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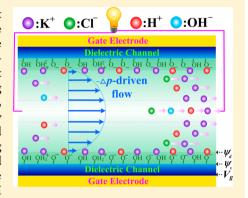
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## Tunable Streaming Current in a pH-Regulated Nanochannel by a **Field Effect Transistor**

Song Xue,<sup>†,‡</sup> Li-Hsien Yeh,\*,<sup>†,§</sup> Yu Ma,<sup>∥</sup> and Shizhi Qian\*,<sup>‡</sup>

Supporting Information

ABSTRACT: Many experimental results demonstrated that ion transport phenomena in nanofluidic devices are strongly dependent on the surface charge property of the nanochannel. In this study, active control of the surface charge property and the streaming current, generated by a pressure-driven flow, in a pHregulated nanochannel using a field effect transistor (FET) are analyzed for the first time. Analytical expressions for the surface charge property and the streaming current/conductance have been derived taking into account multiple ionic species, surface chemistry reactions, and the Stern layer effect. The model is validated by the experimental data of the streaming conductance in the silica nanochannel available in the literature. Results show that the pH-dependent streaming conductance of the gated silica nanochannel is consistent with its modulated zeta potential; however, the salt concentration-dependent streaming conductance might be different from the zeta potential behavior, depending on the solution pH



and the gate potential imposed. The performance of the field effect modulation of the zeta potential and the streaming conductance is significant for lower solution pH and salt concentration. The results gathered are informative for the design of the next-generation nanofluidics-based power generation apparatus.

#### 1. INTRODUCTION

Recent advances in nanofluidics attract considerable attention in using them as promising platforms for diverse applications such as ionic gates, <sup>1,2</sup> ionic diodes, <sup>3–5</sup> energy conversion, <sup>6–10</sup> and single (bio)nanoparticle sensing. <sup>11–13</sup> All of these nanofluidic-based applications rely on accurately analyzing the resulting ionic current signals, determined by the ion transport phenomena in these nanofluidic devices, in various solution properties. <sup>14–16</sup> Many experimental results revealed that the ion transport in nanofluidics can be regulated by modulating the surface charge property at the solid/liquid interface of these nanofluidic devices. Therefore, active control of the surface charge property of nanofluidic devices in various solution properties is crucial for the development of nextgeneration nanofluidics-based apparatus.

To this end, nanofluidic field effect transistors (FETs), 20-26 consisting of electrically controllable gate electrodes patterned along the outer wall surface of the dielectric nanochannels (or nanopores) made of such as silicon dioxide (SiO<sub>2</sub>), silicon nitride (SiN<sub>x</sub>), and aluminum oxide (Al<sub>2</sub>O<sub>3</sub>), have been developed to actively modulate their surface charge property. Control of the surface charge property, in turn, controls the transport of ions, fluid, and biomolecules in nanofluidics by modulating the gate potential imposed on the gate electrode. Many theoretical efforts<sup>27–40</sup> have been made to reveal how to regulate the transport of ions, fluid, and biomolecules in the FET-gated nanofluidic devices. However, these studies have

several limited assumptions, such as a constant surface charge density at the dielectric nanochannel wall, <sup>28–36</sup> consideration of background ionic species only, <sup>27–40</sup> and without considering the Stern layer effect.<sup>28–39</sup> Recently, Guan et al.<sup>41</sup> experimentally demonstrated that the field effect modulation of zeta potential and surface charge density at the gated dielectric channel material (e.g.,  $SiO_2$  and  $SiN_x$ )/electrolyte interface in various solution pH and ionic strength is distinctly different. They concluded that these intrinsic differences result from the surface chemistry reactions of functional groups with H<sup>+</sup> ions at the dielectric/electrolyte interface. Thus, developing a more general and realistic model to elaborate experimental observations in relevant gated nanofluidic devices is highly

Recent experimental studies demonstrated that the streaming current, generated by the pressure-driven flow, in the nanochannel provides a simple and effective scenario for converting hydrodynamics to electrical power.<sup>6–10</sup> This clean energy harvesting system using nanofluidics might open a new way for the development of renewable energy resources. The experimental results show that the streaming current is dependent on the flow of excess counterions, driven by an applied pressure field, in the electric double layer (EDL)

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formed in the vicinity of the charged channel wall. This implies that the surface charge property of the nanochannel and net amount of mobile ionic species in various electrolyte solutions can significantly influence the streaming current behavior. Although several theoretical works have been made for the streaming current in the nanochannel, all of these studies assumed that the liquid phase only contains one kind of cation and anion from the background salt. This assumption, although it simplifies the mathematical analysis, is unrealistic in practice because other ionic species are usually present. For example, the presence of H<sup>+</sup> and OH<sup>-</sup> ions need to be considered inevitably when the solution pH appreciably deviates from neutral.

In an attempt to better understand the aforementioned influences on the streaming current in the nanochannel, we investigate the field effect modulation of the surface charge property and the streaming current/conductance in a long pH-regulated nanochannel under various solution properties (pH and background salt concentration). Analytical expressions are derived for the first time to predict the zeta potential and the streaming current/conductance with the consideration of FET, multiple ionic species, surface chemistry reactions on the dielectric channel wall, and the Stern layer effect. In contrast to most of existing studies on the ion transport in nanofluidics, which focused mainly on the numerical simulations, 8,27–35,37,38,43–46 the present analytical results would provide better insight into the underlying physics and present convenient recipes for utilizing gated nanochannels in relevant applications.

## 2. THEORETICAL ANALYSIS

As schematically shown in Figure 1, we consider a fully developed pressure-driven flow of an aqueous electrolyte solution of relative permittivity  $\varepsilon_f$  in a long pH-regulated nanochannel of height h, width w, and length l. A streaming

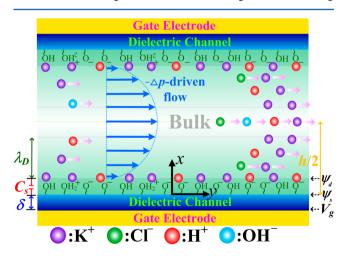


Figure 1. Schematic representation of the field effect regulation of the zeta potential  $(\psi_{\rm d})$  and the streaming current, driven by an applied pressure field  $(-\Delta p)$ , in a pH-regulated nanochannel containing multiple ionic species, H<sup>+</sup>, K<sup>+</sup>, Cl<sup>-</sup>, and OH<sup>-</sup>. Four major regions are considered: the dielectric channel of thickness  $\delta$ , the immobile Stern layer with surface capacitance  $C_{\rm s}$ , the diffusive layer of Debye length  $\lambda_{\rm D}$ , and the bulk solution state of pH and background salt concentration  $C_{\rm KCl}$ .  $V_{\rm g}$  is the gate potential imposed on the gate electrode, and  $\psi_{\rm s}$  is the surface potential stemming from the association and dissociation surface reactions of functional groups on the nanochannel wall.

current,  $I_{\rm str}$ , is induced by a pressure gradient,  $-\Delta p$ , applied across the nanochannel. <sup>42</sup> The nanochannel is equipped with a FET, including a thin dielectric channel layer of thickness  $\delta$  and relativity permittivity  $\varepsilon_{\rm d}$ , and a gate electrode patterned on its outer surface. A gate potential,  $V_{\rm g}$ , is imposed on the gate electrode to regulate the surface charge property and the streaming current in the nanochannel. The Cartesian coordinates x and y with the origin located at the bottom solid/liquid interface are adopted, and  $-\Delta p$  is directed along the y-direction.

We assume the following: (i) The liquid phase is an incompressible Newtonian fluid containing N kinds of ionic species, and the pressure-driven flow is fully developed and parallel to the nanochannel wall (i.e., y-direction). (ii) The Stern layer of a very thin thickness  $\delta_s$  is formed on the nanochannel wall, and ions and fluid inside that layer are immobile and do not contribute to streaming current. (iii) The no-slip plane is located at the Stern layer/diffusive layer interface. (iv) The dielectric channel (e.g., SiO<sub>2</sub>, SiN<sub>x</sub>, and Al<sub>2</sub>O<sub>3</sub>) wall in contact with an aqueous solution is of charge-regulated nature <sup>45,49,50</sup> and bears a uniform surface charge density  $\sigma_s$  along the y-direction. For example, nanochannels made of  $SiO_2$  (or  $SiN_x$ ) and  $Al_2O_3$  bear, respectively, dissociable functional groups  $Si-OH^{45,49}$  and  $Al-OH^{-1/2}$  27,50 capable of undergoing dissociation/association reactions with protons in aqueous solution. (v) The electroviscous effect is neglected, following the treatments of van der Heyden<sup>6,7,42</sup> and Chang and Yang.<sup>47</sup> (vi) The nanochannel height is much smaller than both its width and length  $(h \ll w \text{ and } h \ll l)$  so that the present problem can be approximated as a nanoslit with two infinite parallel plates. (vii) The overlapping of the EDLs of two adjacent nanochannel walls is insignificant, implying that the Debye length is much smaller than the half height of the nanochannel (i.e.,  $\lambda_D = \kappa^{-1} \ll h/2$ ). This assumption holds for most experimental conditions in nanofluidics. For example, the Debye length ranges from 9.6 to 0.3 nm, which is very thin compared to most of h,  $^{7,51-53}$  for the background salt concentration in experiments varying from 1 to 1000 mM. Therefore, the possible presence of the ion concentration polarization, 14,34 arising from the selective transport of counterions and co-ions, can be neglected. Under above assumptions, the distributions of the electric potential, ionic concentrations, and the fluid velocity are uniform in the y-direction.

**2.1. Governing Equations and Boundary Conditions.** Based on the aforementioned assumptions, the electric potentials within the dielectric channel, Stern layer, and liquid,  $\phi$ ,  $\varphi$ , and  $\psi$ , respectively, and the flow field can be described by

$$\frac{\mathrm{d}^2 \phi}{\mathrm{d}x^2} = 0 \quad \text{within the dielectric channel} \quad (-\delta \le x \le 0)$$
(1)

$$\frac{\mathrm{d}^2 \varphi}{\mathrm{d}x^2} = 0 \quad \text{within the Stern layer} \quad (0 \le x \le \delta_{\mathrm{s}}) \tag{2}$$

$$\frac{\mathrm{d}^2 \psi}{\mathrm{d}x^2} = -\frac{\rho_e}{\varepsilon_0 \varepsilon_f} = -\frac{1}{\varepsilon_0 \varepsilon_f} \sum_{i=1}^N F z_i C_{i0} \, \exp\left(-\frac{z_i F \psi}{RT}\right)$$

within the liquid phase 
$$(\delta_s \le x \le h/2)$$
 (3)

(13)

$$\frac{\mathrm{d}^2 u_y}{\mathrm{d}x^2} = \frac{1}{\mu} \frac{\mathrm{d}p}{\mathrm{d}y} \quad \text{within the liquid phase} \quad (\delta_{\mathrm{s}} \le x \le h/2)$$

In the above,  $\rho_e$  is the mobile space charge density;  $z_i$  and  $C_{i0}$  are the valence and the bulk concentration of the ith ionic species, respectively;  $\varepsilon_0$ , F, R, and T are the absolute permittivity of vacuum, Faraday constant, universal gas constant, and absolute temperature, respectively;  $\mu$  and  $u_y$  are the dynamic fluid viscosity and the fully developed pressure-driven fluid velocity in the y-direction, respectively.

The boundary conditions associated with eqs 1–4 are at the gate electrode ( $x = -\delta$ ),

$$\phi = V_{\rm g} \tag{5}$$

at the dielectric channel/Stern layer interface (x = 0),

$$\phi = \varphi = \psi_{\rm s} \tag{6a}$$

$$-\varepsilon_0 \varepsilon_{\rm d} \frac{{\rm d}\phi}{{\rm d}x} + \varepsilon_0 \varepsilon_{\rm f} \frac{{\rm d}\phi}{{\rm d}x} = -\sigma_{\rm s} \tag{6b}$$

at the Stern layer/diffusive layer interface ( $x = \delta_s$ ),

$$\varphi = \psi = \psi_{\rm d} \tag{7a}$$

$$-\varepsilon_0 \varepsilon_f \frac{\mathrm{d}\varphi}{\mathrm{d}x} + \varepsilon_0 \varepsilon_f \frac{\mathrm{d}\psi}{\mathrm{d}x} = 0 \tag{7b}$$

$$u_y = 0 (7c)$$

and at the center of the nanochannel (x = h/2),

$$\psi = \frac{\mathrm{d}\psi}{\mathrm{d}x} = 0 \tag{8a}$$

$$\frac{\mathrm{d}u_{y}}{\mathrm{d}x} = 0 \tag{8b}$$

Equations 6a and 6b imply that the electric potential is continuous but the electric field, which satisfies the Gauss's law, is not at the dielectric channel/Stern layer interface due to the discontinuity of the dielectric permittivities ( $\varepsilon_{\rm d}$  and  $\varepsilon_{\rm f}$ ). Equation 8a depicts that at the center of the nanochannel, the electric potential stemming from the charged nanochannel wall vanishes, and the ionic concentrations reach their bulk values due to the neglect of the EDL overlapping inside the nanochannel.

The analytical solutions to eqs 1 and 2 subject to eqs 5, 6a, and 7a are

$$\phi = \psi_{\rm s} + \frac{\psi_{\rm s} - V_{\rm g}}{\delta} x \tag{9}$$

$$\varphi = \psi_{\rm s} + \frac{\psi_{\rm d} - \psi_{\rm s}}{\delta_{\rm s}} x \tag{10}$$

By substituting eqs 9 and 10 into eqs 6b and 7b and letting the surface capacitance of the Stern layer,  $C_s = \varepsilon_0 \varepsilon_{\rm f}/\delta_{\rm s}$ , we obtain

$$-\varepsilon_0 \varepsilon_{\rm d} \left( \frac{\psi_{\rm s} - V_{\rm g}}{\delta} \right) + C_{\rm s} (\psi_{\rm d} - \psi_{\rm s}) = -\sigma_{\rm s}$$
(11)

$$-C_{\rm s}(\psi_{\rm d} - \psi_{\rm s}) - \sigma_{\rm d} = 0 \tag{12}$$

Here,  $\sigma_{\rm d}$  is the surface charge density of the diffuse layer and can be expressed as

$$\sigma_{d} = -\varepsilon_{0} \varepsilon_{f} d\psi / dx|_{x=\delta_{s}}$$

$$= sign(\psi_{d}) \sqrt{2\varepsilon_{0} \varepsilon_{f} RT \sum_{i=1}^{N} C_{i0} \left[ exp \left( -\frac{z_{i} F \psi_{d}}{RT} \right) - 1 \right]}$$

where  $sign(\psi_d) = 1$  for  $\psi_d > 0$  and  $sign(\psi_d) = -1$  for  $\psi_d < 0$ . It is worth noting that in the absence of the FET, the first term of the left-hand side of eq 11 vanishes and, therefore, eqs 11 and 12 reduce to

$$\psi_{\rm s} - \psi_{\rm d} = \frac{\sigma_{\rm s}}{C_{\rm s}} = \frac{\sigma_{\rm d}}{C_{\rm s}} \tag{14}$$

which is the well-known basic Stern layer model.<sup>49</sup> In short, the Stern layer models to describe the relationship between the surface potential  $(\psi_s)$  and zeta potential  $(\psi_d)$  of the nanochannel in the absence (eq 14) and presence (eqs 11 and 12) of FET are remarkably different.

Suppose that the dielectric channel wall bears dissociable functional groups MOH, capable of undergoing the following dissociation/association reactions: MOH  $\leftrightarrow$  MO $^-$  + H $^+$  and MOH + H $^+$   $\leftrightarrow$  MOH $_2^+$  with equilibrium constants  $K_A = (\Gamma_{\text{MO}^-}[\text{H}^+]_s)/\Gamma_{\text{MOH}}$  and  $K_{\text{B}} = \Gamma_{\text{MOH}_2}^+/(\Gamma_{\text{MOH}}[\text{H}^+]_s)$ , respectively. Here,  $\Gamma_{\text{MOH}}$ ,  $\Gamma_{\text{MO}^-}$ , and  $\Gamma_{\text{MOH}_2}^+$  denote the surface site densities of MOH, MO $^-$ , and MOH $^{2+}$ , respectively;  $[\text{H}^+]_s$  is the molar concentration of H $^+$  ions at the dielectric channel/liquid interface. If we let the total number site density of MOH molecules on the dielectric channel surface  $N_{\text{total}} = \Gamma_{\text{MOH}} + \Gamma_{\text{MO}^-} + \Gamma_{\text{MOH}_2}^+$  and assume that the equilibrium distribution of H $^+$  ions follows the Boltzmann distribution, the surface charge density of the dielectric channel  $\sigma_s$  can be expressed as  $^{40}$ 

$$\sigma_{s} = -FN_{\text{total}} \left\{ \left[ 10^{-pK_{A}} - 10^{-pK_{B}} \left[ 10^{-pH} \exp \left( -\frac{F\psi_{s}}{RT} \right) \right]^{2} \right] \right.$$

$$\left. / \left[ 10^{-pK_{A}} + 10^{-pH} \exp \left( -\frac{F\psi_{s}}{RT} \right) \right] + 10^{-pK_{B}} \left[ 10^{-pH} \exp \left( -\frac{F\psi_{s}}{RT} \right) \right]^{2} \right] \right\}$$

$$(15)$$

where  $pK_i = -\log K_i$  (j = A and B).

To simulate experimental conditions, we assume that the background salt in aqueous electrolyte solution is KCl of background concentration  $C_{\text{KCb}}$  and the solution pH is adjusted by HCl and KOH. This implies that four major kinds of ionic species (i.e., N=4) including K<sup>+</sup>, Cl<sup>-</sup>, H<sup>+</sup>, and OH<sup>-</sup> need to be considered. Let  $C_{10}$ ,  $C_{20}$ ,  $C_{30}$ , and  $C_{40}$  (in mM) be their bulk concentrations, respectively. Electroneutrality yields the following relations:  $^{55,56}$   $C_{10}=C_{\text{KCl}}$   $C_{20}=C_{\text{KCl}}+10^{(-\text{pH}+3)}-10^{-(14-\text{pH})+3}$ ,  $C_{30}=10^{(-\text{pH}+3)}$ , and  $C_{40}=10^{-(14-\text{pH})+3}$  for pH  $\leq$  7;  $C_{10}=C_{\text{KCl}}-10^{(-\text{pH}+3)}+10^{-(14-\text{pH})+3}$ ,  $C_{20}=C_{\text{KCl}}$ ,  $C_{30}=10^{(-\text{pH}+3)}$ , and  $C_{40}=10^{-(14-\text{pH})+3}$  for pH > 7.

**2.2. Analytical Multi-Ion Model (MIM).** The electroneutrality condition results in  $C_0 = C_{10} + C_{30} = C_{20} + C_{40} = C_{\text{KCI}} + 10^{(-\text{pH}+3)}$  for pH  $\leq 7$  and  $C_{\text{KCI}} + 10^{-(14-\text{pH})+3}$  for pH > 7. Equation 3, therefore, can be rewritten as

$$\frac{\mathrm{d}^2 \psi}{\mathrm{d}x^2} = \frac{RT\kappa^2}{zF} \sinh\!\left(\frac{zF\psi}{RT}\right) \quad \text{within the liquid phase}$$
 
$$\left(\delta_{\mathrm{s}} \le x \le h/2\right) \tag{16}$$

where  $z=z_1=-z_2$  and  $\kappa^{-1}=\lambda_{\rm D}=(\varepsilon_0\varepsilon_{\rm f}RT/2z^2F^2C_0)^{1/2}$  is the Debye length.

Solving eq 16 subject to eqs 7a and 8a, one gets

$$\psi = \frac{2RT}{zF} \ln \left[ \frac{1 + \exp(-\kappa x) \tanh(zF\psi_{d}/4RT)}{1 - \exp(-\kappa x) \tanh(zF\psi_{d}/4RT)} \right]$$
(17)

and, therefore, the charge density of the diffusive layer is

$$\sigma_{\rm d} = \frac{2\varepsilon_0 \varepsilon_{\rm f} \kappa RT}{zF} \sinh \left( \frac{zF \psi_{\rm d}}{2RT} \right) \tag{18}$$

By integrating eq 4 twice with the boundary conditions described by eqs 7c and 8b, one obtains the pressure-driven flow velocity,

$$u_{y} = \frac{1}{2\mu} \frac{dp}{dy} (x^{2} - hx)$$
 (19)

where  $-dp/dy = -\Delta p/l$  is the applied pressure gradient across the nanochannel.

Substituting eqs 15, 17, and 18 into eqs 11 and 12, we have the following implicit expressions relating the surface potential  $(\psi_s)$  to the zeta potential  $(\psi_d)$  of the nanochannel:

$$-\varepsilon_{0}\varepsilon_{d}\left(\frac{\psi_{s} - V_{g}}{\delta}\right) + C_{s}(\psi_{d} - \psi_{s})$$

$$= FN_{\text{total}}\left\{\left[10^{-pK_{A}} - 10^{-pK_{B}}\left[10^{-pH} \exp\left(-\frac{F\psi_{s}}{RT}\right)\right]^{2}\right]\right\}$$

$$\left[10^{-pK_{A}} + 10^{-pH} \exp\left(-\frac{F\psi_{s}}{RT}\right) + 10^{-pK_{B}}\left[10^{-pH} \exp\left(-\frac{F\psi_{s}}{RT}\right)\right]^{2}\right]\right\}$$
(20)

and

$$-C_{s}(\psi_{d} - \psi_{s}) = \frac{2\varepsilon_{0}\varepsilon_{f}\kappa RT}{zF} \sinh\left(\frac{zF\psi_{d}}{2RT}\right)$$
(21)

For given conditions, one can easily use the Matlab function fsolve to determine both  $\psi_s$  and  $\psi_d$  by simultaneously solving eqs 20 and 21. Then, the electric potential  $(\psi)$  and the surface charge density of the diffusive layer  $(\sigma_d)$  can be probed by eqs 17 and 18, respectively, based on the resulting  $\psi_d$ .

The streaming current  $(I_{\rm str})$  through the nanochannel can be exactly evaluated by (see the detailed derivation in the Supporting Information)

$$I_{\text{str}} = 2w \int_{\delta_{s} \to 0}^{h/2} \rho_{\varepsilon}(x) u_{y}(x) dx$$

$$= \frac{w\varepsilon_{0}\varepsilon_{f}h \psi_{d} \Delta p}{\mu l} - \frac{4w\varepsilon_{0}\varepsilon_{f}RT\Delta p}{\mu zF\kappa l}$$

$$\left[\ln\left(\frac{1+A \exp(-\kappa h/2)}{1-A \exp(-\kappa h/2)}\right) \ln\left(\frac{2}{1-A \exp(-\kappa h/2)}\right) + \operatorname{dilog}\left(\frac{2}{1-A \exp(-\kappa h/2)}\right) + \operatorname{dilog}\left(\frac{1+A \exp(-\kappa h/2)}{1-A \exp(-\kappa h/2)}\right)\right] - \left[\ln\left(\frac{1+A}{1-A}\right) \ln\left(\frac{2}{1-A}\right) + \operatorname{dilog}\left(\frac{1+A}{1-A}\right) + \operatorname{dilog}\left(\frac{2}{1-A}\right)\right]$$

$$+ \operatorname{dilog}\left(\frac{2}{1-A}\right)\right]$$

$$(22)$$

where  $A = \tanh(zF\psi_d/4RT)$  and dilog() represents the dilogarithm function. Once  $I_{\rm str}$  is obtained, the streaming conductance ( $G_{\rm str}$ ) of the nanochannel can be determined by  $^{42}$ 

$$\begin{split} G_{\text{str}} &= I_{\text{str}}/(-\Delta p) \\ &= -\frac{w\varepsilon_0 \varepsilon_f h \psi_d}{\mu l} + \frac{4w\varepsilon_0 \varepsilon_f RT}{\mu z F \kappa l} \\ &\left[ \ln \left( \frac{1 + A \, \exp(-\kappa h/2)}{1 - A \, \exp(-\kappa h/2)} \right) \right. \\ &\left. \ln \left( \frac{2}{1 - A \, \exp(-\kappa h/2)} \right) \right. \\ &\left. + \operatorname{dilog} \left( \frac{2}{1 - A \, \exp(-\kappa h/2)} \right) \right. \\ &\left. + \operatorname{dilog} \left( \frac{1 + A \, \exp(-\kappa h/2)}{1 - A \, \exp(-\kappa h/2)} \right) \right] \\ &\left. - \left[ \ln \left( \frac{1 + A}{1 - A} \right) \ln \left( \frac{2}{1 - A} \right) + \operatorname{dilog} \left( \frac{1 + A}{1 - A} \right) \right. \\ &\left. + \operatorname{dilog} \left( \frac{2}{1 - A} \right) \right] \end{split} \right] \end{split}$$

According to eqs 20–23,  $\psi_{\rm d}$ ,  $I_{\rm str}$ , and, accordingly,  $G_{\rm str}$  are functions of the gate potential  $(V_{\rm g})$ , the surface capacitance of the Stern layer  $(C_{\rm s})$ , the physicochemical properties of the dielectric channel wall (i.e.,  $N_{\rm total}$ , pK<sub>A</sub>, pK<sub>B</sub>,  $\varepsilon_{\rm d}$ , and  $\delta$ ), and the solution properties (i.e., pH,  $C_{\rm KCl}$ , and  $\varepsilon_{\rm f}$ ). It is worth noting that the present analytical MIM for the surface charge property and the streaming current/conductance in a gated nanochannel with and without FET control is more realistic and rigorous than most of the previous ones  $^{6-8,28-40,42-48}$  due to the consideration of multiple ionic species, the Stern layer effect, and the surface chemistry reactions of the dielectric channel wall. The influence of H<sup>+</sup> and OH<sup>-</sup> ions becomes significant when the solution pH is sufficiently high and low.

**2.3.** Analytical MIM Solution under the Debye–Hückel Approximation. Under the Debye–Hückel approximation (i.e.,  $|\psi_s| \ll RT/zF$ ), eqs 15 and 16 can be further approximated, respectively, to<sup>40</sup>

$$\sigma_{\rm s} = -FN_{\rm total} \left[ \frac{\Phi}{\Omega} + \left( \frac{F\psi_{\rm s}}{RT} \right) \left( \frac{\Pi}{\Omega} + \Lambda \right) \right]$$
(24)

and

$$\frac{\mathrm{d}^2 \psi}{\mathrm{d}x^2} = \kappa^2 \psi \quad \text{ within the liquid phase } \quad \left(\delta_{\mathrm{s}} \leq x \leq h/2\right) \tag{25}$$

In the above,  $\Omega=10^{-pK_A}+10^{-pH}+10^{-pK_B-2pH}, \ \Phi=10^{-pK_A}+10^{-pK_B-2pH}, \ \Pi=2\times 10^{-pK_B-2pH}, \ \text{and} \ \Lambda=\Phi(10^{-pH}+\Pi)/\Omega^2.$  Solving eq 25 subject to eqs 7a and 8a gives

$$\psi = \frac{\psi_{\rm d}}{\sinh(\kappa h/2)} \sinh\left[\kappa \left(\frac{h}{2} - \kappa\right)\right]$$
(26)

Therefore, the charge density of the diffusive layer  $\sigma_{\rm d}$  can be described by

$$\sigma_{\rm d} = \frac{\varepsilon_0 \varepsilon_{\rm f} \kappa \psi_{\rm d}}{\tanh(\kappa h/2)} \tag{27}$$

By substituting eqs 24 and 27 into eqs 11 and 12, we obtain

$$\begin{split} &-\varepsilon_{0}\varepsilon_{\mathrm{d}}\!\!\left(\frac{\psi_{\mathrm{s}}-V_{\mathrm{g}}}{\delta}\right) - \frac{\varepsilon_{0}\varepsilon_{\mathrm{f}}\kappa\psi_{\mathrm{d}}}{\tanh(\kappa h/2)} \\ &= FN_{\mathrm{total}}\!\left\{\frac{\Phi}{\Omega} + \left(\frac{F\psi_{\mathrm{s}}}{RT}\right)\!\!\left(\frac{\Pi}{\Omega} + \Lambda\right)\right\} \end{split} \tag{28}$$

and

$$-C_{s}(\psi_{d} - \psi_{s}) = \frac{\varepsilon_{0}\varepsilon_{f}\kappa\psi_{d}}{\tanh(\kappa h/2)}$$
(29)

Solving eqs 28 and 29 yields

and

$$\begin{split} \psi_{\rm d} &= \left\{ C_{\rm s} / \left[ C_{\rm s} + \left( \varepsilon_0 \varepsilon_{\rm f} \kappa / \tanh \left( \frac{\kappa h}{2} \right) \right) \right] \right. \\ &\times \left[ \left[ \varepsilon_0 \varepsilon_{\rm d} V_{\rm g} - \delta F N_{\rm total} \left( \frac{\Phi}{\Omega} \right) \right] \right. \\ &\left. / \left[ \varepsilon_0 \varepsilon_{\rm d} + \left[ \delta \varepsilon_0 \varepsilon_{\rm f} \kappa C_{\rm s} / \left[ C_{\rm s} \tanh \left( \frac{\kappa h}{2} \right) + \varepsilon_0 \varepsilon_{\rm f} \kappa \right] \right] \right. \\ &\left. + \left( \frac{\delta F^2 N_{\rm total}}{RT} \right) \left( \frac{\Pi}{\Omega} + \Lambda \right) \right] \right\} \end{split}$$

$$(31)$$

 $I_{
m str}$  and  $G_{
m str}$  can be further approximated, respectively, by (see the detailed derivation in the Supporting Information)

$$I_{\rm str} = \frac{w\varepsilon_0 \varepsilon_f \psi_d \Delta p}{\mu l} \left\{ h + \frac{2[1 - \cosh(\kappa h/2)]}{\kappa \sinh(\kappa h/2)} \right\}$$
(32)

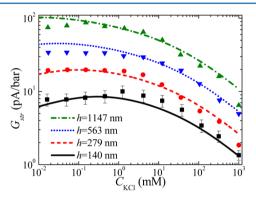
and

$$G_{\rm str} = -\frac{w\varepsilon_0 \varepsilon_{\rm f} \psi_{\rm d}}{\mu l} \left\{ h + \frac{2[1 - \cosh(\kappa h/2)]}{\kappa \sinh(\kappa h/2)} \right\}$$
(33)

### 3. RESULTS AND DISCUSSION

To validate the derived models, section 3.1 compares the predictions of the streaming conductance,  $G_{\rm str}$ , in a silica nanochannel from the analytical MIM to the existing experimental data available in the literature. The analytical MIM with the fitted parameters (i.e.,  $N_{\rm total}$ , p $K_A$ , p $K_B$ , and  $C_s$ ) are then used to verify the applicability of that under the Debye–Hückel approximation in section 3.2, and to investigate the field effect regulation of the zeta potential and the streaming conductance in a gated silica nanochannel under various solution properties (pH and salt concentration) in sections 3.3 and 3.4. The relevant physical parameters used in the calculations are  $\varepsilon_0 = 8.85 \times 10^{-12}$  C V<sup>-1</sup> m<sup>-1</sup>,  $\mu = 10^{-3}$  kg m<sup>-1</sup> s<sup>-1</sup>, F = 96487 C mol<sup>-1</sup>, R = 8.31 J K<sup>-1</sup> mol<sup>-1</sup>, T = 298 K,  $\varepsilon_{\rm f} = 78.5$ , and  $\varepsilon_{\rm d} = 3.9$  (SiO<sub>2</sub>).

**3.1.** Verification of the Analytical MIM by Experimental Data. The applicability of the present analytical MIM (eqs 20–23 in section 2.2) is first verified by the experimental data of van der Heyden et al., where the streaming conductance,  $G_{\rm str}$ , in a silica nanochannel of width w=50  $\mu{\rm m}$  and length l=4.5 mm was conducted at the applied pressure  $\Delta p=-4$  bar and pH = 8. Figure 2 depicts the



**Figure 2.** Dependence of the streaming conductance ( $G_{\rm str}$ ) in a silica nanochannel on the background salt concentration  $C_{\rm KCl}$  for various nanochannel heights. Symbols: experimental data of van der Heyden et al. <sup>42</sup> at  $\Delta p = -4$  bar,  $w = 50~\mu{\rm m}$ ,  $l = 4.5~{\rm mm}$ , and pH = 8; lines: results of the present analytical MIM at  $C_{\rm s} = 0.42~{\rm F/m^2}$ ,  $N_{\rm total} = 4~{\rm nm^{-2}}$ ,  $pK_{\rm A} = 8$ , and  $pK_{\rm B} = 2.5$ .

dependence of  $G_{\text{str}}$  on the background salt concentration  $C_{\text{KCl}}$ for various nanochannel heights ranging from 140 to 1147 nm. As shown in Figure 2, the predictions from our analytical MIM (lines), with the same parameters  $C_s = 0.42 \text{ F/m}^2$ ,  $N_{\text{total}} = 4$ nm<sup>-2</sup>, p $K_A$  = 8, and p $K_B$  = 2.5, agree well with the experimental data of van der Heyden et al.<sup>42</sup> (symbols). The fitted parameters (i.e.,  $C_s$ ,  $N_{total}$ ,  $pK_A$ , and  $pK_B$ ) and the corresponding isoelectric point of the silica nanochannel (e.g., 2.75) are also consistent with those reported in the literature (e.g.,  $N_{\text{total}}$  = 3.8–8 nm<sup>-2</sup>, p $K_A$  = 6–8, p $K_B$  = 0–3, and  $C_s$  = 0.15–2.9 F/m<sup>2</sup>,<sup>7,42,45</sup> and the isoelectric point is about 2–3.5<sup>57</sup> for the dielectric channel made of silica). It should be pointed out that only one set of the fitted parameters based on our model is used to describe the experimental data of the streaming conductance in a silica nanochannel with various channel heights. This is much better than the model proposed by van der Heyden et al., 42 where they used different fitted parameters to describe the behaviors of the streaming conductance in the silica nanochannels with various heights. This might be caused by the neglection of multiple ionic species and the association

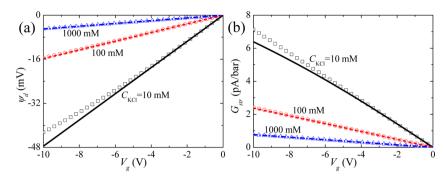


Figure 3. Zeta potential  $\psi_d$  (a) and streaming conductance  $G_{\rm str}$  (b) as a function of the gate potential  $V_{\rm g}$  for various background salt concentrations  $C_{\rm KCl}$  at pH = 3. Symbols denote the results of the analytical MIM, and lines in (a) and (b) denote the results from the closed-form Debye—Hückel approximation based on eqs 31 and 33, respectively.

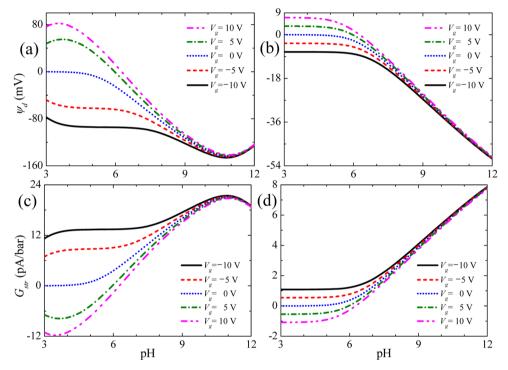


Figure 4. Zeta potential  $\psi_d$  (a, b) and streaming conductance  $G_{\rm str}$  (c, d) as a function of the solution pH for various gate potential  $V_{\rm g}$  at the background salt concentration  $C_{\rm KCI}=1$  mM (a, c) and 500 mM (b, d).

reaction of silanol (Si–OH) groups on the nanochannel wall in their study. Therefore, the predicted values of  $C_{\rm s}=0.42~{\rm F/m^2}$ ,  $N_{\rm total}=4~{\rm nm^{-2}}$ , p $K_{\rm A}=8$ , and p $K_{\rm B}=2.5$ , are then used in the following discussions. For illustration, we consider a FET-gated nanochannel with height  $h=200~{\rm nm}$ , width  $w=50~\mu{\rm m}$ , length  $l=4.5~{\rm mm}$ , and the thickness of the dielectric layer  $\delta=30~{\rm nm}$ .

**3.2. Verification of the Analytical MIM Solution under the Debye–Hückel Approximation.** The applicability of the analytical MIM solutions under the Debye–Hückel approximation (i.e.,  $|\psi| \ll 25.7$  mV) for the zeta potential,  $\psi_{\rm d}$  (eq 31), and the streaming conductance,  $G_{\rm str}$  (eq 33), in a gated silica nanochannel is examined in Figure 3. In this figure, the variations of  $\psi_{\rm d}$  and  $G_{\rm str}$  as a function of the applied gate potential  $V_{\rm g}$  for various background salt concentrations  $C_{\rm KCI}$  at pH = 3 are plotted in Figure 3a and b, respectively. Figure 3 clearly shows that the results of  $\psi_{\rm d}$  and  $G_{\rm str}$  obtained from the closed-form analytical MIM solutions (eqs 31 and 33 in section 2.3) match well with those from the implicit solution based on the analytical MIM (eqs 20–23 in section 2.2). An excellent agreement between the results of  $\psi_{\rm d}$  and  $G_{\rm str}$  obtained from the

above two models is observed when  $|\psi_d|$  is below 25.7 mV at small  $V_{\rm g}$  and high  $C_{\rm KCl}$ . Even if  $|\psi_{\rm d}|$  is between 25.7 and 47.6 mV at large  $V_g$  and low  $C_{KCl}$ , a maximum relative error of about 10.6% between the closed-form analytical MIM expressions and the exact implicit solution obtained from the analytical MIM for  $\psi_{\rm d}$  and  $G_{\rm str}$  is obtained, as depicted in Figure 3. Therefore, we conclude that the present closed-form analytical MIM solutions are capable of accurately predicting the general trends of  $\psi_d$  and  $G_{\rm str}$  for  $|\psi_{\rm d}| \le 47.6$  mV, especially when the salt concentration is sufficiently high, which is the typical condition encountered in FET-gated nanofluidics applications. 20,25-27 Figure 3b also suggests that  $G_{\rm str}$  is larger for lower  $C_{\rm KCl}$ . This agrees with the experimental observations for the streaming current (or conductance), 6,7,42 and is because both the EDL thickness and the zeta potential (Figure 3a) of the nanochannel increase with a decrease in the salt concentration. These two combined effects lead to more net charges  $(2w\int_{\delta_{\epsilon}}^{h/2}\rho_{\epsilon}(x)dx)$  within the nanochannel carried by the pressure-driven flow. However, the salt concentration dependence of the streaming current/

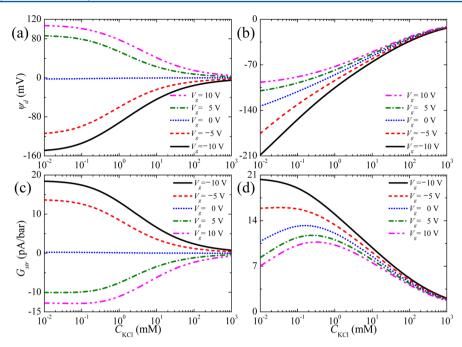


Figure 5. Zeta potential  $\psi_d$  (a, b) and streaming conductance  $G_{str}$  (c, d) as a function of the background salt concentration  $C_{KCI}$  for various gate potential  $V_g$  at the solution pH = 4 (a, c) and 8 (b, d).

conductance in the nanochannel is inconsistent with that of the ionic current/conductance, which decreases with a decrease in the salt concentration. This is because the ionic current/conductance in nanofluidics is dominated by the net ionic concentration,  $\sum_{i=1}^{N} C_{i0}$ , in the bulk electrolyte solution (not mobile net charges,  $\rho_e$ ).

**3.3. Influence of Solution pH.** Figure 4 depicts the influence of the solution pH on the field effect regulation of the zeta potential,  $\psi_d$ , and the streaming conductance,  $G_{\text{str}}$ , for various gate potentials,  $V_g$ , at two levels of the background salt concentration, C<sub>KCl</sub>. This figure clearly shows that the zeta potential,  $\psi_{\mathrm{d}}$ , and, accordingly, the streaming conductance,  $G_{\mathrm{str}}$ , of the nanochannel can be actively tuned from negative to positive by the gate potential,  $V_{\rm g}$ . Similar behavior has been observed experimentally in the studies of the field effect control of the zeta potential in nanofluidics<sup>20,41</sup> and can be further utilized to control the transport of ions, fluid, and biomolecules. 20,25-27,35,41 Figure 4 also reveals that the performance of the field effect modulation of  $\psi_d$  (Figure 4a,b) and  $G_{\text{str}}$  (Figure 4c,d) is remarkable at low solution pH and becomes unremarkable at sufficiently high solution pH. This is because the proton concentration increases with decreasing solution pH, leading to less negatively charged SiO dissociated from the silanol (SiOH) functional groups on the nanochannel surface and, therefore, a smaller  $\sigma_s$  and lesser counterions electrostatically attracted to the channel surface, therefore, makes the FET easiler to tune its zeta potential. According to eqs 22 and 23, since the streaming current/ conductance of the nanochannel strongly depends upon the magnitude of its zeta potential, a superior tuning efficiency of the streaming current by the FET in nanofluidics at low solution pH is observed in Figure 4c,d.

It is interesting to note in Figure 4 that the field effect regulation behaviors of  $\psi_{\rm d}$  and  $G_{\rm str}$  versus the solution pH depend significantly upon the levels of the applied gate potential  $V_{\rm g}$  and the background salt concentration  $C_{\rm KCI}$ . If the FET is floating ( $V_{\rm g}=0$  V) and a negative gate potential is

applied ( $V_g$  < 0 V), Figure 4b,d reveals that the magnitude of  $\psi_d$ and, accordingly,  $G_{\text{str}}$  increase monotonically with the solution pH at high salt concentration  $C_{KCl} = 500$  mM. On the other hand, at relatively low salt concentration  $C_{KCl} = 1$  mM (Figure 4a,c), both  $|\psi_d|$  and  $G_{\text{str}}$  increase with the solution pH when it is low and show a local maximum when the solution pH is sufficiently high. The behavior that  $|\psi_d|$  and, accordingly,  $G_{\rm str}$ increase with increasing pH is expected due to an increase in  $|\sigma_s|$ . However, an increase in the solution pH, when it deviates appreciably from 7, also results in an increase in the ionic strength (a decrease in the EDL thickness). If the behavior of  $\psi_d$  is dominated by the effect of an increase in the ionic strength, which becomes significant when  $C_{KCl}$  is sufficiently low,  $|\psi_d|$  decreases accordingly. This explains why  $|\psi_d|$  and, accordingly, G<sub>str</sub> decrease with an increase in the solution pH for pH > 11 at  $C_{\rm KCl}$  = 1 mM, as shown in Figure 4a,c.

If a positive gate potential is applied (i.e.,  $V_g > 0$  V), Figure 4a,b shows that  $\psi_d$  ( $G_{str}$ ) remains negative (positive) at high solution pH and becomes positive (negative) at low solution pH. Note that when the solution pH is low, both  $\psi_d$  and  $|G_{str}|$ show an apparent local maximum as the solution pH varies at low salt concentration  $C_{KCl} = 1$  mM (Figure 4a,c) but decrease monotonically with increasing pH at high salt concentration  $C_{\rm KCl}$  = 500 mM (Figure 4b,d). The former can be attributed to an increase in the ionic strength when the solution pH declines significantly from 7, thus, lowering the modulated zeta potential of the nanochannel. This effect becomes significant when the background salt concentration is sufficiently low, as described previously. From Figure 4, it is worth concluding that for a fixed  $C_{\rm KCV}$  the behavior of  $G_{\rm str}$  as the solution pH varies is consistent with that of  $\psi_d$  because of the significant zeta potentialdependent streaming current (or conductance) behavior in the nanochannel, according to eqs 22 and 23.

**3.4.** Influence of Background Salt Concentration. Figure 5 depicts the influence of the background salt concentration,  $C_{\text{KCI}}$  on the field effect regulation of the zeta potential,  $\psi_{\text{d}}$ , and the streaming conductance,  $G_{\text{str}}$  for various

gate potentials,  $V_g$ , at two levels of the solution pH. This figure shows that at low solution pH = 4,  $\psi_d$  and, accordingly,  $G_{\rm str}$ , is modulated from negative to positive as  $V_g$  varies; however, only the magnitude of  $\psi_d$  and  $G_{\rm str}$  can be tuned for the considered region of  $V_g$  ranging from -10 to 10 V at relatively high solution pH = 8. These behaviors are consistent with those in Figure 4 and can be attributed to a higher surface charge density of the nanochannel, thus making the FET harder to regulate the zeta potential and the corresponding electrokinetic transport phenomena in the nanochannel. Figure 5 also suggests that the degree of the field effect regulation of  $\psi_d$  (Figure 5a,b) and  $G_{\rm str}$  (Figure 5c,d) is significant if  $C_{\rm KCl}$  is low and becomes insignificant if  $C_{\rm KCl}$  is sufficiently high. In this case, a higher gate potential is required to effectively tune the zeta potential and streaming current in the nanochannel.

Figure 5a,b reveals that regardless of the levels of pH and  $V_{\sigma I}$ the magnitude of  $\psi_d$  decreases monotonically with increasing  $C_{\rm KCl}$ . This is because the EDL thickness decreases with an increase in the salt concentration, resulting in more counterions gathered near the nanochannel wall and, thus, lowering its effective charge. It is interesting to note in Figure 5c,d that for the considered region of  $C_{KCl}$ , the behaviors of  $G_{str}$  with  $C_{KCl}$ depend upon the levels of pH and  $V_{\rm g}$ . If the solution pH is low (Figure 5c), the magnitude of  $G_{\rm str}$  increases with decreasing C<sub>KCl</sub> in the high salt concentration regime and reaches a nearly saturated value (plateau) in the low salt concentration regime. On the other hand, if the solution pH is high (Figure 5d),  $G_{\text{str}}$ increases first and then attains a plateau as C<sub>KCl</sub> decreases for the relatively high negative gate potentials (i.e.,  $V_g = -5$  and -10 V) and shows a local maximum for the floating FET (i.e.,  $V_{\rm g}$  = 0 V) and the positive gate potentials (i.e.,  $V_{\rm g}$  = 5 and 10 V). The local maximum of  $G_{\rm str}$  extends to higher  $C_{\rm KCl}$  for larger positive  $V_{\rm g}$ . The behavior that  $G_{\rm str}$  increases with a decrease in C<sub>KCl</sub> in the high salt concentration regime can be attributed to the combined effects of a greater  $|\psi_d|$  (shown in Figure 5a,b) and a thicker EDL. However, if  $C_{KCl}$  further declines to a critically low regime, because the major counterions (K+ ions) from the background salt KCl become very dilute,  $G_{\rm str}$  shows a decreasing tendency with a decrease in  $C_{KCl}$ . Note that if the solution pH is sufficiently low, the other counterions (H<sup>+</sup> ions) dissociated from HCl and water becomes dominant. Therefore, the aforementioned dilute effect of  $K^+$  ions as  $C_{KCl}$  decreases becomes relatively insignificant. This is why  $G_{\rm str}$  shows a plateau for lower  $C_{KCl}$  at the low solution pH, as seen in Figure

## 4. CONCLUSIONS

For the first time, we investigate the field effect control of the surface charge property and the streaming current/conductance, generated by a pressure-driven flow, in a FET-gated silica nanochannel under various solution properties (background pH and salt concentration). Taking practical effects such as multiple ionic species, surface chemistry reactions, and the Stern layer into account, we derived analytical expressions, including implicit and explicit ones, to estimate the surface charge property and the streaming current/conductance tuned by a FET. The implicit analytical multi-ion model (MIM) is validated by comparing its predictions to the existing experimental data of the streaming conductance in the silica nanochannels with various channel heights. The explicit analytical MIM based on the Debye-Hückel approximation is valid especially when the magnitude of the zeta potential is less than the thermal potential, which often holds for relatively

high salt concentration, in accordance with typical nanofluidicsbased experimental conditions. The results clearly show that the zeta potential as well as the streaming current/conductance can be actively tuned by the FET. The performance of the zeta potential and streaming conductance modulation by FET is better when the background salt concentration and pH are low. The developed model predicts that the dependence of the streaming conductance on the solution pH is consistent with the dependence of the zeta potential. However, that dependence on the salt concentration might be different from the dependence of the zeta potential, depending on the levels of the solution pH and the gate potential. For example, for relatively high solution pH, the magnitude of the zeta potential of the nanochannel increases with decreasing background salt concentration, but the streaming conductance increases first and then decreases (or exhibits a plateau) with a decrease in the salt concentration.

#### ASSOCIATED CONTENT

## **S** Supporting Information

The detailed derivation of eqs 22, 23, 32, and 33. This material is available free of charge via the Internet at http://pubs.acs.org.

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#### Notes

The authors declare no competing financial interest.

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