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Characterization of tissue structure at varying length scales using temporal diffusion spectroscopy[†]

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The concepts, theoretical behavior and experimental applications of temporal diffusion spectroscopy are reviewed and illustrated. Temporal diffusion spectra are obtained using oscillating-gradient waveforms in diffusion-weighted measurements, and represent the manner in which various spectral components of molecular velocity correlations vary in different geometrical structures that restrict or hinder free movements. Measurements made at different gradient frequencies reveal information on the scale of restrictions or hindrances to free diffusion, and the shape of a spectrum reveals the relative contributions of spatial restrictions at different distance scales. Such spectra differ from other so-called diffusion spectra which depict spatial frequencies and are defined at a fixed diffusion time. Experimentally, oscillating gradients at moderate frequency are more feasible for exploring restrictions at very short distances which, in tissues, correspond to structures smaller than cells. We describe the underlying concepts of temporal diffusion spectra and provide analytical expressions for the behavior of the diffusion coefficient as a function of gradient frequency in simple geometries with different dimensions. Diffusion in more complex model media that mimic tissues has been simulated using numerical methods. Experimental measurements of diffusion spectra have been obtained in suspensions of particles and cells, as well as *in vivo* in intact animals. An observation of particular interest is the increased contrast and heterogeneity observed in tumors using oscillating gradients at moderate frequency compared with conventional pulse gradient methods, and the potential for detecting changes in tumors early in their response to treatment. Computer simulations suggest that diffusion spectral measurements may be sensitive to intracellular structures, such as nuclear size, and that changes in tissue diffusion properties may be measured before there are changes in cell density. Copyright © 2010 John Wiley & Sons, Ltd.

Keywords: diffusion MRI; diffusion spectroscopy; oscillating gradients; tissue structure

INTRODUCTION

Self-diffusion describes the process by which molecules migrate from place to place within a fluid via random movements. The randomness is a consequence of frequent intermolecular collisions that are a characteristic of Brownian motion. Even in a uniform fluid in an infinite space, the mean distance moved by a

molecule in a given time interval is limited by the average speed of molecular motions (which depends strongly on temperature and molecular weight) and the likelihood of encountering another mass in a collision that may cause a change in direction. Inherently, therefore, diffusion connotes the influence of collisions that introduce hindrances to unrestricted molecular displacements. In pure water, these collisions happen very

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Abbreviations used: ADC, apparent diffusion coefficient; BCNU, 1,3-bis(2-chloroethyl)-1-nitrosourea; DWI, diffusion-weighted imaging; OGSE, oscillating-gradient spin echo; PGSE, pulsed-gradient spin echo; RF, radio-frequency.

frequently, and each molecular jump is very small. For water molecules in dilute solutions of other small molecules, the number and nature of such collisions may not be much different from the pure solvent, so that the rate of water diffusion is little changed. However, as the concentration and size of solutes increase, the rate of water diffusion may be expected to decrease. When the sizes and spacings of structures that hinder diffusion become comparable with the distance moved in the time over which movements are observed experimentally, the motion appears to be restricted and the measured diffusion rate reflects the number and nature of such barriers. This appears to be the case for water molecules in cellular tissues, but, at present, we do not possess a clear idea of what structures are responsible for affecting free diffusion at different spatial and temporal scales.

Stochastic processes can be described by various statistical properties. For water molecules undergoing self-diffusion, an important parameter is the instantaneous particle velocity \mathbf{v} , which, in a pure liquid, changes randomly with time at a rate that depends on the collision frequency. In a simple liquid, there is little correlation between the values of \mathbf{v} at different times (t), even when these are spaced closely together, and so the *autocorrelation* function of $\mathbf{v}(t)$ is very narrow. However, when there are spatial obstructions that hinder diffusion over multiple collisions, the velocity acquires a degree of correlation over time that depends on the dimensions and spacings of the obstructions. The shape of the autocorrelation function of \mathbf{v} then contains information about the structure of the medium (1). Formally, this autocorrelation A can be written as:

$$A(t) = \langle \mathbf{v}(\tau) \mathbf{v}(t + \tau) \rangle \quad [1]$$

where the average is over all values of the interval τ . The spectral density of the molecular velocity correlations is given by the Fourier transform of A , which corresponds to a frequency-dependent diffusion tensor, $\mathbf{D}(\omega)$ (2):

$$D_{ij} = \int_0^\infty dt' \exp(i\omega t') \langle v_i(t') v_j(0) \rangle \quad [2]$$

where i and j refer to the Cartesian directions x , y and z . For free diffusion, A is essentially infinitesimally narrow, and the spectrum of the tensor $\mathbf{D}(\omega)$ is flat to a very high frequency, of the order of the intermolecular collision frequency. However, when diffusion is restricted, the autocorrelation function broadens and acquires a negative dip, consistent with a picture in which barriers rectify isotropic diffusion and induce negative correlations between the velocities at different times (2–4). Then, $\mathbf{D}(\omega)$ is no longer flat, but falls off at low frequencies. The manner in which $\mathbf{D}(\omega)$ disperses with frequency can provide unique information on the structure of the medium. The characterization of materials by measurement of the diffusion spectrum is termed *temporal* diffusion spectroscopy, as distinct from other diffusion techniques, such as q -space approaches, that record spectra of *spatial* frequencies or wavevectors (4,5). The theory and interpretation of temporal diffusion spectra, together with experimental applications, have been discussed previously by others, for example, in (2,3,6).

A diffusion spectrum can be measured at single, specific frequencies, or the contributions of multiple frequencies can be simultaneously assessed by an appropriate choice of diffusion gradient. In general, if a diffusion-weighting gradient $\mathbf{g}(t)$ is

applied, its time integral is f :

$$\mathbf{f}(t') = \int_0^{t'} \mathbf{g}(t) dt \quad [3]$$

This has a frequency spectrum $\mathbf{F}(\omega)$:

$$\mathbf{F}(\omega) = \int_{-\infty}^{\infty} dt \exp(i\omega t) \int_0^t \gamma \mathbf{g}(t') dt' \quad [4]$$

The echo amplitude following a diffusion-weighting gradient, $\mathbf{g}(t)$, is given (2) by:

$$S = S_0 \exp \left[-\frac{1}{\pi} \int_0^{\infty} \mathbf{F}(\omega) \mathbf{D}(\omega) \mathbf{F}(-\omega) d\omega \right] \quad [5]$$

where S_0 is the signal magnitude in the absence of the diffusion-weighting gradient. $\mathbf{F}(\omega)$ can be considered as a sampling function which determines the weightings of different contributions of the spectrum $\mathbf{D}(\omega)$ to the measurement. In practice, for a gradient in any single direction, $\mathbf{F}(\omega)$ is a vector whose magnitude is the pulse modulation, $F(\omega)$. When it has a narrow spectral spread, only narrow ranges within $\mathbf{D}(\omega)$ contribute to the diffusion signal losses. Appropriately designed oscillating-gradient waveforms can be used to sample $\mathbf{D}(\omega)$ at well-defined frequencies and, by changing this frequency, the shape of $\mathbf{D}(\omega)$ can be determined. It should be noted that conventional pulsed-gradient spin echo (PGSE) measurements of the apparent diffusion coefficient (ADC) use relatively long diffusion intervals and gradient pulses of finite width. From eqns (3)–(5), these correspond to the assessment of the integrated contributions of a small range of values of $\mathbf{D}(\omega)$ centered around $\omega=0$, and do not distinguish the contributions of the high-frequency part of the spectrum.

We have implemented and evaluated temporal diffusion spectra in various model, cell and animal systems by implementing oscillating-gradient spin echo (OGSE) pulse sequences. Below, we summarize some of these studies and discuss the advantages of this approach compared with other methods. In particular, we emphasize that conventional MRI methods used to measure diffusion in tissues reflect the integrated effects of a variety of structural features, including those arising at a relatively large spatial scale, on the order of a cell diameter, such as cell membranes. Many other factors may influence the free movement of water, including changes in intracellular organization and the presence of smaller scale restrictions, but their effects will be indistinguishable in the presence of restrictions occurring over larger dimensions if the measurement is made with conventional methods. Studies of ADC with PGSE methods record signal changes caused by diffusion over a specific interval, the diffusion time Δ . Because of technical constraints on the design of gradients and the overall sensitivity of MRI, almost all current and published measurements of ADC correspond to the regime of ‘long’ diffusion intervals. In practice, Δ is at least several milliseconds, and so, by using the Einstein relation, ADC reflects the influence of restricting boundaries on the order of $>5\text{--}15 \mu\text{m}$. Thus, differences between tissues detected by current PGSE methods, such as changes in cellularity in tumors, reflect alterations in the number, permeability and separation of boundaries on the whole-cell scale. Such ADC

measurements include the effects of restricting boundaries on at least this dimension, and are incapable of providing insights into the factors affecting diffusion at finer scales within the cells and pores within tissues, unless Δ is very short. Furthermore, they cannot reveal the scale of the boundaries unless measurements are made in a regime before all molecules encounter the restricting barrier in the time Δ . This is not usually practical using PGSE methods because extremely strong gradients are needed to produce measurable diffusion attenuation in times of less than 1 ms. Oscillating-gradient techniques at even moderate frequencies are capable of detecting restrictions to diffusion displacements over a specific spatial scale much smaller than the diameter of a single cell, thereby resulting in a greater sensitivity, specifically to the contributions of variations in subcellular structures to the measured ADC. In this review of recent studies, we analyze the theoretical basis of temporal diffusion spectra, show how such measurements are expected to behave in various simple geometries, and illustrate the use of this method for providing greater image contrast and detecting increased structural heterogeneity in tumors. We also show how this method can be more sensitive to early changes in the treatment response of tumors.

EXPERIMENTAL APPROACH

Figure 1 shows pulse sequences that may be used to acquire diffusion spectra. In our experimental work, we first began with a sine-modulated gradient waveform, as originally proposed by Gross and Kosfeld (7). For an ideal (infinite duration) sine-modulated gradient pulse of frequency ω_m , the spectral

density of the dephasing takes the form:

$$F(\omega) \propto \Im \left[\int_0^t \sin(\omega_m t') dt' \right] \\ \propto \delta(\omega) - \frac{\pi}{\omega_m} (\delta(\omega + \omega_m) + \delta(\omega - \omega_m)) \quad [6]$$

where \Im denotes the Fourier transform [eqn (4)]. The signal amplitude produced using such a gradient will be affected by both $\mathbf{D}(0)$ and $\mathbf{D}(\omega_m)$. However, for a cosine-modulated gradient pulse, the zero-frequency component does not contribute:

$$F(\omega) \propto \Im \left[\int_0^t \cos(\omega_m t') dt' \right] \\ \propto \frac{i\pi}{\omega_m} (\delta(\omega + \omega_m) - \delta(\omega - \omega_m)). \quad [7]$$

We have designed and implemented pulses to approximate this cosine modulation (4,8). For a relatively long pulse, the power spectrum becomes:

$$|F(\omega)|^2 = \frac{\pi^2 g^2 \gamma^2}{\omega_m^2} [\delta(\omega + \omega_m) - \delta(\omega - \omega_m)]^2. \quad [8]$$

where g is the gradient strength, γ is the gyromagnetic ratio and ω_m is the modulation frequency. In practice, the pulses must be apodized in time in an NMR experiment, which broadens each δ function and the range of spectral components that contribute.

The cosine-OGSE poses the challenge of a sharp initial pulse edge (see Fig. 1). Experimentally, we smoothed this initial transient by replacing the first quarter-cycle cosine with a half-cycle sine-lobe at twice the base frequency, which reduces the need for a very short coil rise time. Sample pulses and

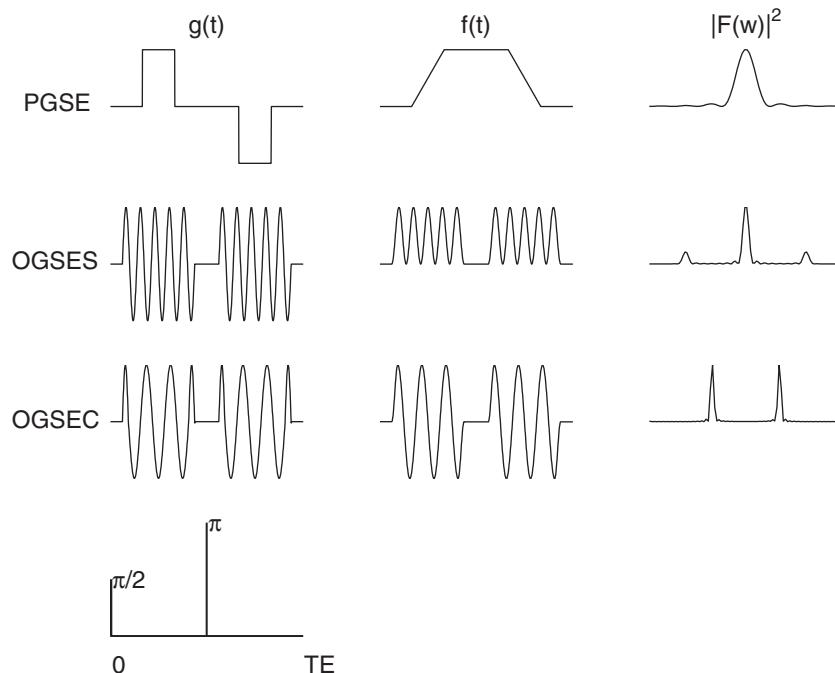


Figure 1. The amplitude (g), time integral (f) and spectra (F) corresponding to sine-modulated (OGSES) and cosine-modulated (OGSEC) oscillating-gradient waveforms. At the top is the pulsed-gradient spin echo (PGSE) waveform for comparison. The PGSE spectrum is centered around zero frequency, whereas the cosine-modulated waveform isolates discrete frequencies.

their spectra are shown in Fig. 1 alongside those of a conventional PGSE sequence. The separation of the diffusion gradient pulses into two halves to allow for the radiofrequency (RF) π -pulse in a spin echo results in a small broadening of the peaks (8).

The b value represents the amount of diffusion weighting imparted by pulsed or oscillating magnetic field gradients. It can be defined as the total power of spin dephasing over the diffusion preparation time:

$$b = \int_0^{2\tau} dt \left[\gamma \int_0^t g(t') dt' \right]^2 \quad [9]$$

For a simple cosine-modulated waveform:

$$b = \frac{\gamma^2 G^2 \sigma}{4\pi^2 f^2} \quad [10]$$

where G is the peak gradient magnitude, f is the frequency and σ is the duration of the waveform.

The effective diffusion time Δ_{eff} for oscillating gradients is not trivially defined in restrictive geometries, similar to the case for time-dependent diffusion coefficients measured using other gradient pulses of finite duration (9). However, it is clear that Δ_{eff} decreases as f , the frequency, increases. Parsons *et al.* (4) adopted the formalism of Fordham *et al.* (9) and showed that $\Delta_{\text{eff}} = 1/4f$ for unrestricted diffusion (the zeroth order case), and how this must be modified for restricting pores. For cosine-modulated gradients oscillating at 1 kHz, the effective diffusion time in free media is approximately 250 μ s, much shorter than typically achieved with PGSE methods.

TEMPORAL DIFFUSION SPECTROSCOPY IN SIMPLE GEOMETRIES

The interpretation of temporal diffusion spectra may be helped by considering how we expect OGSE data to behave for specific simple geometries. To this end, we have evaluated analytical expressions for the behavior of $\mathbf{D}(\omega)$ in simple geometries. The derivation of these expressions was presented in (3,10), where their accuracy was confirmed using elaborate computer simulations. It has been shown previously that the diffusion-weighted echo signal can be described as (2):

$$\begin{aligned} E(2\tau) &= \exp[-\beta(2\tau)] \\ &= \exp \left\{ -\frac{\gamma^2}{2} \int_0^{2\tau} dt_1 \int_0^{2\tau} dt_2 \mathbf{g}(t_1) \langle \mathbf{r}_1(t_1) \mathbf{r}_2(t_2) \rangle \mathbf{g}(t_2) \right\} \quad [11] \end{aligned}$$

where β is the signal echo attenuation factor, τ is half of the echo time, \mathbf{r}_i is the water molecule position at time t_i , \mathbf{g} is the diffusion gradient and $\langle \rangle$ denotes the ensemble average. In the presence of diffusion restrictions, a conditional probability P , which describes the likelihood that a spin at position \mathbf{r}_1 at time t_1 will be at position \mathbf{r}_2 at time t_2 , may be introduced, which can be expressed in a general solution as (3):

$$P(\mathbf{r}_1, t_1 | \mathbf{r}_2, t_2) = \sum_n \exp(-\lambda_n D |t_1 - t_2|) u_n(\mathbf{r}_1) u_n^*(\mathbf{r}_2) \quad [12]$$

where D is the intrinsic diffusion coefficient and $u_n(\mathbf{r})$ are orthogonal functions that describe the geometry. By substituting

eqn (12) into eqn (11), Stepisnik (3) obtained the signal echo attenuation:

$$\begin{aligned} \beta(2\tau) &= \frac{\gamma^2}{2} \int_0^{2\tau} dt_1 \int_0^{2\tau} dt_2 \int_V d\mathbf{r}_1 \int_V d\mathbf{r}_2 \rho(\mathbf{r}_1, t_1) P(\mathbf{r}_1, t_1 | \mathbf{r}_2, t_2) \mathbf{r}_1 \mathbf{g}(t_1) \mathbf{r}_2 \mathbf{g}(t_2) \\ &\quad \frac{1}{2} \sum_n B_n \int_0^{2\tau} dt_1 \int_0^{2\tau} dt_2 \exp(-\lambda_n D |t_2 - t_1|) g(t_1) g(t_2) \end{aligned} \quad [13]$$

where ρ is the spin density, $\mathbf{g}(t) = \hat{g}(t)\hat{\mathbf{g}}$, and $\hat{\mathbf{g}}$ is a unit vector along the gradient direction. B_n and λ_n are structure-dependent coefficients. Assuming a uniform distribution of spins (set equal to unity):

$$B_n = \int_V d\mathbf{r}_1 \int_V d\mathbf{r}_2 \hat{\mathbf{g}} \hat{\mathbf{r}}_1 \hat{\mathbf{g}} \hat{\mathbf{r}}_2 u_n(\mathbf{r}_1) u_n(\mathbf{r}_2) \quad [14]$$

B_n and λ_n describe the specific geometrical features of any system and, once known, they allow the diffusion attenuation to be computed for different times. For example, for diffusion between two impermeable planes separated by a distance d , where the gradient is perpendicular to the planes:

$$B_n = \frac{8d^2}{(2n-1)^4 \pi^4} \text{ and } \lambda_n = \frac{\pi^2 (2n-1)^2}{d^2}. \quad [15]$$

For diffusion inside an impermeable cylindrical geometry with a radius R and gradients in the direction perpendicular to the axis of the cylinder:

$$B_n = \frac{2(R/\mu_n)^2}{\mu_n^2 - 1} \text{ and } \lambda_n = \left(\frac{\mu_n}{R} \right)^2. \quad [16]$$

where μ_n is the n th root of $J_1'(\mu) = 0$ and J_1 is a Bessel function of the first kind. For a spherical geometry, the expression for B_n is:

$$B_n = \frac{2(R/\mu_n)^2}{\mu_n^2 - 2} \quad [17]$$

and λ_n are the same as for a cylindrical geometry, except μ_n becomes the n th root of $\mu J_{3/2}'(\mu) - \frac{1}{2} J_{3/2}(\mu) = 0$ (3).

For diffusion inside an impermeable spherical shell ($a < r < b$), we derived the analytical expression for the conditional probability (10) as:

$$\begin{aligned} P(\mathbf{r}, t | \mathbf{r}_0, 0) &= \frac{3}{4\pi(b^3 - a^3)} \\ &\quad + \sum_{n=1}^{\infty} \sum_{m=1}^{\infty} A_{nm} U_n(\lambda_{nm} r) P_n(\cos \theta) \\ &\quad \times U_n(\lambda_{nm} r_0) P_n(\cos \theta_0) \exp(-\lambda_{nm}^2 Dt) \end{aligned} \quad [18]$$

where:

$$A_{nm} = \frac{(2n+1)\lambda_{nm}^6 a^3 b^3}{2\pi \left\{ a^3 [\lambda_{nm}^2 b^2 - n(n+1)] \left[\frac{j_n'(\lambda_{nm} a)}{j_n'(\lambda_{nm} b)} \right]^2 - b^3 [\lambda_{nm}^2 a^2 - n(n+1)] \right\}} \quad [19]$$

$$U_n(\lambda_{nm} r) = y_n'(\lambda_{nm} a) j_n(\lambda_{nm} r) - j_n'(\lambda_{nm} a) y_n(\lambda_{nm} r) \quad [20]$$

and λ_{nm} is the m th root of the equation:

$$y_n'(\lambda_{nm} a) j_n'(\lambda_{nm} b) = j_n'(\lambda_{nm} a) y_n'(\lambda_{nm} b), \quad [21]$$

where $j_n(r) = r^{-1/2} J_{n+1/2}(r)$ and $y_n(r) = r^{-1/2} Y_{n+1/2}(r)$, $J_{n+1/2}$ and $Y_{n+1/2}$ are Bessel functions of the first and the second kind,

respectively. Equations (18) and (21) yield the B_n coefficient for this geometry as:

$$B_n = \frac{2a^3 b^3 [j'_1(\lambda_n a) - j'_1(\lambda_n b)]^2}{\lambda_n^2 (b^3 - a^3) \{a^3 (\lambda_n^2 b^2 - 2) j'_1 2(\lambda_n a) - b^3 (\lambda_n^2 a^2 - 2) j'_1 2(\lambda_n b)\}}. \quad [22]$$

Based on the theory introduced above, we derived analytical expressions for the diffusion-induced echo attenuation obtained with the cosine-OGSE waveform in these simple situations (10). Using a gradient g at frequency ω for a duration σ , analytical expressions for signal echo attenuation can be obtained. The result is:

$$\beta(2\tau) = 2(\gamma g)^2 \sum_n \frac{B_n \lambda_n^2 D^2}{(\lambda_n^2 D^2 + \omega^2)^2} \left\{ \frac{\lambda_n^2 D^2 + \omega^2}{(\lambda_n D)} \left[\frac{\sigma}{2} + \frac{\sin(2\omega\sigma)}{4\omega} \right] - 1 + \exp(-\lambda_n D\sigma) + \exp(-\lambda_n D\tau)(1 - \cosh(\lambda_n D\sigma)) \right\} \quad [23]$$

where D is the intrinsic diffusion coefficient and τ is half of the echo time. We have previously reported our computational approach to simulating diffusion effects in NMR using a finite difference approach (11). These analytical expressions have been validated by comparing their predictions with those of computer simulations of diffusion in simple systems (10).

Diffusion between two parallel planes

The elementary case of diffusion between two infinitely large impermeable parallel planes using the cosine-OGSE waveform is shown in Fig. 2 for different separations of the planes. This example illustrates the major physical effects of restricted diffusion and how these interact with the OGSE parameters. A one-dimensional gradient was considered perpendicular to the planes and the distance between the planes was varied from 1 to 10 μm , the latter corresponding to a typical human cell size. Figure 2 shows the behavior of $\mathbf{D}(\omega)$ for different frequencies. At low frequencies, ADC is highly reduced (highly restricted) for all spacings of the planes, but ADC shows a very rapid increase with increasing diffusion gradient frequency that depends on the spacing. This is equivalent to the observation that ADC measured by PGSE methods tend to zero as the diffusion time Δ tends to infinity. For the larger separations, at frequencies beyond 1 kHz, there is little dispersion and ADC is close to the case of free water.

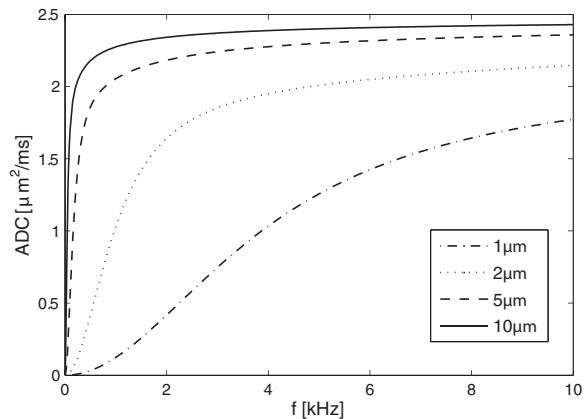


Figure 2. Calculated values of the apparent diffusion coefficient (ADC) as a function of frequency for diffusion between two infinite impermeable planes for different spacings. The dispersion with increasing frequency is initially much more rapid for larger separations.

For the smaller separations, ADC is still only a small fraction of the free value even at frequencies of 2 kHz. These curves illustrate an important practical point: if the gradient waveform contains very low frequencies, ADC for all these geometries is similar, and therefore, in a PGSE diffusion-weighted image, there would be very little contrast between structures with different spacings. However, if a gradient at, for example, 1 kHz is used, there would be a large difference in the signals from each of these samples, and so there would be contrast between regions of different structure. The magnitude of the contrast would depend on the specific frequency used, and this can be ‘tuned’ to maximize the distinctions between structures of specific spatial length scales.

Diffusion in other simple restricted compartments

Figure 3 depicts the behavior of ADC as a function of frequency in other simple geometries. Figure 3a shows the result of evaluating the analytical expression for diffusion in a cylinder of infinite length with an impermeable surface for different diameters of 1–10 μm . The gradient is applied perpendicular to the long axis of the cylinder. Figure 3b shows the results for diffusion in spheres of different diameter. Qualitatively, these graphs are similar to the case for the infinite plane. Again, tuning the gradient frequency to a specific high frequency will increase the distinction between two objects of different size. Using even a moderate frequency (a few

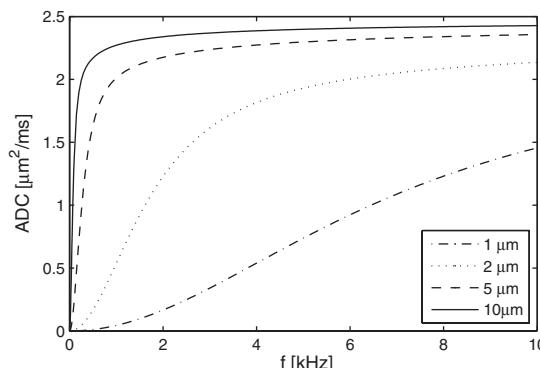
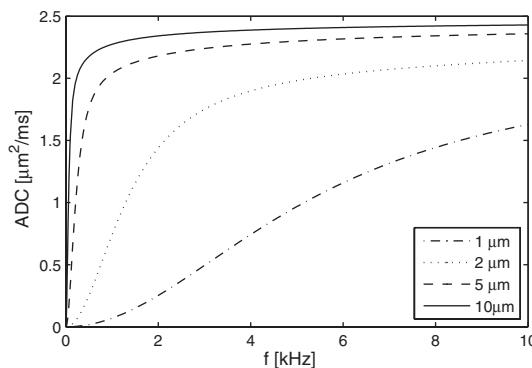


Figure 3. Theoretical behavior of the apparent diffusion coefficient (ADC) as a function of frequency for restricted diffusion in a single compartment. (a) Left: diffusion in cylinders of different diameters. (b) Right: diffusion in spheres of different diameters. The differences in ADC values for different-sized compartments depend on the selection of the gradient frequency.

hundred hertz) will provide greater contrast between objects smaller than 10 μm than the use of low- or zero-frequency measurements, in which all sizes show restricted behaviors.

Diffusion in more complex multicompartment systems

Xu *et al.* (10) have expanded on the use of these theoretical behaviors in simple geometries and employed computer simulations to study diffusion in more realistic, tissue-mimicking systems. For example, cylinders placed on a square lattice may roughly simulate white matter or other fibrous materials. Figure 4 shows an array of infinitely long cylinders, each with an impermeable surface, in which water may be either inside a cylinder or in the spaces between them. Figure 4 also shows the manner in which ADC of water would behave as a function of frequency. In this case, the diffusion gradients are perpendicular to the axis of the cylinders. It has been reported that water exchange between axons and the extracellular space is intermediate or slow (12), and so here the interface permeability was

again set equal to zero. There is restricted diffusion inside the cylinder and hindered diffusion in the extracellular space (13). The total signal echo attenuation from such a model tissue is then simply the sum of the signals arising from the two compartments:

$$E = f_{\text{axon}} \exp(-\beta(2\tau)) + (1 - f_{\text{axon}}) \exp(-bD_{\text{ex}}), \quad [24]$$

where $\beta(2\tau)$ is the signal echo attenuation of water inside axons, D_{ex} is the hindered diffusion coefficient of the extracellular space and f_{axon} is the volume fraction of axons. It should also be noted that Fig. 4 also implicitly shows how the fractional anisotropy of the cylinders would depend on the choice of frequency.

In Xu *et al.* (10), we reported the behavior of OGSE spectral measurements in a more realistic model consisting of close-packed spherical cells, each containing a spherical nucleus (see Fig. 5). In this model system, there are three distinct compartments containing water, corresponding to intranuclear, cytoplasmic and extracellular spaces. Each component can be ascribed its own intrinsic parameters, including proton density, T_2 and water self-diffusion coefficient. To highlight the effects of diffusion only,

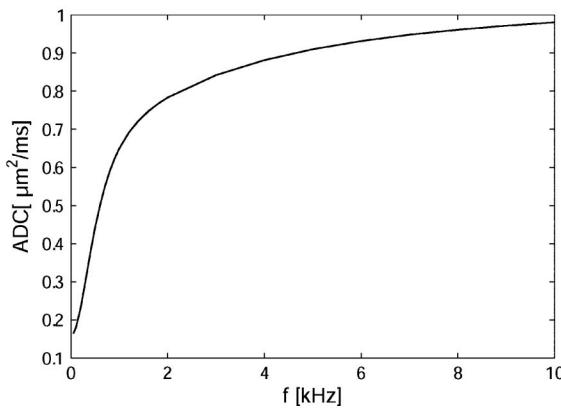
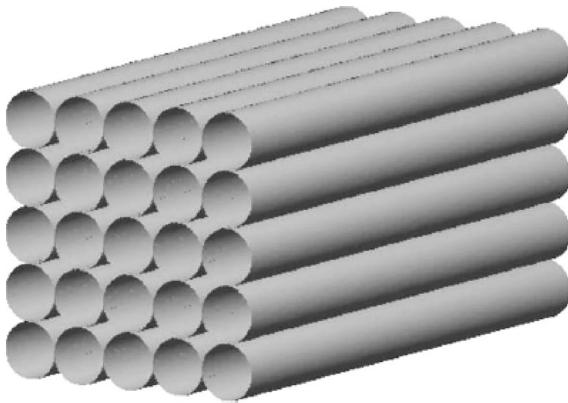


Figure 4. Left: array of cylindrical fibers considered as a simple model of white matter. Right: predicted behavior of the apparent diffusion coefficient (ADC) as a function of frequency. For this curve, the intra- and extracellular diffusion coefficients are taken as 1.0 and 2.0 $\mu\text{m}^2/\text{ms}$, respectively, the cylinders have a diameter of 1.96 μm and the lattice spacing is 2.1 μm , so that the cylinder volume fraction is 75.25%. Other details of the simulation are given in (10). Note the sharp inflection of the curve between 1 and 2 kHz for this size system.

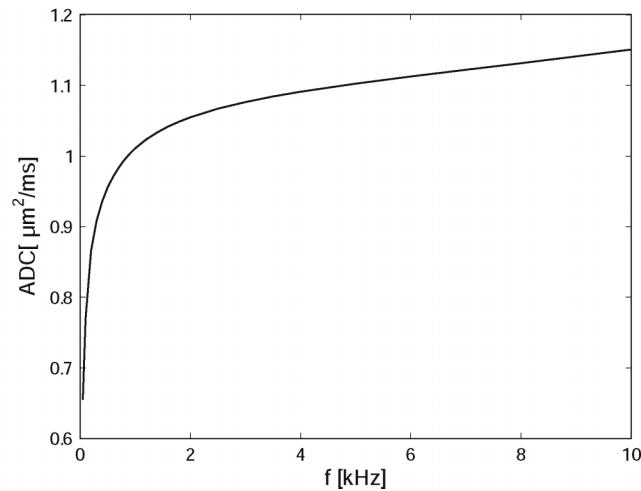
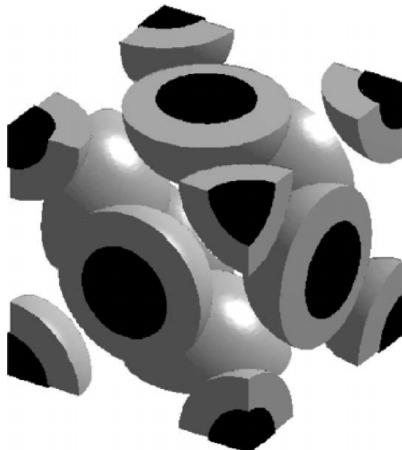


Figure 5. Left: array of close-packed spherical cells (gray) containing spherical nuclei (black) considered as a simple model of tissues. Right: predicted behavior of the apparent diffusion coefficient (ADC) as a function of frequency. For this curve, the intranuclear, cytoplasmic and extracellular diffusion coefficients are taken as 1.31, 0.48 and 1.82 $\mu\text{m}^2/\text{ms}$, respectively, the 'cells' have a diameter of 10 μm , the nuclei are 7.5 μm and the lattice spacing is 10.6 μm , and so the cellular volume fraction is only 39.6%. Other details of the simulation are given in (10). Note the sharp inflection of the curve at around 1 kHz for this size system.

proton density and T_2 values were assumed to be homogeneous. For the OGSE method, the effective diffusion time can be smaller than a few milliseconds (corresponding to gradient frequencies higher than a few hundreds of hertz). In contrast, the intracellular water exchange lifetime has been reported to be two orders of magnitude larger, e.g. the HeLa cell intracellular water lifetime was estimated to be 119 ± 14 ms (14). Therefore, we can neglect the influence of the water exchange between intra- and extracellular spaces during the OGSE measurements. Similarly, for the nuclear envelope separating intranuclear and cytoplasmic compartments, water exchange across the nuclear envelope can be ignored in OGSE measurements with short diffusion times (10). Consequently, all the interfaces between the compartments in the tissue model can be effectively modeled as impermeable if the OGSE method is implemented with relatively high gradient frequencies. As a result, the total signal can be modeled as a sum of independent signals, each arising from one compartment.

The diffusion inside the intranuclear and cytoplasmic spaces is considered to be restricted, and the diffusion in the extracellular space was modeled as hindered and ascribed a constant diffusion coefficient. The total signals can then be expressed as:

$$E = f_{\text{nuc}} \exp(-\beta_{\text{nuc}}) + f_{\text{cyto}} \exp(-\beta_{\text{cyto}}) + (1 - f_{\text{nuc}} - f_{\text{cyto}}) \exp(-bD_{\text{ex}}) \quad [25]$$

where β_{nuc} and β_{cyto} represent the signal echo attenuation of intranuclear and cytoplasmic spaces, respectively, and f_{nuc} and f_{cyto} represent the proton fractions (equal to volume fractions because the proton density is assumed to be homogeneous). The signal echo attenuation was simulated and then fitted to eqn (25). All cell structural parameters used in the simulation were chosen from published experimental results (15,16): intrinsic diffusion coefficients: for nucleus, $1.31 \mu\text{m}^2/\text{ms}$; for cytoplasm, $0.48 \mu\text{m}^2/\text{ms}$; for extracellular space, $1.82 \mu\text{m}^2/\text{ms}$. Spherical cells were given a diameter of $10 \mu\text{m}$, spacing $10.6 \mu\text{m}$ for neighboring cells, and each cell contained a central spherical nucleus with a diameter of $7.5 \mu\text{m}$. Figure 5 shows the behavior of ADC as a function of frequency for this system.

A more complex model was analyzed using computer simulations by Xu *et al.* (17), where the effects of finite permeabilities of the restricting membranes and the effects of cell density (cellularity) were explicitly considered. The observed relation

between ADC and cellularity in conventional PGSE measurements is probably a reflection of the effects of water molecules encountering different numbers of cell membranes in the diffusion time, but no separate information can be obtained about structural variations that might occur on subcellular scales. In studies of cancer, although cell density may be useful as an indicator of tumor aggressiveness or metastatic capacity, it is plausible that more specific insights into tumor status may be provided by developing methods that are sensitive to intracellular changes. To assess such effects, we considered a computer model similar to the above close-packed spheres, but in which each restricting membrane was assigned a finite (nonzero) permeability and the cell density and nuclear to cell size ratios were varied. Diffusion was simulated for conventional and OGSE methods. The results show that conventional measurements with the PGSE method at typical diffusion times cannot selectively probe variations within samples that occur only over short length scales, and therefore are relatively insensitive to intracellular structure. However, results using OGSE methods at moderate gradient frequencies may be affected by variations in cell nuclear size, and can distinguish tissues that differ only over subcellular length scales (Fig. 6). In particular, using realistic values, we predicted that we should be able to distinguish tissues that have the same cell density, but different ratios of the nuclear to cell volume, in circumstances in which PGSE measurements would not provide significant contrast (17). Such effects may not be restricted to just the nucleus – there are other intracellular membranes with large surface areas, and changes in their properties may also affect the signals. The ability of OGSE methods to be able to detect changes within cells, without gross changes in cellularity, is a major potential advantage over conventional PGSE methods for some applications, such as detecting the early response of tumors to treatment, as shown below.

EXPERIMENTAL MEASUREMENTS OF TEMPORAL DIFFUSION SPECTRA

Early experimental studies in model systems

We first studied model systems that were suspensions in deionized water of polystyrene latex microspheres of various

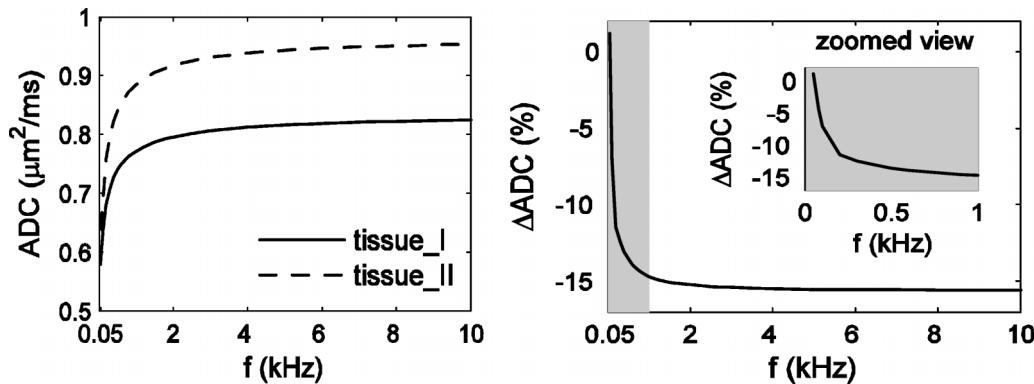


Figure 6. The apparent diffusion coefficient (ADC) is calculated as a function of frequency for two tissues, each with the same cell density, but with different-sized nuclei, and all other parameters identical. In tissue I, the nucleus to cell volume ratio is only 6.2%, whereas, in tissue II, it is 22%, and so less intracellular water is confined within the faster diffusing nuclear compartment. At low frequencies, the ADC values are barely different, whereas significant differences (and thus contrast in images) are expected at frequencies beyond approximately 200 Hz. For this simulation, the 'cells' had a diameter of $10 \mu\text{m}$ and the membrane permeabilities were $0.024 \mu\text{m}/\text{ms}$. The cellular volume fraction was fixed and only the nuclear size was varied. Other details of the simulation are given in Xu *et al.* (17) [figure adapted from (17)].

diameters: 1–400 µm. These studies were reported in (4) and (8). The samples were centrifuged to induce close packing. Measurements were made at 200 MHz in a 30 cm bore 4.7 T superconducting magnet using an imaging gradient insert with maximum gradient strength of 100 gauss/cm. Oscillating diffusion gradient waveforms were 30 ms in duration and of variable frequency. For each frequency, the gradient amplitude was adjusted so that the b values were the same. The total width of the two pulses was $2\sigma = 60$ ms, and so the width of the frequency peak in $F(\omega)$ was, in all cases, 16.67 Hz. Images were collected for values of N (the number of oscillations in each gradient pulse) from 1 to 30, sampling the diffusion spectrum from 33.33 to 1000 Hz in 33.33 Hz increments. The measured diffusion spectra for nine packed bead samples plus a uniform gel are plotted in Fig. 7. Superimposed on the data are the best fits to the data using equations derived by Stepinik (18) for the theoretical spectra in spherical geometry. Two parameters were

extracted: the pore size and D_0 . Figure 8 shows the pore sizes calculated from these fits plotted against the known bead sizes. The finite offset of the linear fit is caused by an overestimation of the pore size in the smallest beads. Higher frequencies of gradient oscillation would be necessary to improve these fits. In Parsons *et al.* (4), we also reported the use of a simple model to extract values of S/V , the surface to volume ratio of the pores in this system.

OGSE spectra in packed cells – extending the frequency range

Using a special gradient system capable of gradients up to 3500 g/cm and frequencies to 3.5 kHz, we studied the dispersion of $\mathbf{D}(\omega)$ in samples of packed cells. Cell pellets do not usually mimic intact tissues closely but, in previous work, we observed that ADC at long diffusion intervals was inversely proportional

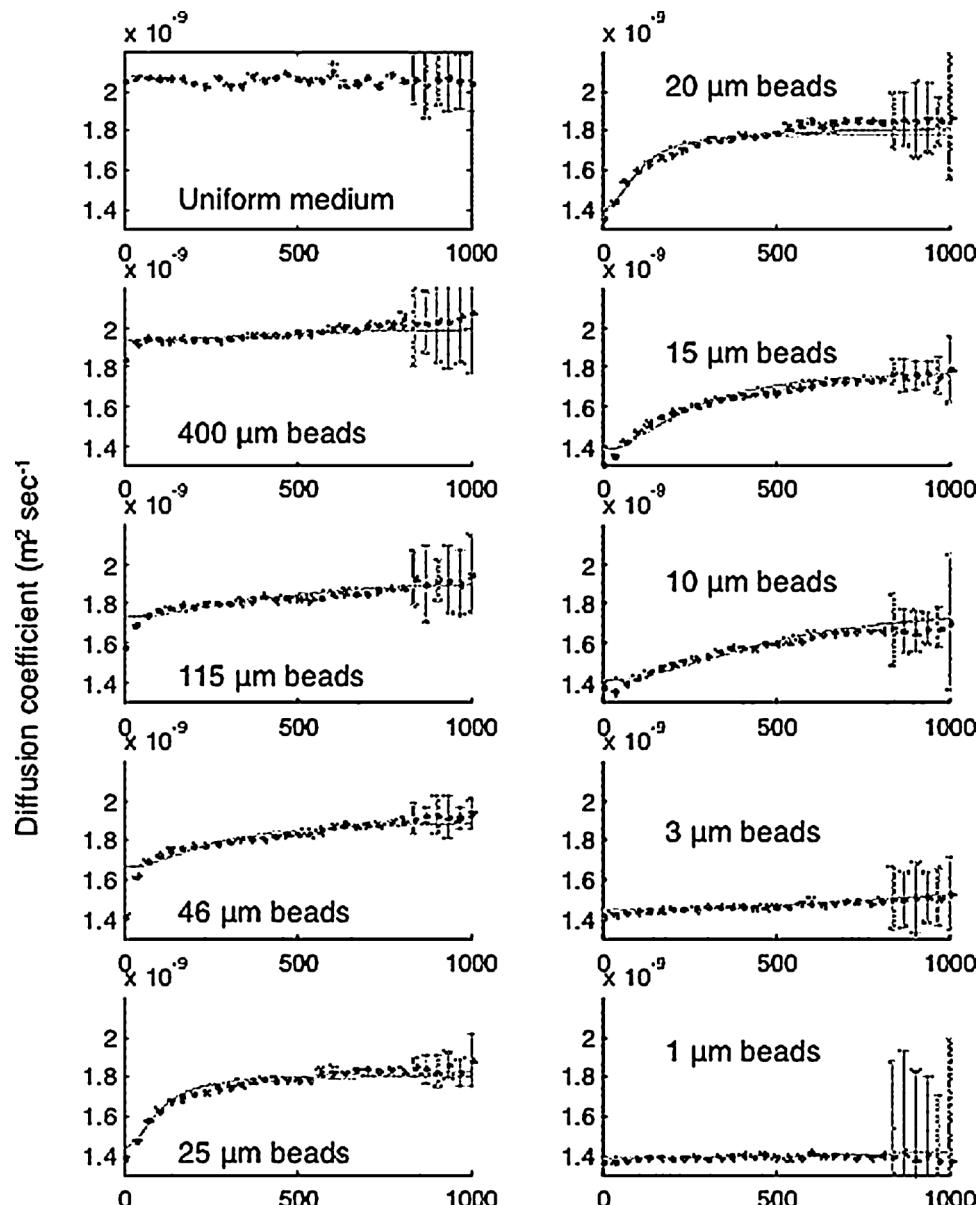


Figure 7. Measured apparent diffusion coefficient (ADC) values for samples of close-packed beads, obtained at different gradient frequencies, with fits to theoretical expressions for diffusion in spherical geometry [details reported in (8)].

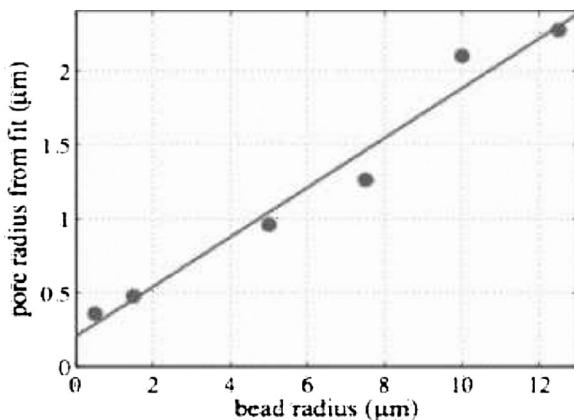


Figure 8. Fitted pore size plotted against bead size for samples with diameters from 1 to 25 μm . The slope of the line of the best fit is 0.084, which corresponds to the ratio of pore size to bead radius [details reported in (8)].

to the cell density (15). In packed human leukemia (HL-60) pellets suspensions, OGSE methods have been used to measure ADC at oscillation frequencies up to 3 kHz (effective diffusion times for uniform media down to 80 μs). These data are shown in Fig. 9. Rapid increases in ADC occur over the range zero to approximately 300 Hz, after which there is a much more gradual and continuous increase at higher frequencies beyond 3 kHz. These data suggest that, in these cells, diffusion is reduced below the free water value by hindrances on a scale much below the dimensions of whole cells, and that, even at very short diffusion times, there are still hindrances that reduce ADC significantly below that of free water. Xu *et al.* (10) considered how OGSE experimental spectra could be fitted to theoretical expressions in order to extract structural parameters, such as cell sizes, using the simple two-compartment model considered earlier for spherical cells. Such an approach can provide information on tissue structure not readily obtainable by other means.

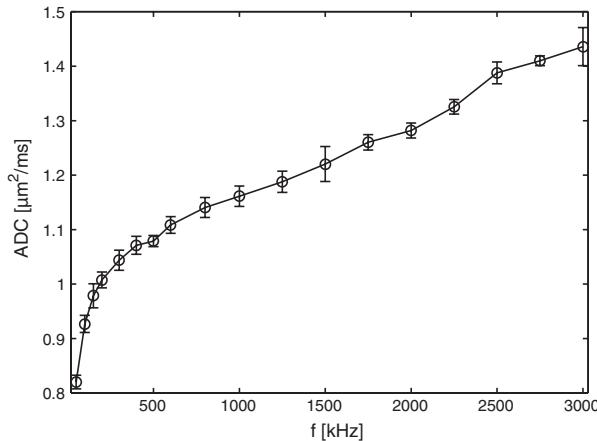


Figure 9. Apparent diffusion coefficient (ADC) as a function of frequency from oscillating-gradient spin echo (OGSE) measurements in packed cells. The error bars are the standard deviation for data obtained by averaging 10 different measurements. ADC increases rapidly at low frequencies and more gradually at higher frequencies. Even at 3 kHz, there is little evidence that the curve is flattening to its asymptotic value.

OGSE studies *in vivo*

Oscillating-gradient methods can be readily implemented on modern animal imaging systems equipped with typical state-of-the-art imaging gradients. In earlier work, with gradients capable of reaching 100 g/cm, oscillating gradients were used to probe the frequency dependence of water diffusion in the gray matter of normal and globally ischemic rat brain (19). These oscillating-gradient measurements measured $D(\omega)$ for brain water over the range 0–500 Hz, corresponding to diffusion times for uniform media of between 9.75 ms and 375 μs , an order of magnitude shorter than previously studied *in vivo*. Over this range, $D(\omega)$ increased as much as 24% *in vivo* and 50% post-mortem (see Fig. 10). The results in rat brain were found to be consistent with restricted diffusion and the known microanatomy of gray matter. Differences between normal and post-mortem data were consistent with an increase in water restriction, and tentatively suggest that physical changes following the onset of ischemia occur on a scale of about 2 μm , similar to a typical cellular dimension in gray matter. The diffusion studies in this paper did not fully reach the short diffusion time regime, and thus we were limited in the ability to extract other parameters.

Temporal diffusion spectra in tumors

Diffusion measurements have proven to be useful in both small animal and clinical imaging for characterizing the state and response of tumors, and reveal information on tissue characteristics, such as cellularity, not obtainable by other means. As emphasized earlier, conventional measurements of ADC reveal the effects of restrictions to free diffusion on a specific spatial scale determined by a diffusion time interval, which is several micrometers, because for technical reasons the diffusion time must be at least several milliseconds. Variations in ADC may thus

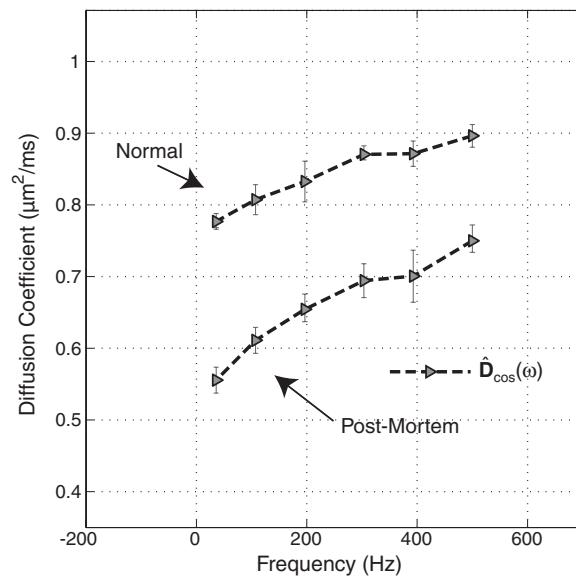


Figure 10. Mean apparent diffusion coefficients (ADCs) from cortical gray matter of five rats (error bars are the standard deviation across rats) for oscillating-gradient spin echo (OGSE) cosine waveforms as a function of frequency. The top data are from normal rats, *in vivo*, and the bottom data are from the post-mortem images. Details of these measurements were reported in (19).

be dominated by variations in the density of restricting barriers of this spacing, corresponding to variations in cell density, and no specific information is available from ADC measurements about structural changes that occur at a smaller scale. For example, if changes occur within cells before there are changes in cell density, these cannot be distinguished.

By measuring diffusion spectra using oscillating-gradient waveforms, we can obtain information on diffusion in the regime in which inferences can be drawn about changes in intracellular tissue structures that modify diffusion before there are changes in cell density. We have been encouraged by our first studies looking at the effects of treatment of tumors and the use of OGSE measurements of ADC as an early biomarker of successful treatment responses.

We recently reported a preliminary assessment of tumors using OGSE methods (20). We applied OGSE methods to map ADC at specific frequencies in rats bearing glioblastoma tumors *in vivo* and *ex vivo* to illustrate the increased contrast and structural information that is achievable using such techniques. By demonstrating an increased contrast in calculated ADC maps, at moderately high frequency (240 Hz), as well as quantitatively different ADCs measured in pathological regions, we demonstrated the benefit of OGSE techniques over currently employed techniques for evaluating microscopic variations in tumor microstructure (20).

Figure 11 shows maps of ADC obtained in one representative animal for different gradient frequencies. The ADC map obtained

at the lowest frequency, 30 Hz, is similar to that obtained by the PGSE method, as expected. However, as the oscillation frequency is increased, there is increased contrast between the tumor and surrounding tissues, and new features appear within the heterogeneous tumor volume. These features correspond to regions in which the degree of restriction to diffusion varies more at shorter time and distance scales than in surrounding tissues.

Plots of ADC versus oscillation frequency for two regions of interest (within tumor and normal brain) from one representative animal are shown in Fig. 12. For each frequency, the corresponding mean displacement for free diffusion predicted by theory is also displayed. At the lowest frequency of 30 Hz, the effective diffusion time is approximately 8.3 ms, and ADC is similar to that measured by PGSE methods over an interval of 15 ms. However, as the oscillation frequency increases, and the effective diffusion time decreases, there is a clear departure in ADC from that measured with PGSE methods. For example, at an oscillation frequency of 150 Hz ($\Delta_{\text{eff}} \approx 1.7$ ms), ADC calculated using OGSE is approximately 20% larger than that calculated using PGSE, and becomes 48% larger at 240 Hz ($\Delta_{\text{eff}} \approx 1.0$ ms).

ADC in contralateral gray matter was found, in general, to be smaller than that in tumor, and to increase less with frequency, with the mean value for gray matter varying from $0.60 \pm 0.06 \mu\text{m}^2/\text{ms}$ at 30 Hz to $0.79 \pm 0.06 \mu\text{m}^2/\text{ms}$ at 240 Hz (errors for values averaged across animals are reported as the standard error of the mean).

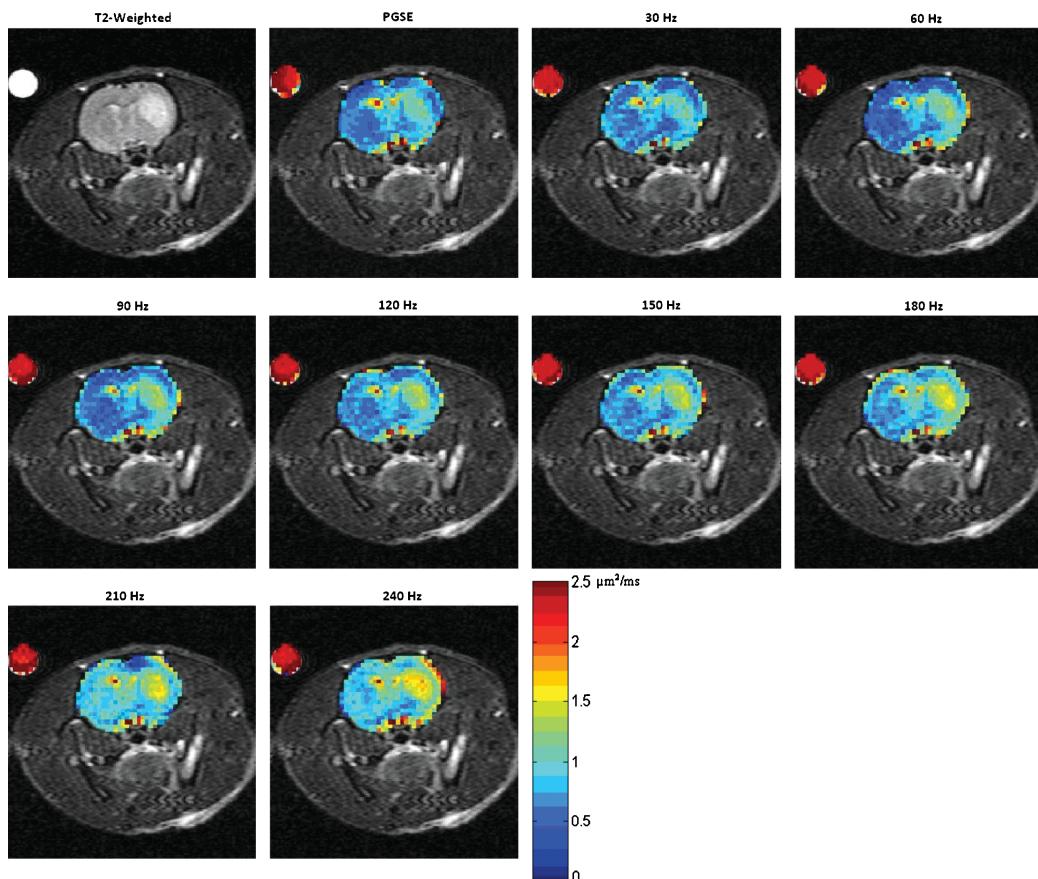
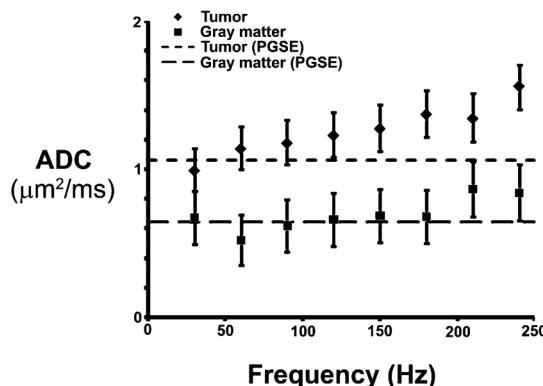


Figure 11. Apparent diffusion coefficient (ADC) maps of rat brain with tumor obtained using different gradient frequencies. Top row: T₂-weighted image and ADC obtained using the conventional pulsed-gradient spin echo (PGSE) sequence, which is not much different from the low-frequency oscillating-gradient spin echo (OGSE) results. At high frequency, more contrast and new features emerge within the tumor in particular. Details of these experiments were reported in (20).



estimated length scale (microns)	4.1	3.1	2.6	2.3	2.1	2.0	1.8	1.8	PGSE 5.5
maximum length scale (microns)	6.5	4.6	3.7	3.2	2.9	2.6	2.5	2.3	8.4

Figure 12. Plots of apparent diffusion coefficient (ADC) versus oscillation frequency for two regions of interest (within tumor and normal brain) from one representative animal. For each frequency, the corresponding mean displacement for free diffusion predicted by theory is also displayed [from (19)]. OGSE, oscillating-gradient spin echo; PGSE, pulsed-gradient spin echo.

In a more recent study, male rats bearing intracranial 9L glioblastoma were treated with the chemotherapeutic drug 1,3-bis(2-chloroethyl)-1-nitrosourea (BCNU) (carmustine) (21). Figure 13 shows the T_2 -weighted MR images (left) and ADC maps by conventional PGSE (center) and OGSE (using a gradient frequency of 240 Hz, right). The top row shows the images obtained 11 days post-inoculation: the middle and bottom rows show the results 24 h and 72 h post-treatment. The greater contrast and heterogeneity in the OGSE data should be noted,

suggesting that there is less restriction at finer scales. In addition, changes in ADC compared with control (untreated animals) appear earlier (24 h), and are more marked, in OGSE images after treatment than in conventional methods. In tumors that responded to treatment, preliminary examination of histological data suggested that these changes correspond to reductions in mean nuclear size rather than in cell density or other factors. These initial data suggest that OGSE techniques, capable of assessing diffusion effects over much shorter spatial scales, are able to reveal a greater range of spatial features within the tumor microenvironment, and may be more sensitive than conventional methods as early indicators of treatment response.

CONCLUSIONS

Temporal diffusion spectroscopy, as described here, is different from diffusion \mathbf{q} -space imaging or other analyses of diffusion measurements. In \mathbf{q} -space imaging, the propagator is usually defined at a given diffusion time and has spatial and directional dependences over a large range of \mathbf{q} -space. In contrast, in temporal diffusion spectroscopy, the effective diffusion times are changed by changing diffusion gradient frequencies, and thus a spectrum of diffusion rates can be measured which describe the biological tissue microenvironment. It may be assumed that the use of a high-frequency gradient is merely a way to achieve short effective diffusion times, and that equivalent information may be obtained using conventional pulsed gradients with short diffusion times. Experimentally, oscillating gradients of sufficient strength and frequency are more readily implemented in small samples and animals than are high-amplitude short pulsed gradients, and that alone makes the method attractive. However, it should be emphasized that different physical insights are obtained using the frequency analysis above, and there are potential practical advantages of using a discrete frequency

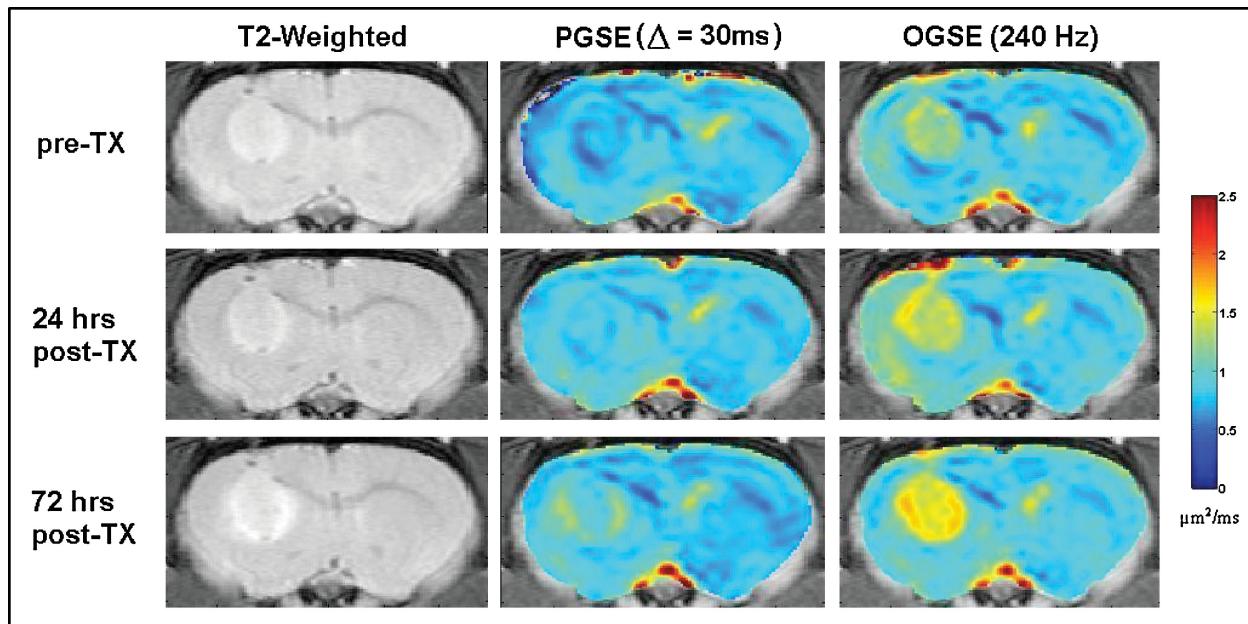


Figure 13. T_2 -weighted MR images (left) and apparent diffusion coefficient (ADC) maps by pulsed-gradient spin echo (PGSE) (center) and oscillating-gradient spin echo (OGSE) (240 Hz, right) of 9L gliosarcoma *in vivo*. Top: 11 days post-inoculation; Middle and bottom: 24 h and 72 h post-treatment with 1,3-bis(2-chloroethyl)-1-nitrosourea (BCNU) (carmustine). Note the greater contrast and heterogeneity in OGSE data, suggesting less restriction at finer scales: changes in ADC appear earlier (24 h) and are more marked in OGSE images after treatment (21).

rather than a short pulsed gradient. The latter will always correspond to sampling the diffusion spectrum at multiple frequencies around zero, whereas specific frequencies can be sampled using sinusoidal gradients. The contrast between tissues may be greater at a discrete, moderately high frequency than at low frequencies, as suggested by our theoretical consideration of simple geometries above and our preliminary studies in tumors.

Our efforts to extend measurements *in vivo* and in cells to higher frequencies have revealed interesting new insights into what scales of obstructions cause diffusion coefficients to be so small in biological samples. In packed cells, the observation that $D(\omega)$ does not appear to flatten out, even at frequencies >3 kHz, suggests that there are significant hindrances to diffusion over scales much less than the cell size, even though protein solutions and simple gels of similar density show no such effects. Such data imply the existence of larger, more discrete structures than isolated macromolecules that affect diffusion.

The ability to detect early changes in tumors during a course of treatment is a potentially important application of diffusion imaging, and the ability to detect changes within tumors before there are frank reductions in cell density may be a significant advantage of OGSE methods over PGSE techniques. Simulations and theory predict that changes at subcellular levels may be discernible at high gradient frequencies, which can distinguish such effects from larger scale changes. Our preliminary findings of increased contrast and spatial heterogeneity, and earlier changes after treatment, in animal models, at even moderate frequencies, are encouraging and justify further studies.

Just as PGSE methods are limited in their ability to probe very short diffusion times because of limitations on gradient strength, OGSE methods are similarly constrained in practice. As the frequency of gradient modulation increases, in order to keep echo times reasonable, the gradient amplitude must increase to produce large b factors. In practice, this will limit the application of OGSE methods to human scanners using currently available gradients. However, in the preclinical domain, gradient systems suitable for achieving quite high gradient frequencies are routinely available and in operation. We anticipate that these will find increasing application for the acquisition of temporal diffusion spectra and OGSE-weighted images in small animals.

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