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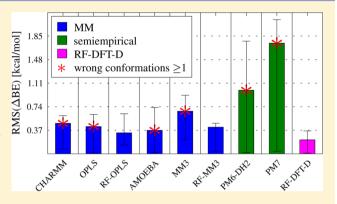


Accuracy of Dispersion Interactions in Semiempirical and Molecular Mechanics Models: The Benzene Dimer Case

Karol Strutyński,† José A. N. F. Gomes,† and Manuel Melle-Franco*,‡

Supporting Information

ABSTRACT: The benzene dimer is arguably the simplest molecular analogue of graphitic materials. We present the systematic study of minima and transition states of the benzene dimer with semiempirical and molecular mechanics (MM) methods. Full minimizations on all conformations were performed and the results, geometries, and binding energies were compared with CCSD(T) and DFT-D results. MM yields the best results with three force fields MM3, OPLS, and AMOEBA, which reproduced nine out of the ten stationary points of the benzene dimer. We obtained new parameters for MM3 and OPLS that successfully reproduce all structures of the benzene dimer and showed improved accuracy over DFT-D in most dimer geometries. Semiempirical models were, unexpect-



edly, less accurate than MM methods. The most accurate semiempirical method for the benzene dimer is PM6-DH2. DFT-D was the only Hamiltonian that reproduced the variations of energy with geometry from CCSD(T) calculations accurately and is the method of choice for energies of periodic and molecular calculations of graphitic systems. In contrast, MM represents an accurate alternative to calculate geometries.

■ INTRODUCTION

Carbon nanomaterials like fullerenes, carbon nanotubes, 2-4 and graphene^{5,6} have explosively developed into a very active field of research in which computer models have played a fundamental role. van der Waals (vdW) interactions are the driving force for the packing of graphitic materials; from graphite to carbon nanotubes⁷ passing trough multishell fullerenes,⁸ multiwall carbon nanotubes⁹ and carbon peapods.^{10–12} van der Waals forces are also fundamental for modeling the interaction of graphitic materials with their environment, for instance with nanoliquids, ^{13,14} biological membranes, ¹⁵ and proteins ¹⁶ and in noncovalent functionalization. 17,18

Dispersion interactions are intrinsically hard to model with ab initio quantum methods. The models that describe them with consistently good accuracy (e.g., coupled cluster methods 19-21) are feasible only for small molecules. Density functional theory (DFT) models are more popular as they are orders of magnitude more efficient. In a previous work we analyzed how accurately different DFT Hamiltonians reproduce dispersion interactions in the benzene dimer.²² In the present work we will extend that study to semiempirical and molecular mechanics models.

Benzene dimer (BD) is arguably the simplest molecular analogue of graphite. Experimental data on the benzene dimer are scarce: the interaction energy is about -2.4 kcal/mol, and

although the exact geometry of the BD is not experimentally known, the minimum is most likely a T-shaped structure.²

In contrast, the benzene dimer has been the object of many theoretical investigations that also yielded a very shallow binding. 25-28 Most recent and accurate theoretical studies yield two almost isoenergetic minima (PDa and TTb) and, at least, eight transition states (Figure 1). 27,29

Graphite and the benzene dimer share the same dispersion interactions. In fact, models with accurate dispersion on BD are also accurate on graphite. 22 The weak binding together with the availability of highly accurate data make benzene dimer a stringent test for dispersion for polyaromatic hydrocarbons and, ultimately, for graphite.

METHODS

The accuracy of models with very different computational costs, namely density functional theory, semiempirical methods, and molecular mechanics methods against reference data at the CCSD(T) level will be presented. The same methodology and metrics used in our previous work on DFT models was used.²²

The CCSD(T) method is widely considered the gold standard of quantum chemistry models and was used as

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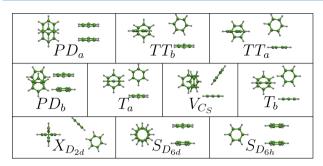


Figure 1. Benzene dimer conformations: parallel displaced (PD), sandwich type (S), T-shaped (T), tilted T-shaped (TT), V-shaped (V), and X-shaped (X) configurations. The subscript of the configuration indicates the symmetry of the molecule or the position of one molecule with respect to the other (a, over atom; b, over bond).

reference; stationary points and their binding energies were extrapolated to the complete basis set calculated at the CCSD(T)/aug-cc-pVDZ level,²⁷ and the potential energy surface (PES) was calculated at the CCSD(T)/aug-cc-pVQZ* level of theory.²⁵ DFT calculations were run with a home version of NWchem 6.1.1³⁰ that is available on request. Semiempirical calculations were performed with MOPAC 2012.^{31,32} Molecular mechanics calculations were run with the Tinker software suite.^{33–35}

RESULTS

To quantify the capacity to reproduce geometries and binding energies of BD minima and transition states for all Hamiltonians, we performed full geometry optimizations starting from CCSD(T) geometries. The differences in binding energy between the reference CCSD(T) data and the investigated methods are shown in Table 1. Table 2 quantifies the ability to reproduce the CCSD(T) geometries. Metrics based on root-mean-square differences in molecular structures and energies for all the conformations with stable stationary points are included as an indicator of overall performance for each method.

DFT-D Method. DFT-D methods are based on DFT Hamiltonians augmented with a classical $1/R^6$ dispersion term. DFT-D has already been used to study the benzene dimer. Recently, we presented a new set of DFT-D parameters for BD derived to be applicable in periodic quantum

chemistry calculations. Those parameters were obtained using a relaxed fiting (RF) procedure where the geometries are relaxed within the fitting scheme and consequently follow the optimization of the parameters. DFT-D parameters obtained from relaxed fitting (RF-DFT-D) yield improved accuracy and robust parameters. In fact, RF-DFT-D using the BLYP functional was one of the most accurate DFT models for benzene dimer as found by the authors. For simplicity we will only discuss here a DFT-D parametrization with a double- ζ basis set, as it is computationally more efficient. Note that the RF-DFT-D parameters with larger basis sets are substantially more accurate.

Semiempirical Methods. Semiempirical (SE) Hamiltonians are based on the Hartree–Fock formalism with a number of approximations. Most notably, some computationally expensive integrals are fitted to experimental data. Similarly to DFT, SE methods were recently augmented with classical corrections. The SE-D methods presented in this study are PM6-DH2³⁹ and PM6-DH+⁴⁰ (which are equivalent for the benzene dimer) and the recent PM7.⁴¹ In addition to SE-D methods, we also tried AM1,⁴² RM1,⁴³ MNDO,⁴⁴ and PM6,³¹ which, due to poor performance, will be reported in the Supporting Information.

PM7 and PM6-DH2 are generally overbinding and fail to to reproduce some BD conformations. PM7 favors sandwich type conformations over PD conformations (Table 1), and consequently, the PD_a minimum is not reproduced. PM6-DH2 yields improved energetics and fails only with two conformations, TT_a and V_{C_s} (the latter being a problematic conformation for most models). For the sandwich conformations, interaction energies are too binding with errors up to 100% and 180% for PM6-DH2 and PM7, respectively.

Molecular Mechanics. Molecular mechanics models are typically based on point particles centered on atomic nuclei interacting via mathematical functions fitted to reproduce empirical and/or quantum derived properties. We have studied all force fields available in the TINKER suite with explicit aromatic carbon parameters, namely, MM2, ⁴⁵ MM3, ⁴⁶ CHARMM22, ^{47–49} OPLS, ⁵⁰ and MMFF ⁵¹ force fields. Additionally, two polarizable models, the model for benzene by Dang ^{52,53} and the AMOEBA09 force field, ^{54–56} were included.

The intermolecular interactions in benzene dimer in MM are described by the sum of the Coulumbic and van der Waals

Table 1. Binding Energy Errors^a

								RF		BE
conf	CHARMM	OPLS	AMOEBA	MM3	PM6-DH2	PM7	OPLS	MM3	DFT-D	CCSD(T)
PD_a	-0.53	-0.62	0.06	-0.22	0.88	2.09	-0.22	-0.43	-0.33	-2.73
TT_b	-0.54	-0.51	-0.21	-0.86	0.02	0.53	-0.17	-0.46	-0.01	-2.82
TT_a	-0.54	-0.51	-0.19	-0.85	0.03	0.54	-0.16	-0.44	0.02	-2.80
PD_b	-0.43	-0.46	0.04	-0.22	0.88	2.11	-0.22	-0.42	-0.30	-2.72
T_a	-0.60	-0.55	-0.55	-0.92	-0.09	0.62	-0.14	-0.41	-0.08	-2.70
V_{C_s}	-0.45	-0.48	0.02	-0.24	0.86	2.09	-0.15	-0.43	-0.03	-2.74
T_b	-0.19	-0.16	0.19	-0.45	0.44	0.93	0.20	-0.04	0.36	-2.40
$\mathbf{X}_{D_{2d}}$	-0.39	-0.38	-0.73	-0.78	-0.32	-0.04	-0.30	-0.38	0.29	-1.79
$S_{D_{6d}}$	0.09	-0.01	0.37	0.66	1.77	3.12	0.63	0.48	0.14	-1.71
$S_{D_{6h}}$	0.08	-0.02	0.33	0.64	1.75	3.11	0.62	0.48	0.15	-1.71
RMS	0.43	0.42	0.37	0.67	1.00	1.74	0.33	0.42	0.22	

[&]quot;Positive values indicate energies that are more binding than the reference (BE_{CCSD(T)}). The root mean square (RMS) gives a measure of the overall accuracy. Values in bold show conformations that switch during geometry optimization. All values are in kcal/mol.

Table 2. Root Mean Square Deviation of the Optimized Geometries (RMSD, Å) and the Root Mean Square (RMS) for Each Method Presented as a Measure of the Overall Performance^a

								RF	
conf	CHARMM	OPLS	AMOEBA	MM3	PM6-DH2	PM7	OPLS	MM3	DFT-D
PD_a	0.40	0.41	0.05	0.01	0.16	$S_{D_{6h}}$	0.07	0.05	0.12
TT_b	0.12	0.09	0.19	0.15	0.23	0.15	0.05	0.07	0.11
TT_a	0.11	0.09	0.22	0.16	T_b	0.13	0.05	0.07	0.11
PD_b	\mathbf{V}_{C_s}	\mathbf{V}_{C_s}	0.06	0.01	0.19	$\mathbf{S}_{D_{6d}}$	0.07	0.05	0.12
T_a	0.07	0.05	0.07	0.09	0.07	0.07	0.03	0.05	0.04
V_{C_s}	0.29	0.15	PD_b	PD_b	PD_b	$\mathbf{S}_{D_{6d}}$	0.05	0.01	0.08
T_b	0.03	0.02	0.01	0.04	0.11	0.12	0.05	0.08	0.07
$\mathrm{X}_{D_{2d}}$	0.06	0.05	0.12	0.19	0.02	0.02	0.02	0.04	0.02
$S_{D_{6d}}$	0.06	0.06	0.15	0.13	0.19	0.06	0.06	0.06	0.07
$S_{D_{6h}}$	0.06	0.06	0.14	0.12	0.19	0.06	0.06	0.06	0.07
RMS	0.29	0.29	0.28	0.24	0.31	0.37	0.05	0.06	0.09

^aFor switched conformations, the new conformation is indicated in bold.

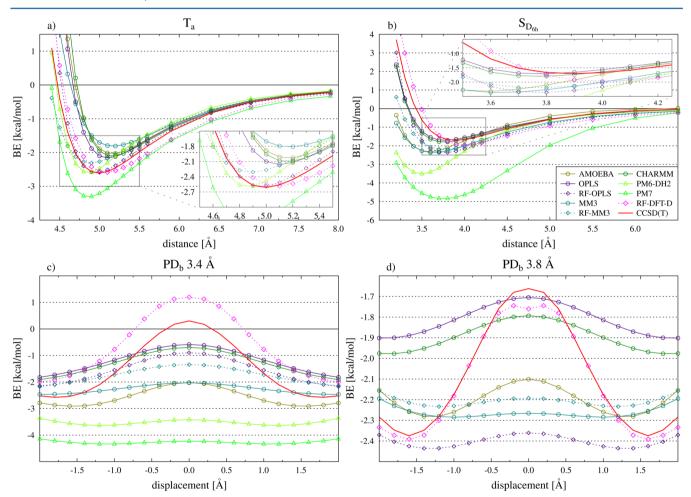


Figure 2. Binding energies (BE [kcal/mol]) of the potential energy surface of benzene dimer. For the T_a and $S_{D_{6h}}$ conformations the center of mass distance is plotted on the X-axis, for the PD_b conformations it indicates the displacement of the benzene molecules. The SE-D curves for PD_b 3.8 Å are not shown, as they are strongly overbinding, and are presented in the Supporting Information.

terms. The Coulumbic interactions are calculated from point charges that are fitted to reproduce the electrostatic potential around the molecule derived from quantum calculations. The vdW term includes an attractive $1/R^6$ term and a repulsive term resulting from the electron density overlap that gives atoms, in these classical models, their volume. In fact, for BD, the

energetics and geometries in MM models and in DFT-D arise from the balance between electrostatic forces and dispersion attractive interaction. In addition, intermolecular polarization adds a third term for polarizable models. The MM3, AMOEBA, CHARMM, and OPLS force fields are accurate and will be discussed here (the full table with results for all MM models can be found in the Supporting Information). Interestingly, MM3, AMOEBA, CHARMM, and OPLS all fail in one conformation, either PDb or VC that is unstable over the other. The quality of geometries, which do not switch, are quite similar for all force fields and PM6-DH2. AMOEBA and MM3 produce the best energies and geometries, outclassing DFT-D geometries in some cases. We refined the vdW parameters for benzene with the relax fitting procedure in the OPLS and MM3 force fields. For the intermolecular interactions the MM3 and OPLS share the same point charges but differ in the vdW potentials; OPLS has a Lennard-Jones type potential with an 1/ R¹² repulsive term, whereas MM3 has Buckingham type potential with an exponential term. Both force fields have parameters for many small organic molecules but differ in scope. MM3 intermolecular interactions for aromatic carbon were fitted to several crystals and graphite.⁵⁷ Benzene parameters in OPLS were fitted to reproduce experimental observables from benzene liquid trough Monte Carlo simulations.⁵⁰ Also MM3 includes the semiempirical Parisser-Pople-Par Hamiltonian that is able to reproduce fullerenes and polyaromatic hydrocarbons bond alternation.

Binding energies for RF-OPLS and RF-MM3 show increased accuracy yet inferior to RF-DFT-D. Interestingly, the accuracy of the dimer geometries is highly improved (Table 2) and similar to or better than that for RF-DFT-D in most cases.

Lennard-Jones type potentials are unable to account for the energy difference between AA and AB graphite.⁵⁸ In the following section we will study this issue with potential energy surface (PES) calculations.

Potential Energy Surfaces. The energy of T-shaped and sandwich BD conformations at increasing distances and the sliding of benzene in the parallel displaced (PD) conformation were studied and are shown in Figure 2. All methods reproduce the overall shape of the PES for T_a (Figure 2a) and $S_{D_{oli}}$ (Figure 2b) conformations. This is not surprising, as these curves correspond to the dissociation of the dimer and all vdW interactions sharing a $1/R^6$ term produce qualitatively similar results. The largest discrepancy is for SE-D methods, which show too large binding energies for the $S_{D_{oli}}$ conformations.

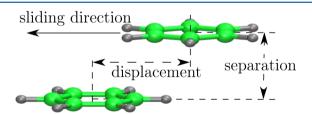


Figure 3. Sliding motion of the PD_b conformation.

Figure 3 shows the geometric parameters of the sliding motion that transforms the PD_b into the $S_{D_{6d}}$ conformation. The benzene molecules are separated by 3.5 Å in the PD_b conformation (with the displacement of 1.70 Å), and 3.9 Å for the $S_{D_{6d}}$ conformation. For the sliding motion (Figure 2c,d), the best performance is for RF-DFT-D followed by MM models with Lennard-Jones potentials, namely OPLS, RF-OPLS, and CHARMM, followed by AMOEBA and RF-MM3. The MM3 energy profile is too smooth whereas PM6-DH2 and PM7 profiles are wrong as they favor sandwich conformations over

PD ones^b. All methods except the RF-DFT-D systematically underestimate the energy difference between both conformations at all separations. Also for most MM models in this study, sandwich and parallel displaced structures yielded similar energies whereas in CCSD(T) they differ by 1 kcal/mol. This is also the reason why binding energies are typically more accurate for one of those conformations than the other (compare Figure 2 with Table 1).

A registry-dependent intermolecular potential with an anisotropic term aimed to reproduce π orbitals repulsive interactions reproduces accurately the sliding in graphite with molecular mechanics. The fact that RF-OPLS and RF-MM3, though improving geometries and energetics, still fail to reproduce the PES is due to limitations of the repulsive terms of the potentials. Furthermore, this limitation accounts for the frictionless motion observed in encapsulated fullerenes with MM models. 10

As a final test, we studied the PES of the C_{60} -benzene complex using RF-DFT-D, SE-D, and MM (a full description of these results is available in the Supporting Information).

In the PES, the benzene is situated over a [5,6] bond and then the fullerene is rotated perpendicular to the [5,6] bond (Figure 4). The results are presented in Figure 5. The RF-DFT-

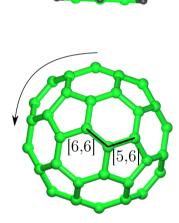


Figure 4. Potential energy surface geometries for the C_{60} -benzene complex (direction of fullerene rotation).

D minimum corresponds to the conformations in which the benzene is above a [6,6] bond. RF-MM3 and PM6-DH2 produce average interaction energies similar to that produced by the RF-DFT-D method but yield an energy profile that is too smooth. The energies more similar to RF-DFT-D are obtained for RF-MM3, vouching for the transferability of RF-MM3 parameters. RF-OPLS, CHARMM, and OPLS are too repulsive and are not binding.

CONCLUSIONS

The RF-DFT-D and relax fitted force fields (RF-MM3 and RF-OPLS) were able to reproduce the geometries of all stationary points of the benzene dimer with good accuracy. The MM3, OPLS, and AMOEBA failed only in one stationary point. Despite the improvement, the RF reparametrized force fields were unable to reproduce the energetics of the sliding motion in parallel displaced conformations. This is likely due to intrinsic limitations of vdW interaction used in each model. In most cases, the SE-D methods were less accurate than MM3 or OPLS, which are the method of choice after DFT-D. The most

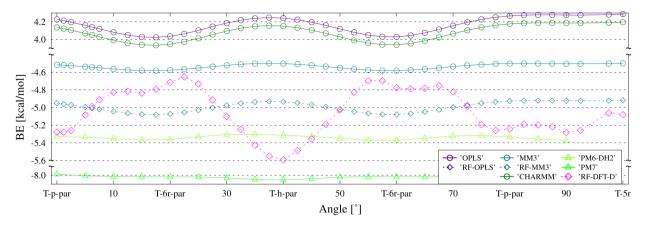


Figure 5. Binding energy (BE [kcal/mol]) of the C_{60} -benzene scan. The angle corresponds to rotations of the fullerene along the C_2 axis so that the benzene faces both types of fullerene bonds and rings. OPLS and CHARMM produced interaction energies around +4 kcal/mol, for the RF-OPLS force field interaction energies are around +2.6 kcal/mol. The AMOEBA force field calculations failed to converge and are not shown.

accurate SE method was PM6-DH2. In the PES of the $\rm C_{60}-$ benzene complex, RF-MM3 and PM6-DH2 showed binding energies similar to those of RF-DFT-D but still failed to reproduce its variations. RF-DFT-D is the method of choice of this study as it gives good geometries and reasonable energetics in all tests. MM3/OPLS/CHARM/AMOEBA/PM6-DH2 perform similarly, yet AMOEBA is not suitable for periodic systems (the polarization algorithm is not suitable for infinite systems). Unexpectedly, the SE methods perform worse than MM. For this reason, we advise the use of PM6-DH2 only for systems lacking parameters for MM.

Summing up, MM models, and specifically relax fitted models, are able to reproduce CCSD(T) calculated BD geometries with high accuracy. In contrast, DFT-D was the only method found to yield accurate binding energetics. MM or SE methods are not advised for accurate, relative or absolute, interaction energies of graphitic materials. RF-MM3 is the advised method for MM calculations. For computational efficiency, we recommend single point calculations at the DFT-D level on MM obtained geometries.

ASSOCIATED CONTENT

S Supporting Information

Tables and figures of binding energies obtained from all methods investigated. Description of the relaxed fitting method and parameters, and the full description of the C_{60} -benzene system. This material is available free of charge via the Internet at http://pubs.acs.org

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Notes

The authors declare no competing financial interest.

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ADDITIONAL NOTES

^aThe data for the benzene dimer presented here corresponds to the RF-6/6-31G in the original paper.

^bSE-D results for PD_b 3.8 Å are not shown, as they were highly overbinding.

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