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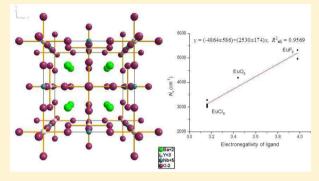
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# Double Perovskite Structure: A Vibrational and Luminescence Investigation Providing a Perspective on Crystal Field Strength

Wenyu Li, <sup>†</sup> Lixin Ning, <sup>‡</sup> and Peter A. Tanner\*, §

**ABSTRACT:** The luminescence spectra of Eu<sup>3+</sup> doped in a series of double perovskite lattices Ba<sub>2</sub>LnMO<sub>6</sub> (Ln = Y, Gd; M = Nb, Ta) have been recorded at room temperature and 10 K. Together with FT-IR and FT-Raman spectra and aided by DFT vibrational energy calculations, assignments have been made for the crystal field levels of the  ${}^5\mathrm{D}_I$  (J=0,1) and  ${}^7\mathrm{F}_I$  (J=0-2) multiplets. The luminescence spectra are consistent with monoclinic symmetry of these systems. The crystal field parameters from the fitting of the energy level data set of Ba<sub>2</sub>YNbO<sub>6</sub>:Eu<sup>3+</sup> enable the crystal field strength to be calculated, and the order of magnitude is Cl<sup>-</sup> < O<sup>2-</sup> < F<sup>-</sup> for the EuX<sub>6</sub><sup>n-</sup> (n = 6 for halogen, 9 for oxide) moieties. For these systems, an empirical linear relationship between crystal field strength and electronegativity of ligand X has been found. By



contrast, the nephelauxetic series from the depression of the Slater parameter  $F^2$  is  $Cl^- \approx O^{2-} > F^- >$  free ion for these systems.

# **■ INTRODUCTION**

The double perovskite structures of Ba<sub>2</sub>Ln(III)M(V)O<sub>6</sub> comprise the large alkaline earth cation Ba<sup>2+</sup> in the 12coordinated A-site and the Ln3+ and M5+ cations located at octahedral sites in the lattice. Figure 1 shows the structure of Ba<sub>2</sub>YNbO<sub>6</sub> plotted from the X-ray data from Fu and IJdo. The NbO<sub>6</sub> and YO<sub>6</sub> octahedra link at corners in a three-dimensional framework. The Goldschmidt tolerance factor,  $t = (r_A + r_O)/$  $[\sqrt{2(r_{\rm B}+r_{\rm O})}]$ , of simple cubic perovskites ABO<sub>3</sub> is close to 1.0, whereas values between 0.75 and 1.0 are associated with distortion to tetragonal or lower symmetries. For double perovskites, the mean radius of Ln(III) and M(V) replaces  $r_{\rm B}$  in the expression for the tolerance factor. The t values for eight Ba<sub>2</sub>Ln(III)M(V)O<sub>6</sub> systems investigated by Lavat and Baran<sup>2</sup> were between 0.91 and 0.99, and they were assumed to be cubic ordered perovskites (space group  $Fm\overline{3}m$ , Z=4) in that<sup>2</sup> and some other studies.<sup>1,3–7</sup> However, lower symmetry space groups have been proposed for these materials from other vibrational and X-ray diffraction studies. This is not unexpected, given the large difference in ionic radii between, for example, Nb<sup>5+</sup>(VI) 0.64 Å and Y<sup>3+</sup>(VI) 0.9 Å. The difficulties in establishing the structures of double perovskites have been discussed by Kennedy et al.8

The double perovskites have found various important applications, besides phosphors, in materials science. Nanorods of Ba<sub>2</sub>YNbO<sub>6</sub> have been embedded in YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7</sub> films in order to improve flux pinning in magnetic fields. Other applications include a lead-free ultrasonic transducer for microelectronics, solid oxide fuel cells, and microwave tunable

systems. 10-12 The band gaps of Ba<sub>2</sub>YTaO<sub>6</sub> and Ba<sub>2</sub>YNbO<sub>6</sub> are 4.6 and 3.8 eV, respectively. The valence band is mainly composed of O(2p) orbitals, whereas the conduction band arises from the interaction between oxygen and transition metal t<sub>2g</sub> orbitals for which the overlap increases when replacing a 4d ion with a more electropositive 5d ion.<sup>14</sup>

The luminescence of Ba<sub>2</sub>GdNbO<sub>6</sub> doped with Eu<sup>3+</sup> has been reported as a stick diagram by Blasse et al.4 The local site symmetry of Eu<sup>3+</sup> was assumed to be  $O_h$ , and the strong selfquenching of emission was attributed to exchange coupling via the NbO<sub>6</sub> moiety since the Eu-Eu separation is quite large (6 Å). An alternative explanation was offered by Qi et al. 15 in their study of the optical spectra of Ba<sub>2</sub>NdNbO<sub>6</sub>. A crystal disorder of ~1% would be scarcely detectable by X-ray diffraction. In such a case, the separation of some Eu3+ ions would, however, be much smaller (3.6 Å) when occupying both of the Gd3+ and Nb<sup>3+</sup> sites in Ba<sub>2</sub>GdNbO<sub>6</sub>, providing a self-quenching pathway.

The luminescence of several double perovskites doped with the probe ion Eu<sup>3+</sup> has been investigated in the present study for a dual purpose. First, the interpretation of the lowtemperature spectra of the Eu<sup>3+</sup> ion in crystals is welldocumented and can provide an indication of the site symmetry (or symmetries) of this impurity ion. This is simple because the electronic ground state ( ${}^{7}F_{0}$ ) and the luminescent state ( ${}^{5}D_{0}$ ) are both nondegenerate, and the observation of multiple <sup>5</sup>D<sub>0</sub>

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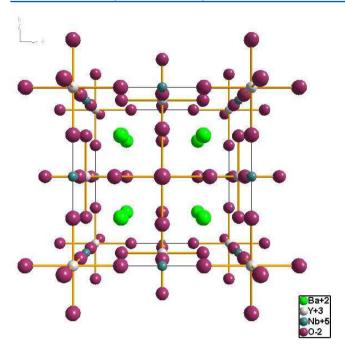


Figure 1. Structure of  $Ba_2YNbO_6$  viewed along the c crystal axis (data from ref 1).

 $\rightarrow$  <sup>7</sup>F<sub>0</sub> emission bands indicates the presence of multiple sites. The comparison of band intensities for the transitions enabled by magnetic dipole and forced electric dipole mechanisms, as well as the patterns of band splittings, provides additional site symmetry information. The description of the vibrational behavior of the crystal system using a first-principles calculation was useful for the understanding of the electronic spectra. The second motivation for this work utilized the (pseudo-) octahedral symmetry of the EuO<sub>6</sub> 9- moiety, where theoretical parametrization is at a minimum, to gain a deeper understanding of metal-ligand interactions. The most concise way of summarizing such interactions lies in the crystal field strength parameter, subsequently defined. It transpires that the combination of results from this work with those from octahedral  $EuX_6^{3-}$  (X = Cl, F) systems provides a link between crystal field strength and electronegativity of X.

# **■ EXPERIMENTAL SECTION**

The neat or doped double perovskites samples were prepared by a standard solid-state reaction method from the starting materials of BaCO<sub>3</sub> (Aldrich, 99.999%), Ln<sub>2</sub>O<sub>3</sub> (Sigma-Aldrich, 99.999%), Nb<sub>2</sub>O<sub>5</sub> (Strem, 99.999%), Ta<sub>2</sub>O<sub>5</sub> (Strem, 99.999%) in stoichiometric amounts, and the dopants of Eu<sub>2</sub>O<sub>3</sub> (Sigma-Aldrich, 99.999%). The masses of the starting materials Ba<sub>2</sub>CO<sub>3</sub>, Ta<sub>2</sub>O<sub>5</sub>, and Nb<sub>2</sub>O<sub>5</sub> were 1.973, 1.105, and 1.329 g, respectively. The dopant ion concentrations were nominally 0.1 atom % to 10 atom % for Eu<sup>3+</sup>. The appropriate mixture was ground, placed in a ceramic crucible, and prefired in air at 1000 °C for 12 h to decompose BaCO<sub>3</sub>. The products were then reground, put into a platinum crucible, and sintered at 1200 °C for 24 h, and then at 1300 and 1400 °C for 48 h. In each step, the products were reground homogeneously.

X-ray powder diffraction (XRD) patterns were acquired on a Siemens D500 diffractometer using Cu K $\alpha$  ( $\lambda$  = 1.54056 Å) at 40 kV and 30 mA with a scanning rate of 1.2° min<sup>-1</sup> in the angle range from 10° to 80°. The FT-IR absorption spectra of all the related samples in discs or nujol mulls were recorded at

room temperature in the range from 400 to 4000 cm<sup>-1</sup> using a Nicolet FT-IR instrument with resolution 4 cm<sup>-1</sup>. FT-Raman spectra of all the related samples in pellet form were recorded at room temperature by a Perkin-Elmer Spectrum 2000 spectrometer using a resolution of 4 cm<sup>-1</sup>. Room temperature excitation and emission spectra (resolution ~3 nm) were recorded by a Jobin-Yvon Fluoromax-3 spectrofluorometer using a xenon lamp as the light source, and the signal was detected by a Hamamatsu R636 photomultiplier. Highresolution emission spectra were recorded at resolution between 2-4 cm<sup>-1</sup> by an Acton 0.5 m monochromator having a 1200 groove mm<sup>-1</sup> grating blazed at 500 nm, and a backilluminated SpectruMM CCD detector, using an Optical Parametric Oscillator (Panther) pumped by the third harmonic of a Surelite Nd:YAG pulsed laser. The signal was collected at 90°. The sample was housed in an Oxford Instruments closed cycle cryostat.

# **■ THEORETICAL SECTION**

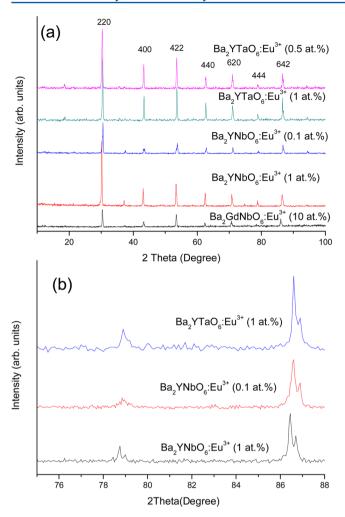
Computational Method. The first-principles calculations were carried out using the DFT plane-wave code VASP<sup>16</sup> with the GGA-PBE exchange-correlation functional. <sup>17</sup> The 5s<sup>2</sup>5p<sup>6</sup>6s<sup>2</sup> electrons on Ba, the 4s<sup>2</sup>4p<sup>6</sup>4d<sup>1</sup>5s<sup>2</sup> electrons on Y, the 4s<sup>2</sup>4p<sup>6</sup>4d<sup>4</sup>5s<sup>1</sup> electrons on Nb, and the 2s<sup>2</sup>2p<sup>4</sup> electrons on O were treated as valence electrons in the calculations. The interaction between the valence electrons and the core was described using the projected augmented wave (PAW) method. 18,19 As a first step in determining the vibrational frequencies, the lattice and internal parameters of the Ba<sub>2</sub>YNbO<sub>6</sub> primitive cell were optimized until the total forces on each ion were less than  $10^{-4}$  eV Å $^{-1}$ . The  $\Gamma$ -point vibrational frequencies were then computed by a finite-difference approach with a step size of 0.02 Å at 0 K. To ensure the convergence of results, the cutoff energy for the plain-wave basis was set to 400 eV, the criterion for electronic minimization was 10<sup>-6</sup> eV, and a  $6 \times 6 \times 6$  Monkhorst-Pack k-point grid (63 irreducible k points) was used to sample the Brillouin zone.

# ■ RESULTS AND DISCUSSION

**XRD Powder Patterns.** Some powder X-ray diffraction patterns of the europium-doped barium double perovskites are displayed in Figure 2a. Two points are notable. First, all of the patterns are dominated by lines strongly resembling the primitive cubic perovskite but many lines are clearly split (a scale enlargement is provided in Figure 2b). This indicates that the room temperature crystal symmetries are lower than cubic. Second, there is a shift to smaller  $\theta$  values for the more highly doped Eu³+ samples of Ba₂YMO<sub>6</sub> (M = Nb, Ta) resulting from a lattice expansion. For example, the peak at 30.2° in the 1% sample is at 30.6° in the 0.1% doped sample. This is consistent with the greater ionic radius of Eu³+(VI) 0.947 Å compared with Y³+(VI) 0.9 Å.

**Vibrational Frequency Calculations.** The optimization gave the values of the lattice parameter of  $Ba_2YNbO_6$  as 8.4534 Å, and the internal parameter for oxygen as x = 0.2641. The corresponding experimental values are 8.4316 Å and 0.2665, respectively.<sup>1</sup>

In the space group  $Fm\overline{3}m$ , the irreducible representations of the  $\mathbf{k}=0$  normal modes of vibration of  $Ba_2LnMO_6$  systems transform as  $A_{1g}(R)+E_g(R)+2T_{2g}(R)+T_{1g}(rot)+4T_{1u}(IR)+T_{1u}(ac)$ , where the notation in brackets denotes Raman or infrared activity, and rot and ac are rotational and acoustic



**Figure 2.** (a) Powder X-ray diffraction patterns of europium-doped barium double perovskites. A scale expansion is shown in panel b.

modes. The  $A_{1g}$  and  $E_g$  modes involve only oxygen motion, but barium ions move additionally for the  $T_{2g}$  mode. The  $A_{1g}$  mode is a breathing mode of the octahedron, whereas in the  $E_g$  mode, when four coplanar oxygens move toward the octahedron center, the other two oxygen ions move outward. The reported Raman spectrum of  $Ba_2MnWO_6$  using 476 nm excitation is an excellent example of the expected 4-band Raman spectrum,

with the  $A_{1g}$  peak much stronger than  $E_g$ .<sup>7</sup> Similar vibrational data for  $Ba_2GdSbO_6$  are included in Table 1, column 8.<sup>5</sup>

The calculated vibrational energies for  $Ba_2YNbO_6$ , under the  $Fm\overline{3}m$  space group, are listed in Table 1, column 3, with approximate mode descriptions given in column 2. Vibrational data for  $Ba_2YMO_6$  from the present study are shown in Figure 3, and salient energies from  $Ba_2YNbO_6$  are listed in Table 1, columns 4 (from our results) and 5 (from previous studies). The agreement with calculation is reasonable.

It is evident, however, from the IR and Raman spectra of  $Ba_2YNbO_6$  that more bands are present than those expected for a cubic system. The studies of Dias et al.  $^{20-25}$  have arbitrarily fitted Lorentzian lines to the Raman spectra of double perovskites and then equated the number of lines to those predicted for certain symmetries. This fitting method has been criticized elsewhere  $^{26,27}$  and described as mathematic rather than crystallographic. Symmetry lowering from the  $Fm\overline{3}m$  space group can result from cation ordering in combination with the corner-linked tilting of the octahedral units and/or distortion of the octahedra. Group—subgroup relationships establish the space group possibilities upon tilting of one axis to be from  $Fm\overline{3}m$  to I4/m or P4/mnc and then to  $P2_1/c$ . Rietveld analysis of the room temperature X-ray data of  $Ba_2LnNbO_6$  (Ln = Gd, Eu) gave structures consistent with the  $P2_1/n$  space group.

The vibrational frequency calculation was also performed in the space group I4/m for Ba<sub>2</sub>YNbO<sub>6</sub>, and we do not report this calculation in detail because two imaginary frequencies were then found. As expected, the vibrational degeneracies were removed but the gap between the calculated A<sub>1g</sub> mode (795 cm<sup>-1</sup>) and the E<sub>g</sub> modes (551, 539 cm<sup>-1</sup>) remained large. This is contrary to the experimental Raman spectra, where a feature at 747 cm<sup>-1</sup> is observed. It therefore does not appear that this band is related to the descent in symmetry to I4/m, but presumably it arises in the descent to lower symmetry. Two previous reports may also be relevant. Yashima et al.<sup>31</sup> observed a peak at 811 cm<sup>-1</sup> in the Raman spectrum of YNbO<sub>4</sub>, but the frequency was rather lower (at 778 cm<sup>-1</sup>) in Y<sub>3</sub>NbO<sub>7</sub>. In the latter compound, and in the defect fluorite solid solutions  $Y_{100-x}Nb_xO_{150+x}$  (20 < x < 25), it was suggested that disorder exists so that some Nb ions substitute for Y and O substitutes for oxygen vacancy. Second, from the Raman and synchrotron X-ray diffraction study of Ba<sub>2</sub>YTaO<sub>6</sub>, Zhou et al.<sup>32</sup> provided evidence that the peak at 747 cm<sup>-1</sup> in Ba<sub>2</sub>YTaO<sub>6</sub> increases in intensity after ball-milling the sample, which serves to create

Table 1. Vibrational Modes and Their Calculated and Experimental Energies in Some Double Perovskite Systems<sup>a</sup>

|   |                                  |       | Ba <sub>2</sub> YNbO <sub>6</sub> <sup>c</sup> |                     |              |               |   |
|---|----------------------------------|-------|--|---------------------|--------------|---------------|---|
| $O_h$ symmetry mode   | approx. description <sup>b</sup> | calcd | obs  | obs <sup>2,20</sup> | $Ba_2YTaO_6$ | $Ba_2GdNbO_6$ | Ba <sub>2</sub> GdSbO <sub>6</sub> <sup>5</sup> |
| $A_{g}$   | Nb-O sym str                     | 804   | 811 R  | 800 R               | 841 R        | 810 R         | 762 R   |
|   | O-Nb-O str                       | 551   | 538 R  | 534 R               | 562 R        | 537 R         | 575 R   |
| $egin{aligned} \mathbf{E_g} \\ \mathbf{T_{1u}} \end{aligned}$ | Nb-O antisym str                 | 525   | 556 IR   | 556 IR              | 567 IR       | 530 IR        | 627 IR  |
| $\mathrm{T}_{\mathrm{2g}}$                                    | O-Nb-O bend                      | 363   | 384 R  | 372 R               | 390 R        | 380 R         | 375 R   |
| $\mathrm{T_{1u}}$   | Y-O antisym str                  | 303   | 337 IR   | 337 IR              |              |               |   |
| $\mathrm{T_{1u}}$   | O-Y-O bend                       | 192   |  |                     |              |               |   |
| $T_{2u}$  | O-Y-O bend                       | 163   |  |                     |              |               |   |
| $\mathrm{T}_{\mathrm{2g}}$                                    | lattice                          | 95    |  | 95 R                |              |               | 105 R   |
| ${ m T_{1u}}$   | lattice                          | 92    |  |                     |              |               |   |
| $\mathrm{T_{1u}}$   | acoustic                         |       |  |                     |              |               |   |

<sup>&</sup>quot;Unless indicated otherwise, the data are from the present study. "Sym, symmetric; str, stretch; antisym, antisymmetric. "Calcd, calculated; Obs, observed; R, Raman; IR, infrared.

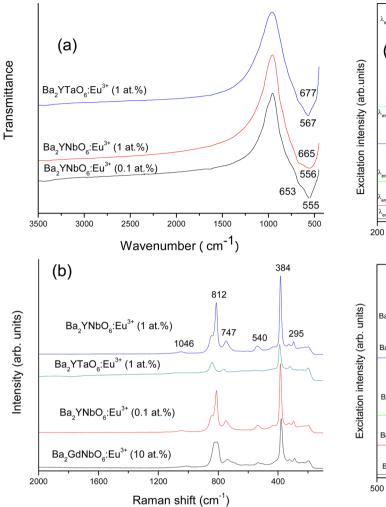


Figure 3. Infrared (a) and Raman (b) spectra of Eu<sup>3+</sup>-doped barium double perovskites at room temperature.

defect sites. This band was in fact assigned to the cubic E<sub>g</sub> mode by these authors, which is considered to be unlikely from our calculations. The presence of disorder was found to inhibit the cubic-tetragonal transition at ~260 K in this material, and it was concluded that prolonged sample heating is necessary in order to establish long-range ordering of Ta and Y atoms. Hammink et al. gave a similar conclusion for the ordering between In3+ and Ta5+ cations in Ba2InTaO6 from Rietveld profile analysis of X-ray diffraction data, 26 and a high degree of short-range order was proposed for the Fe/Mo cation antisite defects in Sr<sub>2</sub>FeMoO<sub>6</sub>.

Room Temperature Electronic Spectra. The room temperature excitation and emission spectra of some double perovskites doped with Eu3+ are shown in Figure 4, and all spectra show similar characteristics for the Eu<sup>3+</sup> transitions. Some of the terminal multiplet terms are marked in Figure 4a. The absorption occurs from the  ${}^{7}F_{0}$  and  ${}^{7}F_{1}$  multiplets at room temperature. The spectral resolution is not adequate for band assignments of crystal field levels. The emission spectra (Figure 4b) exhibit maximum intensity at ~595 nm and differ considerably from those reported by Xiao and Yan<sup>33</sup> but are consistent with the emission spectrum of Blasse et al.<sup>4</sup> and Yu et al.<sup>34</sup> The room temperature charge transfer excitation and emission bands of Ba<sub>2</sub>YNbO<sub>6</sub> and Ba<sub>2</sub>YTaO<sub>6</sub> have been reported at 314, 263 nm (excitation) and 530, 390 nm

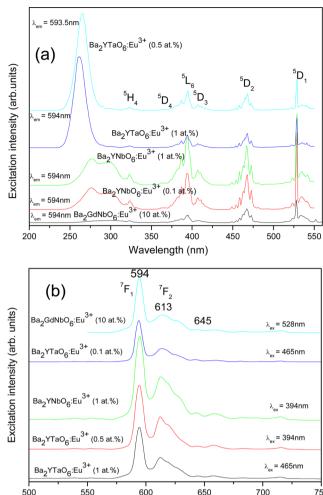


Figure 4. Room temperature excitation (a) and emission (b) spectra of europium-doped double perovskites. Some of the terminal multiplet terms are indicated. The excitation is from  ${}^{7}F_{0,1}$ , whereas the emission is from <sup>5</sup>D<sub>0</sub>.

Wavelength (nm)

550

(emission), respectively. 13 The maxima in the room temperature excitation spectra (Figure 3a) are at 262 nm and 277, 305 nm, respectively for Ta-O and Nb-O charge transfer bands, but the corresponding emission bands are almost quenched via energy transfer to Eu<sup>3+</sup>. Yu et al.<sup>34</sup> have reported the room temperature <sup>5</sup>D<sub>0</sub> lifetime in Ba<sub>2</sub>GdNbO<sub>6</sub>:Eu (10 at. %) to be 2.26 ms. The radiative (natural) lifetime of the  $^5D_0$  state may be estimated by the comparison of the integrated areas of emission,  $I[^5D_0 \rightarrow {}^7F_1]/I[^5D_0 \rightarrow {}^7F_j; J = 0-6]$  and taking the spontaneous emission probability of  $^5D_0 \rightarrow {}^7F_1$  to be 14.65 s<sup>-1</sup> in vacuo.<sup>35</sup> By assuming a refractive index of 2.1 <sup>36</sup> and employing the integrated areas at room temperature, the <sup>5</sup>D<sub>0</sub> natural lifetime is then estimated to be 7.4 ms in  $Ba_2GdNbO_6{:}Eu^{3+}$  (10 at. %). By using the observed lifetime above, this infers an internal quantum efficiency of 31%.

The CIE coordinates of  $Ba_2YNbO_6$ :  $Eu^{3+}$  (0.1 at. %) emission spectrum, excited by 459.7 nm radiation at 100 K, are (0.602, 0.398), similar to those of the Ba<sub>2</sub>YNbO<sub>6</sub>:Eu<sup>3+</sup> (1 at. %) spectrum excited by 467 nm radiation at room temperature (0.612, 0.386). These color coordinates lie at the edge of the color gamut on the chromaticity diagram, representing maximum saturation for orange-red.

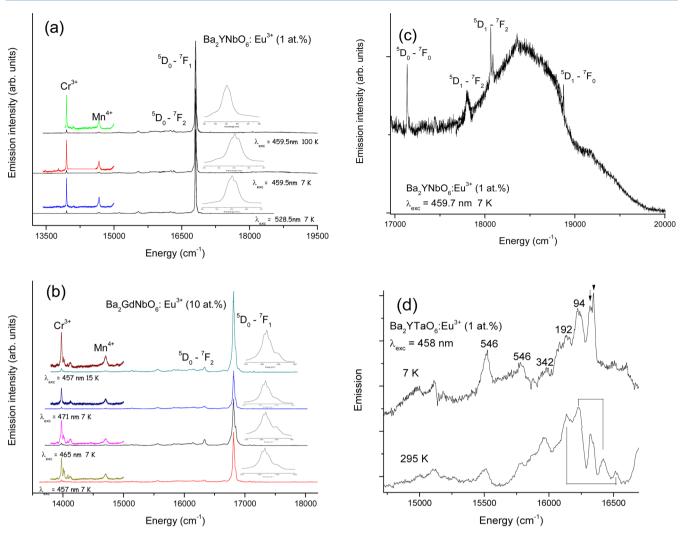


Figure 5. Emission spectra of  $Eu^{3+}$ -doped double perovskites: (a,b) 10 K survey spectra of  $Ba_2YNbO_6$ : $Eu^{3+}$  and  $Ba_2GdNbO_6$ : $Eu^{3+}$ . Scale expansions of the  $^5D_0 \rightarrow ^7F_1$  bands are indicated; (c) region between 20 000 and 16 950 cm $^{-1}$  of the 10 K  $Ba_2YNbO_6$  spectrum on an expanded scale; (d) region between 16 670 and 14 730 cm $^{-1}$  of the 10 and 295 K  $Ba_2YTaO_6$  spectra on an expanded scale.

Low Temperature Electronic Spectra. The survey 10 K emission spectra of the Eu<sup>3+</sup>-doped Ba<sub>2</sub>LnNbO<sub>6</sub> (Ln = Y,Gd) systems are displayed in Figure 5a,b, employing energy scales. In each case, the  $^5D_0 \rightarrow {}^7F_1$  magnetic dipole transition at  $\sim 595$ nm ( $\sim$ 16 800 cm<sup>-1</sup>) dominates the entire spectrum. The insets in these figures show that this band is split into 3 components in each case, so that the highest possible site symmetry point group of Eu<sup>3+</sup> comprises a  $C_2$  axis. The relative intensities of the  $^5\mathrm{D}_0 \to {}^7\mathrm{F}_1$  and  $^5\mathrm{D}_0 \to {}^7\mathrm{F}_2$  bands show a sharp contrast to those of Ba<sub>2</sub>LaNbO<sub>6</sub> doped with Eu<sup>3+</sup>, where the latter features dominate.<sup>37</sup> In the present case, the dominance of  ${}^5D_0 \rightarrow {}^7F_1$ indicates centrosymmetry, or very near centrosymmetry, for the  $\text{EuO}_6^{\,9-}$  moiety. The  $\text{Eu}^{3+}$  site symmetry alternatives are then  $C_{2h}$  or  $C_i$ . Unfortunately, just as in the emission spectra of Ba<sub>2</sub>LaNbO<sub>6</sub>,<sup>37</sup> the lower energy regions of the emission spectra of our samples comprise bands due to the luminescence of Mn<sup>4+</sup> and Cr<sup>3+</sup> which are not further reported. We were therefore unable to measure the Eu<sup>3+</sup>emission in these spectral regions. Our analysis is therefore curtailed to the  ${}^5D_{0,1} \rightarrow {}^7F_{0,1,2}$ transitions of Eu<sup>3+</sup>.

Figure 5c shows the enlargement of the 459.7 nm excited 7 K spectrum of  $Ba_2YNbO_6$ : $Eu^{3+}$  (1 at. %) between 20 000 and 16 950 cm $^{-1}$ . Some sharp features due to  $Eu^{3+}$  overlay the

broadband structure peaking at ~18 430 cm<sup>-1</sup> (542 nm) corresponding to the Nb–O charge transfer emission. The highest energy band, at 18 875 cm<sup>-1</sup>, corresponds to the  $^5D_1 \rightarrow ^7F_0$  transition, whereas bands due to  $^5D_1 \rightarrow ^7F_2$  are observed at 18 088, 18 064, and 17 803 cm<sup>-1</sup>. The appearance of the  $^5D_0 \rightarrow ^7F_0$  band at 17 136 cm<sup>-1</sup> indicates a slight deviation from centrosymmetry.

The emission spectra of Ba<sub>2</sub>YTaO<sub>6</sub>:Eu<sup>3+</sup> between 16 675 and 14 730 cm<sup>-1</sup> at 7 K and room temperature are shown in Figure 5d. The higher energy bands are associated with the  ${}^5D_0 \rightarrow {}^7F_2$ transition. The correspondence of Stokes and anti-Stokes features is indicated in the room temperature spectrum, and this enables the vibrational assignments shown in the 7 K spectrum to be made. The inferred zero phonon lines of this transition are masked by the nearby variable-intensity bands, indicated by vertical arrows in the upper figure. These features are associated with forced electric dipole transitions at Eu<sup>3+</sup>defect sites. The assigned vibration at 94 cm<sup>-1</sup> in the upper figure is associated with the  $T_{2g}/T_{1u}$  modes, whereas the 192, 342, and 546 cm<sup>-1</sup> vibrations correspond to  $T_{1u}$  modes. The latter energy is rather smaller than that in the infrared spectrum of bulk Ba<sub>2</sub>YTaO<sub>6</sub> since it shows, according to the local luminescent probe Eu<sup>3+</sup>, a slight weakening of the Ta-O

bond when the cation  $Y^{3+}$  is replaced by the 5.2% larger  $Eu^{3+}$ ion.

**Crystal Field Calculations.** The deduced energy levels of  ${\rm Eu}^{3+}$  are fairly similar for the  ${\rm Ba_2LnMO_6:Eu}^{3+}$  systems investigated herein so that only the data for the  ${\rm Ba_2YNbO_6}$  host is discussed. The calculation of electronic energy levels for the  ${\rm 4f}^6$  configuration employed the f-shell programs of Professor M. F. Reid in which the energy levels were derived by simultaneous diagonalization of various parametrized interaction Hamiltonians. The details of such calculations can be found in ref 38. Only the energy level values for the  ${}^7{\rm F}_J$  (J=0-2) and  ${}^5{\rm D}_J$  (J=0,1) have been determined by experiment. For  ${\rm Ba_2YNbO_6}$ , the determined energies are listed in Table 2,

Table 2. Energy Level Fit for Eu<sup>3+</sup> Levels in Ba<sub>2</sub>YNbO<sub>6</sub>

| $^{2S+1}L_{J}\Gamma$          | calcd <sup>a</sup> | $\operatorname{exptl}^b$ | calcd - exptl |
|-------------------------------|--------------------|--------------------------|---------------|
| <sup>7</sup> F <sub>0</sub> A | 0                  | 0                        | 0             |
| $^{7}$ F $_{1}$ T             | 350                | 332                      | 18            |
| $^{7}$ F $_{2}$ E             | 803                | 797                      | 6             |
| T                             | 1070               | 1067                     | 3             |
| $^{7}F_{3}$ A                 | 1735               |                          |               |
| T                             | 1921               |                          |               |
| T                             | 1950               |                          |               |
| $^{7}F_{4}$ T                 | 2604               |                          |               |
| E                             | 2906               |                          |               |
| T                             | 3048               |                          |               |
| A                             | 3155               |                          |               |
| $^{7}F_{5}$ T                 | 3731               |                          |               |
| E                             | 3759               |                          |               |
| T                             | 3828               |                          |               |
| T                             | 4088               |                          |               |
| <sup>7</sup> F <sub>6</sub> E | 4744               |                          |               |
| T                             | 4780               |                          |               |
| A                             | 4846               |                          |               |
| T                             | 5316               |                          |               |
| T                             | 5346               |                          |               |
| A                             | 5376               |                          |               |
| $^5D_0$ A                     | 17152              | 17137                    | 15            |
| $^5D_1$ T                     | 18863              | 18872                    | -10           |
|                               |                    |                          |               |

 $<sup>^</sup>a$ Calculated energy using the parameters in Table 3.  $^b$ Corrected barycenter energy.

from the experimental values of 325, 332, and 338 cm<sup>-1</sup> ( ${}^{7}F_{1}$ ) and 785, 809, and 1067 ( ${}^{7}F_{2}$ ). The conversion of the nondegenerate crystal field level energies to those appropriate for Oh symmetry was made by using the level barycenters so that only 6 experimental energy levels are available (Table 2). The octahedral point group  $(O_h)$  of the rare-earth site imposes two independent crystal field parameters,  $B_{40}$  and  $B_{60}$ . The values of the Slater parameters,  $F^2$ , for Coulomb interaction between the 4f electrons,  $\zeta(4f)$  for the spin-orbit interaction, and the two crystal-field parameters were varied simultaneously within certain allowed ranges and optimized until the best agreement was obtained between the calculated and observed energy levels. Thus, the total number of variable parameters in the fit was equal to 4. The ratios  $F^4/F^2$  (= 0.77235) and  $F^6/F^2$ (= 0.54016) and the values of the configuration interaction parameters,  $\alpha$ ,  $\beta$ , and  $\gamma$ , as well as the k=0 magnetic interaction parameters  $M^{k}$  ( $M^{2} = 0.56 M^{0}$ ;  $M^{4} = 0.38 M^{0}$ ) were held fixed and equal to those of the elpasolite compound Cs2NaEuCl6. The resulting parameter values are listed in column 2 of Table 3, and the calculated 4f<sup>6</sup> crystal field energy levels are given in column 2 of Table 2. It is noted that the parameter values for Eu<sup>3+</sup> in Ba<sub>2</sub>YNbO<sub>6</sub> apply to a small data set comprising the <sup>5</sup>D<sub>1</sub> (J = 0.1) and  ${}^{7}F_{I}$  (J = 0-2) multiplets. Nevertheless, the values of the Slater and spin-orbit coupling parameters represent the lowest ones in the table. The comparison of the  $F^2$  and  $\zeta(4f)$ values in Table 3 with those of the free Eu<sup>3+</sup> ion, namely, 113 551 cm<sup>-1</sup> and 1414 cm<sup>-1</sup>, <sup>40,41</sup> respectively, shows decreases of ~30% and 7%, respectively. Such decreases are normally associated with nephelauxetic effects, as an expansion of the 4f electron cloud in a crystal. The expected nephelauxetic effect (i.e., depression of  $F^2$ ) for the centroid shift of EuX<sub>6</sub> is Cl<sup>-</sup> >  $O^{2-} > F^{-} >$  free ion,<sup>42</sup> and in the present case,  $Cl^{-} \approx O^{2-}$ . The nephelauxetic effect is notably weaker for Eu<sup>3+</sup> in 12coordination (Cs2NaEu(NO2)6, Table 2) due to the considerably longer Eu-O bond distance.<sup>45</sup> The Eu-O bond distances in the Eu $(O_2N)_6^{3-}$  and Eu $O_6^{9-}$  moieties are 2.65  $\pm$ 0.2 Å<sup>45</sup> and 2.247 Å.<sup>1</sup>

The parameters  $B_{20}$  and  $B_{22}$  of the Hamiltonian  $B_{20}C_{20}+B_{22}$  ( $C_{22}+C_{2-2}$ ) are responsible for the splitting of the  $^7F_1$  ( $O_h$ ) J=1 level. On the basis of the symmetry considerations, this level will split into the  $|J,M_J\rangle$  states  $|1,0\rangle$ ,  $|1,1\rangle-|1,-1\rangle$ , and  $|1,1\rangle+|1,-1\rangle$  (with normalization factors neglected). The relative energies and the energy ordering of these states depend on the magnitude and sign of the  $B_{20}$  and  $B_{22}$  parameters. The use of

Table 3. Energy Parameter Values for Some Eu<sup>3+</sup> Crystalline Systems<sup>a</sup>

|                      | value (cm <sup>-1</sup> )                            |                                   |   |                         |  |
|----------------------|--|-----------------------------------|---|-------------------------|--|
|                      | Ba <sub>2</sub> YNbO <sub>6</sub> :Eu <sup>3+b</sup> | Cs₂NaEuCl <sub>6</sub>            | Cs <sub>2</sub> NaYF <sub>6</sub> :Eu <sup>3+</sup> | $Cs_2NaEu(NO_2)_6^b$    |  |
| parameter            | $NbO_6(O_h)$   | $\operatorname{EuCl}_6(O_h)^{39}$ | $\operatorname{EuF_6}(O_h)^{43}$                    | $EuO_{12}(T_h)^{44,45}$ |  |
| $F^2$                | 79186  | 79688(109)                        | 83789(50)   | 82149                   |  |
| $\zeta(4\mathrm{f})$ | 1308   | 1331(2)                           | 1323(13)  | 1331                    |  |
| $B_{40}$             | 2707   | 1936(23)                          | 3138(65)  | -327                    |  |
| $B_{60}$             | 88   | 245(16)                           | 382(42)   | -260                    |  |
| $B_{62}$             |  |                                   |   | -1680                   |  |
| N                    | 6  | 77                                | 21  | 22                      |  |
| $n_{ m p}$           | 4  | 11                                | 4   | 7                       |  |
| $\delta_2^{}$        | 10.5   | 14.2                              | 31.5  | 18.9                    |  |

<sup>&</sup>lt;sup>a</sup>The parameter values (in cm<sup>-1</sup>):  $\alpha$  = 27.7,  $\beta$  = -1272,  $\gamma$  = 1461,  $M^0$  = 2.13,  $P^0$  = 195,  $T^2$  = 278,  $T^3$  = 40,  $T^4$  = 40,  $T^6$  = -546,  $T^7$  = 244,  $T^8$  = 241, were fixed with the values taken from the fit of Cs<sub>2</sub>NaEuCl<sub>6</sub>. The ratios  $F^4/F^2$  (= 0.77235) and  $F^6/F^2$  (= 0.54016) were held fixed. N number of energy levels fitted;  $n_{\rm p}$  number of adjustable parameters;  $\delta_2$  mean deviation of fit. Values in parentheses indicate uncertainties. <sup>b</sup>No uncertanties available.

parameter values  $B_{20} = -37.3$  cm<sup>-1</sup> and  $B_{22} = -15.3$  cm<sup>-1</sup> provides calculated  $^7F_1$  energies (in cm<sup>-1</sup>) of 341, 350, and 359, which are in the best agreement with the experimental results for Ba<sub>2</sub>YNbO<sub>6</sub>:Eu<sup>3+</sup>. These parameter values are small when compared with  $B_{40}$  and indicate a small deviation from octahedral symmetry. Fixing the magnitudes of these parameter values but changing their signs gave the following conclusions. First, the signs of  $B_{20}$  and  $B_{22}$  have no influence on the level energies but do affect the character of the levels. That is, only from the experimental energies, the signs of the  $B_{20}$  and  $B_{22}$  parameters cannot be uniquely determined. Second, if  $B_{20}$  is negative, then  $^7F$  |1 0 $\rangle$  is the lowest state, whereas if  $B_{20}$  is positive, then  $^7F$  |1,0 $\rangle$  is the highest state. The sign of  $B_{22}$  decides the relative ordering of the |1,1 $\rangle$  – |1,-1 $\rangle$  and |1,1 $\rangle$  + |1,-1 $\rangle$  states.

A comparison of the calculated parameters can be made with those from some related previous studies. Wakeshima et al. 46 have stated, from magnetic susceptibility measurements, that the spin—orbit coupling constant for Eu 3+ in Ba 2Eu Ir O6 is 364 cm -1. This value is in fact the calculated energy difference between the  $^7F_0$  and  $^7F_1$  multiplet states and in the absence of *J*-mixing would be equal to  $\zeta(4f)/6$ . Zhou et al. 13 have investigated the luminescence of Ba 2YMO (M = Nb, Ta) doped with Yb 3+ at room temperature. The spectra were assigned to Yb 3+ at an octahedral site in this host. From the experimental determination of four energy levels of Yb 3+ in Ba 2YNbO 6, the crystal field parameters were calculated as (in cm -1)  $B_{40} = 2165$ ,  $B_{60} = 122$ . These values are in reasonable agreement with the present study.

The scalar crystal field strength parameter, which measures the average ligand field effect, is defined by Auzel and Malta as  $^{47,48}$ 

$$N_{\rm v} = \left[ \sum_{k,q} \frac{4\pi}{2k+1} B_{k,q}^2 \right]^{1/2}$$

It has been demonstrated that the relationship between  $N_{\rm v}$  and the maximum crystal field splitting of a multiplet is linear. <sup>47,48</sup> For lanthanide ions, the crystal field strength has been proposed to follow a different trend from the nephelauxetic series, namely,  ${\rm Cl}^- < {\rm F}^- < {\rm O}^{2-.42}$  Some values of  $N_{\rm v}$  for EuX<sub>6</sub> (X = Cl, F, O) and EuO<sub>12</sub> systems are listed in Table 4. Variations in the value of  $N_{\rm v}$  for a given system are

Table 4. Scalar Crystal Field Strengths of Some High Symmetry Eu<sup>3+</sup> Systems

| system  | moiety (symmetry) | range of $N_{\rm v}~({\rm cm}^{-1})$ | refs      |
|---|-------------------|--------------------------------------|-----------|
| Cs <sub>2</sub> NaYF <sub>6</sub> :Eu <sup>3+</sup> | $EuF_6(O_h)$      | 4970-5317                            | 43, 49    |
| BaYNbO <sub>6</sub> :Eu <sup>3+</sup>               | $EuO_6(O_h)$      | 4195                                 | this work |
| Cs <sub>2</sub> NaEuCl <sub>6</sub>                 | $EuCl_6(O_h)$     | 3000-3293                            | 39, 50    |
| $Cs_2NaEu(NO_2)_6$                                  | $EuO_{12}(T_h)$   | 2447                                 | 44        |

mainly due to (i) the different number of crystal field levels fitted in the energy parametrization, due to the variation of crystal field parameters for different multiplet terms; (ii) fitting errors, due to holding certain parameters at assumed constant values. The above trend is not followed since  $N_{\rm v}$  is clearly the greatest for the fluoride system. Herein, we have found another relationship for  $N_{\rm v}$ . It is found that  $N_{\rm v}$  is linearly related to the electronegativity of X for the EuX<sub>6</sub> systems (Figure 6) with the equation given in the figure. The rather scarce crystal field data sets reported from the electronic spectra of LnBr<sub>6</sub><sup>3-</sup>

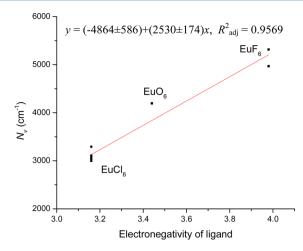


Figure 6. Empirical relationship between crystal field strength and electronegativity of X in  $EuX_6$ .

systems<sup>50,51</sup> do not show a consistent trend across the lanthanide series. The value of  $N_{\rm v}$  for Ln = Tb is 2323 cm<sup>-1,51</sup> Using the equation in Figure 6 together with the electronegativity 2.96 for Br, the predicted value of  $N_{\rm v}$  for EuBr<sub>6</sub><sup>3-</sup> (expected to be greater) is 2625 cm<sup>-1</sup> with a ~6% fitting error.

Comparison with Ab initio Calculation. Visser et al. have performed a molecular open shell configuration interaction calculation using the Dirac–Coulomb Hamiltonian for the  $4f^6$  configuration of  $Eu^{3+}$  in octahedral symmetry for the  $EuO_6^{\,9-}$  moiety.  $^{52}$  It was found necessary to utilize an embedded cluster model in order to simulate the crystal field splittings. The calculated energies of some levels were (in cm $^{-1}$ )  $^7F_1$  364,  $^7F_2$  895 and 1113, and  $^5D_0$  20 231. While the lower levels have an error of 12% or less, the  $^5D_0$  level is 18% above the experimental value herein, and the  $T_{2g}\!-\!E_g$  splitting of  $^7F_2$  is underestimated by 20%. This serves to demonstrate the simulation difficulties and inaccuracies of ab initio methods compared with crystal field parametrizations.

#### CONCLUSIONS

Two questions have been addressed in this article. First, since there are no abrupt changes in the luminescence spectrum on cooling from room temperature to 10 K, the luminescence probe of Eu<sup>3+</sup> indicates that the structure of the Ba<sub>2</sub>LnMO<sub>6</sub> systems is monoclinic. This conclusion is based upon the complete removal of cubic degeneracies, for example, in the <sup>5</sup>D<sub>0</sub>  $\rightarrow$  <sup>7</sup>F<sub>1</sub> transition, where 3 bands are observed. Furthermore, the dominance of the intensity of the  $^5D_0 \rightarrow {}^7F_1$  transition in the emission spectrum shows that the Eu<sup>3+</sup> ion is situated at a centrosymmetric site of  $C_{2h}$  or  $C_i$  symmetry. The appearance of the very weak  ${}^5D_0 \rightarrow {}^7F_0$  transition is consistent with a slight distortion from centrosymmetry of the EuO6 moiety, which could be due to crystal disorder. These results are in line with the crystal structure determinations of Henmi et al.<sup>30</sup> who concluded that the space group of these crystal systems is P2<sub>1</sub>/  $n_i$ , which implies the site symmetry of  $C_i$  for the doped Eu<sup>3+</sup> ion. The present results contrast with the previously reported emission spectrum of Ba<sub>2</sub>LaNbO<sub>6</sub>:Eu<sup>3+</sup> where the forced electric dipole transition  ${}^5D_0 \rightarrow {}^7F_2$  is dominant and the loss of centrosymmetry of Eu<sup>3+</sup> is more apparent.<sup>37</sup> The vibrational spectra of Ba<sub>2</sub>YNbO<sub>6</sub> show considerably more bands than those expected from the  $Fm\overline{3}m$  space group, but at present, because

of computational limitations, we are unable to perform a DFT calculation using  $P2_1/n$ .

Although the presence of the impurities  ${\rm Cr}^{3^+}$  and  ${\rm Mn}^{4^+}$  in our samples severely limits the spectral information attainable, some conclusions have been made that relate the  ${\rm EuO_6}^{9^-}$  system in the context of other  ${\rm EuX_6}^{3^-}$  moieties. The empirical linear relationship between crystal field strength and electronegativity has been found for the  ${\rm EuCl_6}^{3^-}$ ,  ${\rm EuO_6}^{9^-}$ , and  ${\rm EuF_6}^{3^-}$  moieties. While this can be qualitatively understood by the increase in covalency in the direction from the hexafluoro to the hexachloro systems, the wider applicability of this relationship and its theoretical justification are now the subject of further research.

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#### **Notes**

The authors declare no competing financial interest.

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# REFERENCES

- (1) Fu, W. T.; IJdo, D. J. W. J. Solid State Chem. 2006, 179, 1022.
- (2) Lavat, A. E.; Baran, E. J. Vibrat. Spectrosc. 2003, 2, 167.
- (3) Kurian, J.; Nair, K. V. O.; Sajith, P. K.; John, A. M.; Koshy, J. Appl. Superconduct 1998, 6, 259.
- (4) Blasse, G.; Bril, A.; Nieuwpoort, W. C. J. Phys. Chem. Solids 1966, 27, 1587.
- (5) Vijayakumar, C.; Padma Kumar, H.; Solomon, S.; Thomas, J. K.; Wariar, P. R. S.; John, A. *J. Alloys Compd.* **2009**, 480, 167.
- (6) Karunadasa, H.; Huang, Q.; Ueland, B. G.; Schiffer, B.; Cava, R. J. Proc. Natl. Acad. Sci. 2003, 100, 8097.
- (7) Fujioka, Y.; Frantti, J.; Kakihana, M. J. Phys. Chem. B 2006, 110, 777.
- (8) Kennedy, B. J.; Saines, P. J.; Kubota, Y.; Minakata, C.; Hano, H.; Kato, K.; Takata, M. *Mater. Res. Bull.* **2007**, 42, 1875.
- (9) Feldmann, D. M.; Holesinger, T. G.; Maiorov, B.; Foltyn, S. R.; Coulter, J. Y.; Apodaca, I. Supercond. Sci. Technol. 2010, 23, 095004.
- (10) Chan, H. L. W.; Choy, S. H.; Chong, C. P.; Li, H. L.; Liu, P. C. K. Ceram. Int. 2008, 34, 773.
- (11) Anderson, H. U. Solid State Ionics 1992, 52, 33.
- (12) Tagantsev, A. K.; Sherman, V. O.; Astafiev, K. F.; Venkatesh, J.; Setter, N. J. Electroceram. 2003, 11, 5.
- (13) Zhou, W.-L.; Zhang, Q.-L.; Gao, J.-Y.; Liu, W.-P.; Ding, L.-H.; Yin, S.-T. Chin. Phys. B 2011, 20, 016101.
- (14) Eng, H. W.; Barnes, P. W.; Auer, B. M.; Woodward, P. M. J. Solid State Chem. 2003, 175, 94.
- (15) Qi, X.; Gallagher, H. G.; Han, T. P. J.; Henderson, B.; Illingworth, B.; Ruddock, I. S. Chem. Phys. Lett. 1997, 264, 623.
- (16) Kresse, G.; Furthmüller, J. Phys. Rev. B 1996, 54, 11169.
- (17) Perdew, P.; Burke, K.; Ernzerhof, M. Phys. Rev. Lett. 1996, 77, 3865.
- (18) Blöchl, P. E. Phys. Rev. B 1994, 50, 17953.
- (19) Kresse, G.; Joubert, D. Phys. Rev. B 1999, 59, 1758.
- (20) Dias, A.; Sá, R. G.; Moreira, R. L. J. Raman Spectrosc. 2008, 39, 1805.
- (21) Moreira, R. L.; Abdul Khalam, L.; Sebastian, M. T.; Dias, A. J. Eur. Ceram. Soc. **2007**, 27, 2803.
- (22) Dias, A.; Khalam, L. A.; Sebastian, M. T.; Moreira, R. L. J. Solid State Chem. 2007, 180, 2143.
- (23) Dias, A.; Abdul Khalam, L.; Sebastian, M. T.; Lage, M. M.; Matinaga, F. M.; Moreira, R. L. Chem. Mater. 2008, 20, 5253.

- (24) Dias, A.; Lage, M. M.; AbdulKhalam, L.; Sebastian, M. T.; Moreira, R. L. Chem. Mater. 2011, 23, 14.
- (25) Dias, A.; Abdul Khalam, L.; Sebastian, M. T.; Paschoal, C. W. A.; Moreira, R. L. Chem. Mater. 2006, 18, 214.
- (26) Hammink, T. S.; Fu, W. T.; IJdo, D. J. W. J. Solid State Chem. 2011, 184, 848.
- (27) Meneghini, C.; Ray, S.; Liscio, F.; Bardelli, F.; Mobilio, S.; Sarma, D. D. *Phys. Rev. Lett.* **2009**, *103*, 046409.
- (28) Glazer, A. M. Acta Crystallogr., Sect. A: Found. Crystallogr. 1975, 31, 756.
- (29) Howard, C. J.; Kennedy, B. J.; Woodward, P. M. Acta Crystallogr., Sect. B: Struct. Sci. 2003, 59, 463.
- (30) Henmi, K.; Hinatsu, Y.; Masaki, N. M. J. Solid State Chem. 1999, 148, 353.
- (31) Yashima, M.; Lee, J.-H.; Kakihana, M.; Yoshimura, M. J. Phys. Chem. Solids 1997, 58, 1593.
- (32) Zhou, Q.; Kennedy, B. J.; Kimpton, J. A. J. Solid State Chem. 2011, 184, 729.
- (33) Xiao, X. Z.; Yan, B. J. Alloys Compd. 2007, 433, 246.
- (34) Yu, C. C.; Liu, X. M.; Yu, M.; Lin, C. K.; Li, C. X.; Wang, H.; Lin, J. J. Solid State Chem. 2007, 180, 3058.
- (35) Werts, M. H. V.; Jukes, R. T. F.; Verhoeven, J. W. Phys. Chem. Chem. Phys. 2002, 4, 1542.
- (36) Dutta, A.; Sinha, T. P. Solid State Commun. 2010, 150, 1173.
- (37) Tanner, P. A.; Pan, Z. Inorg. Chem. 2009, 48, 11142.
- (38) Liu, G. K. In Spectroscopic Properties of Rare Earths in Optical Materials; Liu, G. K., Jacquier, B., Eds.; Springer: Berlin, Germany, 2005; pp 1–89.
- (39) Duan, C.-K.; Tanner, P. A. J. Phys. Chem. A 2010, 114, 6055.
- (40) Görller-Walrand, C.; Binnemans, K. Handbook on the Physics and Chemistry of Rare Earths, Eds.; Gschneidner, K. A., Jr., Eyring, L.; Elsevier Science B. V.: Dordrecht, The Netherlands, 1996; Chapter 155, Vol. 23, p 168.
- (41) Cowan, R. D. The Theory of Atomic Structure and Spectra; University of California: Berkeley, CA, 1981.
- (42) Shen, Y. R.; Holzapfel, W. B. Phys. Rev. B 1995, 52, 12618.
- (43) Tanner, P. A.; Liu, Y.-L.; Edelstein, N.; Murdoch, K.; Khaidukov, N. M. J. Phys.: Condens. Matter 1997, 9, 7817.
- (44) Tanner, P. A.; Li, W.; Ning, L. Inorg. Chem. 2012, 51, 2997.
- (45) Barnes, J. C.; Al-Rasoul, K.; Harkins, P. J. Chem. Soc. Pak. 1980,
- (46) Wakeshima, M.; Harada, D.; Hinatsu, Y.; Masaki, N. J. Solid State Chem. 1999, 147, 618.
- (47) Auzel, F. Mater. Res. Bull. 1979, 14, 223.
- (48) Auzel, F.; Malta, O. L. J. Phys. 1983, 44, 201.
- (49) Thorne, J. R. G.; Jones, M.; McCaw, C. S.; Murdoch, K. M.; Denning, R. G.; Khaidukov, N. M. J. Phys.: Condens. Matter 1999, 11, 7851.
- (50) Tanner, P. A.; Ravi Kanth Kumar, V. V.; Jayasankar, C. K.; Reid, M. F. J. Alloys Compd. 1994, 215, 349.
- (51) McCaw, C. S.; Murdoch, K. M.; Denning, R. G. Mol. Phys. 2003, 101 427
- (52) Visser, O.; Visscher, L.; Aerts, P. J. C.; Niewpoort, W. C. J. Chem. Phys. 1992, 96, 2910.