares-fit polynomial to quadratic order in 1/2R. The symbol at 1/2R = 0 is the extrapolated value and it agrees precisely with Eq. (8) to the significant figures given there.

in the higher concentration case. The observed Kr-Kr distributions, analyzed with the extrapolation procedure of Krüger, et al.<sup>33,34</sup> (FIG. 7), yield  $B_2 \approx -60 \text{ cm}^3/\text{mol}$ . The thermodynamic analysis interconnecting these two approaches shows that they are closely consistent with each other. This provides support for both approaches.

## VI. ACKNOWLEDGEMENT

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