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AquaEnv: An Aquatic Acid-Base Modelling Environment in R

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Abstract AquaEnv is an integrated software package for aquatic chemical model generation focused on ocean acidification and antropogenic CO₂ uptake. However, the package is not restricted to the carbon cycle or the oceans: it calculates, converts, and visualizes information necessary to describe pH, related CO₂ air—water exchange, as well as aquatic acid—base chemistry in general for marine, estuarine or freshwater systems. Due to the fact that it includes the relevant acid—base systems, it can also be applied to pore water systems and anoxic waters. AquaEnv is implemented in the open source programming language R, which allows for a flexible and versatile application: AquaEnv's functionality can be used stand-alone as well as seamlessly integrated into reactive-transport models in the R modelling environment. Additionally, AquaEnv provides a routine to simulate and investigate titrations of water samples with a strong acid or base, as well as a routine that allows for a determination of total alkalinity and total carbonate values from recorded titration curves using non-linear curve-fitting.

Keywords Acid-base chemistry \cdot pH modelling \cdot Ocean acidification \cdot Reactive-transport models \cdot Marine estuarine and freshwater systems \cdot CO₂ air-sea exchange \cdot In silico titration \cdot TA determination

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1 Introduction

With increasing concerns about climate change and ocean acidification (Caldeira and Wickett 2003; Royal Society 2005; IPCC 2007; Gazeau et al. 2007; Guinotte and Fabry 2008; Doney et al. 2009), there is a strong demand for computational tools that enable a quantitative description of the acid–base chemistry of natural waters. These tools are needed from both a modelling point of view as well as from an experimental perspective. Due to increasing complexity in model descriptions of aquatic ecosystems, biogeochemical models now often require the capability of pH prediction and full acid–base speciation (Luff et al. 2001; Caldeira and Wickett 2005; Jourabchi et al. 2005; Vanderborght et al. 2007; Doney et al. 2007; Blackford and Gilbert 2007; Zeebe et al. 2008; Aloisi 2008; Hofmann et al. 2008, 2009a). However, computational tools that describe acid–base speciation are also of interest to observational and experimental scientists: current methods to calculate total alkalinity (and total inorganic carbon) from measured titration curves, are based on fitting numerical models of the acid–base chemistry of the given water sample (Dickson 1981; DOE 1994; Anderson et al. 1999; Dickson et al. 2007).

Currently, there are two computational tools available that describe the acid-base chemistry of natural waters and the ocean carbon system in particular: the CO₂SYS program (Lewis and Wallace 1998; Pierrot et al. 2006; van Heuven et al. 2009) and the extension package seacarb (Lavigne et al. 2008) for the open-source programming language R (R Development Core Team 2005). Both programs perform two basic tasks:

- 1. The calculation of various physical parameters (dissociation constants, solubility constants of calcite and aragonite, Henry's constant of CO₂, etc.) as a function of temperature, salinity, and pressure
- The calculation of pH, the associated acid-base speciation (including the calculation
 of all parameters of the CO₂ system), and the saturation state with respect to calcite
 and aragonite.

CO₂SYS is the oldest program, but has a limited scope and is mainly focused on the ocean carbonate system. Although the phosphate and silicate systems are additionally incorporated as acid-base equilibria, only the carbonate speciation is provided in the output. Originally, the CO₂SYS program was distributed either as a compiled Microsoft DOS program (Lewis and Wallace 1998) or as a Microsoft Excel spreadsheet (Pierrot et al. 2006), which makes the program static and inflexible. This way, CO₂SYS was difficult to link to an external biogeochemical model code. Recently, a MATLAB version of CO₂SYS has been released (van Heuven et al. 2009). Although that allows for some flexibility, the core function is still very rigid and tailored to the needs of an ocean researcher measuring properties of samples in the laboratory or in the field: it is a tool for the experimental scientist rather than a modelling tool. Next to the non-intuitive interface of the CO₂SYS MATLAB function which uses variable types indicated by numbers instead of variable names, the MATLAB routine shares a shortcoming with the other CO₂SYS versions: it does not provide the dissociation constants as output, they are only calculated and used internally. Furthermore, the user is restricted to MATLAB which is a commercial, proprietary program and might not be at the disposal of every scientist. The package seacarb, however, is implemented in the open-source programming language R. The R framework provides vast capabilities of preprocessing, statistical postprocessing, and visualization of data. Recently, R has also evolved into a suitable platform for biogeochemical and reactive-transport model development (Soetaert and Herman 2009), as powerful packages for numerical integration of differential equations (e.g. deSolve Soetaert et al. 2008),



rootfinding (e.g. rootSolve Soetaert 2008), and reactive-transport modelling (Soetaert and Meysman 2009, e.g. ReacTran) have been developed. The R platform is excellently suited for rapid prototyping of biogeochemical models, since it combines an interpreted programming language with the possibility to embed legacy FORTRAN code that enables fast numerical calculations.

Here, we report on the new R package AquaEnv that substantially extends the capabilities of both CO₂SYS and seacarb. Compared to the seacarb package, AquaEnv can be applied to hyposaline systems (see Sect. 2), and it calculates a number of additional quantities, such as the buffer factor, various partial derivatives of total alkalinity, and ionization fractions that are useful for studying and modelling the effect of biogeochemical processes on pH (Hofmann et al. 2008, 2009a,b). Compared to CO₂SYS, AquaEnv additionally includes the $\left[\sum NH_4^+\right]$, $\left[\sum H_2S\right]$, $\left[\sum H_3PO_4\right]$, $\left[\sum Si(OH)_4\right]$, $\left[\sum HNO_3\right]$, and $\left[\sum HNO_2\right]$ acid—base systems, which makes it applicable to sediment pore water and anoxic systems. In addition, a number of more advanced applications are included in AquaEnv. These enable the improved interfacing with numerical biogeochemical models, the generation of "in silico" titrations, and the determination of total alkalinity (and total carbonate) values from measured titration curves by non-linear optimization (inverse modelling).

The AquaEnv package can be obtained from the Comprehensive R Archive Network (CRAN): http://cran.r-project.org/package=AquaEnv or from the R-forge website: http://r-forge.r-project.org/projects/aquaenv/. General information and tutorials about R can be found on the R project homepage: http://www.r-project.org/.

Please note that, at appropriate places throughout the paper, we supply boxes with R code fragments illustrating the usage of AquaEnv. These code fragments should serve as starting points for the inclined reader to explore AquaEnv whilst reading this publication. More detailed R scripts using AquaEnv are provided in the electronic appendix.

2 AquaEnv in Mesohaline and Oligohaline Environements

As mentioned above, the main novel features of AquaEnv are the implementation of quantities for the pH modelling approach given by Hofmann et al. (2008, 2009a,b), the titration simulation, and the alkalinity determination routines. Another important advantage of AquaEnv is that it can also be applied to mesohaline and oligohaline environments.

In AquaEnv, salinity (S) and temperature (t) relationships for dissociation constants as given in Table 1 are implemented. If there are multiple relations per dissociation constant implemented, the first one in the list is the default choice in AquaEnv.

This means, in AquaEnv, the default choice of S, t relations for dissociation constants is valid for a salinity range of 0–45, except for the relation for K_HS04. However since DOE (1994), Zeebe and Wolf-Gladrow (2001), and Dickson et al. (2007) all recommend the Dickson (1990b) formulation for K_HS04, we chose to make that our default choice. Applying AquaEnv to salinities below 5 using this default setting is still acceptable, since K_HS04 is mainly needed for pH scale conversions from and to the total and seawater scale. However, in brackish and freshwater (model) applications, the NBS scale and the free scale are normally used, where K_HS04 is less important as it plays no role for conversions between the NBS scale and the free scale. The influence of K_HS04 via association or dissociation of the $HSO_4^- \rightleftharpoons H^+ + SO_4^{2-}$ system on total alkalinity and pH is minute (free scale pH values differ in the sixth digit if different K_HS04 formulations are used).



Constant	Original reference	S, t range given in	S range	t range (°C)
K_W	Millero (1995)	Original reference	0–45	0–45
K_HSO4	Dickson (1990b)	Original reference	5-45	0-45
	Khoo et al. (1977)	Millero (1995) (inferred)	0-45	0-45
K_HF	Dickson and Riley (1979a)	Millero (1995) (inferred)	0-45	0-45
	Perez and Fraga (1987)	Original reference	10-40	9–33
K_HxCOx	Roy et al. (1993b) (adapted)	Millero (1995)	0-45	0-45
	Lueker et al. (2000)	Original reference (inferred)	19-43	2–35
	Millero et al. (2006)	Original reference	0-50	0-50
K_BOH3	Dickson (1990a)	Millero (1995)	0-45	0-45
K_NH4	Millero (1995)	Original reference	0-45	0-45
K_H2S	Millero et al. (1988)	Millero (1995)	0-45	0-45
K_HxPO4	Millero (1995)	Original reference	0-45	0-45
K_SiOH4	Millero et al. (1988)	Millero (1995)	0-45	0-45

Table 1 S, t relationships with associated S and t ranges as implemented in AquaEnv

Following Millero (1995), we adapted the formulation of Roy et al. (1993b) to low salinities. In Millero (1995), it is stated that for S < 5, the fresh water formula (based on Millero (1979)) should be used and for $S \ge 5$ the seawater formula derived in Roy et al. (1993b). However, both formulations do not always intersect at S = 5. The true intersection with respect to salinity S is a function of temperature t. In AquaEnv, we first calculate this intersection by numerical root finding and then decide which formulation to use. This practise results in a continuous function with respect to S (i.e. the discontinuity at S = 5 is removed). However, as can be seen in Fig. 1, a non-differentiability remains at the intersection, which leads to non-differentiabilities in the salinity dependencies of concentrations (see also Fig. 2 in Sect. 4.6)

Nevertheless, the user can choose to use the Khoo et al. (1977) formulation for K_HSO4 which is, as can be inferred from Millero (1995), valid down to S = 0.

Most important for the pH chemistry of aquatic systems with a high dissolved inorganic carbon concentration, like many estuaries, is the choice of the S, t relations for the first and the second dissociation constant of the carbonate system. We implement the relation by Roy et al. (1993b), adapted to low salinities as described by Millero (1995) (see caption of Table 1) and the relation by Millero et al. (2006), which are both explicitly valid down to S = 0. seacarb only implements the original version of Roy et al. (1993b), not adapted to low salinities, and the relation of Lueker et al. (2000), which are not valid below S = 5 and S = 19, respectively. Figure 1 plots all four relations against salinity in the oligohaline and mesohaline region.

It becomes clear that in the oligohaline realm (S < 5), there are big differences between the relations that are explicitly defined for low salinities and the ones that are not, this can also be seen in Fig. 2. AquaEnv implements two S, t relations for the first and second dissociation constant of the carbonate system (K_C02 and K_HC03) that are valid down to S = 0, whilst seacarb implements none.

This means, AquaEnv provides an advantage over seacarb for oligohaline and mesohaline systems, since (1) it implements S, t relations for K_CO2 and K_HCO3 that are valid down to S = 0 and (2) it implements the conversion from and to the NBS scale for brackish and freshwater, which is not implemented in seacarb. In general, one can choose more S, t relationships in AquaEnv than one can in seacarb. CO₂SYS can handle low salinities, but, as mentioned above, is restricted to a narrow choice of acid—base systems that are considered in the calculations, making it unsuitable for pore water and anoxic systems. However, CO₂SYS does provide more choices of S, t relations for the CO₂



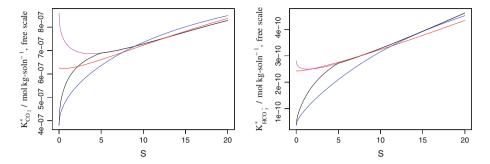


Fig. 1 Salinity dependence of four different S, t relationships of the first (*left panel*) and second (*right panel*) dissociation constant of the carbonate system. *Magenta line* Roy et al. (1993b), not adapted to low salinities (as implemented in seacarb); *red line* Lueker et al. (2000), not valid below S = 19 (implemented in seacarb and AquaEnv); *black line* Roy et al. (1993b), adapted to low salinities (as implemented in AquaEnv); *blue line* Millero et al. (2006), valid down to S = 0 (implemented in AquaEnv)

system, since this is its main focus. It offers the same choice of S, t relations for K_HSO4 as does AquaEnv, but less choices for K_HF.

3 Structure of the AquaEnv Package and an aquaenv Object

The functionality in the seacarb package is established by calls to separate R functions. Rather than implementing separate functions for each feature, AquaEnv adopts a more integrated approach. Almost all functionality is contained within one generic function, termed aquaenv, which creates structured objects of the aquaenv class (encoded as an R list with multiple components), termed "aquaenv objects" in what follows. Components within an aquaenv object contain all information (physical parameters, acid—base dissociation constants, chemical speciation, partial derivatives, etc.) that can be calculated from the given input parameters. Whilst an underdeterminated system (too few input parameters) prompts an error message, an overdetermined system (too many input parameters) prompts AquaEnv to display a message that informs the user how calculated and suplied values differ. Information is obtained by selecting the appropriate element from the aquaenv object. At the same time, AquaEnv also includes individual functions that calculate quantities like acid—base dissociation constants separately.

Once created, aquaenv objects can be used in generic plotting and data processing commands, that have been specifically created for the aquaenv class. aquaenv objects can be converted to an R data.frame, which can be further postprocessed with standard R routines. Similarly, an R data.frame can be converted to an aquaenv object, for the use of aquaenv object specific plotting facilities provided in AquaEnv. Furthermore, the aquaenv objects can be used as input argument supplying initial conditions in the titration and TAfit functions, which respectively simulate an in silico titration and perform the inverse modelling of titration data to obtain total alkalinity values.



Appendix 7.1 details the complete structure of an *aquaenv* object. For each component, the name, physical units and a short explanation are listed. Appendix 7.2 gives all relevant mathematical formulae as well as physical and chemical constants, with respective literature references, used for calculation of components of an *aquaenv* object.

4 Basic Applications

4.1 Physical and Chemical Parameters

AquaEnv provides routines that calculate the key physical and chemical parameters involved in the acid–base chemistry of natural waters. These include the stoichiometric equilibrium constants (K^*) for the major acid–base systems (carbonate, ammonia, sulphide, nitrate, nitrite, phosphate, silicate, borate, sulphate, and fluoride), the ion product of water, the Henry's constants (K_0) that govern the solubility of CO_2 and O_2 , as well as the solubility products ($K_{\rm sp}$) for calcite and aragonite. These parameters are all calculated according to a standard (S, t, t) format, i.e., as a function of salinity (t), temperature in t0 minus the gauge pressure or applied pressure (t0) which represents the total pressure (t0) minus the atmospheric pressure (t1) (Millero et al. 2008; Feistel 2008). Instead of the gauge pressure t2, the total pressure t3 or the water depth t4 can also be given as input parameters. All required mathematical expressions were compiled from various sources in literature as discussed in Appendix 7.2.

Note that in AquaEnv, three different S, t dependencies for the first and the second dissociation constant of the carbonate system are implemented: the relation by Roy et al. (1993a) adapted to be also applicable to low salinities as described by Millero (1995); the relation by Lueker et al. (2000) which is recommended by Dickson et al. (2007) but which is not applicable to low salinities; and the relation introduced by Millero et al. (2006) which covers a salinity range from 0 to 40 and which is, amongst other relations, also used in CO₂SYS. The relation by Roy et al. (1993a) is used by default in AquaEnv, and the other two relations can be employed by setting the flag k1k2 to "lueker" or "millero". In the same way, two different relations for the dissociation constant of hydrogen fluoride can be used: the relation by Dickson and Riley (1979a) (default in AquaEnv) and the relation by Perez and Fraga (1987) (as advised by Dickson et al. (2007); flag khf set to "perez" in AquaEnv). Similarly, two different relations for the dissociation constant of hydrogen sulphate can be used: the relation by Dickson (1990b), as recommended by DOE (1994); Zeebe and Wolf-Gladrow (2001); Dickson et al. (2007) (default in AquaEnv), and the relation by Khoo et al. (1977) as used in, e.g., Roy et al. (1993b); Millero (1995); Lewis and Wallace (1998) (flag khso4 set to "khoo" in AquaEnv).



Our goal was to arrive at an internally consistent parameter set, where all quantities are expressed using the same concentration units and the same pH scale (molinity and free pH scale: see discussion below). To achieve this, appropriate conversions were applied, using auxiliary variables like seawater density calculated as a function of salinity and temperature, and ionic strength calculated as a function of salinity (see Appendix 7.2). These auxiliary variables are also stored as components in *aquaenv* objects and can thus be accessed by the user (As mentioned, a full list of names of components contained in *aquaenv* objects is given in Appendix 7.1).

```
A <- aquaenv(S=35, t=10)
A$K_CO2
A$K_HF
A$I
A$density

B <- aquaenv(S=35, t=10, k1k2="lueker", khf="perez")
B$K_CO2
B$K_HF
```

4.2 Seawater Composition

For some biogeochemical applications, the detailed ionic composition of seawater is required. AquaEnv calculates this composition from salinity (according to DOE 1994; Dickson et al. 2007), determining the total borate concentration ($[\sum B(OH)_3]$), the total sulphate concentration ($[\sum H_2SO_4]$), the total fluoride concentration ($[\sum HF]$), and the ion concentrations of Cl^- , Br^- , Na^+ , Mg^{2+} , Ca^{2+} , K^+ , and Sr^{2+} . Note that the values for $[\sum B(OH)_3]$, $[\sum H_2SO_4]$, $[\sum HF]$ can also be given as input (in mol/kg-solution) upon construction of an *aquaenv* object, and in that case, they override the default values calculated from salinity.

```
A <- aquaenv(S=35, t=10)
A$SumBOH3
c(A$Mg, A$Ca, A$Br)
A <- aquaenv(S=35, t=10, SumBOH3=0.0007)
A$SumBOH3
```

4.3 pH Scales and Unit Conversions

Acid-base calculations are always characterized by a specific choice of the concentration unit (molarity = mol/l, molality = mol/kg-H₂O, or molinity = mol/kg-solution) and the pH scale (free scale, total scale, seawater scale, and NBS scale, all based on a specific concentration unit: see discussion on pH scales in Dickson (1984), Lewis and Wallace (1998), and Zeebe and Wolf-Gladrow (2001)). To ensure the accuracy and consistency of the calculations, it is vital to consider the issue of concentration units and pH scales. Often, it is only specified that calculations are performed in gravimetric units (i.e., mol/kg). However, with increasing salinity, the difference between the two gravimetric units, molality and molinity, becomes significant, and so, the choice of concentration units must be made explicit. Similarly, the differences between pH scales are significant, especially at



higher salinities (Zeebe and Wolf-Gladrow 2001). Each pH scale is linked to its own specific set of values for the stoichiometric equilibrium constants. Using a mixture of pH scales for equilibrium constants (K^*) and pH values thus will lead to erroneous speciation calculations.

In AquaEnv, the input, output, and internal calculations are all stated in SI units (except for the pressure unit, which is bar instead of Pascal for the gauge pressure and atm instead of Pascal for the fugacities.), molinity, and on the free pH scale. To be consistent with Lewis and Wallace (1998), the NBS pH scale in AquaEnv is based on the proton concentration in mol/kg-H₂O, while all other pH scales are based on mol/kg-soln. Both the input parameters and the components of an *aquaenv* object can be converted between different concentration units and pH scales using the generic AquaEnv function convert. Furthermore, the factors for conversion between molality and molinity (molal2molin) and between the free, total and seawater pH scale (free2tot, free2sws, etc.) are components of an *aquaenv* object. The mathematical relations underlying these conversion functions are also detailed in Appendix 7.2.

```
A <- aquaenv(S=35, t=10, TA=0.002, SumCO2=0.002)
convert(A$SumBOH3, "conc", "molin2molar", S=35, t=10)
convert(A$K_CO2, "KHscale", "free2sws", S=35, t=10)
convert(A$pH, "pHscale", "free2tot", S=35, t=10)
A$molal2molin
B <- convert(A, "mol/kg-soln", "umol/kg-H20", 1e6/A$molal2molin, "unit")
```

The conversion from and to the NBS pH scale requires the activity coefficient for protons in solution (Durst 1975; Dickson 1981; Zeebe and Wolf-Gladrow 2001). In AquaEnv, we opted for a simple and direct approach: we implemented the Davies equation (as stated in Zeebe and Wolf-Gladrow 2001) to calculate the proton activity coefficient. Since the NBS scale is mainly used for fresh and brackish waters and not for open ocean waters, we choose not to invest time in the implementation of a detailed and intricate ion-interaction model (Pitzer model) as given by Millero and Pierrot (1998). The Davies equation is valid up to an ionic strength of I = 0.5 mol/kg-H₂O (Zeebe and Wolf-Gladrow 2001) and hence, up to a salinity S of \sim 25. Above this salinity, the conversion from and to the NBS pH scale as implemented in AquaEnv should be regarded as approximate.

4.4 Acid–Base Speciation Calculations

Given suitable input parameters, AquaEnv calculates the full speciation of all acid–base systems in the solution at hand. As output, one obtains an *aquaenv* object containing the concentrations of all dissociated species in the system, the related ionization fractions (i.e., the ratios of dissociated concentrations over total concentrations), the fugacity of CO_2 , as well as the saturation state $\Omega = [Ca^{2+}][CO_3^{2-}]/K_{sp}$ for calcite and aragonite.

The speciation calculation consists essentially of two steps: the pH is first computed numerically, followed by the analytical calculations that describe the speciation. Numerically, the pH calculation comes down to the solution of a set of non-linear algebraic equations as determined by the mass action equations of the acid-base systems. In AquaEnv, this non-linear system is solved using the iterative approximation approach described by Follows et al. (2006), which is based on the repeated analytical solution of a



quadratic equation derived from the mass action equations of the carbonate system only. In cases where this approach does not converge, e.g. in cases with very low or zero total dissolved inorganic carbon concentration ($[\sum CO_2]$), the R function uniroot is employed which implements an interval based root finding algorithm. If only the pH needs to be calculated without a full speciation, one can set the flag speciation to FALSE.

A full speciation (i.e., all concentrations of the CO_2 system as well as of all other acidbase systems) is calculated from salinity, temperature, and pressure (determining the stoichiometric equilibrium constants), the total concentrations associated with acid-base systems present ($[\sum CO_2]$, $[\sum NH_4^+]$, $[\sum H_2S]$, $[\sum HNO_3]$, $[\sum HNO_2]$, $[\sum H_3PO_4]$, $[\sum Si(OH)_4]$, $[\sum B(OH)_3]$, $[\sum H_2SO_4]$, $[\sum HF]$), as well as total alkalinity ([TA]), or pH, or the carbon dioxide fugacity (fCO_2), or the carbon dioxide concentration ($[CO_2]$). Some of the quantities above have default values and do not need to be supplied. That means, for example, the parameter pairs ([TA], $[\sum CO_2]$), ([TA], pH), (pH, $[\sum CO_2]$) (fCO_2 , $[\sum CO_2]$), ($[CO_2]$, [TA]), etc. allow for the calculation of a full speciation. If too much information is provided (i.e. an overdetermined system is created), a message is displayed, stating how calculated and provided numbers differ.

```
A <- aquaenv(S=35, t=10, SumCO2=0.002, pH=8)
c(A$TA, A$CO2, A$BOH3)

A <- aquaenv(S=35, t=10, SumCO2=0.002, TA=0.002136459)
c(A$pH, A$CO2)

A <- aquaenv(S=35, t=10, SumCO2=0.002, CO2=2.172711e-05)
c(A$pH, A$TA, A$fCO2)

A <- aquaenv(S=35, t=10, SumCO2=0.002, fCO2=0.0004951574)
A$pH

A <- aquaenv(S=35, t=10, SumCO2=0.002, TA=0.002136459, speciation=FALSE)
A$pH
A$BOH3

A <- aquaenv(S=35, t=10, SumCO2=0.002, CO2=2e-5, fCO2=5e-4)
A <- aquaenv(S=35, t=10, SumCO2=0.002, pH=8, TA=0.0021)
```

Furthermore, it is possible to calculate $[\sum CO_2]$ and a full speciation from a suitable set of input parameters. To that end, the input value NULL needs to be assigned to the argument SumCO2 and one of the pairs pH and $[CO_2]$, pH and $[CO_2]$, pH and $[CO_2]$, or [TA] and $[CO_2]$ and $[CO_2]$, or [TA] and $[CO_2]$ and

```
aquaenv(S=35, t=10, SumCO2=NULL, pH=8, fCO2=0.0005)$SumCO2
aquaenv(30, 15, SumCO2=NULL, pH=8, TA=0.002)$SumCO2
aquaenv(25, 20, p=10, SumCO2=NULL, TA=0.002, CO2=2e-5)$SumCO2
aquaenv(S=35, t=10, p=100, SumCO2=NULL, TA=0.002, fCO2=0.0005)$SumCO2
```



4.5 Buffer Factor, Partial Derivatives of Total Alkalinity, and Revelle Factor

Theory states that total alkalinity can be specified as a function of the proton concentration and both the total concentrations and the dissociation constants (K_i^*) of the various acidbase systems.

$$[TA] = f([H^+], \left[\sum CO_2\right], \left[\sum NH_4^+\right], \left[\sum H_2S\right], \dots, K_i^*)$$
(1)

Recently, it has been shown that the partial derivatives of this expression are crucial in the description of pH dynamics and proton cycling in natural waters (a detailed explanation of proton cycling in natural waters is beyond the scope of this publication. The interested reader is referred to our other publications on this subject: Hofmann et al. 2008, 2009a,b). In particular, they play a key role in the construction of pH models. The most important partial derivative is the buffer factor β , which is related to buffer quantities introduced by Morel and Hering (1993), Frankignoulle (1994), and Stumm and Morgan (1996), but which is defined differently

$$\beta = -\frac{\partial[TA]}{\partial[H^+]} \tag{2}$$

Similarly, the partial derivatives of alkalinity with respect to the concentrations of the other total quantities are important

$$\frac{\partial[TA]}{\partial[\sum CO_2]}, \frac{\partial[TA]}{\partial[\sum NH_4^+]}, \frac{\partial[TA]}{\partial[\sum H_2S]}, \dots$$
 (3)

In AquaEnv, all these partial derivatives are calculated via analytical expressions and are accessible to the user as components of an *aquaenv* object.

Furthermore, [TA] is a function of the dissociation constants (K_i^*) of the various acidbase systems which, in turn, are functions of salinity S, temperature t, and pressure p. If these dissociation constants are calculated on one pH scale and then converted to another pH scale, they become functions of $[\sum H_2SO_4]$ and $[\sum HF]$ as well (see also Hofmann et al. 2009a). In general,

$$K_i^* = f\left(S, t, p, \left[\sum H_2 SO_4\right], \left[\sum HF\right]\right)$$
 (4)

Hofmann et al. (2009a) show that the products of the partial derivatives of [TA] with respect to the dissociation constants K_i^* and the partial derivative of the dissociation constants K_i^* with respect to one of their variables are needed for their explicit pH modelling approach. Therefore, AquaEnv numerically calculates

$$\sum_{i} \frac{\partial [TA]}{\partial K_{i}^{*}} \frac{\partial K_{i}^{*}}{\partial S}, \sum_{i} \frac{\partial [TA]}{\partial K_{i}^{*}} \frac{\partial K_{i}^{*}}{\partial t}, \sum_{i} \frac{\partial [TA]}{\partial K_{i}^{*}} \frac{\partial K_{i}^{*}}{\partial p}, \sum_{i} \frac{\partial [TA]}{\partial K_{i}^{*}} \frac{\partial K_{i}^{*}}{\partial [\sum H_{2}SO_{4}]}, \sum_{i} \frac{\partial [TA]}{\partial K_{i}^{*}} \frac{\partial K_{i}^{*}}{\partial [\sum HF]}$$

$$(5)$$

and provides these quantities as components of an aquaenv object.

Note that it is not necessary to indicate which variables are held constant when specifying a partial derivative if an exhaustive list of independent variables is given for the dependent variable, as it is the case here.



```
A <- aquaenv(35, 10, 100, SumCO2=0.002, pH=8.2, dsa=TRUE) c(A$dTAdKdKdS, A$dTAdKdKdT, A$dTAdKdKdp) c(A$dTAdKdKdSumH2SO4, A$dTAdKdKdSumHF)
```

Furthermore, as a related quantity, the well-known Revelle factor (e.g. Zeebe and WolfGladrow 2001) which is defined as

$$RF_0 = \left(\frac{d[CO_2]}{[CO_2]} \middle/ \frac{d[\sum CO_2]}{[\sum CO_2]}\right)_{|TA| = const.}$$
(6)

is numerically calculated in AquaEnv (see Appendix 7.2.12 for details) and provided as component of an *aquaenv* object.

```
A <- aquaenv(35, 10, 100, SumCO2=0.002, pH=8.2, dsa=TRUE, revelle=TRUE)
A$revelle
```

Details of how to use the partial derivatives of total alkalinity in reactive-transport models are given in (Hofmann et al. 2008, 2009a,b). Furthermore, Sect. 5.1 provides simple example models employing some of these quantities.

4.6 Sensitivity Analysis

One of the input variables for the function aquaenv may be a vector. All other input variables are then assumed to be constant. As a result, an *aquaenv* object is created which contains vectors of the respective components as functions of the input vector. Together with the plotting functionality specific for *aquaenv* objects, this enables a simple form of sensitivity analysis and its visualization. Figure 2 shows how AquaEnv can be used to

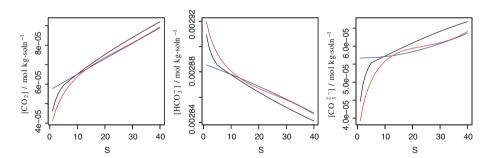


Fig. 2 Using AquaEnv to visualize the sensitivity of the carbonate speciation towards changes in salinity S. Black line using a salinity dependence for the first and second dissociation constants of the carbonate system as given in Roy et al. (1993b) with a freshwater formulation for salinities below 5, as recommended by Millero (1995) (these functions are used by default in AquaEnv). Blue line using a salinity dependence for the first and second dissociation constants of the carbonate system as given in Lueker et al. (2000), as recommended by Dickson et al. (2007) (these functions can be used in AquaEnv by setting the flag k1k2 to the value "lueker"). Red line using a salinity dependence for the first and second dissociation constants of the carbonate system as given in Millero et al. (2006) (these functions can be used in AquaEnv by setting the flag k1k2 to the value "millero"). Note that [TA] and $[\sum CO_2]$ have been kept constant at 0.003 mol/kg-solution. Note further that $[\sum B(OH)_3]$, $[\sum H_2SO_4]$, and $[\sum HF]$ are calculated from salinity. The plotted effect of changes in S on the carbonate speciation is thus twofold: via the salinity dependence of the dissociation constants and via the salinity dependence of $[\sum B(OH)_3]$, $[\sum H_2SO_4]$, and $[\sum HF]$



visualize how salinity variations in estuaries change the carbonate speciation (and pH; not shown). The code fragment below produces the three panels of Fig. 2 in separate plot windows.

```
sys1 <- aquaenv(1:40, 15, SumCO2=0.003, TA=0.003)
sys2 <- aquaenv(1:40, 15, SumCO2=0.003, TA=0.003, k1k2="lueker")
sys3 <- aquaenv(1:40, 15, SumCO2=0.003, TA=0.003, k1k2="millero")
ylim <- range(sys1$C02, sys2$C02, sys3$C02)</pre>
plot(sys1, xval=1:40, xlab="S", what="CO2", ylim=ylim,
     ylab=expression(paste("[", CO[2], "] / mol", " kg-soln"^"-1")))
plot(sys2, xval=1:40, xlab="S", what="CO2", ylim=ylim, col="blue",
     newdevice=FALSE, setpar=FALSE, ylab="")
par(new=TRUE)
plot(sys3, xval=1:40, xlab="S", what="CO2", ylim=ylim, col="red",
     newdevice=FALSE, setpar=FALSE, ylab="")
ylim <- range(sys1$HCO3, sys2$HCO3, sys3$HCO3)</pre>
plot(sys1, xval=1:40, xlab="S", what="HCO3", ylim=ylim,
     ylab=expression(paste("[", HCO[3]^"-", "] / mol", " kg-soln"^"-1")))
par(new=TRUE)
plot(sys2, xval=1:40, xlab="S", what="HCO3", ylim=ylim, col="blue",
     newdevice=FALSE, setpar=FALSE, ylab="")
par(new=TRUE)
plot(sys3, xval=1:40, xlab="S", what="HCO3", ylim=ylim, col="red",
     newdevice=FALSE, setpar=FALSE, ylab="")
ylim <- range(sys1$CO3, sys2$CO3, sys3$CO3)</pre>
plot(sys1, xval=1:40, xlab="S", what="CO3", ylim=ylim,
     ylab=expression(paste("[", CO[3]^"2-", "] / mol", " kg-soln"^"-1")))
par(new=TRUE)
plot(sys2, xval=1:40, xlab="S", what="CO3", ylim=ylim, col="blue",
     newdevice=FALSE, setpar=FALSE, ylab="")
par(new=TRUE)
plot(sys3, xval=1:40, xlab="S", what="CO3", ylim=ylim, col="red",
     newdevice=FALSE, setpar=FALSE, ylab="")
```

4.7 Data Visualization

The plot.aquaenv function is the generic plotting method for aquaenv objects (within the R object-oriented programming environment, this function can be called as plot without the .aquaenv suffix). This plotting method visualizes the information contained in an aquaenv object in a multifunctional way. (1) It can be used to visualize the sensitivity of a system with respect to changes in one input parameter (Fig. 2). (2) The plot.aquaenv function can be used to create Bjerrum plots which are the classical textbook way of displaying the speciation of acid—base systems as a function of pH (e.g. Zeebe and Wolf-Gladrow 2001). (3) plot.aquaenv can generate "cumulative" plots that can be used to, e.g., visualize the partitioning of dissolved inorganic carbon into



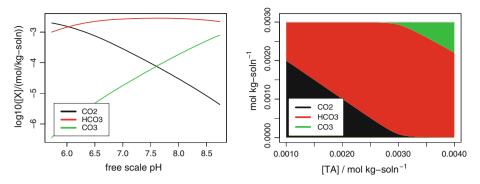


Fig. 3 Examples for the Bjerrum-plot and cumulative-plot functionality of AquaEnv

carbon dioxide, bicarbonate, and carbonate, or to partition the total rate of change of protons into contributions by different processes. The usage and syntax of the plot.aquaenv function is detailed in its R help file as well as in the package vignette of AquaEnv. The following code fragment gives an impression of the capability of the plot.aquaenv function. The last two plot calls produce graphs as shown in Fig. 3. Furthermore, Sect. 5.2 provides examples of how Bjerrum plots can be created using the titration function in combination with the plot.aquaenv function, and Sect. 5.1 provides another example for the cumulative plotting functionality.

```
A <- aquaenv(35, 15, SumCO2=0.003, TA=seq(0.001,0.004, 0.0001))

plot(A, xval=A$TA, xlab="[TA]/(mol/kg-soln)")

plot(A, what=c("CO2", "HCO3", "CO3"), bjerrum=TRUE, log=TRUE)

plot(A, xval=A$TA, xlab="[TA]/(mol/kg-soln)", what=c("CO2", "HCO3", "CO3"),

cumulative=TRUE, ylab="mol/kg-soln", ylim=c(0,0.0031))
```

5 Advanced Applications

5.1 AquaEnv in Reactive-Transport Models

When simulating the biogeochemistry of natural waters, one often needs to explicitly deal with pH dynamics. As a result, the corresponding reactive transport models need to include an acid—base speciation routine as a subcomponent. The function aquaenv fits this purpose. At each timestep of a dynamic model, aquaenv can calculate the desired information related to the "acid—base state" of the system (physical parameters, speciation, buffer capacity, partial derivatives etc.). We will show the use of aquaenv by means of a simple example model of a hypothetical aquatic system. Note that the example is an artificial model which is deliberately kept very simple for didactical reasons. Accordingly, it is not fitted to a particular natural system and it does not produce results relevant in reality. That means the used specific numerical values, selection of processes, and kinetic formulations for processes only serve illustrative purposes here and will not be discussed in detail.



Over a time scale of days, the pH chemistry of a hypothetical water reservoir is known to be influenced by two processes: CaCO₃ precipitation and CO₂ exchange across the airwater interface. These two dominant processes can be represented by the reaction equations

$$Ca^{2+} + CO_3^{2-} \rightarrow CaCO_3 \tag{7}$$

$$CO_2(atm) \rightleftharpoons CO_2$$
 (8)

Note that the second reaction represents CO_2 air–sea exchange. It is deliberately written in the style of a chemical reaction here to show that chemical and physical processes can be treated similarly concerning pH modelling according to Hofmann et al. (2008). The associated kinetic rate laws are (Morse 1983; Mucci 1986; Morse et al. 2003; Thomann and Mueller 1987):

$$\mathbf{R}_P = k_P (1 - \Omega)^n \tag{9}$$

$$\mathbf{R}_C = k_C ([\mathbf{CO}_2]_{\text{sat}} - [\mathbf{CO}_2]) \tag{10}$$

In addition, the pH chemistry will also depend on a number of "fast" acid-base dissociation reactions, with characteristic time scales of less than a minute (Zeebe and Wolf-Gladrow 2001). To keep the model suitably simple, only the carbonate system is accounted for

$$CO_2 + H_2O \rightleftharpoons HCO_3^- + H^+ \tag{11}$$

$$HCO_3^- \rightleftharpoons CO_3^{2-} + H^+ \tag{12}$$

The equilibrium mass action equations for these two acid-base reactions are, respectively:

$$K_{\text{CO}_2}^* = \frac{[\text{H}^+] [\text{HCO}_3^-]}{[\text{CO}_2]}$$
 (13)

$$K_{\text{HCO}_{3}^{-}}^{*} = \frac{[\text{H}^{+}][\text{CO}_{3}^{2-}]}{[\text{HCO}_{3}^{-}]}$$
 (14)

As detailed by Hofmann et al. (2009b), there are two main model approaches to arrive at the pH evolution of the water reservoir. In the "alkalinity centred" or "implicit pH modelling approach", one focuses on the effect of the kinetic processes on alkalinity ([TA]) and the total carbonate concentration ([$\sum CO_2$]) in the system. As a result, one obtains two differential equations describing the evolution of [TA] and [$\sum CO_2$]

$$\frac{\mathrm{d[TA]}}{\mathrm{d}t} = -2\mathbf{R}_P \tag{15}$$

$$\frac{\mathrm{d}[\sum \mathrm{CO}_2]}{\mathrm{d}t} = \mathbf{R}_C - \mathbf{R}_P \tag{16}$$

Since the kinetic rate laws (Eqs. 9 and 10) feature concentrations of dissociated species, the integration of Eqs. 15 and 16 requires a two-step approach (e.g. Luff et al. 2001; Follows et al. 2006). Starting with initial values for [TA] and $[\sum CO_2]$, one performs an "equilibration step" that calculates the concentrations of all dissociated species as a function of [TA] and $[\sum CO_2]$. Subsequently, an "integration step" is performed: the kinetic rate terms, which feature the concentrations of the dissociated species $[CO_2]$ and $[CO_3^{2-}]$ are calculated, and the resulting rates of change of [TA] and $[\sum CO_2]$ are passed



on to the integrator which returns new values for [TA] and $[\sum CO_2]$. Those new values, in turn, can be used for another "equilibration step". By repeating this two-step procedure for a suitable sequence of time steps, one eventually obtains the evolution of [TA], $[\sum CO_2]$, pH and all dissociated species over the desired time interval. The function aquaenv can be invoked to conveniently perform the "equilibration step": with one function call, the pH and a full speciation is calculated. The following code fragment represents part of a simple model function that describes pH implicitly via the rates of changes of [TA] and $[\sum CO_2]$. The file "AquaEnv-pHModelling.R" in the electronic appendix contains a model script that employs the respective model function.

An alternative approach to pH modelling was recently proposed (Hofmann et al. 2008, 2009b). The method was termed the "proton-centred" or "explicit" pH modelling approach, as it is based on an explicit evolution equation for the proton concentration. (Note that we are very brief in explaining this method here, since a detailed explanation is given by Hofmann et al. (2008) and (2009b) and is beyond the scope of this publication. However, AquaEnv does implement quantities necessary for this method, so we need to briefly repeat the main ideas.) Rather than using an evolution equation for alkalinity, one integrates following differential equation for the proton concentration

$$\frac{\mathrm{d}[\mathrm{H}^+]}{\mathrm{d}t} = S_P \mathbf{R}_P + S_C \mathbf{R}_C \tag{17}$$

The quantities S_P and S_C are respectively termed the *sensitivities* of pH with respect to CaCO₃ precipitation and CO₂ exchange. They are defined as

$$S_P = \frac{1}{\left(\frac{\partial [TA]}{\partial [H^+]}\right)} \left(-2 + \frac{\partial [TA]}{\partial [\sum CO_2]}\right)$$
(18)

$$S_C = \frac{1}{\binom{\hat{o}[TA]}{\hat{o}[H^+]}} \left(-\frac{\hat{o}[TA]}{\hat{o}[\sum CO_2]} \right)$$
 (19)

These sensitivities thus feature partial derivatives of total alkalinity [TA], which are calculated in a closed analytical form by the function aquaenv. The following code fragment represents part of a simple model function that describes pH explicitly using partial derivatives of [TA]. The file "AquaEnv-pHModelling.R" in the electronic appendix contains a model script that employs the respective model function.



Hofmann et al. (2009b) show that the sensitivities of pH with respect to biogeochemical processes can also be expressed using ionization fractions (Skoog and West 1982; Stumm and Morgan 1996), here of the carbonate system $(c_1 = [CO_2]/[\sum CO_2], c_2 = [HCO_3^-]/[\sum CO_2], c_3 = [CO_3^2]/[\sum CO_2])$

$$S_P = \frac{1}{\left(-\frac{\delta[\text{TA}]}{\delta\left[\sum \text{CO}_2\right]}\right)} (2c_1 + c_2) \tag{20}$$

$$S_C = \frac{1}{\left(-\frac{\hat{o}[\text{TA}]}{\hat{o}\left[\sum \text{CO}_2\right]}\right)} (c_2 + 2c_3) \tag{21}$$

Ionization fractions are calculated by the function aquaenv as well. The following code fragment represents part of a simple model function that describes pH explicitly using ionization fractions. The file "AquaEnv-pHModelling.R" in the electronic appendix contains a model script that employs the respective model function.

As mentioned above, the full implementation of the implicit and explicit pH modelling approaches into R code using the aquaenv function is detailed in the file "AquaEnv-pHModelling.R" in the electronic appendix. The implicit and explicit pH modelling approaches provide exactly the same evolution of pH, alkalinity, the total carbonate concentration, and all other quantities as a function of time (Fig. 4). However, the explicit modelling approach has the important conceptual advantage that it allows a systematic



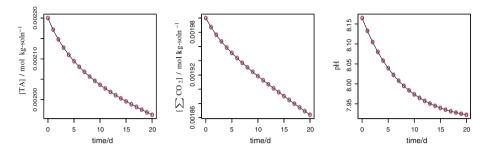


Fig. 4 Comparison of the results of the implicit and explicit pH modelling approaches using the function aquaenv. *Black line* implicit approach, *Blue circles* explicit approach expressing sensitivities of pH with partial derivatives (Eqs. 18 and 19), *Red circles* explicit approach expressing sensitivities of pH using ionization fractions (Eqs. 20 and 21). Initial values and model parameters are given in the R code in the file "AquaEnv-pHModelling.R" in the electronic appendix

investigation of the sensitivity of pH to the associated biogeochemical processes. Equation 17 specifies that the influence of a given process on pH can always be decomposed as a modulating factor, which is the sensitivity of pH with respect to that process, times the process rate. This way, one can attribute the observed pH changes in a given system to a particular processes. Using the plot.aquaenv function, this can be illustrated in a cumulative plot (Fig. 5). If the result of a model run is stored in the variable output (as done in the respective script provided in the file "AquaEnv-pHModelling.R" in the electronic appendix), the following code fragment creates Fig. 5 and saves it to the file "cumulative.eps".

5.2 Titration Simulation

In aquatic chemistry, one important experimental procedure is titration. The function titration within AquaEnv provides a tool to simulate titrations, i.e., to perform "in silico" titrations. The archetypal titration procedure involves an initial water sample to which concentrated monoprotic acid or base is added in a stepwise fashion. The titration function in AquaEnv describes how the composition of a water sample changes due to the addition of titrant solution which can be either a strong acid (typically HCl) or a strong base (typically NaOH). Titration with multiprotic acids is not accounted for.

To simulate a titration using AquaEnv, one proceeds in two steps. First, the composition of the initial water sample has to be specified. This is done via creating an *aquaenv* object by specifying salinity, temperature, and pressure, as well as the initial pH (or equivalently [TA]), and the concentrations of all total quantities. This *aquaenv* object describing the initial conditions will be the first argument of the function titration. As further arguments, one has to specify the mass of the initial sample solution (mass_sample), the concentration of the titrant (conc_titrant), the salinity of the titrant solution (S_titrant), the total mass of titrant solution added (mass_titrant),



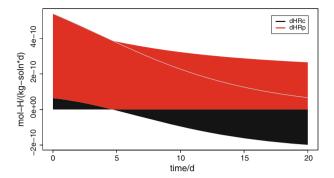


Fig. 5 Cumulative plot of the influences of kinetically modelled processes on the pH using the function plot.aquaenv. The *grey line* represents the net rate of change of the proton concentration over time and the coloured areas signify gross proton production or consumption rates due to the two processes calcium carbonate precipitation and CO₂ air—sea exchange. These gross rates adding up to the net rate represent the contribution of the two processes to the rate of change of protons and thus their influence on pH changes and proton cycling. The method of quantifying influences of processes on the pH and proton cycling is introduced and discussed by Hofmann et al. (2008), Hofmann et al. (2009a), and Hofmann et al. (2009b). **AquaEnv** implements tools to visualize those influences in a cumulative way as shown in this figure. However, a full explanation of the underlying theoretical quantification method is beyond the scope of the present publication

the number of titration steps (steps), and the type of the titrant (either a strong acid indicated by "HCl", or a strong base indicated by "NaOH" as values for the argument type with the default value "HCl"). Note that the titration simulation accounts for changes in the salinity of the titrated solution due to dilution of the original sample by the titrant (which may influence acid-base equilibria), as well as for volume changes and thus also the dilution of concentrations ($[\sum CO_2]$, etc.) due to the addition of titrant. This feature is particularly important for the treatment of pore water samples where typically small volumes and low concentration titrants are used. The logical flag seawater_titrant decides whether the titrant contains borate, sulphate, and fluoride (titration with natural seawater), or not (titration with artificial seawater). Note that, in AquaEnv, only the calculation of [TA] changes due to changes in the total quantities $[\sum B(OH)_3], [\sum H_2SO_4],$ and $[\sum HF]$ when non-seawater concentrations of borate, sulphate, and fluoride are assumed. The S, t, relations of the dissociation constants remain the ones derived for seawater. The usage and syntax of the titration function is detailed in its R help file as well as in the package vignette of AquaEnv. Example titrations expressed in R code are given in the following code fragment and in the file "AquaEnv-TitrationSimulation.R" in the electronic appendix.

Results can be visualized by plotting pH and speciation against the amount of titrant added or any other variable in the *aquaenv* object (Fig. 6). However, an *aquaenv* object containing an in silico titration can also be visualized via Bjerrum plots (Fig. 7). The respective calls to the function plot.aquaenv can be found in the file "AquaEnv-



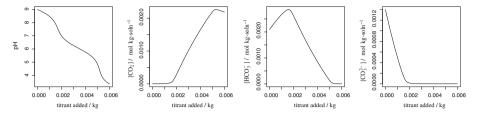


Fig. 6 Visualizing the results of an in silico titration. Note that the CO₂ concentration declines towards the right of the plot. This is due to the fact that the titration function takes into account the dilution of the dissolved inorganic carbonate concentration due to the addition of titrant

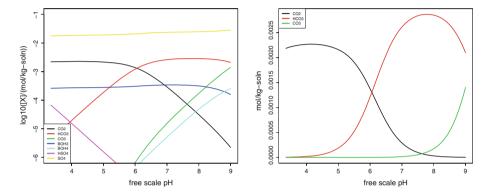


Fig. 7 *Left panel* Bjerrum plot of a selection of concentrations of dissociated species in the example in silico titration, concentrations are plotted on logarithmic scale. *Right panel* Bjerrum-like plot, concentrations are plotted on non-logarithmic scale

TitrationSimulation.R" in the electronic appendix and in the following code fragment: the first block produces the plots in Fig. 6, the second block produces the plots in Fig. 7.

The plots in Fig. 7 differ from the classical textbook Bjerrum graphs (e.g. Zeebe and Wolf-Gladrow 2001) since the effect of dilution due to the addition of titrant is accounted for (this can be seen, for example, in the left panel, in a decrease in $[SO_4^{2-}]$ from high to low pH values which is an effect of a decrease in $[\sum H_2SO_4]$ due to dilution during the titration which started at a high pH. In the right panel, this can be seen by a decrease in $[\sum CO_2]$ (the curves for the three carbonate species added up) from high to low pH values due to dilution). Although one can create a theoretical textbook Bjerrum plot which is not based on a titration experiment by creating an *aquaenv* object with a vector of [TA] values



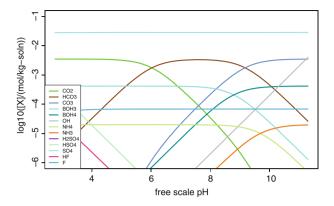


Fig. 8 Classical textbook Bjerrum plot using an in silico titration object

as input (see Fig. 3 and the corresponding code fragment), creating a textbook Bjerrum plot is also possible based on a virtual titration experiment. When simulating a titration with a rather large volume and a concentrated titrant, the volume and salinity corrections are only minor, and one obtains the classical Bjerrum graphs known from textbooks (see Fig. 8 which is produced by the following code fragment. Note that, within the precision of the plot, the total quantities do not change anymore. Note also, that we changed the list of variables to be displayed from Fig. 7, that we changed the colours for the different variables, and that we zoomed in on an interesting section. We did this to illustrate the plotting capabilities of AquaEnv).

5.3 Titration Data Analysis: Obtaining Total Alkalinity and Total Carbonate From Titration Data

The function TAfit is based on a method described in DOE (1994) and Dickson et al. (2007), makes use of the in silico titration function titration provided in AquaEnv, and allows for determining total alkalinity ([TA]), the total dissolved inorganic carbon concentration² ($[\sum CO_2]$), as well as the electrode standard potential (E_0) and the first

² Although it is possible to also determine total dissolved inorganic carbonate concentrations from closed-cell titration data analysis, Dickson et al. (2007) recommend a more accurate method of determining the total dissolved inorganic carbon concentration, not based on titration, but based on expelling all dissolved inorganic carbon in a sample as gaseous CO₂ via acidification and subsequent gas analysis. In that case, total alkalinity can be determined from open-cell titration data (see also the next paragraph).



dissociation constant of the carbonate system (K_{CO2}^*) from measured titration curves (pH versus the mass of titrant added) using an inverse modelling procedure. The Levenberg-Marquardt least squares optimization algorithm as provided in the R package minpack.lm (Elzhov and Mullen 2008) is employed to match calculated and measured titration curves.

The underlying principle of TAfit is simple: it generates an in silico titration curve (using an initial aquaenv object and the supplied parameters conc_titrant, mass_sample, S_titrant, and seawater_titrant which are passed on to the function titration) with arbitrary values for [TA], $[\sum CO_2]$, and E_0 (if an electrode potential curve is used). This in silico titration curve is then compared to the measured curve. In an iterative least-squares procedure, the arbitrary values for [TA], $[\sum CO_2]$, and E_0 are then refined to the "best-fitting" values by matching the calculated and the measured titration curve (by setting the flag verbose to TRUE, the fitting process can be visualized while it is performed). Note that, although TAfit always returns values for [TA] and $[\sum CO_2]$, the $[\sum CO_2]$ value only reflects the value of the original sample if the titration is conducted in a closed vessel to prevent equilibration with the air. Due to uncertainties in the first dissociation constant of the carbonate system K_{CO2}^* , it is sometimes advised to fit this constant in the iterative least-squares procedure as well (this can be specified in TAfit via the logical flag K CO2fit). All other dissociation constants are calculated from salinity, temperature, and pressure. This curve fitting procedure was introduced by Dickson (1981), restated in DOE (1994) and Dickson et al. (2007), and mentioned by Anderson et al. (1999) and Zeebe and Wolf-Gladrow (2001). Additionally, Dickson et al. (2007) employ an open-cell variant of this method: a [TA] value is obtained by fitting only a part of the total titration curve after the sample has been acidified to expel all carbonate from the solution. The function TAfit is also capable of fitting only a part of a titration curve: with the argument datxbegin the amount of titrant added to acidify the sample before the actual titration can be specified. The usage and syntax of the TAfit function is detailed in its R help file as well as in the package vignette of AquaEnv.

Here, the functioning of TAfit is illustrated with a simple example. Dickson (1981) provided a benchmark test for total alkalinity fitting programs in the form of a synthetic dataset. This dataset is included in AquaEnv as the object sample_dickson1981. Dickson (1981) uses fixed values for the equilibrium constants instead of calculating them as functions of salinity and temperature. TAfit allows for providing fixed values for the main dissociation constants, so the values given in Dickson (1981) can be used for the fitting procedure. As shown in the script and associated output in the following code fragment, the values for [TA] and $[\sum CO_2]$ returned by the function TAfit are exactly the same as given in Dickson (1981), i.e., the fitting procedure yields the correct values.

Note that, for computational reasons, Johansson and Wedborg (1982) and Anderson et al. (1999) suggested to switch the dependent and independent variables, i.e., to calculate a theoretical vector of titrant masses instead of a vector of theoretical pH or E values while



calculating the in silico titration curve. This has the advantage that one does not need to solve a non-linear equation system for the pH at every point of every in silico titration. However, due to the fact that in curve fitting algorithms the sum of squares of errors in the dependent variable is minimized, while errors in the independent variable are disregarded, Anderson et al. (1999) concluded that in principle the pH (or *E*) values would be the best choice as dependent variable, as their associated measurement uncertainty is larger than the measurement uncertainty for the amount of titrant added. Since nowadays computational power is not limiting anymore, we implemented the TAfit function of AquaEnv such that pH or *E* serve as dependent variables.

6 Summary

The R-package AquaEnv provides an integrated framework for acid—base speciation calculations and pH modelling. AquaEnv extends the functionality and application domain of packages like CO₂SYS (Lewis and Wallace 1998; Pierrot et al. 2006) and seacarb (Lavigne et al. 2008). The package is not only applicable to seawater, but also to brackish and freshwater environments, and it not only deals with carbonate chemistry, but also includes a large selection of other relevant acid—base systems in natural waters. We adopted an integrated programming style by letting the function aquaenv create objects of a certain class which then can be visualized and processed with the functions plot and convert, but can also be exported to an R data.frame for further processing. AquaEnv cannot only be used as a stand-alone tool for quick calculations or rapid prototyping of models, but it can also be seamlessly integrated with complex biogeochemical models in the R modelling environment. Furthermore, it provides functions that allow to simulate titrations and to calculate alkalinity and total carbonate values from measured titration data.

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7 Appendix

7.1 Components of an aquaenv Object

Maximally, i.e., if enough input data is supplied to define the pH of the system and the flags speciation, dsa, and revelle are set to TRUE, while the flag skeleton is set to FALSE upon calling the aquaenv function, an *aquaenv* object can contain the following components



Appendix

Element	Unit	Explanation
S	"psu" (no unit)	Salinity
t	°C	Temperature
р	bar	Gauge pressure (total pressure minus atmospheric pressure Feistel, 2008)
T	K	Absolute temperature
Cl	% 00	Chlorinity
I	mol/kg-H ₂ O	Ionic strength
P	bar	Total pressure
Pa	bar	Atmospheric pressure
d	m	Depth
density	kg/m ³	(Seawater) density
SumCO2	mol/kg-soln	$[\sum CO_2]$, total dissolved inorganic carbon concentration
SumNH4	mol/kg-soln	$\sum NH_4^+$, total ammonium concentration
SumH2S	mol/kg-soln	$[\sum H_2S]$, total sulfide concentration
SumHN03	mol/kg-soln	\sum HNO ₃], total nitrate concentration
SumHNO2	mol/kg-soln	$[\sum HNO_2]$, total nitrite concentration
SumH3P04	mol/kg-soln	$[\sum H_3PO_4]$, total phosphate concentration
SumSiOH4	mol/kg-soln	$\sum Si(OH)_4$, total silicate concentration
SumBOH3	mol/kg-soln	$[\sum B(OH)_3]$, total borate concentration
SumH2SO4	mol/kg-soln	$[\sum H_2SO_4]$, total sulfate concentration
SumHF	mol/kg-soln	$[\sum HF]$, total fluoride concentration
Br	mol/kg-soln	[Br ⁻], total bromide concentration
ClConc	mol/kg-soln	[Cl ⁻], chloride concentration
Na	mol/kg-soln	[Na ⁺], sodium concentration
Mg	mol/kg-soln	[Mg ²⁺], magnesium concentration
Ca	mol/kg-soln	[Ca ²⁺], calcium concentration
K	mol/kg-soln	[K ⁺], potassium concentration
Sr	mol/kg-soln	[Sr ²⁺], strontium concentration
molal2molin	(mol/kg-soln)/ (mol/kg-H ₂ O)	concentration conversion factor: from molality to molinity
free2tot	_	pH conversion factor: free scale to total scale
free2sws	_	pH conversion factor: free scale to seawater scale
tot2free	_	pH conversion factor: total scale to free scale
tot2sws	_	pH conversion factor: total scale to seawater scale
sws2free	_	pH conversion factor: seawater scale to free scale
sws2tot	_	pH conversion factor: seawater scale to total scale
KO_CO2	mol/(kg-soln*atm)	Henry's constant for CO ₂
K0_02	mol/(kg-soln*atm)	Henry's constant for O ₂
fCO2atm	atm	Atmospheric fugacity of CO ₂
f02atm	atm	Atmospheric fugacity of O ₂
CO2_sat	mol/kg-soln	CO ₂ saturation concentration at an atmospheric fugacity of fCO2atm
02_sat	mol/kg-soln	O_2 saturation concentration at an atmospheric fugacity of f02atm



Element	Unit	Explanation
K_W	(mol/kg-soln) ² , free pH scale	stoichiometric equilibrium ion product of $H_2O:K_W^* = [H^+][OH^-] \label{eq:hamiltonian}$
K_HSO4	mol/kg-soln, free pH scale	Stoichiometric equilibrium constant $K_{\text{HSO}_4^-}^* = [\text{H}^+][\text{SO}_4^{2-}]/[\text{HSO}_4^{-}]$
K_HF	mol/kg-soln, free pH scale	Stoichiometric equilibrium constant $K_{HF}^* = [H^+][F^-]/[HF]$
K_C02	mol/kg-soln, free pH scale	Stoichiometric equilibrium constant $K_{\text{CO}_2}^* = [\text{H}^+][\text{HCO}_3^-]/[\text{CO}_2]$
K_HCO3	mol/kg-soln, free pH scale	Stoichiometric equilibrium constant $K_{\text{HCO}_3^-}^* = [\text{H}^+][\text{CO}_3^-]/[\text{HCO}_3^-]$
K_BOH3	mol/kg-soln, free pH scale	Stoichiometric equilibrium constant $K_{B(OH)_3}^* = [H^+][B(OH)_4^-]/[B(OH)_3]$
K_NH4	mol/kg-soln, free pH scale	Stoichiometric equilibrium constant $K_{NH_4^+}^* = [H^+][NH_3]/[NH_4^+]$
K_H2S	mol/kg-soln, free pH scale	Stoichiometric equilibrium constant $K_{\text{H}_2\text{S}}^* = [\text{H}^+][\text{HS}^-]/[\text{H}_2\text{S}]$
K_H3P04	mol/kg-soln, free pH scale	Stoichiometric equilibrium constant $K_{\text{H}_3\text{PO}_4}^* = [\text{H}^+][\text{H}_2\text{PO}_4^-]/[\text{H}_3\text{PO}_4]$
K_H2P04	mol/kg-soln, free pH scale	Stoichiometric equilibrium constant $K_{\mathrm{H},\mathrm{PO}_{4}^{-}}^{*} = [\mathrm{H}^{+}][\mathrm{HPO}_{4}^{2-}]/[\mathrm{H}_{2}\mathrm{PO}_{4}^{-}]$
K_HP04	mol/kg-soln, free pH scale	Stoichiometric equilibrium constant $K_{\text{HPO}_{4}^{2}}^{*} = [\text{H}^{+}][\text{PO}_{4}^{3-}]/[\text{HPO}_{4}^{2-}]$
K_SiOH4	mol/kg-soln, free pH scale	Stoichiometric equilibrium constant $K_{Si(OH)_4}^* = [H^+][SiO(OH)_3^-]/[Si(OH)_4]$
K_SiOOH3	mol/kg-soln, free pH scale	Stoichiometric equilibrium constant $K_{SiO(OH)_3^-}^* = [H^+][SiO_2(OH)_2^{2-}]/[SiO(OH)_3^-]$
K_HNO2	mol/kg-soln; mol/kg- H_2O ; mol/l	Approximate value for equilibrium constant $K_{\text{HNO}_2}^* = [\text{H}^+][\text{NO}_2^-]/[\text{HNO}_2]$
K_HNO3	mol/kg-soln; mol/kg-H ₂ O; mol/l	Approximate value for equilibrium constant $K_{\text{HNO}_3}^* = [\text{H}^+][\text{NO}_3^-]/[\text{HNO}_3]$
K_H2SO4	mol/kg-soln; mol/kg-H ₂ O; mol/l	Approximate value for equilibrium constant $K_{\text{H}_2\text{SO}_4}^* = [\text{H}^+][\text{HSO}_4^-]/[\text{H}_2\text{SO}_4]$
K_HS	mol/kg-soln; mol/kg-H ₂ O; mol/l	Approximate value for equilibrium constant $K_{\mathrm{HS}^-}^* = [\mathrm{H}^+][\mathrm{S}^{2-}]/[\mathrm{HS}^-]$
Ksp_calcite	(mol/kg-soln) ²	Stoichiometric equilibrium solubility product of calcite $Ksp_{cal}^* = [Ca^{2+}][CO_3^{2-}]_{eq}$
Ksp_aragonite	(mol/kg-soln) ²	Stoichiometric equilibrium solubility product of aragonite $Ksp_{ara}^* = [Ca^{2+}][CO_3^{2-}]_{eq}$
TA	mol/kg-soln	[TA], total alkalinity
рН	-, free scale, based on mol/kg-soln	pH
fCO2	atm,	Fugacity of CO ₂ in the water
CO2	mol/kg-soln	$[CO_2]$
HCO3	mol/kg-soln	[HCO ₃]
CO3	mol/kg-soln	$[CO_3^{2-}]$
вон3	mol/kg-soln	$[B(OH)_3]$
вон4	mol/kg-soln	$[B(OH)_4^-]$



Element	Unit	Explanation
ОН	mol/kg-soln	[OH ⁻]
Н3РО4	mol/kg-soln	$[H_3PO_4]$
H2PO4	mol/kg-soln	$[H2PO_4^-]$
HPO4	mol/kg-soln	$[\mathrm{HPO_4^{2-}}]$
PO4	mol/kg-soln	$[PO_4^{3-}]$
SiOH4	mol/kg-soln	$[Si(OH)_4]$
SiOOH3	mol/kg-soln	$[SiO(OH)_3^-]$
Si020H2	mol/kg-soln	$[SiO_2(OH)_2^{2-}]$
H2S	mol/kg-soln	$[H_2S]$
HS	mol/kg-soln	[HS ⁻]
S2min	mol/kg-soln	$[S^{2-}]$
NH4	mol/kg-soln	[NH ₄ ⁺]
NH3	mol/kg-soln	[NH ₃]
H2SO4	mol/kg-soln	$[H_2SO_4]$
HSO4	mol/kg-soln	$[HSO_4^-]$
SO4	mol/kg-soln	$[SO_4^{2-}]$
HF	mol/kg-soln	[HF]
F	mol/kg-soln	[F ⁻]
HNO3	mol/kg-soln	[HNO ₃]
NO3	mol/kg-soln	$[NO_3^-]$
HNO2	mol/kg-soln	$[HNO_2]$
NO2	mol/kg-soln	$[NO_2^-]$
omega_calcite	_	Saturation state Ω with respect to calcite
omega_aragonite	_	Saturation state Ω with respect to aragonite
revelle	_	Revelle factor RF ₀
c1	_	Ionization fraction $c_1 = [CO_2]/[\sum CO_2]$
c2	_	Ionization fraction $c_2 = [HCO_3^-]/[\sum CO_2]$
с3	_	Ionization fraction $c_3 = [CO_3^{2-}]/[\sum CO_2]$
dTAdSumCO2	_	$\frac{\partial[\text{TA}]}{\partial[\sum \text{CO}_2]}$ with $[\text{TA}] = f([\text{H}^+], [\sum \text{CO}_2],)$
b1	_	Ionization fraction $b_1 = [B(OH)_3]/[\sum B(OH)_3]$
b2	_	Ionization fraction $b_2 = [B(OH)_4^-]/[\sum B(OH)_3]$
dTAdSumBOH3	_	$\frac{\partial [TA]}{\partial [\sum B(OH)_3]} \text{ with } [TA] = f([H^+], [\sum CO_2],)$
so1	_	Ionization fraction $so_1 = [H_2SO_4]/[\sum H_2SO_4]$
so2	_	Ionization fraction $so_2 = [HSO_4^-]/[\sum H_2SO_4]$
so3	_	Ionization fraction $so_3 = [SO_4^{2-}]/[\sum H_2SO_4]$
dTAdSumH2SO4	_	$\frac{\partial [TA]}{\partial [\sum H_2SO_4]} \text{ with } [TA] = f([H^+], [\sum CO_2],)$
f1	_	Ionization fraction $f_1 = [HF]/[\sum HF]$
f2	_	Ionization fraction $f_2 = [F^-]/[\sum HF]$
dTAdSumHF	_	$\frac{\partial [TA]}{\partial [\sum HF]}$ with $[TA] = f([H^+], [\sum CO_2],)$
p1	_	Ionization fraction $p_1 = [H_3PO_4]/[\sum H_3PO_4]$
p2	_	Ionization fraction $p_2 = [H_2PO_4^-]/[\sum H_3PO_4]$
p3	_	Ionization fraction $p_3 = [\text{HPO}_4^{2-}]/[\sum \text{H}_3\text{PO}_4]$
p4	_	Ionization fraction $p_4 = [PO_4^{3-}]/[\sum H_3PO_4]$



Element	Unit	Explanation
dTAdSumH3PO4	_	$\frac{\hat{\circ}[TA]}{\hat{\circ}[\sum H_3PO_4]}$ with $[TA]=f([H^+],[\sum CO_2],)$
si1	_	Ionization fraction $si_1 = [Si(OH)_4]/[\sum Si(OH)_4]$
si2	_	Ionization fraction $si_2 = [SiO(OH)_3]/[\sum Si(OH)_4]$
si3	_	Ionization fraction $si_3 = [SiO_2(OH)_2]/[\sum Si(OH)_4]$
dTAdSumSumSiOH4	_	$\frac{\delta[TA]}{\delta[\sum Si(OH)_4]}$ with $[TA]=f([H^+],[\sum CO_2],)$
s1	_	Ionization fraction $s_1 = [H_2S]/[\sum H_2S]$
s2	_	Ionization fraction $s_2 = [HS^-]/[\sum H_2S]$
s3	-	Ionization fraction $s_3 = [S^2]/[\sum H_2S]$ Note that we do assume S^2 does exist. However, s_3 is very small.
dTAdSumH2S	_	$\frac{\partial [TA]}{\partial \left[\sum H_2 S\right]}$ with $[TA] = f([H^+], [\sum CO_2],)$
n1	_	Ionization fraction $n_1 = [NH_4^+]/[\sum NH_4^+]$
n2	_	Ionization fraction $n_2 = [NH_3]/[\sum NH_4^+]$
dTAdSumNH4	_	$\frac{\partial [TA]}{\partial [\sum NH_{+}^{+}]}$ with $[TA] = f([H^{+}], [\sum CO_{2}],)$
na1	_	Ionization fraction $na_1 = [HNO_3]/[\sum HNO_3]$
na2	_	Ionization fraction $na_2 = [NO_3^-]/[\sum HNO_3]$
dTAdSumHNO3	_	$\frac{\partial [TA]}{\partial [\sum HNO_3]}$ with $[TA] = f([H^+], [\sum CO_2],)$
ni1	_	Ionization fraction $ni_1 = [HNO_2]/[\sum HNO_2]$
ni2	_	Ionization $ni_2 = [NO_2^-]/[\sum HNO_2]$
dTAdSumHNO2	-	$\frac{\delta[TA]}{\delta[\sum HNO_2]}$ with $[TA]=f([H^+],[\sum CO_2],)$
dTAdH	-	$\frac{\hat{\eth}[TA]}{\hat{\eth}[H^+]}\! :$ buffer factor with $[TA]=f([H^+],[\sum CO_2],)$
dTAdKdKdS	_	$\sum_{i} \frac{\partial [TA]}{\partial K_i^*} \frac{\partial K_i^*}{\partial S_i^*} \text{ with } [TA] = f([H^+], [\sum CO_2],, K_i^*)$
dTAdKdKdT	_	$\sum_{i} \frac{c[TA]}{\partial K_{i}^{*}} \frac{cK_{i}^{*}}{\partial t}$ with $[TA] = f([H^{+}], [\sum CO_{2}],, K_{i}^{*})$
dTAdKdKdp	_	$\sum_{i} \frac{\partial [TA]}{\partial K_{i}^{+}} \frac{\partial K_{i}^{+}}{\partial p} \text{ with } [TA] = f([H^{+}], [\sum CO_{2}],, K_{i}^{*})$
dTAdKdKdSumH2SO4	-	$\sum_{i} \frac{\partial [TA]}{\partial K_{i}^{*}} \frac{\partial K_{i}^{*}}{\partial [\sum_{\mathbf{H}_{2} \mathbf{SO}_{4}}]} \text{ with } [TA] = f([\mathbf{H}^{+}], [\sum_{i} \mathbf{CO}_{2}],, K_{i}^{*})$
dTAdKdKdSumHF	-	$\textstyle \sum_{i} \frac{\partial [TA]}{\partial K_{i}^{*}} \frac{\partial K_{i}^{*}}{\partial [\sum HF]} \text{ with } [TA] = f([H^{+}], [\sum CO_{2}],, K_{i}^{*})$

While all important references used to calculate single components of an *aquaenv* object are given in Appendix 7.2, the vignette of the AquaEnv package contains a table with more detailed information. It is listed which is the original reference, how certain formulae changed throughout different papers that reference each other, in which reference the concentration unit and the pH scale are stated, where typograpical errors have been corrected, and where certain properties needed to be inferred. Including this information, here would unnecessary lengthen this appendix.

Note that the components revelle, dTAdKdKdS, dTAdKdKdT, dTAdKdKdp, dTAdKdKdSumH2SO4, and dTAdKdKdSumHF are calculated numerically, and therefore, their calculation (induced via the flags revelle and dsa) is computationally intense. Similarly, calculating K_CO2 and K_HCO3 according to Roy et al. (1993b) which means that the intersection of the formulae for high and low salinity as a function of temperature needs to be calculated, is computationally intense.



7.2 Constants and Formulae

7.2.1 Chemical Constants Used in AquaEnv

Components of list PhysChemConst

absZero	-273.15	°C	(Dickson et al. 2007)	Absolute zero
R	83.14472	bar∗cm³ mol∗K	(Dickson et al. 2007)	Ideal gas constant (=8.314472 $\frac{J}{mol K}$, but the formulae used here (from Millero 1995), need R in $\frac{barsem^3}{mol s K}$
F	96485.3399	C/mol	(Dickson et al. 2007)	Faraday constant
е	79	_	(Zeebe and Wolf-Gladrow 2001)	Relative dielectric constant of seawater
K_HNO2	1.584893e-3	mol/l	(Riordan et al. 2005)	Approximate dissociation constant of HNO ₂ , NBS pH scale, hybrid constant
K_HNO3	23.44	mol/kg-soln	(Boudreau 1996; Soetaert et al. 2007)	Approximate dissociation constant of HNO ₃ , assumed on mol/kg-soln and free pH scale, stoichiometric constant
K_H2SO4	100	mol/kg-soln	(Atkins 1996)	Approximate dissociation constant of H ₂ SO ₄ , assumed on mol/kg-soln and free pH scale, stoichiometric constant
K_HS	1.1e-12	mol/kg-soln	(Atkins 1996)	Approximate dissociation constant of HS, assumed on mol/kg-soln and free pH scale, stoichiometric constant

Components of list MeanMolecularMass and of list ConcRelCl

The list MeanMolecularMass contains mean molecular masses in g/mol. The list is taken from Dickson et al. (2007, Chap. 5, p. 4), values are shown to 5 significant digits where available. The list ConcRelCl contains relative concentrations of key chemical species in seawater with respect to chlorinity³ (DOE (1994, Chap. 5, p. 11) and Dickson et al. (2007, Chap. 5, p. 10)).

	MeanMolecularMass	ConcRelCl
C1	35.453	0.99889
SO4	96.061	0.1400
Br	79.904	0.003473
F	18.998	0.000067
Na	22.990	0.55661
Mg	24.305	0.06626
Ca	40.078	0.02127
K	39.098	0.0206
Sr	87.62	0.00041
В	10.811	0.000232

³ Note that the given values do not sum up to 1, since chlorinity is originally defined as grams of chloride equivalents per kg of sample (which is the same as "‰" see Kremling 1999), i.e., it expresses the amount of only the anions converted to the molecular mass of chloride. Here, however, both anions and cations are listed, and the given values are related to their true molecular weight.



7.2.2 Chlorinity C1 as a Function of Salinity S

Chlorinity C1 (in ‰) is calculated from salinity S using a relation given in DOE (1994, Chap. 5, p. 11) and Zeebe and Wolf-Gladrow (2001, p. 100)

$$c1 = \frac{S}{1.80655} \tag{22}$$

7.2.3 Total Concentrations of Key Chemical Species in Seawater as a Function of Chlorinity C1

As described in DOE (1994, Chap. 5, p. 11) and Dickson et al. (2007, Chap. 5, p. 10), values in lists MeanMolecularMass and ConcRelCl are used to calculate the total concentration [X] (in mol/kg-soln) of chemical species X in seawater⁴ according to the relation

$$[X] = \frac{\text{ConcRelClX}}{\text{MeanMolecularMassX}} \text{Cl}$$
 (23)

7.2.4 Ionic Strength I as Function of Salinity S

According to DOE (1994, Chap. 5, p. 13, 15), Zeebe and Wolf-Gladrow (2001, p. 12), and Roy et al. (1993b, p. 257), I (in mol/kg-H₂O) is calculated as

$$I = \frac{19.924 \,\mathrm{S}}{1000 - 1.005 \,\mathrm{S}} \tag{24}$$

Note that the approximation $I/(\text{mol/kg-solution}) \approx 0.0199201 \text{ S}$ is given in Millero (1982, p. 428.). This relationship converted into mol/kg-H₂O, and the last digits adjusted (from 0.0199201 to 0.019924) results in the formula used here.

7.2.5 Relation Between Water Depth d and Gauge Pressure p

Although the relation between gauge pressure p (total pressure minus atmospheric pressure, see Feistel (2008)) and water depth d can be approximated by p = 0.101325 d in most cases, since p increases per m of water depth d by approximately $\frac{1}{10}$ of 1 atm (=1.01325 bar Dickson et al. (2007, Chap. 5, p. 3)), here, the more accurate relation given by Fofonoff and Millard (1983) as implemented in Soetaert et al. (2009) is used

$$d = \frac{(9.72659 + (-2.2512 \times 10^{-5} + (2.279 \times 10^{-10} - 1.82 \times 10^{-15}p)p)p)p}{g + 1.092 \times 10^{-6}p}$$
(25)

where p is the gauge pressure in dbar (decibar), and g the earth's gravity in m/s^2 g is calculated from the latitude lat (in degrees, -90 to 90, if not given, lat = 0 is assumed) as given in Fofonoff and Millard (1983) and implemented in Soetaert et al. (2009)

$$g = 9.780318 \left(1 + \left(0.0052788 + 2.36 \times 10^{-5} \sin \left(lat \frac{\Pi}{180} \right) \right) \sin \left(lat \frac{\Pi}{180} \right) \right)$$
 (26)

⁴ Note that the solution must have seawater composition, otherwise the relation given here is void.



7.2.6 Seawater density as Function of Salinity S and Temperature t

According to (Millero and Poisson 1981) as reprinted in DOE (1994, Chap. 5, p. 6f) the density of seawater $\rho_{SeaWater}$ (in $\frac{kg}{m^2}$; density in an *aquaenv* object) can be calculated as

$$\rho_{\text{SeaWater}} = \rho_{\text{Water}} + AS + BS^{1.5} + CS^2$$
(27)

$$A = 0.824493 - 4.0899 \times 10^{-3} t + 7.6438 \times 10^{-5} t^2 - 8.2467 \times 10^{-7} t^3$$
 (28)

$$+5.3875 \times 10^{-9} t^4$$
 (29)

$$B = -5.72466 \times 10^{-3} + 1.0227 \times 10^{-4} t - 1.6546 \times 10^{-6} t^{2}$$
(30)

$$C = 4.8314 \times 10^{-4} \tag{31}$$

$$\rho_{\text{Water}} = 999.842594 + 6.793952 \times 10^{-2} \text{t} - 9.095290 \times 10^{-3} \text{t}^2$$
(32)

$$+1.001685 \times 10^{-4} t^3 - 1.120083 \times 10^{-6} t^4 + 6.536332 \times 10^{-9} t^5$$
 (33)

with t representing the temperature in °C and ρ_{Water} the density of fresh water in kg/m³.

7.2.7 Gas-Exchange Constants, Dissociation Constant, and Solubility Products as Functions of Salinity S, (absolute) Temperature T, and Gauge Pressure p

Empirical formulations for the temperature and salinity dependence of all gas-exchange constants, equilibrium constants, and solubility products calculated in AquaEnv can be brought into the generic forms

$$\ln \frac{K_X}{k_0^{\circ}} = A + \frac{B}{T} + C \ln(T) + DT + ET^2$$
 (34)

or

$$\log_{10} \frac{K_X}{k_0^{\circ}} = A' + \frac{B'}{T} + C' \log_{10}(T) + D' T + E' T^2$$
(35)

or

$$\log_{10} \frac{K_X}{k_0^{\circ}} = A'' + \frac{B''}{T} + C'' \ln(T) + D'' T + E'' T^2$$
(36)

with T being the temperature in Kelvin, k_0^o the concentration unit of the constant, and A, B, C, D, E, and the respective variables with a prime (') or two primes (") being functions of salinity S. In the following we will give A, B, C, D, and E, or A', B', C', D', and E' for each calculated constant.

7.2.7.1 Gas-exchange constants (Henry's constants) as functions of salinity S and temperature T The following table shows the coefficients for Eq. 34 of gas-exchange constants in AquaEnv, with fCO₂ being the fugacity of CO₂.



K_C02: solubility of CO2 in seawater

$$A = 0.023517 \, \mathrm{S} - 167.81077 \qquad \qquad \mathrm{CO2_sat} = f \mathrm{CO_2} \, \mathrm{K_CO2}$$

$$B = 9345.17$$

$$C = 23.3585 \qquad \qquad k_0^\circ = \left[\frac{mol}{kg - solution \, atm}\right]$$

$$D = -2.3656 \times 10^{-4} \, \mathrm{S}$$

$$E = 4.7036 \times 10^{-7} \, \mathrm{S}$$

References: Weiss (1974) (original), DOE (1994, Chap. 5, p. 13), Millero (1995, p. 663), Zeebe and Wolf-Gladrow (2001, p. 257), and Dickson et al. (2007, Chap. 5, p. 12)

KO_O2: solubility of O2 in seawater (micro mol per kg-soln and atm)

```
A = -846.9978 - 0.037362 \text{ S}
B = 25559.07
C = 146.4813
D = -0.22204 + 0.00016504 \text{ S}
E = -2.0564 \times 10^{-7} \text{ S}
02\_sat = fO_2 \text{ KO\_O2}
k_0^\circ = \left[\frac{\mu mol}{kg - solution atm}\right]
```

References: derived from Weiss (1970) agrees with data in Murray et al. (1969)

Note that the formulation for K0_O2 has been derived using the formulation for a gravimetric O_2 saturation concentration given in Weiss (1970). It has been converted from ml-O₂/kg-soln to µmol-O₂/kg-soln using the molar volume of O_2 calculated with the virial equation using a first virial coefficient for oxygen at 273.15 Kelvin of -22 cm³/mol Atkins (1996), a value of 8.314472 Nm/(Kelvin mol) for the gas constant R, and an ambient pressure of 101325 N/m². The expression for the Henry's constant has then been created by dividing the expression for the saturation concentration by $fO_2 = 0.20946$ atm (Williams 2004).

7.2.7.2 Stoichiometric acid-base dissociation constants as functions of salinity S and temperature T The following table gives the coefficients for Eqs. 34, or 35, or 36 of stoichiometric acid-base dissociation constants in AquaEnv. Note that if some of the coefficients A to E are not listed, they are to be considered zero. Note also that given references sometimes contain the formulae in different units or on different pH scales. The formulae provided in this table yield the dissociation constants on different pH scales and concentration units. In AquaEnv, constants that are not already on the free pH scale and in mol/kg-soln are converted to the free pH scale and mol/kg-soln.

K_HS04: $HSO_4^- \rightleftharpoons H^+ + SO_4^{2-}$ ("dickson")	Free pH scale
$A = 324.57 \sqrt{\left(\frac{1}{m^{\circ}}\right)} - 771.54 \frac{1}{m^{\circ}} + 141.328$ $B = 35474 \frac{1}{m^{\circ}} + 1776 \left(\frac{1}{m^{\circ}}\right)^{2} - 13856 \sqrt{\left(\frac{1}{m^{\circ}}\right)} - 2698 \left(\frac{1}{m^{\circ}}\right)^{\frac{3}{2}} - 4276.1$ $C = 114.723 \frac{1}{m^{\circ}} - 47.986 \sqrt{\left(\frac{1}{m^{\circ}}\right)} - 23.093$	$ ext{K_HSO4} = \frac{[ext{H}^+]_F [ext{SO}_4^2^-]}{[ext{HSO}_4^2]} \ k^\circ = rac{ ext{mol}}{ ext{kg-H}_2 ext{O}} \ m^\circ = rac{ ext{mol}}{ ext{kg-H}_2 ext{O}}$

References: DOE (1994, c. 5, p. 13), Zeebe and Wolf-Gladrow (2001, p. 260), Dickson (1990b) (original)



K_HSO4 :HSO $_4^- \rightleftharpoons \mathrm{H}^+ + \mathrm{SO}_4^{2-}$ ("khoo")	Free pH scale
$A = 6.3451 + 0.5208 \sqrt{\frac{1}{m^2}}$ $B = -647.59$ $D = -0.019085$	$ ext{K_HSO4} = rac{[ext{H}^+]_{ ext{F}}[ext{SO}_4^{2^-}]}{[ext{HSO}_4^-]} \ k^\circ = rac{ ext{mol}}{ ext{kg-H}_2 ext{O}} \ m^\circ = rac{ ext{mol}}{ ext{kg-H}_2 ext{O}}$

References: Khoo et al. (1977) (original), Roy et al. (1993b), Millero (1995), Lewis and Wallace (1998)

$K_HF : HF \rightleftharpoons H^+ + F^- \text{ ("dickson")}$	Free pH scale
$A = 1.525 \sqrt{\frac{I}{m^{\circ}}} - 12.641$ $B = 1590.2$	$ ext{K_HF} = rac{[ext{H}^+]_F [ext{F}^-]}{[ext{HF}]} \ k^\circ = m^\circ = rac{ ext{mol}}{ ext{kg-H}_F 0}$

References: Dickson and Riley (1979a, p. 91) (original), Dickson and Millero (1987, p. 1783), Roy et al. (1993b, p. 257), DOE (1994, c. 5, p. 15), Millero (1995, p. 664), Zeebe and Wolf-Gladrow (2001, p. 260)

$K_HF : HF \rightleftharpoons H^+ + F^- \text{ ("perez")}$	Total pH scale
$A = -9.68 + 0.111\sqrt{S}$ $B = 874$	$egin{align*} ext{K_HF} &= rac{[ext{H}^+]_F [F^-]}{[ext{HF}]} \ ext{k°} &= rac{ ext{mol}}{ ext{kg-solution}} \end{aligned}$

References: Perez and Fraga (1987, p. 91) (original), Dickson et al. (2007, Chap. 5, p. 14)

 $K_{CO2}: CO_2(aq) + H_2O(\rightleftharpoons H_2CO_3) \rightleftharpoons H^+ + HCO_3^-$ ("roy"; high salinities: S > 5) Total pH scale

$$A = 2.83655 - 0.20760841\sqrt{S} + 0.08468345 S - 0.00654208 S^{\frac{3}{2}}$$

$$B = -2307.1266 - 4.0484 \sqrt{S}$$

$$K = -1.5529413$$

$$K = \frac{\text{mol}}{\text{[CO}_2(\text{aq})]}$$

$$k^{\circ} = \frac{\text{mol}}{\text{kg} - \text{H}_2\text{O}}$$

References: Roy et al. (1993b, p. 254) (original), DOE (1994, c. 5, p. 14), Millero (1995, p. 664), Zeebe and Wolf-Gladrow (2001, p. 255)

 $K_{CO2}: CO_2(aq) + H_2O(\rightleftharpoons H_2CO_3) \rightleftharpoons H^+ + HCO_3^-$ ("roy"; low salinities: $S \le 5$) Total pH scale

$$\begin{array}{ll} A = 290.9097 - 228.39774\,\sqrt{\$} + 54.20871\,\$ - 3.969101\,\$^{\frac{3}{2}} - 0.00258768\,\$^2 \\ B = -14554.21 + 9714.36839\,\sqrt{\$} - 2310.48919\,\$ + 170.22169\,\$^{\frac{3}{2}} \\ C = -45.0575 + 34.485796\,\sqrt{\$} - 8.19515\,\$ + 0.60367\,\$^{\frac{3}{2}} \end{array} \qquad \begin{array}{ll} \text{K_CO2} = \frac{[\text{H}^+][\text{HCO}_3^-]}{[\text{CO}_2(\text{aq})]} \\ k^\circ = \frac{\text{mol}}{\text{kg-H}_2\text{O}} \end{array}$$

References: Roy et al. (1993b, p. 256) (original, based on a temperature dependence restated in Millero (1979), originally given in Harned and Davis (1943). Note that there is a typesetting error in Roy et al. (1993b): the third value for B is 2310.48919, not 310.48919) Millero (1995, p. 664) (the typesetting error is corrected here). Also, here, it is mentioned that this formula should be used for $S \le 5$. Note that both functions do not always intersect at S = 5. The true intersection, a function of t, is calculated and used in AquaEnv

$\text{K_CO2}: \text{CO}_2(\text{aq}) + \text{H}_2\text{O}(\rightleftharpoons \text{H}_2\text{CO}_3) \rightleftharpoons \text{H}^+ + \text{HCO}_3^- \text{ ("lueker")}$	Total pH scale
$A'' = 61.2172 + 0.011555 \mathrm{S} - 0.0001152 \mathrm{S}^2$ $B'' = -3633.86$	$K_{CO2} = \frac{[H^+][HCO_3^-]}{[CO_2(aq)]}$
B'' = -3033.80 C'' = -9.67770	$k^{\circ} = \frac{\text{mol}}{\text{kg-solution}}$

References: Lueker et al. (2000) (original), Dickson et al. (2007, Chap. 5, pp. 13–14)



$\texttt{K_CO2}: CO_2(aq) + H_2O\left(\rightleftharpoons H_2CO_3 \right) \rightleftharpoons H^+ + HCO_3^- \text{ ("millero")}$	SW pH scale
$A'' = 126.34048 - 0.0331 \text{S} + 0.0000533 \text{S}^2 - 13.4191 \sqrt{\text{S}}$ $B'' = -6320.813 + 6.103 \text{S} + 530.123 \sqrt{\text{S}}$ $C'' = -19.568224 + 2.06950 \sqrt{\text{S}}$	$K_CO2 = \frac{[\mathrm{H}^+][\mathrm{HCO}_3^-]}{[\mathrm{CO}_2(\mathrm{aq})]}$ $k^\circ = \frac{\mathrm{mol}}{\mathrm{kg-solution}}$

References: Millero et al. (2006) (original)

K_HCO3: HCO
$$_3^ \rightleftharpoons$$
 H $^+$ + CO $_3^{2-}$ ("roy"; high salinities: S > 5)
 Total pH scale

 $A = -9.226508 - 0.106901773 \sqrt{S} + 0.1130822 S - 0.00846934 S $_2^{\frac{3}{2}}$
 K_HCO3 = $\frac{[H^+][CO_3^2]}{[HCO_3]}$
 $B = -3351.6106 - 23.9722 \sqrt{S}$
 $k^\circ = \frac{mol}{kg-H_2O}$
 $C = -0.2005743$$

References: Roy et al. (1993b, p. 254) (original), DOE (1994, c. 25, p. 15), Millero (1995, p. 664), Zeebe and Wolf-Gladrow (2001, p. 255)

K_HC03 : HCO
$$_3^ \rightleftharpoons$$
 H⁺ + CO $_3^{2-}$ ("roy"; low salinities: S ≤ 5) Total pH scale
$$A = 207.6548 - 167.69908 \sqrt{S} + 39.75854 S - 2.892532 S^{\frac{3}{2}} - 0.00613142 S^2$$

$$B = -11843.79 + 6551.35253 \sqrt{S} - 1566.13883 S + 116.270079 S^{\frac{3}{2}}$$

$$C = -33.6485 + 25.928788 \sqrt{S} - 6.171951 S + 0.45788501 S^{\frac{3}{2}}$$

$$k^\circ = \frac{\text{mol}}{\text{kg-HcO}_3}$$

References: Roy et al. (1993b, p. 256) (original, based on a temperature dependence restated in Millero (1979), originally given in Harned and Scholes (1941)), Millero (1995, p. 664) (here, it is mentioned that this formula should be used for $S \le 5$. Note that both functions do not always intersect at S = 5. The true intersection is a function of t, is calculated in AquaEnv, and is used to decide which formula to use)

K_HC03:
$$HCO_3^- \rightleftharpoons H^+ + CO_3^{2-}$$
 ("lueker")
 Total pH scale

 $A'' = -25.9290 + 0.01781 \, S - 0.0001122 \, S^2$
 K_HC03 = $\frac{[H^+][CO_3^2]}{[HCO_3]}$
 $B'' = -471.78$
 $k^\circ = \frac{m0}{kg-solution}$
 $C'' = 3.16967$

References: Lueker et al. (2000) (original), Dickson et al. (2007, Chap. 5, p. 14)

SW pH scale
K_HCO3 = $\frac{[\mathrm{H}^+][\mathrm{CO}_2^2-]}{[\mathrm{HCO}_3^2]}$ $k^\circ = \frac{\mathrm{mol}}{\mathrm{kg-solution}}$

$\mathtt{K}_\mathtt{W}:\mathtt{H}_2\mathtt{O} ightleftharpoons \mathtt{H}^+ + \mathtt{O}\mathtt{H}^-$	Total pH scale
$A = 148.9652 - 5.977 \sqrt{\$} - 0.01615 \$$ $B = -13847.26 + 118.67 \sqrt{\$}$ $C = -23.6521 + 1.0495 \sqrt{\$}$	$ extstyle K_W = [extstyle H^+][extstyle OH^-] \ k^\circ = \left(rac{ extstyle mol}{ extstyle extst$

References: Millero (1995, p. 670) (original), DOE (1994, c. 5, p. 18) (update 1997 cites Millero (1995)), Zeebe and Wolf-Gladrow (2001, p. 258), Dickson et al. (2007, Chap. 5, p. 16)



$K_BOH3 : B(OH)_3 \rightleftharpoons H^+ + \; B(OH)_4^-$	Total pH scale
$A = 148.0248 + 137.1942\sqrt{\$} + 1.62142 \$$ $B = -8966.90 - 2890.53\sqrt{\$} - 77.942 \$ + 1.728 \$^{\frac{3}{2}} - 0.0996 \2 $C = -24.4344 - 25.085\sqrt{\$} - 0.2474 \$$ $D = 0.053105\sqrt{\$}$	K_BOH3 = $\frac{[\mathrm{H}^+][\mathrm{B}(\mathrm{OH})_4]}{[\mathrm{B}(\mathrm{OH})_3]}$ $k^\circ = \frac{\mathrm{mol}}{\mathrm{kg-solution}}$

References: Dickson (1990a, p. 763) (or.), DOE (1994, c. 5, p. 14), Millero (1995, p. 669), Zeebe and Wolf-Gladrow (2001, p. 262), agrees with data in Roy et al. (1993a)

$K_NH4:NH_4^+ \rightleftharpoons H^+ + NH_3$	SW pH scale
$A = -0.25444 + 0.46532\sqrt{S} - 0.01992 S$ $B = -6285.33 - 123.7184\sqrt{S} + 3.17556 S$	$egin{align*} ext{K_NH4} &= rac{[ext{H}^+][ext{NH}_3]}{[ext{NH}_4^+]} \ k^\circ &= rac{ ext{mol}}{ ext{kg-solution}} \end{aligned}$
D = 0.0001635	Kg-solution

References: Millero (1995, p. 671), Millero et al. (1995) (original), References: corrections of Millero (1995) in Lewis and Wallace (1998) give pH scale

$K_H2S : H_2S \rightleftharpoons H^+ + HS^-$	Total pH scale
$A = 225.838 + 0.3449 \sqrt{s} - 0.0274 s$ $B = -13275.3$ $C = -34.6435$	K_H2S = $\frac{[H^+][HS^-]}{[H_2S]}$ $k^{\circ} = \frac{\text{mol}}{\text{kg-solution}}$

References: Millero (1995, p. 671), Millero et al. (1988) (original), corrections of Millero (1995) in Lewis and Wallace (1998) give pH scale

$\texttt{K_H3PO4}: \texttt{H}_3 \texttt{PO}_4 \rightleftharpoons \texttt{H}^+ + \texttt{H}_2 \texttt{PO}_4^-$	Total pH scale
$A = 115.525 + 0.69171 \sqrt{s} - 0.01844 s$ $B = -4576.752 - 106.736 \sqrt{s} - 0.65643 s$ $C = -18.453$	K_H3P04 = $\frac{[H^+][H_2PO_4^-]}{[H_3PO_4]}$ $k^\circ = \frac{\text{mol}}{\text{kg-solution}}$

References: DOE (1994, Chap. 5, p. 16), Millero (1995, p. 670), (original) Dickson et al. (2007, Chap. 5, p. 15) agrees with data in Dickson and Riley (1979b)

$K_{\mathtt{H}}PO4: H_{\mathtt{2}}PO_{\mathtt{4}}^{-} \rightleftharpoons H^{+} + HPO_{\mathtt{4}}^{2-}$	Total pH scale
$A = 172.0883 + 1.3566 \sqrt{S} - 0.05778 S$ $B = -8814.715 - 160.340 \sqrt{S} + 0.37335 S$ $C = -27.927$	$K_{-}H2P04 = \frac{[H^{+}][HPO_{4}^{2-}]}{[H_{2}PO_{4}^{-}]}$ $k^{\circ} = \frac{\text{mol}}{\text{kg-solution}}$

References: DOE (1994, Chap. 5, p. 16), Millero (1995, p. 670) (original), Dickson et al. (2007, Chap. 5, p. 15), agrees with data in Dickson and Riley (1979b)

$\texttt{K_HPO4}: \texttt{HPO}_4^{2-} \rightleftharpoons \texttt{H}^+ + \texttt{PO}_4^{3-}$	Total pH scale
$A = -18.141 + 2.81197 \sqrt{\$} - 0.09984 \$$ $B = -3070.75 + 17.27039 \sqrt{\$} - 44.99486 \$$	K_HP04 = $\frac{[H^+][PO_4^3^-]}{[HPO_4^2^-]}$ $k^\circ = \frac{\text{mol}}{k_2 \text{-solution}}$

References: DOE (1994, Chap. 5, p. 17), Millero (1995, p. 670) (original), Dickson et al. (2007, Chap. 5, p. 15), agrees with data in Dickson and Riley (1979b)



$K_SiOH4:Si(OH)_4 \rightleftharpoons H^+ + SiO(OH)_3^-$	Total pH scale
$A = 117.385 + 3.5913\sqrt{\frac{1}{m^{\circ}}} - 1.5998\frac{1}{m^{\circ}} + 0.07871\left(\frac{1}{m^{\circ}}\right)^{2}$ $B = -8904.2 - 458.79\sqrt{\frac{1}{m^{\circ}}} + 188.74\frac{1}{m^{\circ}} - 12.1652\left(\frac{1}{m^{\circ}}\right)^{2}$ $C = -19.334$	$K_SiOH4 = \frac{[H^+][SiO(OH)_3^-]}{[Si(OH)_4]}$ $k^\circ = \frac{mol}{kg-H_2O}$ $m^\circ = \frac{mol}{kg-H_2O}$

References: Millero et al. (1988) (original), DOE (1994, Chap. 5, p. 17), References: Millero (1995, p. 671)

$\texttt{K_SiOOH3}: SiO(OH)_3^- \rightleftharpoons \texttt{H}^+ + SiO_2(OH)_2^{2-}$	Total pH scale
A = 8.96 B = -4465.18	$K_SiOOH3 = \frac{[H^+][SiO_2(OH)_2^{2^-}]}{[SiO(OH)_3^{3^-}]}$ $k^{\circ} = \frac{\text{mol}}{\text{kg}_{-H_2O}}$
D = 0.021952	$\kappa = kg_{-H_2O}$

References: Wischmeyer et al. (2003) (original; incl. errata by D. Wolf-Gladrow)

7.2.8 Stoichiometric Solubility Products as Functions of Salinity S and Temperature T

The following table shows the coefficients for Eq. 35 for the stoichiometric solubility products for calcite and aragonite in AquaEnv.

Ksp_calcite: solubility product of calcite

$$A' = -171.9065 - 0.77712\sqrt{S} - 0.07711S + 0.0041249S^{1.5} \qquad \text{Ksp_cal} = [\text{CO}_3^{2-}] [\text{Ca}^{2+}]$$

$$B' = 2839.319 + 178.34\sqrt{S}$$

$$C' = 71.595 \qquad \qquad k_0^{\circ} = \left[\left(\frac{mol}{kg-solution}\right)^2\right]$$

$$D' = -0.077993 + 0.0028426\sqrt{S}$$

References: Mucci (1983) (original), Boudreau (1996, p. 160), (note that the second value for A' is -0.77712 not -0.7712 as cited in Boudreau (1996))

Ksp_aragonite: solubility product of aragonite

References: Mucci (1983) (original), Boudreau (1996, p. 160), (note that the second value for D' is 0.0017276 not 0.001727 as cited in Boudreau (1996))

7.2.9 Pressure Correction of Dissociation Constants and Solubility Products

Pressure has an effect on the stoichiometric acid-base dissociation constants, and the stoichiometric solubility products given in the previous sections. As described in Millero (1995, p. 675) using corrections and assumptions from Lewis and Wallace (1998, p. A-7), the effect of pressure can be accounted for by the equation

$$K_{\text{corr}} = K \left(-\frac{a_0 + a_1 \,t + a_2 \,t^2}{R \,T} \,p + \frac{b_0 + b_1 \,t + b_2 \,t^2}{1000 \,R \,T} \,0.5 \,p^2 \right)$$
(37)



where $K_{\rm corr}$ is the pressure corrected constant, and K is the uncorrected constant, both on matching units, e.g., mol/kg-soln, T is the absolute temperature in Kelvin, t is the temperature in °C, R is the ideal gas constant in (bar cm³)/(mol Kelvin), and p is the gauge pressure (total pressure minus one atm, see Feistel (2008) for a definition) in bar. The a and b coefficients (according to Millero (1995) which is partly a restatement of Millero (1979), corrected by Lewis and Wallace (1998)) for constants in AquaEnv (stored in the data frame DeltaPcoeffs) are given in the following table⁵.

	a_0	a_1	a_2	b_0	b_1	b_2
K_HSO4	-18.03	0.0466	0.3160×10^{-3}	-4.53	0.0900	0
K_HF	-9.78	-0.0090	-0.9420×10^{-3}	-3.91	0.0540	0
K_C02	-25.50	0.1271	0.0000×10^{-3}	-3.08	0.0877	0
K_HCO3	-15.82	-0.0219	0.0000×10^{-3}	1.13	-0.1475	0
K_W	-25.60	0.2324	-3.6246×10^{-3}	-5.13	0.0794	0
K_BOH3	-29.48	0.1622	2.6080×10^{-3}	-2.84	0.0000	0
K_NH4	-26.43	0.0889	-0.9050×10^{-3}	-5.03	0.0814	0
K_H2S	-14.80	0.0020	-0.4000×10^{-3}	2.89	0.0540	0
K_H3P04	-14.51	0.1211	-0.3210×10^{-3}	-2.67	0.0427	0
K_H2P04	-23.12	0.1758	-2.6470×10^{-3}	-5.15	0.0900	0
K_HPO4	-26.57	0.2020	-3.0420×10^{-3}	-4.08	0.0714	0
K_SiOH4	-29.48	0.1622	2.6080×10^{-3}	-2.84	0.0000	0
K_SiOOH3	-29.48	0.1622	2.6080×10^{-3}	-2.84	0.0000	0
Ksp_calcite	-48.76	0.5304	0.0000×10^{-3}	-11.76	0.3692	0
Ksp_aragonite	-45.96	0.5304	0.0000×10^{-3}	-11.76	0.3692	0

Note that, while not stated in Millero (1995), it can be inferred from Lewis and Wallace (1998) and the code given by van Heuven et al. (2009) that the pressure correction is valid for K_HF and H_H2S04 on the free scale and for all other dissociation constants on the seawater pH scale. To be consistent with Lewis and Wallace (1998) and van Heuven et al. (2009), in AquaEnv, all dissociation constants obtained from the original formulae are first converted to the free or seawater scale, respectively, using scale conversion factors with K_HF and H_H2S04 being not pressure corrected. Then, the pressure correction is applied. Subsequently, the dissociation constants are converted to the desired pH scale with scale conversion factors with K_HF and H_H2S04 being pressure corrected.

7.2.10 Conversion Factors

The following list gives the basic concentration and pH scale conversion factors used in AquaEnv. All other conversion factors in the function convert are calculated from the factors given here. Note that the factors given below are multiplicative factors that can be used to convert dissociation constants or proton concentration values. To convert pH values, one needs to use the negative decadal logarithm of the factors below as an additive term. molal2molin denotes conversion from mol/kg-H₂O to mol/kg-soln, free2tot denotes conversion from the free to the total pH scale, free2sws denotes conversion

⁵ Note that in Lewis and Wallace (1998), it is stated that the a values for H_2O and H_2S are *freshwater* values. And that the coefficients for the silicate species are assumed to be the same as the ones for the borate species.



from the free to the seawater pH scale (for a general treatment of the free, total and seawater pH scale see Dickson (1984) and Zeebe and Wolf-Gladrow (2001)), and free2nbs denotes conversion from the free to the NBS pH scale (Durst 1975).

In the previous table, S is salinity, $S_T = [SO_4^{2-}] + [HSO_4^{-}] \approx [SO_4^{2-}]$, $F_T = [HF] + [F^{-}] \approx [F^{-}]$, both in mol/kg-soln, and γ_H^+ is the activity coefficient for the proton. The dissociation constants K_HSO4 and K_HF are on the free pH scale and in mol/kg-soln as well. Note that, as given in Dickson (1984, p. 2303) and Dickson and Riley (1979a, p. 91f), all concentrations appearing in the definition for the total and the seawater pH scale are molal, i.e. mol/kg-H₂O, concentrations. But in Roy et al. (1993b, p. 257) and in DOE (1994, Chap. 4, SOP 6, p. 1), it is stated that concentrations for the seawater and total pH scale are molin, i.e., mol/kg-soln. To be consistent with DOE (1994) and Dickson et al. (2007), mol/kg-soln is chosen here for the free, total, and seawater scale. To be consistent with Lewis and Wallace (1998), the NBS scale in AquaEnv is based on the proton concentration in mol/kg-H₂O.

7.2.11 Activity Coefficient for the Proton

In AquaEnv, a complex ion-interaction model like, e.g., Millero and Pierrot (1998), is not implemented. According to Zeebe and Wolf-Gladrow (2001), the activity coefficient for the proton $\gamma_{\rm H}^+$ can be approximated by the Davies equation as long as the ionic strength of the solution in question remains below 0.5 mol/kg-H₂O. This means for solutions with a salinity of less than 24.48. Since NBS scale pH values are normally not used for open ocean applications but mainly in brackish and fresh waters, the Davies equation has been assumed to be a sufficient approximation for $\gamma_{\rm H}^+$. Important to note, however, is that the conversion from and to the NBS pH scale in AquaEnv for salinities above 24.48 is only an approximation. The Davies equation is used as given in Zeebe and Wolf-Gladrow (2001)

$$\gamma_{\rm H^+} = 10^{-\left(1.82\,10^6\,(\rm e\,T)^{-\frac{3}{2}}\right)\left(\frac{\sqrt{(\rm I)}}{1+\sqrt{(\rm I)}}0.2\,\rm I\right)} \tag{38}$$

where e is the relative dielectric constant of seawater (PhysChemConst\$e in Aqua-Env), T is the temperature in Kelvin, and T is the ionic strength in mol/kg-H₂O. Note that the squared charge of the ion before the brackets with the ionic strength terms which is present in the generic form of the Davies equation has been omitted here since for the proton, this factor is 1.

7.2.12 The Revelle Factor

In Zeebe and Wolf-Gladrow (2001, p. 73), the revelle factor is given as

$$RF_{0} = \left(\frac{d[CO_{2}]}{[CO_{2}]} \middle/ \frac{d[\sum CO_{2}]}{[\sum CO_{2}]}\right)_{[TA]=const.} = \left(\frac{d[CO_{2}]}{d[\sum CO_{2}]}\right)_{[TA]=const.} \frac{[\sum CO_{2}]}{[CO_{2}]}$$
(39)



The subscript "[TA] = const." indicates that this expression is not based on a function of the form

$$[CO_2] = f([H^+], [\sum CO_2]) = \frac{[H^+]^2}{[H^+]^2 + K_{CO_2}^*[H^+] + K_{CO_3}^* K_{HCO_3}^*} [\sum CO_2]$$
(40)

which would have analytical expressions for the partial derivatives $\frac{\partial [CO_2]}{\partial [\sum CO_2]_{[H^+]=const}}$ and

 $\frac{\hat{c}[CO_2]}{\hat{c}[H^+]} \sum_{CO_2 = const}$ (note that the subscripts indicating which variable is held constant can be

omitted since an exhaustive list of variables is given), but on a function of the form

$$[CO_2] = f([TA], \left[\sum CO_2\right]) \tag{41}$$

which does not have an analytical form (since it involves the solution of a non linear system of equations to calculate $[H^+]$ and thus $[CO_2]$), and therefore, there is also no analytical expression for $\frac{\hat{o}[CO_2]}{\hat{o}\left[\sum CO_2\right]_{|TA|=const}}$.

For this reason, in AquaEnv, the Revelle factor (aquaenv object component revelle) is calculated numerically by slightly disturbing $[\sum CO_2]$ and calculating [CO2] for the disturbed and the undisturbed case.

7.2.13 Partial Derivatives of Total Alkalinity

The values for dTAdKdKdS, dTAdKdKdT, dTAdKdKdd, dTAdKdKdSumH2SO4, and dTAdKdKdSumHF are calculated numerically as described in Hofmann et al. (2009a).

The values for dTAdH, dTAdSumCO2, dTAdSumBOH3, dTAdSumH2SO4, and dTAdSumHF are calculated analytically as given in Hofmann et al. (2008).

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