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## Hydrogen peroxide plays a key role in the oxidation reaction of myoglobin by molecular oxygen

#### A computer simulation

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ABSTRACT The stability properties of the iron(II)-dioxygen bond in myoglobin and hemoglobin are of particular importance, because both proteins are oxidized easily to the ferric met-form, which cannot be oxygenated and is therefore physiologically inactive. In this paper, we have formulated all the possible pathways leading to the oxidation of myoglobin to metmyoglobin with each required rate constant in 0.1 M buffer (pH 7.0) at 25°C, and have set up six rate equations for the elementary processes going on in a simultaneous way. By using the Runge-Kutta method to solve these differential equations, the concentration progress curves were then displayed for all the reactive species involved.

In this complex reaction, the primary event was the autoxidation of  $MbO_2$  to metMb with generation of the superoxide anion, this anion being converted immediately and almost completely into  $H_2O_2$  by the spontaneous dismutation. Under air-saturated conditions ( $P_{O_2} = 150 \text{ Torr}$ ), the  $H_2O_2$  produced was decomposed mostly by the metMb resulting from the autoxidation of  $MbO_2$ . At lower pressures of  $O_2$ , however,  $H_2O_2$  can act as the most potent oxidant of the deoxyMb, which increases with decreasing  $O_2$  pressures, so that there appeared a well defined maximum rate in the formation of metMb at  $\sim$ 5 Torr of oxygen. Such examinations with the aid of a computer provide us, for the first time, with a full picture of the oxidation reaction of myoglobin as a function of oxygen pressures. These results also seem to be of primary importance from a point of view of clinical biochemistry of the oxygen supply, as well as of pathophysiology of ischemia, in red muscles such as cardiac and skeletal muscle tissues.

#### INTRODUCTION

During reversible oxygen binding, myoglobin and hemoglobin undergo a slow, but considerable oxidation to the ferric met-form, which cannot be oxygenated and is therefore physiologically inactive. The mechanistic details of this autoxidation reaction, which are of clinical, as well as of chemical importance, have been investigated by a number of authors, but still remain unclear for a full understanding of the overall stoichiometry.

Since the early work of Brooks (1931, 1935) on  $HbO_2$  and that of George and Stratmann (1952, 1954) on  $MbO_2$ , it has long been observed that even at a constant pH, the rate of the oxidation increases with decreasing partial pressure of  $O_2$  and shows a well defined maximum value at approximately the pressure required for each half-saturation ( $P_{50}$ ). Several proposals have therefore been made concerning the mechanism of this oxidation reaction, and these have recently been reviewed from a thermodynamic viewpoint (Shikama, 1984, 1990).

Along with the early work, Brown and Mebine (1969) and Wallace et al. (1982), among others, also agreed that

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Abbreviations used in this paper: Mb, myoglobin; MbO<sub>2</sub>, oxymyoglobin; metMb, metmyoglobin; Mb(II), ferrous myoglobin; Mb(III), ferric myoglobin; Mb(IV), ferryl myoglobin; Hb, hemoglobin; HbO<sub>2</sub>, oxyhemoglobin; metHb, methemoglobin.

the first step in autoxidation of  $MbO_2$  and  $HbO_2$  was the dissociation of the oxygen ligand, followed by the oxidation of the deoxy species by free  $O_2$  to produce metMb or metHb and the superoxide anion. In the case of myoglobin, therefore, the reaction was written as

$$Mb(II)(O_2) \rightleftharpoons Mb(II) + O_2$$

$$Mb(II) + O_2 \stackrel{H^+}{\longrightarrow} metMb(III) + O_2^-.$$

In this scheme, however, the differences in the deoxy species, which allow them to react with oxygen in one instance to become oxygenated and in another instance to become oxidized, were completely unknown (Snyder, 1963). Also, it should be noted here that free dioxygen is a poor electron acceptor with a lower redox potential,  $\epsilon'_0(O_2/O_2^-) = -0.33$  V, than those,  $\epsilon'_0 = +0.046$  V for the Mb(III)/Mb(II) couple (Taylor and Morgan, 1942) and  $\epsilon'_0 = +0.150$  V for the Hb(III)/Hb(II) system (Antonini et al., 1964), and that such a one-electron transfer from the iron(II) to free  $O_2$  cannot occur spontaneously (Shikama, 1990). In addition, the involvement of H<sup>+</sup> was not clear.

Recent kinetic and thermodynamic studies of the stability of native oxymyoglobin have revealed that the superoxide formation is not due to a simple, dissociative loss of  $O_2^-$  from  $MbO_2$ , but is due to a nucleophilic displacement of  $O_2^-$  from  $MbO_2$  by a water molecule or a hydroxyl ion that can enter the heme pocket from the surrounding solvent, so that the iron is converted to the ferric met-form (Satoh and Shikama, 1981; Shikama, 1984, 1985). The reductive displacement of the bound dioxygen as  $O_2^-$  by  $H_2O$  can proceed without any pro-

tonation. Nevertheless, the rate is enormously enhanced by a proton-assisted process which involves the distal histidine (E7) as its catalytic residue by a proton-relay mechanism (Shikama and Matsuoka, 1986; Shikama, 1988). The autoxidation reaction of MbO<sub>2</sub> to metMb can therefore be explained by the following three types of displacement processes:

$$Mb(II)(O_2) + H_2O \rightharpoonup Mb(III)(OH_2) + O_2^-$$

$$Mb(II)(O_2) + H_2O + H^+ \rightharpoonup Mb(III)(OH_2) + HO_2$$

$$Mb(II)(O_2) + OH^- \rightharpoonup Mb(III)(OH^-) + O_2^-.$$

The extent of the contribution of these elementary processes to the observed or overall autoxidation rate can vary with the concentration of H<sup>+</sup> or OH<sup>-</sup> ions. Consequently, the stability of MbO<sub>2</sub> shows a very complicated pH dependence having a parabolic part (Shikama, 1988).

Unfortunately, it seemed that there was no provision in this scheme for the inverse dependence of the autoxidation rate upon oxygen pressure. In this respect, however, it is of great interest to note that hydrogen peroxide can oxidize deoxyMb more than 100 times more easily than oxyMb (Yusa and Shikama, 1987). Since  $H_2O_2$  is produced by dismutation of the superoxide anion generated from the autoxidation of the oxy-form, it must act as at least one of the potent oxidants of the deoxy-form that increases with decreasing  $O_2$  pressures (Tajima and Shikama, 1987).

In this paper, we present a complete kinetic formulation for the autoxidation of MbO<sub>2</sub> to metMb, including several types of the subsequent reactions of myoglobin with H<sub>2</sub>O<sub>2</sub>. In dealing with this complex reaction in a quantitative way, we have carried out a detailed set of numerical analyses by solving the rate equations derived from each elementary processes involved. Such a computer simulation may provide us, for the first time, with a full picture of the oxidation reaction of myoglobin and hemoglobin by molecular oxygen.

### DESCRIPTION OF REACTION PATHWAYS WITH REQUIRED RATE CONSTANTS

It is in the ferrous form that myoglobin and hemoglobin can bind molecular oxygen reversibly and carry out their functions. For oxygen binding to myoglobin, therefore, we may write the equation:

$$Mb(II) + O_2 \frac{k_{on}}{k_{off}} MbO_2.$$
 (1)

In neutral pH range and at 25°C, we adopt here the values of  $k_{\rm on} = 1.64 \times 10^7 \, \rm s^{-1} \, M^{-1}$  and  $k_{\rm off} = 19 \, \rm s^{-1}$  for sperm whale myoglobin having the oxygen dissociation constant of  $K_{\rm D} = 1.15 \times 10^{-6} \, \rm M$ . These were calculated from the literature values given at 20°C, by using the corresponding activation energies (Antonini and Brunori, 1971).

Under air-saturated conditions, however, the oxygenated form of Mb or Hb is considerably oxidized to the ferric met-form with generation of the superoxide anion (Gotoh and Shikama, 1976),

$$MbO_2 \stackrel{k_A}{\rightharpoonup} Mb(III) + O_2^-,$$
 (2)

where  $k_A$  represents the first-order rate constant for the autoxidation reaction of MbO<sub>2</sub>, its magnitude being strongly dependent upon the pH of the solution. At pH 7.0, for instance, we observed the value of  $k_A = 8.1 \times 10^{-3} \, h^{-1}$  for sperm whale MbO<sub>2</sub> in 0.1 M phosphate buffer at 25°C (Shikama and Matsuoka, 1986).

The superoxide anion generated above can easily be converted into hydrogen peroxide with a high rate constant (for instance,  $k_d = 7.2 \times 10^8 \text{ h}^{-1} \text{ M}^{-1}$  in 0.1 mM phosphate buffer at pH 7.4 and 24°C in the absence of heme compounds [Rabani and Nielsen, 1969; Fridovich, 1975]), by the following spontaneous dismutation:

$$2O_2^- + 2H^+ \stackrel{k_d}{\rightharpoonup} H_2O_2 + O_2. \tag{3}$$

Recently, Yusa and Shikama (1987) have found that hydrogen peroxide can induce very rapid oxidation of  $MbO_2$  to metMb. Kinetic and spectrophotometric analyses have revealed that this oxidation proceeds through the formation of ferryl-Mb(IV) from deoxy-Mb(II), which is in equilibrium with  $MbO_2$ , by a two-equivalent oxidation with  $H_2O_2$ . Once the ferryl species is formed, it reacts rapidly with another deoxy-Mb(II) in a bimolecular fashion so as to yield 2 mol of metMb(III). The overall reaction may be written, therefore, as

$$Mb(II) + H_2O_2 \stackrel{k_{\phi}}{\rightharpoonup} Mb(IV) + 2OH^-$$

$$Mb(IV) + Mb(II) \stackrel{fast}{\longrightarrow} 2Mb(III)$$
Sum:  $2Mb(II) + H_2O_2 \rightharpoonup 2Mb(III) + 2OH^-$ . (4)

In this coupled reaction, the rate-determining step was the oxidation of the deoxy species with  $H_2O_2$ , its rate constant being estimated to be on the order of  $k_{\phi} = 1.3 \times 10^7 \, h^{-1} \, M^{-1}$  within equimolar amounts of  $H_2O_2$  to 50  $\mu$ M deoxyMb in 0.1 M phosphate buffer at pH 7.0 and 25°C (Yusa and Shikama, 1987).

On the other hand, we have also found that  $H_2O_2$  produced from the dismutation of  $O_2^-$  can be eliminated or decomposed mostly by the metMb resulting from the normal autoxidation reaction of MbO<sub>2</sub>, via the cyclic formation of the ferryl species as

$$Mb(III) + H_2O_2 \stackrel{k_f}{\to} *Mb(IV) = O + H_2O$$
 (5)

and

\*Mb(IV)=
$$O \stackrel{k_r}{\rightarrow} Mb(III),$$
 (6)

where the values of  $k_{\rm f}=1.6\times10^6\,{\rm h}^{-1}\,{\rm M}^{-1}$  (within fivefold molar excess of  ${\rm H_2O_2}$  to 50  $\mu{\rm M}$  metMb) and  $k_{\rm r}=4.0\times10^{-1}\,{\rm h}^{-1}$  were obtained in 0.1 M phosphate buffer at pH 7.0 and 25°C (Tajima and Shikama, 1987, 1992). As to the reaction of metMb with  ${\rm H_2O_2}$ , intensive studies have recently been made by several authors to elucidate the structure of ferryl myoglobin having an oxene ligand (Sitter et al., 1985; Chance et al., 1986) and also a protein radical centered on a tyrosine residue (Tew and Ortiz de Montellano, 1988; Davies, 1991), represented by \*Mb(IV) = O in this paper. However, the molecular mechanism for the revert reaction (or auto-reduction) of ferryl Mb to the ferric met-form in Eq. 6 remains still open to future study including the possible involvement of H<sup>+</sup>, OH<sup>-</sup>, and H<sub>2</sub>O with a stoichiometric balance (Uyeda and Peisach, 1981).

At this point, it should be noted that the values of the on-rate and off-rate constants of Eq. 1 are very high as compared with the other rate constants involved in the subsequent reactions of myoglobin. It is therefore concluded that the reversible oxygen binding to myoglobin can always proceed very quickly to an equilibrium extent. This conclusion

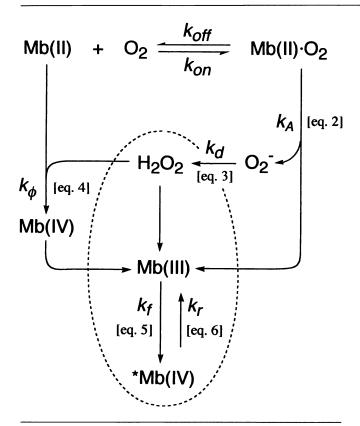


FIGURE 1 A schematic representation of the possible pathways for the oxidation reaction of myoglobin to metmyoglobin by molecular oxygen. Encircled by broken line is a system operating for the decomposition of  $H_2O_2$  in the normal autoxidation reaction of  $MbO_2$ . Stoichiometric balance is not shown here (see text).

would be valid at any time during the course of the oxidation reaction of myoglobin to metmyoglobin.

#### CALCULATIONS AND DISCUSSION

Fig. 1 illustrates in a very schematic way all the possible pathways leading to the oxidation of myoglobin to metmyoglobin by molecular oxygen. The ferryl species produced, not from deoxyMb but from metMb, marked here with an asterisk above the letter of Mb(IV). It is quite clear that  $H_2O_2$ , which is formed by dismutation of the superoxide anion generated from the autoxidation of MbO<sub>2</sub>, plays a key role in this complicated reaction.

Since the deoxy-form is the most preferred target for  $H_2O_2$ , the amount of deoxyMb that is in equilibrium with MbO<sub>2</sub> would become an important factor for the overall stoichiometry of myoglobin oxidation. Under air-saturated conditions ( $P_{O_2} = 150$  Torr), the molar fraction of the deoxy-form is only  $\sim 0.45\%$ , judging from the oxygen dissociation constant ( $K_D$ ). In this case, the  $H_2O_2$  would be eliminated or decomposed mostly, if not completely, by the metMb resulting from the normal autoxidation reaction of MbO<sub>2</sub>, via the cyclic formation of the ferryl species. With decreasing partial pressure of  $O_2$ , on the other hand, the amount of deoxyMb increases rapidly and  $H_2O_2$  would react with it.

In order to confirm these predictions more quantitatively, we have set up six rate equations in a simultaneous way (see Eqs. 7-10, 15, and 16 in the Appendix), and have carried out numerical analyses for the oxidation reaction of myoglobin to its met-form with the aid of a computer (IBM 3081-KX6, VM/SP CMS). To solve an initial-value problem for the differential equations, the Runge-Kutta integration method was employed from a program library (DIVPRK in MATH/LI-BRARY, IMSL). The concentration progress curves for each reactive species were then plotted at intervals of 0.01 h over a period of 100 h. In order to display the early stage (<10 h) of the reaction in great detail, the step size of  $1.56 \times 10^{-4}$  h (0.56 s) was employed for integration, because the same results were obtained for a much smaller step size.

Fig. 2 is a typical computer representation for the autoxidation reaction of MbO<sub>2</sub> to metMb in 0.1 M buffer, pH 7.0, at 25°C. The reaction was started with myoglobin of  $5.0 \times 10^{-5}$  M, the same concentration that we have usually used for the autoxidation rate measurements. Under air-saturated conditions of  $P_{O_2} = 150$  Torr, almost all the myoglobin exists in the oxy-form, so

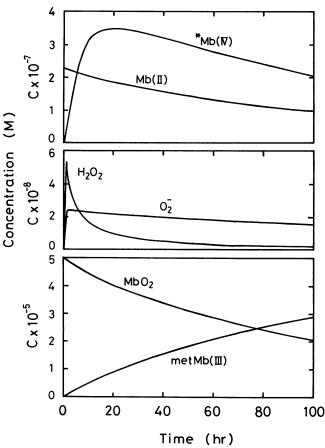


FIGURE 2 The concentration progress curves for each species involved in the autoxidation reaction of MbO<sub>2</sub> to metMb at 25°C in 0.1 M buffer, pH 7.0. The simulation was started with use of 50  $\mu$ M myoglobin under air-saturated conditions.

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that even in the initial concentration, the deoxy-species was found only of an order of  $2.25 \times 10^{-7}$  M.

When MbO<sub>2</sub> is oxidized to metMb, the stoichiometric amount of  $O_2^-$  should be generated. By the very rapid, spontaneous dismutation to  $H_2O_2$ , however, the superoxide level was found to fall immediately into an extremely low concentration on the order of  $10^{-8}$  M. Surprisingly, the resulting  $H_2O_2$  level was also found in the same concentration range as that of  $O_2^-$ , although a small but sharp accumulation of  $H_2O_2$  (less than 6 ×  $10^{-8}$  M at the highest) appeared at the very early stage (within 1 h) of the reaction. These calculations are quite in agreement with our experimental observations:  $H_2O_2$  produced is eliminated mostly, if not completely, by the metMb resulting from the normal autoxidation reaction of MbO<sub>2</sub>, through the cyclic formation of the ferryl species (Tajima and Shikama, 1987, 1992).

At lower pressures of O2, different pathways may occur in the oxidation reaction of myoglobin to metmyoglobin. Fig. 3 shows such a detailed set of calculations at three different pressures of O2. Under air-saturated conditions ( $P_{O_2} = 150$  Torr), it is quite clear that the rate of metmyoglobin formation can be explained almost completely by the normal autoxidation of  $k_A[MbO_2]$ , indicating that most of the H<sub>2</sub>O<sub>2</sub> produced was eliminated by the metMb resulting from MbO<sub>2</sub>. However, the extent of the contribution of the other term,  $k_{\bullet}[Mb(II)][H_2O_2]$ , to the overall formation of metMb increased with decreasing partial pressure of  $O_2$ . At  $P_{O_2} = 0.68$  Torr, for instance, almost half of the metMb formation came from the oxidation of deoxyMb with H<sub>2</sub>O<sub>2</sub>, indicating that most of the H<sub>2</sub>O<sub>2</sub> produced was used up to yield two equivalents of metMb from deoxyMb as described in Eq. 4. This is mainly due to a large increase in the equilibrium concentration of the deoxy species. Furthermore, it seemed that the rate of formation of metMb increases with decreasing partial pressure of O<sub>2</sub>. We have therefore made a first-order plot for the overall oxidation of myoglobin, from the ferrous state as a sum of MbO2 and deoxyMb to the ferric met-form, by the following definition:

the rate of metMb formation

$$\equiv k_{\text{met}} \{ [Mb(II) \cdot O_2] + [Mb(II)] \}.$$

The rate constant of  $k_{\text{met}}$  (h<sup>-1</sup>) was then determined from the slope of each line at each given value of O<sub>2</sub> by a least-squares fitting.

Fig. 4 shows such a computer representation for the oxidation rate of myoglobin to metmyoglobin as a function of  $P_{O_2}$ . There appeared a well defined maximum rate at a partial pressure of  $O_2 \sim 5$  Torr. Increase of the  $O_2$  pressure above  $\sim 40$  Torr was found to have little effect on the oxidation rate, its magnitude at these pressures becoming closer to a constant value of  $k_A = 8.1 \times 10^{-3} \, h^{-1}$  under air-saturated conditions. This result is in good accord with the actual experimental data on the

oxidation of equine myoglobin (George and Stratmann, 1952); the protein showed a maximum oxidation rate at the partial pressure of  $O_2 \sim 2$  Torr in 0.6 M phosphate buffer, pH 5.69 at 30°C. At this stage our calculations would be satisfactory, because the rate constants used here have been derived from other studies in which sections of the oxidation mechanism have been isolated for study.

Other interesting aspects of this  $O_2$ -dependence curve would be demonstrated by changing the values of two relevant parameters. As shown in Fig. 4, the maximum rate of oxidation was found when a set values of  $k_f = 3.0 \times 10^6 \text{ h}^{-1} \text{ M}^{-1}$  and  $k_{\phi} = 6.0 \times 10^7 \text{ h}^{-1} \text{ M}^{-1}$  were employed, both being several times higher than the experimentally measured ones. On the other hand, if we assume both of the values to be zero, there should occur no reaction of myoglobin with  $H_2O_2$ . In this case, the rate of  $k_A[\text{MbO}_2]$  would only be responsible for the formation of metmyoglobin, and the  $O_2$ -dependence curve becomes simply hyperbolic, with no detectable maximum rate of oxidation.

From these numerical examinations assisted with a computer, we can conclude unequivocally that  $H_2O_2$ , which is produced from the dismutation of  $O_2^-$ , plays a crucial role in the oxidation reaction of myoglobin to its met-form at lower pressures of  $O_2$ . These results also lead us to a new view that a good supply of oxygen provides a rather important defense against the oxidation of myoglobin with hydrogen peroxide, one of the most potent oxidants found in situ. This view seems to be of clinical importance in the oxygen supply to red muscles, because ischemia is known to cause abrupt cell destruction in cardiac and skeletal muscle tissues (Levine et al., 1971; Kagen et al., 1975).

#### **APPENDIX**

For numerical analysis, we may write the following rate equations for each elementary step involved in the oxidation reaction of myoglobin.

$$\frac{d}{dt}[O_2^-] = k_A[MbO_2] - k_d[O_2^-]^2$$
 (7)

$$\frac{d}{dt}[H_2O_2] = \frac{1}{2} k_d[O_2^-]^2 - k_f[H_2O_2][Mb(III)]$$

$$-k_{\phi}[H_2O_2][Mb(II)] \quad (8)$$

$$\frac{\mathrm{d}}{\mathrm{d}t} [\mathrm{Mb(III)}] = k_{\mathrm{A}} [\mathrm{MbO_2}] + 2k_{\phi} [\mathrm{H_2O_2}] [\mathrm{Mb(II)}]$$

$$-k_{\rm f}[{\rm H_2O_2}][{\rm Mb(III)}] + k_{\rm r}[*{\rm Mb(IV)}]$$
 (9)

and

$$\frac{d}{dt} [*Mb(IV)] = k_f [H_2O_2] [Mb(III)] - k_r [*Mb(IV)]. \quad (10)$$

Since the total concentration of Mb is given in practice by

$$[Mb]_0 = [MbO_2] + [Mb(II)] + [Mb(III)] + [*Mb(IV)],$$
 (11)

the following relationships should always be valid at any constant value of the partial pressure of  $O_2$ :

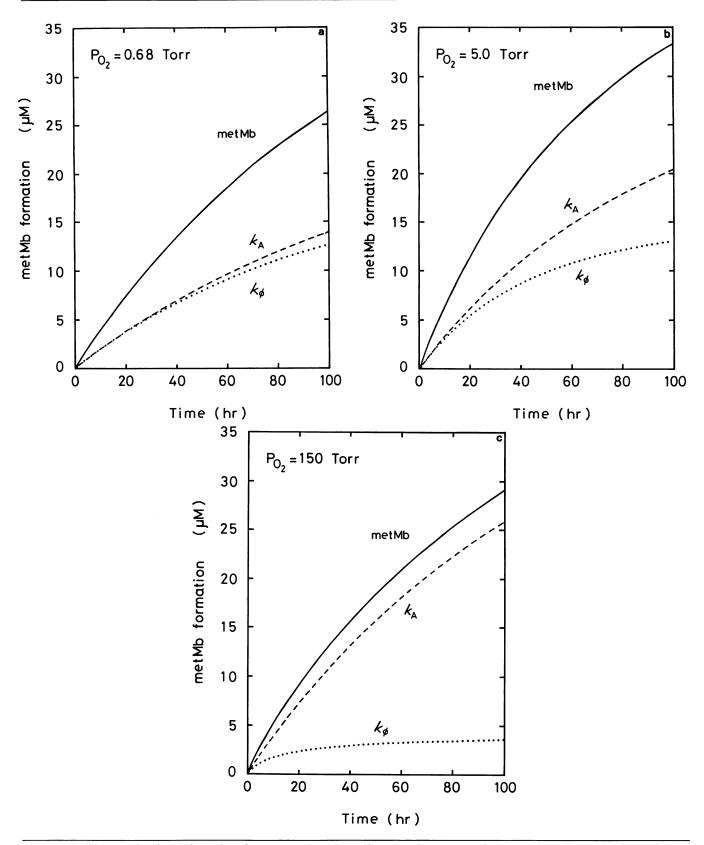


FIGURE 3 Different profiles for the formation of metmyoglobin at three different partial pressures of oxygen. The rate was broken down into two components of  $k_A[MbO_2]$  and  $k_{\phi}[H_2O_2][Mb(II)]$  at 25°C in 0.1 M buffer, pH 7.0. (a)  $P_{O_2} = 0.68$  Torr; (b)  $P_{O_2} = 5.0$  Torr; (c)  $P_{O_2} = 150$  Torr.

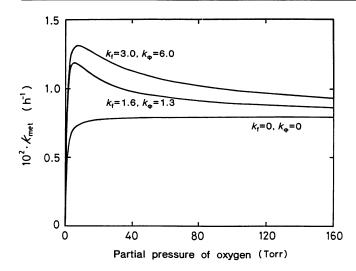


FIGURE 4 Plots for the oxidation rate of myoglobin to metmyoglobin as a function of partial pressures of oxygen. The simulation was carried out using three different set values of the rate constants: (a)  $k_{\rm f} = 3.0 \times 10^6 \, {\rm h^{-1} \, M^{-1}}$  and  $k_{\phi} = 6.0 \times 10^7 \, {\rm h^{-1} \, M^{-1}}$ ; (b)  $k_{\rm f} = 1.6 \times 10^6 \, {\rm h^{-1} \, M^{-1}}$  and  $k_{\phi} = 1.3 \times 10^7 \, {\rm h^{-1} \, M^{-1}}$ ; (c)  $k_{\rm f} = 0$  and  $k_{\phi} = 0$ .

$$[MbO_2] = \{ [Mb]_0 - [Mb(III)] - [*Mb(IV)] \}(\alpha)$$
 (12)

and

$$[Mb(II)] = {[Mb]_0 - [Mb(III)] - [*Mb(IV)]}(1 - \alpha),$$
 (13)

where

$$\alpha = \frac{[\text{MbO}_2]}{[\text{MbO}_2] + [\text{Mb}(\text{II})]} = \frac{[\text{O}_2]}{[\text{O}_2] + K_D}.$$
 (14)

We may therefore differentiate Eqs. 12 and 13 to obtain the following two rate equations:

$$-\frac{\mathrm{d}}{\mathrm{d}t}[\mathrm{MbO}_{2}] = \left\{ \frac{\mathrm{d}}{\mathrm{d}t}[\mathrm{Mb}(\mathrm{III})] + \frac{\mathrm{d}}{\mathrm{d}t}[*\mathrm{Mb}(\mathrm{IV})] \right\} (\alpha)$$
$$= \left\{ k_{\mathsf{A}}[\mathrm{MbO}_{2}] + 2k_{\mathsf{\phi}}[\mathrm{H}_{2}\mathrm{O}_{2}][\mathrm{Mb}(\mathrm{II})] \right\} (\alpha) \tag{15}$$

and

$$-\frac{\mathrm{d}}{\mathrm{d}t} [\mathrm{Mb}(\mathrm{II})] = \left\{ \frac{\mathrm{d}}{\mathrm{d}t} [\mathrm{Mb}(\mathrm{III})] + \frac{\mathrm{d}}{\mathrm{d}t} [*\mathrm{Mb}(\mathrm{IV})] \right\} (1 - \alpha)$$
$$= \left\{ k_{\mathrm{A}} [\mathrm{MbO}_{2}] + 2k_{\phi} [\mathrm{H}_{2}\mathrm{O}_{2}] [\mathrm{Mb}(\mathrm{II})] \right\} (1 - \alpha). \tag{16}$$

For the conversion of the value of  $P_{O_2}$  (Torr) into the molar concentration of  $O_2$  in solution, we used the following equation (Antonini and Brunori, 1971):

$$[O_2] = s \times P_{O_2}$$

where

$$s = 1.69 \times 10^{-6} \text{ M/Torr at } 25^{\circ}\text{C}.$$

The following values were also used for the rate constants and oxygen dissociation constant required in our calculation in 0.1 M buffer, pH 7 at 25°C:

$$k_{\rm A} = 8.1 \times 10^{-3} \, {\rm h}^{-1}, \quad k_{\rm d} = 7.2 \times 10^8 \, {\rm h}^{-1} \, {\rm M}^{-1},$$
 $k_{\phi} = 1.3 \times 10^7 \, {\rm h}^{-1} \, {\rm M}^{-1},$ 
 $k_{\rm f} = 1.6 \times 10^6 \, {\rm h}^{-1} \, {\rm M}^{-1}, \quad k_{\rm r} = 4.0 \times 10^{-1} \, {\rm h}^{-1}, \quad {\rm and}$ 
 $K_{\rm D} = 1.15 \times 10^{-6} \, {\rm M}.$ 

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#### **REFERENCES**

Antonini, E., J. Wyman, M. Brunori, J. F. Taylor, A. Rossi-Fanelli, and A. Caputo. 1964. Studies on the oxidation-reduction potentials of heme proteins. I. Human hemoglobin. J. Biol. Chem. 239:907-917

Antonini, E., and M. Brunori. 1971. Hemoglobin and Myoglobin in Their Reactions with Ligands. North-Holland, Amsterdam. 221– 223.

Brooks, J. 1931. The oxidation of haemoglobin to methaemoglobin by oxygen. *Proc. R. Soc. London Ser. B.* 109:35–50.

Brooks, J. 1935. The oxidation of haemoglobin to methaemoglobin by oxygen. II.—The relation between the rate of oxidation and the partial pressure of oxygen. *Proc. R. Soc. London Ser. B.* 118:560-577.

Brown, W. D., and L. B. Mebine. 1969. Autoxidation of oxymyoglobins. *J. Biol. Chem.* 244:6696-6701.

Chance, M., L. Powers, C. Kumar, and B. Chance. 1986. X-ray absorption studies of myoglobin peroxide reveal functional differences between globins and heme enzymes. *Biochemistry*. 25:1259–1265.

Davies, M. J. 1991. Identification of a globin free radical in equine myoglobin treated with peroxides. *Biochim. Biophys. Acta.* 1077:86– 90

Fridovich, I. 1975. Superoxide dismutases. *Annu. Rev. Biochem.* 44:147-159.

George, P., and C. J. Stratmann. 1952. The oxidation of myoglobin to metmyoglobin by oxygen. 2. The relation between the first order rate constant and the partial pressure of oxygen. *Biochem. J.* 51:418-425.

George, P., and C. J. Stratmann. 1954. The oxidation of myoglobin to metmyoglobin by oxygen. 3. Kinetic studies in the presence of carbon monoxide, and at different hydrogen-ion concentrations with considerations regarding the stability of oxymyoglobin. *Biochem. J.* 57:568–573.

Gotoh, T., and K. Shikama. 1976. Generation of the superoxide radical during autoxidation of oxymyoglobin. *J. Biochem. (Tokyo)*. 80:397–300

Kagen, L., S. Scheidt, L. Roberts, A. Porter, and H. Paul. 1975. Myoglobinemia following acute myocardial infarction. Am. J. Med. 58:177-182.

Levine, R. S., M. Alterman, R. S. Gubner, and E. C. Adams, Jr. 1971.
Myoglobinuria in myocardial infarction. Am. J. Med. Sci. 262:179–183.

Rabani, J., and S. O. Nielsen. 1969. Absorption spectrum and decay kinetics of O<sub>2</sub><sup>-</sup> and HO<sub>2</sub> in aqueous solutions by pulse radiolysis. *J. Phys. Chem.* 73:3736–3744.

Satoh, Y., and K. Shikama. 1981. Autoxidation of oxymyoglobin: A nucleophilic displacement mechanism. J. Biol. Chem. 256:10272– 10275.

- Shikama, K. 1984. A controversy on the mechanism of autoxidation of oxymyoglobin and oxyhaemoglobin: oxidation, dissociation, or displacement? *Biochem. J.* 223:279–280.
- Shikama, K. 1985. Nature of the FeO<sub>2</sub> bonding in myoglobin: an overview from physical to clinical biochemistry. *Experientia*. 41:701–706.
- Shikama, K. 1988. Stability properties of dioxygen-iron(II) porphyrins: an overview from simple complexes to myoglobin. *Coordination Chem. Rev.* 83:73-91.
- Shikama, K. 1990. Autoxidation of oxymyoglobin: an meeting point of the stabilization and the activation of molecular oxygen. *Biol. Rev.* (Cambridge). 65:517-527.
- Shikama, K., and A. Matsuoka. 1986. *Aplysia* oxymyoglobin with an unusual stability property: kinetic analysis of the pH dependence. *Biochemistry*. 25:3898–3903.
- Sitter, A. J., C. M. Reczek, and J. Terner. 1985. Observation of the Fe<sup>IV</sup> = O stretching vibration of ferryl myoglobin by resonance Raman spectroscopy. *Biochim. Biophys. Acta.* 828:229-235.
- Snyder, H. E. 1963. Heme dissociation and autoxidation of myoglobin. *Biochim. Biophys. Acta.* 69:200–202.
- Tajima, G., and K. Shikama. 1987. Autoxidation of oxymyoglobin: an

- overall stoichiometry including subsequent side reactions. *J. Biol. Chem.* 262:12603–12606.
- Tajima, G., and K. Shikama. 1992. Decomposition of hydrogen peroxide by metmyoglobin: a cyclic formation of the ferryl intermediate. *Int. J. Biochem.* In press.
- Taylor, J. F., and V. E. Morgan. 1942. Oxidation-reduction potentials of the metmyoglobin-myoglobin system. *J. Biol. Chem.* 144:15–20.
- Tew, D., and P. R. Ortiz de Montellano. 1988. The myoglobin protein radical: Coupling of Tyr-103 to Tyr-151 in the H<sub>2</sub>O<sub>2</sub>-mediated cross-linking of sperm whale myoglobin. *J. Biol. Chem.* 263:17880–17886.
- Uyeda, M., and J. Peisach. 1981. Ultraviolet difference spectroscopy of myoglobin: assignment of pK values of tyrosyl phenolic groups and the stability of the ferryl derivatives. *Biochemistry*. 20:2028–2035.
- Wallace, W. J., R. A. Houtchens, J. C. Maxwell, and W. S. Caughey. 1982. Mechanism of autoxidation for hemoglobins and myoglobins. Promotion of superoxide production by protons and anions. J. Biol. Chem. 257:4966–4977.
- Yusa, K., and K. Shikama. 1987. Oxidation of oxymyoglobin to metmyoglobin with hydrogen peroxide: involvement of ferryl intermediate. *Biochemistry*. 26:6684-6688.

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