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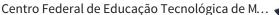
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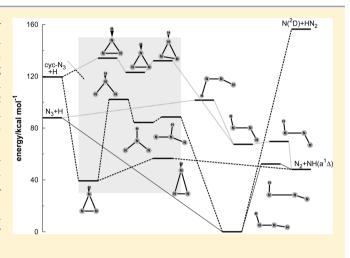
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# Accurate Study of the Two Lowest Singlet States of HN<sub>3</sub>: Stationary Structures and Energetics at the MRCI Complete Basis Set Limit

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ABSTRACT: The two lowest singlet potential energy surfaces of the hydrazoic acid are explored using high-level quantum chemistry calculations, revealing isomeric forms, transition states, and a new path for the nitrogen ring-closing mechanism in the ground state. The reaction of cvc-N<sub>2</sub> with hydrogen is shown to proceed through a barrierless path that dissociates to  $N_2 + NH(^1\Delta)$  without reaching the HN<sub>3</sub> global minimum. Several intersections between the two states are localized for both N<sub>3</sub> isomers near the N<sub>3</sub> + H dissociation. The energies of stationary structures and dissociation asymptotes are obtained with the multireference configuration interaction method at the complete basis set limit. A comparison with recent experimental data regarding the H-N<sub>3</sub> bond strength and the dissociation barrier in the excited state shows that the present results are of chemical accuracy  $(\sim 1 \text{ kcal mol}^{-1}).$ 



# 1. INTRODUCTION

The hydrazoic acid (HN<sub>3</sub>) is a species of growing concern in the atmosphere due to its pollutant character<sup>1</sup> and belongs to a class of energetic molecules. Its decomposition in the lowest electronic state

$$HN_3(\tilde{X}^l\!A') \rightarrow N_2(^l\!\Sigma_g^+) + NH(^l\!\Delta) \eqno(1)$$

$$\rightarrow N_3(^2A', ^2A'') + H$$
 (2)

$$\rightarrow HN_2(^2A') + N(^2D) \tag{3}$$

as well as the spin-forbidden dissociation to NH( $^{3}\Sigma^{-}$ ) have been studied experimentally<sup>2-7</sup> using different techniques, with the exception of the channel in eq 3 due to the high energy required to break the terminal NN bond and form the metastable HN2 radical.

Theoretically, the spin-allowed and spin-forbidden dissociations in the lowest electronic states into  $N_2$  + NH have been investigated by different authors. Specifically, Alexander et al. 10 provided an accurate prediction of the relevant geometries and energies of the barriers for dissociation, using the multireference configuration interaction method with Davidson's correction, MRCI(Q). <sup>11,12</sup>

Dissociation of the excited states has also been studied, with photodissociation experiments conducted  $^{13-17}$  for the channel in eq 1 showing large differences in the rotational population of the products. The channel in eq 2, which involves higher energies, has also been assessed<sup>18–21</sup> using shorter wavelengths. Theoretically, it was shown<sup>22</sup> that such photodissociation involves mainly the lowest excited singlet state  $(1^1A'')$ , with ab

initio calculations being employed to explain the experimentally observed results. More recently, Fang<sup>23</sup> analyzed this process by performing ab initio calculations on the <sup>1</sup>A', <sup>1</sup>A", and <sup>3</sup>A" states. He carried out optimizations of the stationary structures by constraining the system to  $C_s$  symmetry from complete active-space self-consistent field calculations (CASSCF) with a reduced active space (8 valence electrons in 7 active orbitals CASSCF(8,7)), the energies being refined using the multireference MP2 approach.<sup>24</sup> Furthermore, two-dimensional quantum mechanical wavepacket calculations of the photodissociation dynamics were performed by Cook et al.<sup>25</sup> using a potential energy surface (PES) constructed with the stateaveraged (both the  $\tilde{X}^1A'$  and  $\tilde{A}^1A''$  carried an equal weight) CASSCF approach in order to support their experimental findings.<sup>21</sup>

After the first experimental evidence on production of cyclic  $N_3$  isomer (cyc- $N_3$ ),  $^{26}$  a nitrogen ring-closing mechanism from photodissociation of  $HN_3$  was studied by Zhang et al.,  $^{27}$ showing experimental evidence of the formation of cyc-N<sub>3</sub>. A theoretical description of the reaction path has also been reported using the full valence CASSCF(16,13) approach with the correlation-consistent<sup>28,29</sup> basis set cc-pVTZ, followed by energy refinement with MRCI(Q)/aug-cc-pVTZ calculations.

Despite all theoretical efforts to understand the chemistry of the hydrazoic acid, the barriers for dissociation in the excited singlet state lack accurate theoretical prediction to compare with the experimental values, and the whole topology of the

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ground PES remains as yet unexplored. Furthermore, most previous calculations are constrained to planar geometries and do not report harmonic vibrational frequencies. The aim of this work is to provide a detailed and accurate analysis of the structure and energetics of both ground and excited singlet states, which, for symmetric configurations, belong to the A' and A" symmetries, respectively. This will include nonplanar configurations, contributing to the understanding of the possible reaction paths and making a first step toward the construction of a global analytical representation. The paper is organized as follows. Section 2 describes the ab initio calculations and extrapolation schemes, while sections 3–6 gather the major results. The conclusions are in section 7.

# 2. AB INITIO CALCULATIONS AND EXTRAPOLATION SCHEME

Geometry optimizations at the CASSCF level have been performed in the  $C_1$  symmetry point group by considering all six degrees of freedom of the system with basis sets of the correlation-consistent family. 28,29 Preliminary calculations were performed with the VDZ basis set (the cc-pVXZ and aug-ccpVXZ basis will be abbreviated hereafter as VXZ and AVXZ, respectively; X is the cardinal number), including the quadratic steepest descent reaction path following, in order to understand the connections between the predicted transition states and local minima. However, the geometries reported in this work as well as harmonic vibrational frequencies were obtained at the CASSCF/AVQZ level, where only the 1s orbitals of the nitrogen atoms were kept doubly occupied and, hence, the active space consisted of 16 electrons in 13 molecular orbitals (16,13). Because the optimization is performed in  $C_1$ symmetry, the excited structures had to be optimized as the upper state in a two-state averaged CASSCF calculation, while the ground state was optimized via single-state calculations. On each stationary structure found, the energy was refined by single-point calculations (in C<sub>s</sub> symmetry) via the MRCI- $(Q)^{11,12}$  method, with AVTZ and AVQZ basis sets, followed by extrapolation to the complete basis set (CBS) limit. This is a soundful approach that has recently been shown 30-33 to give excellent results for the HO<sub>x</sub> radicals and advocated to be of general utility.

The extrapolation of the raw CASSCF energies has been performed with the two-point protocol proposed by Karton and Martin<sup>34</sup> (originally utilized for the Hartree–Fock energies but shown<sup>35</sup> to perform accurately also for the CASSCF energy)

$$E_X^{\text{CAS}}(\mathbf{R}) = E_{\infty}^{\text{CAS}}(\mathbf{R}) + B/X^{5.34} \tag{4}$$

where the basis sets are indicated by subscripts (the CBS limit corresponds to  $X=\infty$ ) and  $\mathbf R$  is a six-dimensional vector describing the geometry. Such extrapolations are carried out pointwisely, with  $E_\infty^{\mathrm{CAS}}$  and B being parameters to be determined from a fit to the AVTZ and AVQZ energies.

To extrapolate the dynamical correlation for systems with a large number of electrons, where calculations with a basis set larger than quadruple- $\zeta$  are unaffordable, the uniform singlet-and triplet-pair extrapolation<sup>35</sup> (USTE) method has been used because this has been shown to consistently perform better than traditional schemes (see, e.g., the original paper). In the present approach, the extrapolated dynamical correlation energy  $(E_{\infty}^{dc})$  is obtained from a fit to the pair (T,Q) of raw

ones (thus obtained with the AVTZ and AVQZ basis) by using the form

$$E_X^{\text{dc}} = E_\infty^{\text{dc}} + \frac{A_3}{(X - 3/8)^3} + \frac{A_5^{(0)} + cA_3^n}{(X - 3/8)^5}$$
 (5)

which provides  $E_{\infty}^{\rm dc}$  and  $A_3$ ; the parameters  $A_5^{(0)}$ , c, and n have been shown elsewhere  $^{35}$  to be independent of the system and determined universally for a given post-Hartree–Fock method. These are listed in Table 1 for the coupled cluster and MRCI methods.

Table 1. USTE Extrapolation Parameters<sup>35</sup>

method	$A_5^{(0)}[E_{ m h}]$	$c[E_{ m h}^{1-(n)}]$	n
MRCI	0.0037685459	-1.17847713	1.25
CCSD	0.16606993	-1.42225121	1.00

In regions close to the minima, where the system may be described by single-reference-based methods, coupled cluster singles and doubles with perturbative triples  $(CCSD(T)^{36})$  as well as density functional theory (DFT) calculations were performed. All calculations have been carried out using the MOLPRO package.<sup>37</sup>

#### 3. DECOMPOSITION OF HN<sub>3</sub>

The structure of the  $HN_3$  molecule at equilibrium (hereafter set as the reference energy) has been optimized through CASSCF/AVQZ and CCSD(T)/AVTZ calculations. Table 2 shows that

Table 2. Geometry and Vibrational Frequencies of  $\mbox{HN}_3$  at Equilibrium

	exp. <sup>38,39</sup>	CAS/AVQZ	CCSD/AVTZ	ref 23 <sup>a</sup>
$R_{\rm N_1N_2}/a_0$	2.143	2.144	2.147	2.149
$R_{N_2N_3}/a_0$	2.349	2.374	2.361	2.349
$R_{\mathrm{HN_3}}/a_0$	1.918	1.940	1.926	1.910
$\hat{HN_3N_2}/deg$	108.8	107.5	108.5	107.3
$N_1\hat{N}_2N_3/deg$	171.3	171.5	171.3	173.7
$\omega_1/\mathrm{cm}^{-1}$	527	524	522	
$\omega_2/\mathrm{cm}^{-1}$	587	600	590	
$\omega_3/\mathrm{cm}^{-1}$	1151	1153	1169	
$\omega_4/\mathrm{cm}^{-1}$	1265	1313	1286	
$\omega_5/\mathrm{cm}^{-1}$	2140	2184	2193	
$\omega_6/\mathrm{cm}^{-1}$	3497	3394	3494	
ZPE/kcal mol <sup>-1</sup>	13.10	13.10	13.23	

<sup>&</sup>lt;sup>a</sup>At the CASSCF(8,7)/VDZ level of theory.

both methods agree nicely with the experimental values.<sup>38,39</sup> As expected, the equilibrium structure is well-described by the single-reference coupled cluster method, with the inclusion of dynamical correlation providing a minor improvement over the CASSCF geometries. We have also performed a single-point MRCI(Q)/AVTZ calculation at both the experimental geometry and the point optimized by CASSCF/AVQZ, with the difference found to be only of 0.002 kcal mol<sup>-1</sup>, which, as noted above, supports the procedure<sup>30–33</sup> utilized in the present work for optimizing the geometries.

In order to assess the accuracy of the ab initio results, we compare our prediction of the  $H-N_3$  bond energy with the accurate experimental measurement<sup>21</sup> using the technique of H-atom Rydberg photofragment translational spectroscopy. As can be seen from Table 3, our CBS extrapolated result of 87.94

 $Table \ 3. \ Dissociation \ Energies \ (in \ kcal \ mol^{-1}) \ Relative \ to \ the \ Global \ Minimum, \ Including \ Other \ Results^{10,21,23,27,40,41} and the substitution of the lattice of the la$ 

	ZPE	CAS/AVQZ	MRCI(Q)/AVTZ	MRCI(Q)/AVQZ	CBS/MRCI(Q)	exp.	other
$H + N_3(lin)$	5.83 <sup>b</sup>	79.69(72.42)	93.78(83.51)	94.63(87.63)	95.21(87.94)	$88.54 \pm 0.14^d$	87.7, <sup>e</sup> 85.3 <sup>f</sup>
$H + cyc-N_3$	3.91 <sup>b</sup>	116.10(106.91)	126.04(116.85)	127.64(118.45)	128.67(119.48)		117 <sup>f</sup>
$N + HN_2$	$8.37^{c}$	152.41(147.68)	157.00(152.27)	159.50(154.77)	161.11(156.38)		

<sup>&</sup>lt;sup>a</sup>The results in parentheses are ZPE-corrected. <sup>b</sup>Reference 40. <sup>c</sup>Reference 41. <sup>d</sup>Reference 21. <sup>e</sup>Reference 10. <sup>f</sup>Reference 23. <sup>f</sup>Reference 27.

Table 4. Properties of the Stationary Points for the Ground-State PES<sup>a</sup>

	$S_2$	$\mathrm{M}_{C_{2 u}}$	$S_3$	$\mathbf{M}_{C_s}$	$S_4$
$R_{N_1N_2}/a_0$	2.390	2.419	2.583	2.958	3.885
$R_{N_2N_3}/a_0$	2.390	2.419	2.583	2.958	3.885
$R_{\mathrm{HN}_2}/\mathrm{a}_0$	2.000	1.952	1.938	1.956	1.966
$N_1\hat{N}_2N_3/deg$	159.6	101.9	76.87	45.20	31.67
$H\hat{N}_2N_3/deg$	100.2	129.1	120.4	101.1	90.21
$H\hat{N}_2N_1/deg$	100.2	129.1	120.4	101.1	90.21
$\omega_1/\mathrm{cm}^{-1}$	350	486	690	569	322
$\omega_2/\mathrm{cm}^{-1}$	468i	861	953	716	391i
$\omega_3/\mathrm{cm}^{-1}$	630	1165	1135	1030	400
$\omega_4/\mathrm{cm}^{-1}$	1024	1392	1225	1433	1031
$\omega_5/\mathrm{cm}^{-1}$	1585	1530	1539i	1715	2131
$\omega_6/\mathrm{cm}^{-1}$	3141	3274	3394	3259	3254
ZPE	9.62	12.45	10.58	12.47	10.20
CAS/AVQZ	96.23	86.98	110.93	39.70	52.92
MRCI(Q)/AVTZ	90.06	83.31	101.74	38.31	57.01
MRCI(Q)/AVQZ	91.28	84.32	103.55	39.34	58.56
CBS/MRCI(Q)	92.04	84.99	104.66	39.95	59.54
CBS/MRCI(Q) + ZPE	88.56	84.34	102.14	39.32	56.64
Cho et al. <sup>42</sup>	86.9	78.1	118.6	37.7	

<sup>&</sup>quot;Geometry and vibrational frequencies at the CASSCF/AVQZ level and energies are given in kcal mol-1 relative to the global minima.

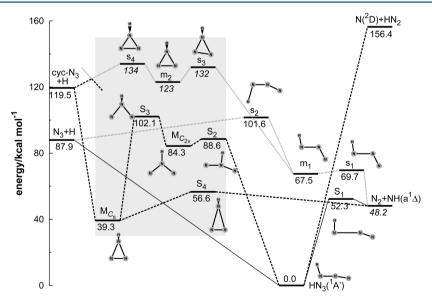


Figure 1. Potential energy profile at the CBS/MRCI(Q) level of theory, including ZPE corrections. The solid lines connecting the structures correspond to the main dissociation paths in the ground state, while the dashed ones are theoretically proposed. The gray dotted lines are relative to the upper state, and the numbers in italic are not at the CBS level. $^{10,27}$ .

kcal mol<sup>-1</sup> differs from the experimental value by only 0.6 kcal mol<sup>-1</sup>, while the error in the measurement is  $\pm 0.14$  kcal mol<sup>-1</sup>. Such accuracy can therefore be expected for the other energies calculated in this work, where no experimental data are available. It is worth noting that the results of Alexander et al., <sup>10</sup> performed before this experimental measurement, compare similarly well, with a deviation of 0.8 kcal mol<sup>-1</sup>; thus, the  $N_2$  +

NH dissociation energy as well as the barrier for this channel calculated in that work can be expected to be of similar accuracy. Because this channel has already been analyzed<sup>8–10</sup> thoroughly by ab initio methods, we do not make any further calculations there.

For the dissociation energy relative to the cyc-N<sub>3</sub> asymptote, our CBS extrapolation of 119.5 kcal mol<sup>-1</sup> differs from the

value of Zhang et al.  $^{27}$  by 2.5 kcal mol $^{-1}$  at the MRCI(Q)/AVTZ level, a result that we have also reproduced in Table 3 in order to extrapolate to the CBS limit. To the best of our knowledge, there is no prediction of the  $HN_2 + N$  dissociation energy available in the literature; it is calculated here at the CBS/MRCI(Q) limit. The enormous energy required to open this channel makes the  $HN_2$  radical very unstable in reaction with atomic hydrogen. Indeed, our CASSCF calculations suggest that this reaction occurs without a barrier if the NNN bond angle is strongly bent from its nearly linear structure at the equilibrium  $HN_3$  molecule. In fact, for ground-state  $HN_3$ , the only barrier in the exit channels seems to be the one relative to  $N_2 + NH$  dissociation.  $^{10}$ 

# 4. STATIONARY STRUCTURES AND REACTION PATHS IN THE GROUND STATE

The stationary structures found in this work and their properties are gathered in Table 4, while an overview of the stationary structures and reaction paths on both ground and excited potential energy surfaces of  $HN_3$  is displayed in the energy diagram of Figure 1, which shows the predicted structures from this work together with others previously reported. M stands for minimum and S for saddle point, while the upper-state counterparts have the same notation as those in the lower case.

As can be seen, starting from the equilibrium structure of HN<sub>3</sub> in its nearly linear trinitrogen shape and following the reaction path for bending the NNN angle, a saddle point  $(S_2)$  is reached corresponding to a hydrogen atom migration from a terminal nitrogen to the central one with an energy of 88.56 kcal mol<sup>-1</sup> above the global minimum (unless mentioned otherwise, the energies given in this discussion are CBS/ MRCI(Q) including the zero-point energy (ZPE) correction relative to the global minimum). This saddle point is a firstorder transition state, with an imaginary frequency of 468 cm<sup>-1</sup> that corresponds to a planar HNN bending mode. Following the minimum-energy path, a local metastable  $C_{2\nu}$  minimum (M<sub>C2</sub>) is obtained lying at 84.34 kcal mol<sup>-1</sup> and with a metastability of 4.22 kcal mol<sup>-1</sup>. It is interesting to note that for these two structures, and subsequent ones, the NH bond length is similar to its value on the separated imidogen molecule, with the fundamental vibration corresponding to the stretching mode of this bond  $(\omega_6)$  lying also close to the fundamental in isolated imidogen ( $\sim$ 3200 cm<sup>-1</sup>).

With further bending of the NNN angle from the  $M_{C_{2\nu}}$  structure, a nonplanar saddle point is reached  $(S_3)$ . It belongs to the  $C_s$  point group due to a plane of symmetry cutting the NH bond and lies 17.8 kcal mol<sup>-1</sup> above  $M_{C_{2\nu}}$ . From Table 4, one can clearly see that while the NNN angle progressively decreases, both NN bond lengths slowly increase when following this reaction path. It is thus fair to expect that it will lead to dissociation to cyc-N<sub>3</sub>, which has a bond angle of 49.2° and two bond distances of 2.8 a<sub>0</sub>. The imaginary frequency of the  $S_3$  transition state corresponds to a simultaneous bend of both NNN and HNN angles without loosing the  $C_s$  plane of symmetry.

The final step toward dissociation to cyc-N<sub>3</sub>, passes through a relatively deep minimum that has also a nonplanar  $C_s$  structure  $(M_{C_s})$ . Interestingly, the NNN angle and NN bond lengths in  $M_{C_s}$  exceed the values of the final cyc-N<sub>3</sub> form, and thus, the progressive change in these variables (observed through this

path) cannot be observed in this way. In fact, the NH bond length in  $M_{C_s}$  shows that it is a highly bound feature rather than a mere structure along the dissociation path. Thus,  $M_{C_s}$  may be thought of as a stable structure formed from the abstraction of a H atom by cyc-N<sub>3</sub>. The CASSCF calculations show that this abstraction reaction occurs without an energy barrier, suggesting that cyc-N<sub>3</sub> can easily recombine with H atoms to generate the  $M_{C_s}$  isomer.

The reactivity of cyc-N<sub>3</sub> with some atmospheric species has been considered theoretically  $^{43,44}$  in order to assess its stability. Although the cyc-N<sub>3</sub> + H<sub>2</sub>O reaction has shown large barriers,  $^{44}$  it was found to lead to cyc-N<sub>3</sub>H + OH, which seems to correspond to the M<sub>C<sub>s</sub></sub> here reported. However, a previously unknown nonplanar transition state (S<sub>4</sub>) (which connects M<sub>C<sub>s</sub></sub> directly with the N<sub>2</sub> + NH( $^1\Delta$ ) fragments) was found in this work and indicates that such an isomer may dissociate, especially if formed with a large energy content as would be the case in the cyc-N<sub>3</sub> + H reaction. Although no experiments have been carried out for this process, it seems that this isomer of HN<sub>3</sub> could be detected experimentally from N<sub>2</sub> + NH( $^1\Delta$ ) collisions.

During the course of this work, another group also found the  $S_2$ ,  $M_{C_2}$ ,  $S_3$ , and  $M_{C_s}$  structures using multireference MP2 calculations. <sup>42</sup> Our results, however, are different in that we give vibrational frequencies and ZPE corrections (which are fundamental for comparing with the experiments) and are also more reliable due to their CBS/MRCI(Q) nature.

Further geometry optimizations have been performed at the CCSD(T)/AVTZ level followed by extrapolating the energy using the USTE(T,Q) method in order to compare with previous results. Due to its single-reference nature, the CCSD(T) optimizations often find convergence problems, and only the two new minima are examined at this level, with the results presented in Table 5. The validity of the CCSD(T) approach is analyzed with the T1 and D1 diagnostics  $^{45-47}$  and also by inspecting the coefficient of the dominant configuration in the CI vector of a CASSCF/AVQZ calculation. It is clear from Table 5 that the  $M_{C_s}$  structure is more suitably described

Table 5. Optimized Minima at the CCSD(T) and DFT Levels (without ZPE correction) Using the AVTZ basis. Energies in kcal mol<sup>-1</sup> Relative to the Global Minima

	CCS	D(T)	DFT		
	$\mathbf{M}_{C_{2\nu}}$	$M_{C_s}$	$\mathbf{M}_{C_{2 u}}$	$\mathbf{M}_{\mathcal{C}_s}$	
$R_{\mathrm{N_1N_2}}/a_0$	2.412	2.926	2.373	2.922	
$R_{\mathrm{N_2N_3}}/\mathrm{a_0}$	2.413	2.926	2.373	2.922	
$R_{\mathrm{HN}_2}/a_0$	1.937	1.941	1.954	1.938	
$N_1 \hat{N}_2 N_3 / deg$	100.4	45.77	96.32	45.04	
$\hat{\text{HN}}_2\text{N}_3/\text{deg}$	129.8	101.7	131.8	102.3	
$\hat{\text{HN}_2}\text{N}_1/\text{deg}$	129.8	101.7	131.8	102.3	
T1	0.026	0.015			
D1	0.075	0.033			
CI coeff.a	0.882	0.931			
AVTZ	85.67	37.99	97.29	46.11	
AVQZ	86.61	38.91			
CBS	87.23	39.45			

"Coefficient of the dominant configuration on the CI vector as calculated at the CASSCF/AVQZ level.

by a single configuration than  $M_{C_{2\nu}}$  due to its lower T1 and D1 values and larger coefficient of the dominant configuration (note that  $M_{C_{2\nu}}$  was even found to slightly deviate from its symmetric configuration). Although a general good agreement between the MRCI(Q) and CCSD(T) energies is obtained, the  $M_{C_{2\nu}}$  values show larger differences than  $M_{C_{2\nu}}$  which is not surprising due to the above-mentioned multireference character.

Although the MRCI(Q) energies obtained in this work provide accurate ab initio estimates, it is currently unaffordable to calculate a grid over the whole configurational space to obtain a global analytical representation. Therefore, the values here reported offer benchmark results to asses the validity of different DFT functionals or other cost-effective approaches for a future calculation and modeling of the whole potential energy surface. Preliminary calculations employing the B3LYP<sup>48</sup> functional (which has been considered appropriate to calculate the geometry and fundamental frequencies of HN<sub>3</sub> at equilibrium<sup>49</sup>) were performed on the  $M_{C_{2\nu}}$  and  $M_{C_3}$  structures, also using the AVTZ basis set for consistency. The results show reasonable agreement with the CASSCF geometries and vibrational frequencies, but the calculated energy differs appreciably, as shown in Table 5.

#### 5. EXCITED SINGLET STATE

After the system is photoexcited to the  $\tilde{A}^1A''$  state, decomposition follows quickly given the energy content of the excited molecule. The lowest-energy decomposition (see eq 1) leads to  $N_2 + NH(^1\Delta)$ , and the experiments <sup>14,16,17</sup> suggest that it occurs directly without a strong potential barrier along the HN-NN bond distance. This has been corroborated by early theoretical calculations,<sup>22</sup> although Fang<sup>23</sup> has found a small barrier of 0.2 kcal mol<sup>-1</sup> (including ZPE correction) at the CASPT2 level, arguing that it was not inconsistent with the experiments. Note that the absence of such a barrier leads to the conclusion that there is no true minimum in this region of the excited-state PES. Note further that prior to the abovementioned work, there was no information (theoretical or experimental) about this structure. More recent and accurate calculations with a larger active space have reported such a minimum,<sup>27</sup> thus corroborating the existence of the barrier. Indeed, our CASSCF(16,13)/AVQZ results also predict this transition state (named s<sub>1</sub>) with an imaginary frequency of 589 cm<sup>-1</sup>, while the CBS/MRCI(Q) calculations show it to lie 2.2 kcal mol<sup>-1</sup> above the trans minimum (Table 6).

The dissociation to  $N_3$  + H is believed to occur through a reaction barrier in the excited state  $(s_2)$  rather than through internal conversion to the  $^1A''$  or  $^3A''$  states, which was experimentally measured to be  $13.15 \pm 2.29$  kcal mol $^{-1}$  above the dissociation channel. Previous theoretical work on this barrier shows some disagreement, with Lock et al. Predicting it to be >3.3 kcal mol $^{-1}$ , while Fang's calculations yield 27.9 kcal mol $^{-1}$ . Our best result at the CBS/MRCI(Q) level of 13.70 kcal mol $^{-1}$  shows perfect agreement with the experimental value, thus validating the employed methodology (see also elsewhere  $^{30-33}$ ) also for the upper state.

Between the above two barriers lies therefore the  $HN_3(^1A'')$  minimum, which has a trans configuration with the NNN moiety further from linearity than that for the ground state. This implies that if the system is excited from the region of the ground-state minimum to the correspondent Franck–Condon

Table 6. Properties of the Excited-State Stationary Points<sup>a</sup>

	m <sub>1</sub> -trans	m <sub>1</sub> -cis	$\mathbf{s}_1$	$s_2$
$R_{N_1N_2}/a_0$	2.248	2.254	2.194	2.248
$R_{\mathrm{N_2N_3}}/\mathrm{a_0}$	2.749	2.763	3.073	2.352
$R_{\rm HN_3}/a_0$	1.959	1.974	1.963	2.768
$N_1\hat{N}_2N_3/deg$	120.2	119.3	118.9	155.9
$H\hat{N}_3N_2/deg$	101.2	102.9	97.38	106.6
∠HNNN/deg	180.0	0.0	180.0	0.0
$\omega_1/\mathrm{cm}^{-1}$	433	245	257	471
$\omega_2/\mathrm{cm}^{-1}$	508	468	475	526
$\omega_3/\mathrm{cm}^{-1}$	648	642	589i	898
$\omega_4/\mathrm{cm}^{-1}$	1337	1347	1188	1162
$\omega_5/\mathrm{cm}^{-1}$	1700	1670	1751	1614
$\omega_6/\mathrm{cm}^{-1}$	3272	3166	3256	1770i
ZPE	11.29	10.78	9.90	6.68
CAS/AVQZ	72.63	74.08	74.16	105.9
MRCI(Q)/AVTZ	67.32	69.51	70.44	106.2
MRCI(Q)/AVQZ	68.53	70.74	71.93	107.3
CBS/MRCI(Q)	69.31	71.52	72.87	108.1
CBS/ MRCI(Q)+ZPE	67.50	69.20	69.67	101.6
exp. <sup>21</sup>				$101.7 \pm 2.4$

 $^a{\rm Geometry}$  and vibrational frequencies at the CASSCF/AVQZ level and energies given in kcal  ${\rm mol}^{-1}$  relative to the global minima.

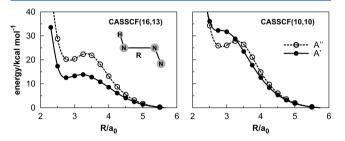
region of the upper PES, it will experience a considerable gradient in this coordinate. This minimum has also a cis counterpart that, to the best of our knowledge, has not been optimized before. Our results show it to lie only 1.7 kcal mol $^{-1}$  above the trans and showing bond lengths similar to it. Interestingly, an isomerization transition state on the torsion coordinate does not seem to exist, although a one-dimensional cut along this coordinate shows a maximum with  $\angle HNNN=90^{\circ}$ . This happens because such a maximum is not a real transition state if the NN coordinate (leading to dissociation) is considered. The cis and trans isomer dissociation paths are thus independent, with the dissociation for  $\angle HNNN$  fixed at  $90^{\circ}$  showing a decay in energy with no stationary structure.

The region of the excited PES corresponding to structures with the NNN angle largely in cyclic form was studied by Zhang et al.<sup>27</sup> and is displayed in Figure 1. In their study, a mechanism for explaining the formation of cyc-N<sub>3</sub> in photodissociation was proposed through ab initio calculations. This process involves however a first excitation from the ground to a third excited singlet state followed by internal conversion to the excited state studied in this work, through a conical intersection and subsequent bond cleavage, as shown in Figure 1.

# 6. SURFACE CROSSINGS

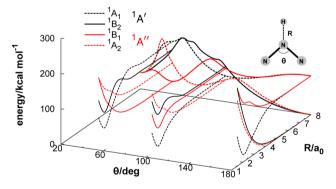
The presence of surface crossings could change the picture of the direct photodissociation in the upper state. For example, in case there is a crossing between ground and excited singlet states, the excited molecule could cross back to the ground state and dissociate from there. This mechanism was considered by Fang<sup>23</sup> for the dissociation to  $N_2 + NH(^1\Delta)$ , where one such intersection was found and optimized in state-averaged CASSCF(8,7)/VDZ calculations, but the conclusion was that this is not a probable event given that the crossing lies higher in energy than  $s_1$ . We have also searched for crossings between the two PESs in several regions of configurational space but rarely found them. Indeed, even the crossing reported by Fang<sup>23</sup>

could not be supported, except if reducing the active space to CASSCF(10,10); see Figure 2. We therefore believe that the reduced active space CASSCF(8,7) utilized by Fang<sup>23</sup> is not suitable for this part of the PES.



**Figure 2.** CASSCF/VDZ energy profile along the NN bond length showing the incorrect behavior of the calculations with reduced active space.

The only region of the PES where we have found crossings is close to dissociation to the N<sub>3</sub> fragment. The linear form of N<sub>3</sub> is Renner-Teller degenerate (see eqs 1 and 3), and the interaction with the H atom splits the degeneracy into the two singlet sheets here considered (ignoring the triplet states). On the other hand, the cyc-N<sub>3</sub> fragment is nondegenerate and correlates only to ground singlet state (which for some configurations may not correspond to the A' symmetry due to the presence of crossings), and therefore, a dissociation path from the excited state to cyc-N3 must find a surface intersection, as indicated in Figure 1. Due to the complexity of the electronic states of the N<sub>3</sub> fragment for different bond angles, 40,50 we have found several crossings close to the dissociation into this channel, which occurs for highly symmetric attacks of the H atom  $(C_{\infty\nu}, C_{2\nu}, \text{ and } C_{3\nu})$ . For example, Figure 3 shows the  $C_{2\nu}$  approach of a H atom with the



**Figure 3.** CASSCF/VDZ cuts for the dissociation to  $N_3$  + H restricting to  $C_{2\nu}$  geometries and optimizing the NN bond lengths for each point. The back part of the graph shows the optimized bending curve for the dissociated  $N_3$ .

NN bond lengths being relaxed; A' states are in black, and A" states are in red. Note though that the minimum-energy path for the cyc- $N_3$  + H reaction proceeds without a barrier through a non- $C_{2\nu}$  path (A' symmetry). For other symmetrical parts of the PES, such as the ground state near  $S_2$  and  $S_3$ , we have found no crossings between the two PESs. Although there are crossings between higher excited states, the two PESs here considered appear to be well-separated at the strong interaction region, which is quite unusual for polyatomics.

#### 7. CONCLUDING REMARKS

We have investigated the stationary structures and reaction paths of ground- and excited-singlet PESs of the hydrazoic acid using state-of-the-art ab initio calculations with CBS extrapolation. Comparison with two recent experimental measurements shows chemical accuracy, which validates the employed methodologies. Indeed, the accuracy of our predictions should hold for other structures with no experimental counterpart. Among the results, we have predicted minima and transition states in the ground-state PES, as well as a description for the H-abstraction reaction of cyc-N<sub>3</sub>. With geometries and vibrational frequencies optimized at the full-valence CASSCF/AVQZ level and energies refined with MRCI(Q) followed by CBS extrapolation, <sup>30–33</sup> the results here reported offer a benchmark to test the validity of other approaches in describing the global representation of the PES, namely, single-reference-type ones such as DFT and coupled cluster.

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#### Notes

The authors declare no competing financial interest.

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