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# A Pseudoatom in a Cage: Trimetallofullerene $Y_3@C_{80}$ Mimics $Y_3N@C_{80}$ with Nitrogen Substituted by a Pseudoatom

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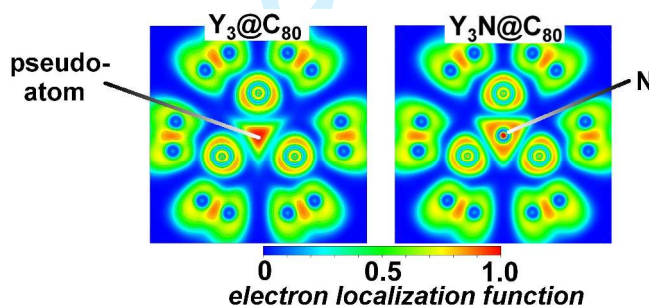
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### Abstract

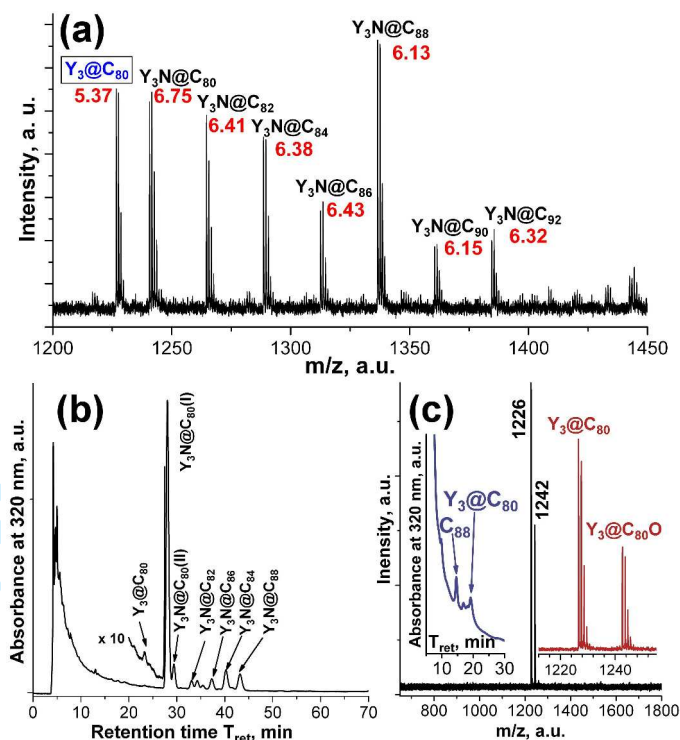
$Y_3C_{80}$  obtained in the synthesis of nitride clusterfullerenes  $Y_3N@C_{2n}$  ( $2n = 80-88$ ) by the reactive atmosphere method is found to be a genuine trimetallofullerene,  $Y_3@C_{80}$ , with low ionization potential and divalent state of yttrium atoms. DFT studies of the electronic structure of  $Y_3@C_{80}$  show that this molecule mimics  $Y_3N@C_{80}$  with the pseudoatom (PA) instead of the nitrogen atom. Topology analysis of the electron density and electron localization function show that yttrium atoms form Y-PA bonds rather than direct Y-Y bonds. Molecular dynamics simulations show that the  $Y_3PA$  cluster is as rigid as  $Y_3N$  and rotates inside the fullerene cage as a single entity.

Keywords: endohedral metallofullerene, non-nuclear attractor, pseudoatom, electron localization function, topological analysis

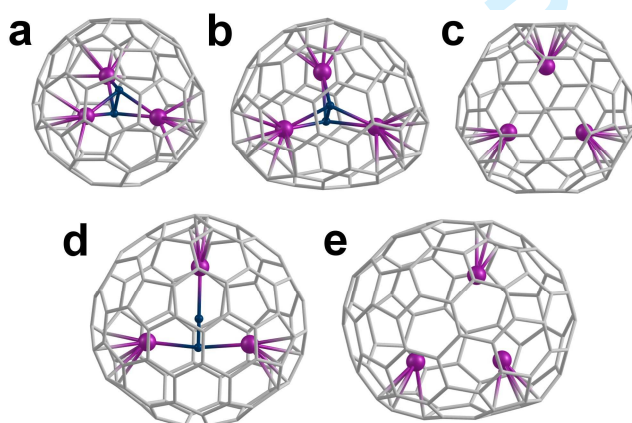
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The class of fullerenes which have atoms, ions or clusters in their inner space is referred to as endohedral fullerenes.<sup>1, 2</sup> Importantly, most of the species found in endohedral fullerenes are unstable in the separate form and can be stabilized only inside the fullerene cage. Encapsulated clusters range in size and can comprise up to the seven atoms (as in  $\text{Sc}_4\text{O}_3@\text{C}_{80}$ <sup>3, 4</sup>). However, the high content of a metal in endohedral metallofullerenes (EMFs) can be achieved only in the form of clusters with non-metals (such as nitrogen in  $\text{M}_3\text{N}@\text{C}_{2n}$ ,<sup>5-13</sup> CH in  $\text{Sc}_3\text{CH}@\text{C}_{80}$ ,<sup>14</sup> carbide unit in  $\text{M}_{2,3}\text{C}_2@\text{C}_{2n}$ ,<sup>15-20</sup> or oxygen in  $\text{Sc}_4\text{O}_{2,3}@\text{C}_{80}$ <sup>3</sup>). Well-characterized conventional EMFs are limited to molecules containing one or two metal atoms. Though a larger number of encapsulated metal atoms has been reported, their characterization is mostly limited to mass-spectrometry data, and there has been no evidence showing that the isolated species with three metal atoms such as  $\text{Er}_3@\text{C}_{74}$ ,<sup>21</sup>  $\text{Tb}_3@\text{C}_{80}$ ,<sup>22</sup> or  $\text{Dy}_3@\text{C}_{98}$ ,<sup>23</sup> are conventional trimetallofullerenes. Moreover, the EMF long thought to be a trimetallofullerene,  $\text{Sc}_3@\text{C}_{82}$ ,<sup>24</sup> has been recently proved to be a carbide clusterfullerene  $\text{Sc}_3\text{C}_2@\text{C}_{80}$ .<sup>18</sup> Thus, the question whether EMFs can encapsulate three metal atoms in the form of the trimetallic cluster, in which metal-metal interactions are not mediated by the non-metal, is still an open matter. In our studies on the synthesis of EMFs by the "reactive gas atmosphere"<sup>8</sup> method we have systematically detected the species  $\text{M}_3@\text{C}_{80}^+$  (M=Y, Dy, Sc) in the positive-mode LDI mass spectra of the raw fullerene extracts (Fig. 1). At the same time, these species were not found in the negative mode, and our efforts to isolate these compounds have not been successful up to date presumably because of the low yield and stability of these species. In this work we describe a tri-yttrium endohedral fullerene and employ DFT calculations to show that  $\text{M}_3\text{C}_{80}$  species are genuine trimetallofullerenes, which have peculiar electronic structure with a non-nuclear maximum of the electron density (also referred to as "pseudoatom").



**Figure 1.** (a) LDI mass spectrum of the raw yttrium-EMF extract. The spectrum is measured in the positive mode, only the range with the most intense peaks is shown; DFT-computed ionization potentials (eV) are listed in red for each compound; (b) HPLC trace of the same extract (two 4.6×250mm Buckyprep columns; flow rate 1.6 ml/min; toluene as eluent; 40°C); (c) mass-spectrum of the fraction collected at 19 min at the Buckyprep-M column (the inset shows Buckyprep-M HPLC trace of the fraction which was collected at 21-27 min using the Buckyprep column).



**Figure 2.** DFT-optimized molecular structures: (a)  $Y_3C_2@C_{78}-D_{3h}(5)$ ; (b)  $Y_3C_2@C_{78}-C_2(22010)$ ; (c)  $Y_3@C_{80}-I_h(7)$ ; (d)  $Y_3C_2@C_{96}-D_2(186)$ ; (e)  $Y_3@C_{98}-C_2(166)$ . Carbon atoms of the fullerene cage are shown in grey, carbons atoms in the carbide units are dark blue, yttrium atoms are violet.

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## Results and Discussion

**Molecular Structure of  $Y_3C_{80}$ .** It has been shown that the carbon cage isomerism in EMFs depends on the number of the electrons formally transferred from the endohedral metal atoms to the cage. A common oxidation state of Y in EMFs is 3+ as in  $Y_3N@C_{80}$  or  $Y_2C_2@C_{82}$ . For  $Y_3@C_{80}$  this would imply the huge number of 9 electrons transferred to the carbon cage as well as strong Coulomb repulsion between the endohedral Y atoms in the trimetallic cluster not mediated by the negatively charged nitride or carbide species. Hence, we suggest that the 3+ state of Y in  $Y_3C_{80}$  can be realized only in the carbide cluster,  $Y_3C_2$ , with  $Y_3C_2@C_{78}$  as the structural model for  $Y_3C_{80}$ . Note that the Y-based carbide clusterfullerene,  $Y_2C_2@C_{82}$ , is one of the most abundant products in the synthesis of Y-based EMFs, while the  $Y_3C_2$  can be obtained in a separate form.<sup>25</sup> As possible cage isomers of  $Y_3C_2@C_{78}$  we have considered two lowest energy isomers of  $C_{78}^{6-}$ ,  $D_{3h}(5)$  and  $C_2(22010)$  (Fig. 2).<sup>26</sup> Alternatively, Y can adopt the formal 2+ oxidation state as in  $Y_2@C_{82}$ ,<sup>20</sup> in which we have recently found the covalent Y–Y bond.<sup>27</sup> The  $(Y^{2+})_3$  cluster donates 6 electrons to the cage, and the most probable cage isomer is hence  $I_h(7)$  as in all other EMFs with a  $C_{80}$  cage.<sup>7, 28</sup> Kobayashi et al. has shown that if a  $Sc_3$  cluster might be encapsulated in the  $C_{82}$  carbon cage, then Sc atoms would adopt the 2+ oxidation state in  $Sc_3@C_{82}$ .<sup>29</sup>

DFT calculations at the PBE/TZ2P level have shown that  $Y_3@C_{80}-I_h(7)$  is by 287 and 431 kJ/mol more stable than  $Y_3C_2@C_{78}-C_2(22010)$  and  $Y_3C_2@C_{78}-D_{3h}(5)$  isomers, respectively. Thus, DFT shows that the lowest energy form of  $Y_3@C_{80}$  is the genuine trimetallofullerene; an analogous structure can be also proposed for  $Tb_3@C_{80}$  described in ref. 22. In  $Y_3@C_{80}$ , three Y atoms are coordinated to the centers of hexagons and form a symmetric triangle with the Y–Y distance of 3.562 Å, (compare to 3.656 Å in  $Y_2@C_{82}$ , 3.934 Å in  $Y_2@C_{79}N$ , and 3.566 Å in  $Y_3N@C_{80}$  computed at the same level of theory). Y–C distances in the Y-coordinated hexagon span the range of 2.415–2.429 Å.

DFT calculations also showed that the high intensity of the  $Y_3@C_{80}^+$  species in the positive-mode mass-spectra of the raw Y-fullerene extracts can be explained by the small ionization potential (IP) of

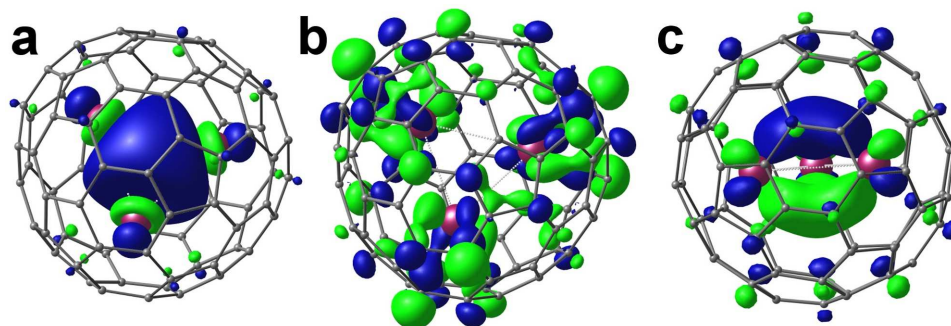


$Y_3@C_{80}$ , 5.37 eV, as compared to 6.1–6.8 eV for  $Y_3N@C_{2n}$  ( $2n = 78–92$ ) (IPs are computed as the energy difference between PBE/TZ2P optimized structures of the neutral and cationic forms). Note that in the  $Y_3N@C_{2n}$  family, the lowest ionization potential is predicted for  $Y_3N@C_{88}$ , which therefore exhibits the highest intensity in the positive mode mass spectra (while the most abundant product according to HPLC is  $Y_3N@C_{80}$ ). This prediction agrees with cyclic voltammetry studies of  $M_3N@C_{2n}$  clusterfullerenes ( $M = Gd, Pr, Nd$ ,  $2n = 80, 84, 86, 88$ ) which showed that  $M_3N@C_{88}$  has the lowest oxidation potentials.<sup>30, 31</sup> The fact that the predicted ionization potential of  $Y_3@C_{80}$  is substantially smaller even than the value for  $Y_3N@C_{88}$  indicates that the actual yield of  $Y_3@C_{80}$  is quite low. Besides, the ease of its oxidation is probably the main reason why the current attempts to isolate these species in considerable amounts have not been successful. Indeed, we have found that  $Y_3@C_{80}$  dominates in the fraction eluted at 19 min in Buckyprep-M column (Fig. 1b,c), however in the mass spectrum of this fraction the signal of  $Y_3@C_{80}$  is accompanied by the large signal of the oxide,  $Y_3@C_{80}O$ , which was formed during the work-up procedures. Interestingly, PBE/TZ2P-computed electron affinity (EA) of  $Y_3@C_{80}$ , 2.61 eV, is very close to the value predicted at the same level of theory for  $Y_3N@C_{80}$  (2.56 eV). Comparably low EA value of  $Y_3@C_{80}$  is quite remarkable for the paramagnetic endohedral metallofullerene (for comparison, PBE/TZ2P EA of  $Y@C_{82}$  is 3.64 eV). PBE/TZ2P EA values for the series of  $Y_3N@C_{2n}$  ( $2n = 78–92$ ) molecules are also found in the range of 2.34–2.65 eV. Comparison to the IP and EA values for the experimentally available isomers of higher fullerenes  $C_{76}–C_{84}$  shows that both IP and EA values of  $M_3N@C_{2n}$  molecules are considerably lower than those of the empty fullerenes (see Table S1 in Supporting Information for more details); specifically, for EAs, the difference is in the order of 0.8 eV. As a result, mass-spectrometric measurements of nitride clusterfullerene samples are seriously complicated even by the trace amounts of the empty fullerenes; at the same time, such problems are not encountered for in the positive ion mode.

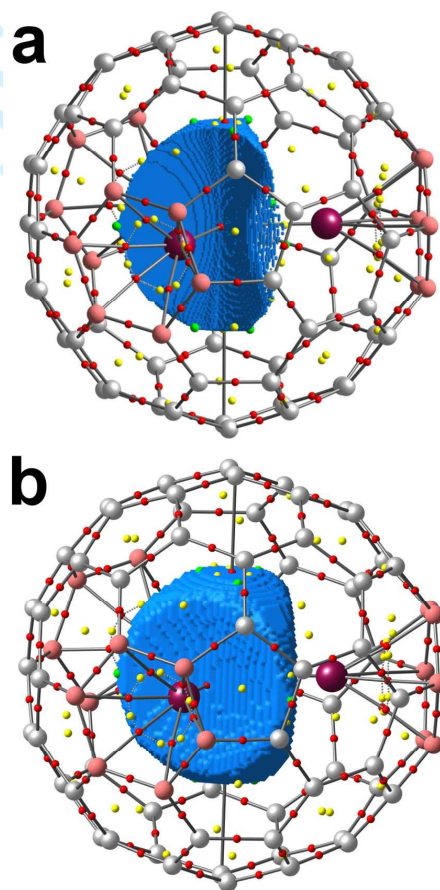
It should be noted that formation of  $Y_3@C_{80}$  is somehow facilitated in the "reactive gas atmosphere" method, while these species were not observed when  $N_2$  gas was used as the source of nitrogen.<sup>32</sup> At the

1 same time, the  $Y_2@C_{79}N$  reported by Dorn and co-workers<sup>32, 33</sup> was not formed in noticeable amounts  
2 under our conditions.  
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5 In the view of the recent isolation of  $Dy_3@C_{98}$ ,<sup>23</sup> we have also studied the possible isomers of  
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7  $Y_3C_2@C_{96}$  and  $Y_3@C_{98}$ . For each fullerene, ten lowest energy  $C_{2n}^{6-}$  cage isomers were considered,<sup>34</sup>  
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9 and for each cage isomer two-three conformers (different in the orientation of the internal cluster with  
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11 respect to the cage) were computed. These calculations have shown that the most stable structures of  
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13  $Y_3C_2@C_{96}$  and  $Y_3@C_{98}$  are based on the  $C_{96}-D_2(186)$  and  $C_{98}-C_2(166)$  cage isomers, respectively, and  
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15 that the former is by 50 kJ/mol lower in energy. This energy difference is not so large to definitively  
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17 rule out conventional trimetallic EMFs  $M_3@C_{98}$ , but formation of the carbide clusterfullerenes  
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19  $M_3C_2@C_{96}$  appears to be more likely in this case.  
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**Figure 3.** Molecular orbitals of  $Y_3@C_{80}$ : (a) HOMO; (b) SOMO; (c) LUMO+2 (this orbital resembles  $p_z$ -like orbital of the pseudoatom).



**Figure 4.** Molecular graphs of  $Y_3@C_{80}$  (a) and  $Y_3N@C_{80}$  (b). Yttrium atoms are violet, carbon atoms are gray or pink (if bonded to Y); bond, ring, and cage critical points are red, yellow, and green, respectively. Bader volumes of the non-nuclear attractor in  $Y_3@C_{80}$  and the nitrogen atom in  $Y_3N@C_{80}$  are shown in blue.

**Electronic structure of  $Y_3@C_{80}$ .** Since Y atoms in  $Y_3@C_{80}$  are in the formal +2 oxidation state, a complex Y–Y bonding situation can be expected in this molecule. Fig. 3a,b shows HOMO and SOMO orbitals of  $Y_3@C_{80}$ . The highest two-fold occupied orbital is totally symmetric and is predominantly formed by the combination of 5s atomic orbitals of Y atoms. Similar orbitals are known for metal clusters and their description as "interstitial" orbitals was given by Goddard et al.<sup>35</sup> SOMO of  $Y_3@C_{80}$  is mainly localized on the cage, the Y contribution being relatively small.

Further details of the bonding in  $Y_3@C_{80}$  are obtained from the topological analysis of the electronic density using quantum theory of atoms-in-molecule<sup>36</sup> (QTAIM) and electron localization function<sup>37–39</sup> (ELF) approaches. A molecular graph of  $Y_3@C_{80}$  is shown in Fig. 4a. According to QTAIM, each Y atom bears the charge of +1.35 (the same value is found in  $Y_2@C_{82}$ <sup>27</sup>) and exhibits six bond-paths to the carbon atoms of the nearest hexagon. The  $\delta(Y,C)$  delocalization indices (i.e. Y–C bond orders) for the Y coordinated hexagon span the range of 0.18–0.21. Y–cage bonding pattern in  $Y_3@C_{80}$  is similar to that found in  $Y_3N@C_{80}$  (Fig. 4b), which also exhibits six bond paths to the carbon cage for each Y atom. However, the charge of the Y atom in  $Y_3N@C_{80}$  is significantly larger (+1.90), while  $\delta(Y,C)$  delocalization indices are smaller (0.15–0.17). The total number of the electron pairs shared between each Y atom and the cage,  $\delta(Y, \text{cage})$ , is 2.46 (compare to 2.35 in  $Y_2@C_{82}$  or 1.77 in  $Y_3N@C_{80}$ ).

The similarity of the  $Y_3@C_{80}$  and  $Y_3N@C_{80}$  is further emphasized when the intra-cluster bonding is analyzed. Surprisingly, we have not found an evidence for direct Y–Y bonds in  $Y_3@C_{80}$ . Instead, the non-nuclear attractor (NNA, i.e. the maximum of the electron density also referred to as "pseudoatom") is found in the center of the molecule, and each Y atom forms a bond path to the NNA. Thus, the NNA in  $Y_3@C_{80}$  mimics the nitrogen atom, and the bonding in the  $Y_3$  cluster is similar to that in  $Y_3N$ . In fact, molecular graphs of  $Y_3@C_{80}$  and  $Y_3N@C_{80}$  are completely isomorphic (i.e., they exhibit the same number and similar location of critical points, including the presence of BCPs between N or NNA and the cage carbon atom as well as multiple ring and cage critical points, see Fig. 4). A pseudoatomic nature of the NNA can be also emphasized by the analysis of the molecular orbitals. The interstitial

orbital (Fig. 3a) can be understood as an s-like orbital of the pseudoatom (it is the only double-occupied orbital of the pseudoatom). Besides, we have also found a  $p_z$ -like orbital of the pseudoatom (Fig. 3c) among the low-energy vacant orbitals of  $Y_3@C_{80}$ . However, there is certainly no quantitative correspondence between NNA and the nitrogen, since the charge of NNA is only  $-0.19$  ( $-0.24$  if cc-pVTZ basis set is used for Y), while the charge of N in  $Y_3N@C_{80}$  is  $-1.83$ . Besides, the Y–NNA bond critical points (BCPs) are located very close to the NNA, while the Y–N BCPs are approximately between the atoms. The Bader volume of NNA is also much smaller (Fig. 4) than that of the nitrogen. Therefore, the NNA can be considered as a weakly charged "soft and small" ion. Finally, in spite of the absence of Y–Y bond-paths,  $\delta(Y,Y)$  indices in  $Y_3@C_{80}$  are rather large,  $0.29$ , while  $\delta(Y,NNA)$  values are relatively small,  $0.08$ , which is not surprising taking into account small volume and electron population of the NNA. In  $Y_3N@C_{80}$ ,  $\delta(Y,Y)$  indices are negligible ( $0.02$ ), while  $\delta(Y,N)$  indices are  $0.72$ . The topology of the electron density in  $Y_3@C_{80}$  is only slightly altered by the removal of one electron. In the  $Y_3@C_{80}^+$ , Bader charge of Y atoms is increased to  $+1.45$ , while the  $\delta(Y, cage)$  index is  $2.37$ . NNA population,  $-0.160$ , and  $\delta(Y,NNA)$  and  $\delta(Y,Y)$  values,  $0.08$  and  $0.29$ , respectively, are almost identical to those in the neutral  $Y_3@C_{80}$  molecule.

Pendas *et al.* have shown that the formation of NNA is possible at certain interatomic distances for almost all dimers of the first three periods.<sup>40</sup> However, for most elements equilibrium distances are usually larger than those, at which NNA are formed. The notable exception is Li, and NNAs are typical for Li clusters<sup>41</sup>; for other alkaline metals, the equilibrium distances can be close to the values at which NNAs can exist, and their formation can be achieved at an increased pressure. In general, it was shown that the formation of NNA is more likely for the light elements, while for the heavier elements equilibrium interatomic distances are usually much larger than those at which NNAs can be formed.<sup>40</sup> To our knowledge, the possibility of NNA has been discussed neither for such heavy elements as yttrium nor for fullerenes. At the same time we should note that NNA was not found in  $Y_2@C_{82}$  even when the Y–Y distance is reduced to  $2.456 \text{ \AA}$  (*viz.* equilibrium distance of  $3.656 \text{ \AA}$ ). Thus, formation of

NNAs appears to be more probable in polyatomic clusters. Our analysis shows a clear relationship between the presence of interstitial orbital and NNA, and hence NNAs can be probably found in many other metal clusters in which this option has not been considered yet.

Recently, with the use of scanning tunneling microscopy and plane-wave DFT calculations, Petek and coworkers discovered highly delocalized atom-like orbitals in  $C_{60}$  (referred to by the authors as "superatom" molecular orbitals, SAMOs).<sup>42, 43</sup> The authors have shown that the origin of such orbitals is the exchange-correlation potential of spherical  $C_{60}$  molecule and hence analogous orbitals can be expected for spherical molecules of other types. The authors have also found that while in  $C_{60}$  such orbitals lay more than 3 eV above the LUMO, they can be stabilized by doping the fullerene with the metal atoms, especially those with high ionization potentials. In  $Cu@C_{60}$ , SAMO orbital was found to be occupied. However, with stabilization of SAMOs, they have been also becoming more localized in the inner part of the carbon cage, loosing their diffuse nature. One can find clear parallels between SAMOs and interstitial orbitals, discovered by Goddard *et al.* for the metal clusters.<sup>35, 44</sup> This can be especially well seen for the tetrahedral metal clusters, in which s-like orbital localized at the center of the cluster is formed from the linear combinations of the atomic s-orbitals. We have already mentioned that the HOMO of  $Y_3@C_{80}$  resembles interstitial orbital of the  $Y_3$  cluster. Following the results of Petek *et al.*,<sup>43</sup> one can expect that SAMOs of the carbon cage should be also affected by the  $Y_3$  cluster. Moreover, it is natural to expect that the s-type SAMO of the cage can hybridize with the cluster orbitals. At the same type, low symmetry of the cluster should also break the cage symmetry hence affecting the SAMOs and probably causing their mixing with the atom-localized orbitals. Since SAMOs cannot be fully revealed in the atomic-centered basis set, we have performed additional calculations of  $Y_3@C_{80}$  molecule using plane-wave basis set. First, we have ensured that the method of theory and the code used in this work reproduce SAMOs found by Petek *et al.*<sup>42, 43</sup> in  $C_{60}$ . In close agreement with the data from Ref. <sup>42</sup>, the s-type SAMO was found 3.25 eV above the LUMO, followed by the p-type SAMOs at 3.88 eV above the LUMO. Calculations for the  $Y_3@C_{80}$  revealed that the atom-localized



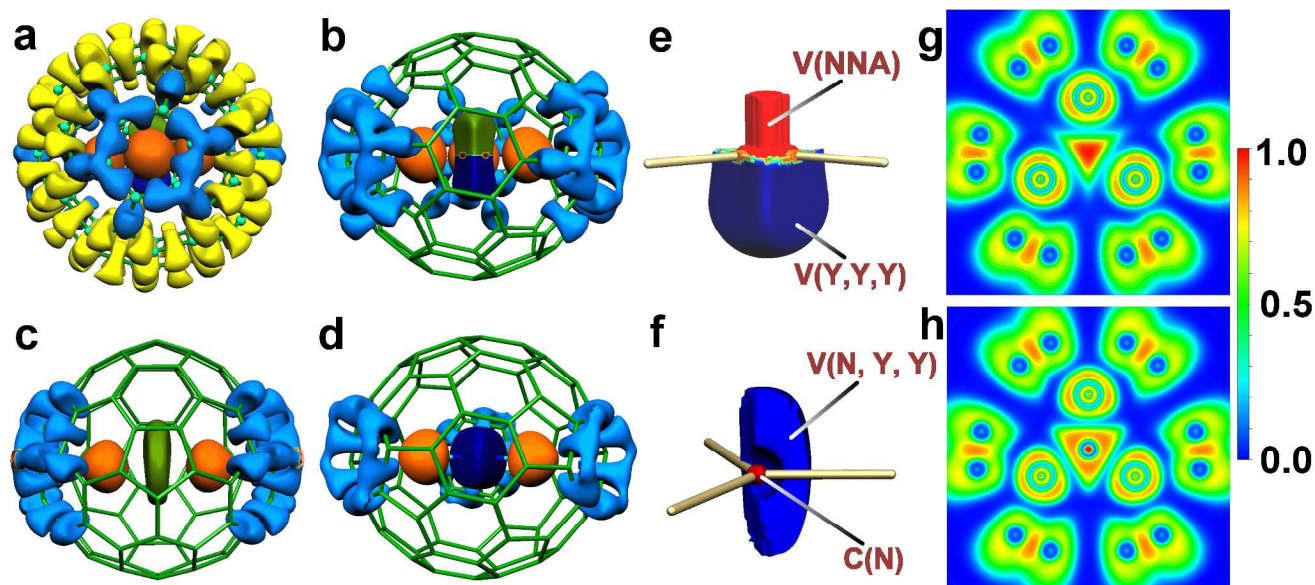
basis set reliably describes the orbitals shown in Fig. 1a and b, and that no new MO states are found in the energy range of the frontier orbitals. The SAMO contribution to the LUMO of  $Y_3@C_{80}$  can be seen when the orbital is plotted with low isovalues, but it is clear that, just like in the case of  $Cu@C_{60}$ , this orbital is mostly constrained to be inside the carbon cage (hence atomic basis set is sufficient for its correct description). We have found some orbitals with the SAMO contribution in the range of 0–3 eV above the LUMO, but in all of them the contribution of the metal-localized orbitals or the  $\pi$ -type cage contribution are dominating. The true SAMOs are found only at much higher energies, beyond 3 eV above the LUMO of  $Y_3@C_{80}$  (see Table S3 for more details on MOs of  $Y_3@C_{80}$ ).

One should distinguish "pseudoatomic" (or "superatomic") orbitals formed by the spherical potential (and probably modulated by the endohedral atoms or cluster, such as  $Y_3$  cluster in  $Y_3@C_{80}$ ) and "pseudoatoms" or "non-nuclear attractors" revealed in the topological analysis of the electron density. The orbitals are the objects in the Hilbert space, while the latter are the real-space phenomena. Furthermore, the orbitals are generated by the positive charge, while non-nuclear attractor of the electron density is the center of the negatively-charged basin. Yet, there is a genetic relationship between these objects in that the s-type atomic-like orbitals have the orbital-density maximum at the center of the generating potential, and when such s-orbitals are occupied, the maximum of the electron density emerges in this point.

Fig. 5 shows the spatial distribution of electron localization function (ELF) in  $Y_3@C_{80}^+$ ,  $Y_2@C_{82}$  and  $Y_3N@C_{80}$ . Formation of the chemical bond in terms of ELF can be visualized as polysynaptic valence basins. For instance, disynaptic valence carbon-carbon basins,  $V(C,C)$ , are typical for the fullerenes (see Fig. 5a). Y-cage bond formation can be clearly visualized by the transformation of the valence disynaptic  $V(C,C)$  basins into the trisynaptic  $V(Y,C,C)$  basins, which are more spatially expanded than  $V(C,C)$  at the same ELF isovalue<sup>45</sup> (Fig. 5a). Stronger Y-cage interactions in  $Y_3@C_{80}$  and  $Y_2@C_{82}$  compared to  $Y_3N@C_{80}$  are reflected in the larger number of  $V(Y,C,C)$  basins found in these molecules (Fig. 5b-d). If the presence of the NNA is not taken into account in ELF analysis, two trisynaptic

V(Y,Y,Y) basins with an occupation of  $0.94 e$  each are found in  $Y_3@C_{80}^+$ . When NNA is also considered, valence V(NNA) basin with occupation  $0.19 e$  is found, while occupations of V(Y,Y,Y) basins is reduced to  $0.84 e$ . The total occupation of these basins is close to 2, showing that they mainly originate from the density of the interstitial orbital, which is well localized in the center of the cage. In  $Y_2@C_{82}$ , one disynaptic V(Y,Y) basin with the occupation of 1.71 is found. For comparison, an analogous analysis of  $Y_3N@C_{80}$  exhibits core nitrogen C(N) basin and three trisynaptic valence V(N,Y,Y) basins (Fig. 5d,f), each occupied by 2.43 electrons. While the number of electrons in the intra-cluster basins is different, their shapes and spatial distribution are very similar in  $Y_3@C_{80}^+$  and  $Y_3N@C_{80}$ . Moreover, if the number of electrons contributed by the nitrogen atom is subtracted from the total population of V(N,Y,Y) basins in  $Y_3N@C_{80}$ , the remaining number of 2.3 electrons is close to the total occupation of V(Y,Y,Y) and V(NNA) basins in  $Y_3@C_{80}^+$ . The similarity of the intracluster basin sets in  $Y_3@C_{80}^+$  and  $Y_3N@C_{80}$  can be especially well seen in the ELF mapped in the plane of  $Y_3$  atoms (Fig. 5g,h). Note that the structuring of the outermost core shell of Y atoms induced by the bond formation<sup>39</sup> is also very similar in two molecules.



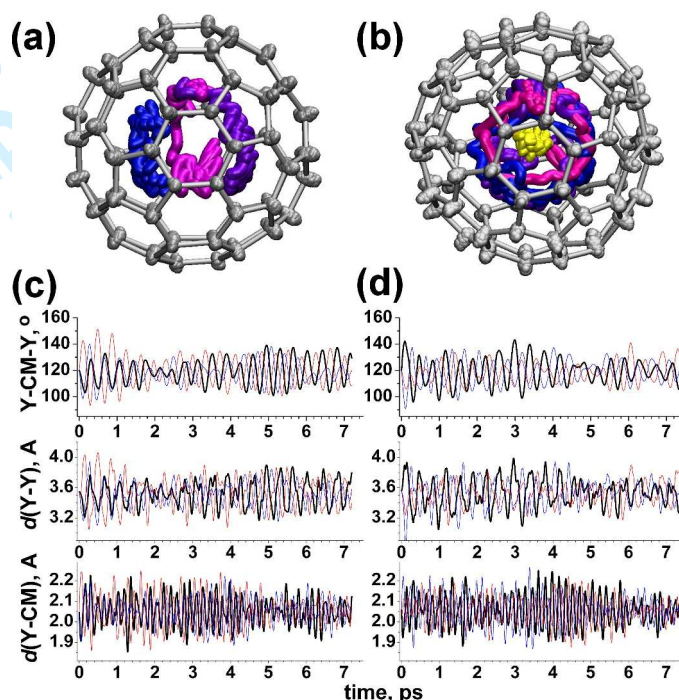


**Figure 5.** Spatial distribution of electron localization function (ELF): (a-d) ELF (isovalue 0.72) in  $Y_3@C_{80}^+$  (a, b),  $Y_2@C_{82}$  (c) and  $Y_3N@C_{80}$  (d); color code for basins: yellow –  $V(C,C)$ , light green –  $C(C)$ , light blue –  $V(Y,C,C)$ , orange –  $C(Y)$ , dark blue/green –  $V(Y,Y,Y)$ ,  $V(Y,Y)$  and  $V(N,Y,Y)$ ; valence  $V(C,C)$  and core  $C(C)$  basins are not shown in (b-d); (d-f) Enlarged view of ELF in the  $Y_3$  (e) and  $Y_3N$  (f) clusters; one  $V(Y,Y,Y)$  for  $Y_3$  and two  $V(N,Y,Y)$  basins for  $Y_3N$  are not shown; (g-h) 2D map of ELF in  $Y_3@C_{80}^+$  (g) and  $Y_3N@C_{80}$  (h) in the plane of the yttrium atoms. Shell structure of the N and Y atoms can be clearly seen.

**Molecular Dynamics Simulations.** To study the dynamic stability of the  $Y_3$  cluster inside the carbon cage we have performed molecular dynamics (BOMD) simulations of  $Y_3@C_{80}^+$  and  $Y_3N@C_{80}$  (since our calculations have shown that the intra-cluster bonding situation in  $Y_3@C_{80}$  and  $Y_3@C_{80}^+$  is virtually the same, BOMD calculations were performed for the closed-shell cation to facilitate longer propagation time). Fig. 6a,b show snapshots of MD trajectories of the two species followed for 7 ps after equilibration at 300 K for 0.6 ps. The averaged temperature over the trajectory was 271 K for  $Y_3@C_{80}^+$  and 297 K for  $Y_3N@C_{80}$ .  $M_3N$  clusters are known to rotate freely in  $M_3N@C_{80}$ , at least at the NMR time-scale.<sup>5, 46, 47</sup> Our simulations show that over the period of 4 ps, the  $Y_3N$  cluster accomplished rotation by almost  $360^\circ$  around one of its Y–N bond. Then rotation axis was switched, resulting in long curved trajectories for all Y atoms. Displacements of the nitrogen atoms are also significantly larger than those of the cage carbon atoms, which is the result of the coupled cluster rotation and nitrogen-out-of-plane vibration (the latter exhibits rather large amplitude in these condition; note that for the static  $Y_3N@C_{80}$  at 0 K, PBE/TZ2P predicted frequency of this mode is only  $99\text{ cm}^{-1}$ ). The  $Y_3$  cluster in  $Y_3@C_{80}^+$  also exhibits considerable displacements over the period of 7 ps, however displacement amplitudes are slightly smaller than in the  $Y_3N$  cluster. We propose that the stronger Y–cage bonding revealed in  $Y_3@C_{80}$  by QTAIM as compared to  $Y_3N@C_{80}$  results in somewhat more hindered rotation of the cluster compared to  $Y_3N$ . At the same time, smaller displacements of the  $Y_3$  cluster can be also caused by the lower averaged temperature over the trajectory. In any case, displacements of the  $Y_3$  cluster observed over 7 ps are still rather large and hence free rotation of the cluster is expected at the longer timescale.

To analyze the changes of the cluster structure in the course of the MD run, we have plotted selected structural parameters of the cluster as a function of time in Fig. 6c,d. Following the position of the NNA in  $Y_3@C_{80}^+$  along the trajectory is still too computationally demanding, and hence we analyzed the changes of the angles between two yttrium atoms and the center of mass (CM) of the molecule as well as the deviations of the Y–CM distances. For the sake of comparison, analogous parameters are also

studied for the  $Y_3N$  cluster in  $Y_3N@C_{80}$ . Because of the displacements of the nitrogen atom, Y–CM–Y angles and Y–CM distances are not equal to the Y–N–Y angles and Y–N distances. However, we have found that Y–CM–Y and Y–N–Y angles do correlate very well. At the same time, vibrations of the Y–N bonds in  $Y_3N@C_{80}$  occur with higher frequencies and smaller amplitude variations of the Y–CM distances.



**Figure 6.** Molecular dynamics simulations. Trajectories of  $Y_3@C_{80}^+$  (a) and  $Y_3N@C_{80}$  (b) followed for 7 ps in the microcanonical ensemble after equilibration of the molecules at 300 K for 0.6 ps (carbon atoms are grey, yttrium atoms are blue, violet, and magenta, nitrogen atom is yellow; fuzzy positions of the carbon atoms are due to the vibrations of the carbon cage); c–d, variation of Y–CM–Y angles, Y–Y and Y–CM distances in  $Y_3@C_{80}^+$  (c) and  $Y_3N@C_{80}$  (d) over the MD trajectory. All three possible parameters are shown for each item as thick black and thin red and blue curves. The scale is the same for (c) and (d), equilibration period was 0.6 ps in each case.

Fig. 6c,d shows that over the trajectory, the Y–CM–Y angles in both  $Y_3$  and  $Y_3N$  clusters oscillate around  $120^\circ$  with the deviations barely exceeding  $20^\circ$ . Likewise, the Y–Y and Y–CM distances also oscillate around their equilibrium distances with the amplitudes of ca 0.4 and 0.2 Å. Therefore, both clusters are rather rigid. While this result is more or less trivial for the  $Y_3N$  cluster, which has strong polar covalent Y–N bonds,<sup>27</sup> this is an interesting finding for the  $Y_3$  cluster in  $Y_3@C_{80}^+$ . Importantly, the rigidity of the  $Y_3$  cluster is very similar to that of the  $Y_3N$ .

In summary, we have shown that  $M_3@C_{80}-I_h(7)$  species are likely to be genuine trimetallofullerenes with the non-nuclear maximum of the electron density in the center of the  $M_3$  cluster, which thus mimics the nitrogen atom in the  $M_3N@C_{80}-I_h(7)$  nitride clusterfullerenes. At the same time, we have shown that formation of carbide clusterfullerenes  $M_3C_2@C_{96}-D_2(186)$  is more likely than formation of conventional trimetallofullerenes,  $M_3@C_{98}$ . QTAIM analysis of  $Y_3@C_{80}$  reveals that yttrium atoms are bonded to NNA, and that there are no direct Y–Y bond paths in  $Y_3@C_{80}$ . While further molecular dynamics simulation with longer equilibration, longer system propagation and better temperature control are needed to provide the quantitative description of the cluster dynamics in these molecules, our present study clearly shows that the  $Y_3$  cluster is rather rigid and tends to rotate inside the cage as a single entity, while variation of the structural parameters of the cluster over the trajectory are in the same range as found for the  $Y_3N$  cluster in the  $Y_3N@C_{80}$ . Thus, dynamics and electronic structure of the  $Y_3$  cluster strongly resemble those of  $Y_3N$ . In few words, yttrium atoms do not "notice" when the nitrogen atom is removed from  $Y_3N@C_{80}$  and sustain the same bonding pattern and dynamical stability in  $Y_3@C_{80}$  as in the nitride clusterfullerene. Further work on the isolation of EMFs with trimetallic clusters for their further structural characterization is in progress in our group.

## Experimental details

The vaporization of graphite rods packed with the mixture of Yttrium metal and graphite powder (the ratio is 1:15) was conducted under the modified Krätschmer-Huffmann DC-arc discharging method in reactive gas atmosphere with  $\text{NH}_3$  as a nitrogen source (atmosphere composition: ammonia 20 mbar and helium 200 mbar). After dc-arc discharging, the soot was pre-extracted by acetone and then Soxhlet-extracted by  $\text{CS}_2$  for 20 h. HPLC isolation running in a Hewlett-Packard instrument (series 1100), a linear combination of two analytical 4.6x250 mm Buckyprep (the first step) or Buckyprep-M (the second step) columns (Nacalai Tesque, Japan) was applied with toluene as the eluent (flow rate 1.6 ml/min; 40°C). Laser-desorption ionization (LDI) time-of-flight mass spectra were measured using Biflex III system (Bruker, Germany) without matrix.

## Details of computations

Optimization of the molecular structure of all species reported in this work was performed using PBE functional<sup>48</sup> and TZ2P-quality basis set (full-electron {6,3,2}/(11s,6p,2d) for C and N atoms, and SBK-type effective core potential for Y atoms with {5,5,4}/(9s,9p,8d) valence part) implemented in the PRIRODA package.<sup>49, 50</sup> This basis set is abbreviated in the manuscript as "TZ2P". The code employed expansion of the electron density in an auxiliary basis set to accelerate evaluation of the Coulomb and exchange-correlation terms.<sup>49</sup>

For the topological analysis, the electron density of EMFs was calculated at the B3LYP level with the use of Firefly/PC GAMESS package<sup>51</sup> and 6-311G\* basis set for C and N atoms and full-electron TZVP {8,6,5}/(19s,14p,9d) basis set for Y atoms<sup>52</sup>. QTAIM (quantum theory of atoms in molecules) analysis of the electron densities was performed with the use of AIMAll code (Version 08.05.04, <http://aim.tkgristmill.com>). The PROMEGA algorithm was used for the integration, since less time-demanding PROAIM algorithm often failed, especially for the yttrium atoms and the carbon atoms to which they are bonded. ELF (electron localization function) analysis was performed using TopMoD 09 suite.<sup>53</sup> In the view of the ambiguities of the ELF definition for the open shell systems and similar



1 bonding situation in  $Y_3@C_{80}$  and  $Y_3@C_{80}^+$ , ELF calculations were performed for the closed shell  
2  
3  $Y_3@C_{80}^+$  cation.  
4

5 Plane-wave DFT calculation were performed using CPMD code,<sup>54</sup> PBE functional and Trouiller-  
6  
7 Martins norm-conserving pseudopotentials for Y and C atoms.<sup>55</sup>  $Y_3@C_{80}$  molecule was placed inside  
8  
9 the center of the simple-cubic cell with the cell parameter of 26.4 Å (50 Bohr), the plane-wave cut-off of  
10  
11 100 Ry was used throughout the calculations.  
12  
13

14 Velocity Verlet algorithm with the time step 1.5 fs was used in Born-Oppenheimer molecular  
15  
16 dynamics (BOMD) calculations. The energies and gradients were computed with PRIRODA using PBE  
17  
18 functional and above mentioned basis set for the nitrogen and yttrium atoms, while the basis set for the  
19  
20 carbon atoms was reduced by one polarization d function. Molecules were first equilibrated at 300 K for  
21  
22 0.6 ps by rescaling velocities when the deviation of the instant temperature from 300 K exceeded 20 K.  
23  
24 Then, the trajectory was followed without thermostat (i.e., in microcanonical ensemble).  
25  
26  
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28 Visualization of the computational results was done using ChemCraft<sup>56</sup> (Fig. 2-4), Molekel<sup>57</sup> (Fig. 5a-  
29  
30 f), VESTA<sup>58</sup> (Fig. 5g-h) and VMD<sup>59</sup> (Fig. 6a-b).  
31  
32

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42  
43 affinities in the context of this work are highly appreciated.  
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47 **Supporting Information Available.** Isotopic distribution for  $Y_3@C_{80}$ , DFT-computed EA and IP  
48  
49 values for a series of  $Y_3N@C_{2n}$  molecules,  $Y_3@C_{80}$ ,  $Y_2C_2@C_{82}$ ,  $Y@C_{82}$  and selected empty higher  
50  
51 fullerenes; relative energies of  $Y_3@C_{98}$  and  $Y_3C_2@C_{96}$  isomers; additional details of molecular  
52  
53 dynamics simulations; MOs of  $Y_3@C_{80}$  obtained in the plane-wave calculations.  
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