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# Relationship between the Broad OH Stretching Band of Methanol and Hydrogen-Bonding Patterns in the Liquid Phase

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The OH stretching ( $\nu_{OH}$ ) band of methanol observed in condensed phase has been analyzed in terms of hydrogen-bonding patterns. Quantum chemical calculations for methanol clusters have revealed that broadening of the  $\nu_{OH}$  envelope is reasonably reproduced by considering nearest and next-nearest neighbor interactions through hydrogen bonding. Because the hydrogen bond formed between donor (D) and acceptor (A) is cooperatively strengthened or weakened by a newly formed hydrogen bond at D or A, we have proposed the following notation for hydrogen-bonding patterns of monohydric alcohols:  $a_D D A d_A a_A$ , where a is the number of protons accepted by D ( $a_D$ ) or A ( $a_A$ ), and  $d_A$  is the number of protons donated by A. The indicator of the hydrogen-bond strength, which is given by  $M_{OH} = a_D + d_A - a_A$ , is correlated well with the  $\nu_{OH}$  wavenumber of the methanol molecule D participating in the  $a_D D A d_A a_A$  pattern. The correlation between  $M_{OH}$  and the hydrogen-bonding energy of the  $a_D D A d_A a_A$  pattern has also been deduced from the calculation results for the clusters. The  $\nu_{OH}$  bands of methanol measured in the CCl<sub>4</sub> solution and pure liquid have been successfully analyzed by the method proposed here.

#### 1. Introduction

Methanol is a highly structured liquid at ambient temperature, in which the molecules interact with each other through hydrogen bonding. The measurement of the OH stretching ( $\nu_{OH}$ ) band has proved to be a sensitive indicator of the strength of the hydrogen bond.  $^{1-4}$  The  $\nu_{\mathrm{OH}}$  band shows a drastic change in its wavenumber and intensity depending upon the formation of hydrogen bond. The  $\nu_{\rm OH}$  envelope of methanol in condensed phase has a broad feature, which is generally attributed to the presence of various hydrogen-bonded aggregates. In this context, the  $\nu_{OH}$  bands for methanol clusters have attracted keen interests.  $^{5-16}$  The monomer, dimer, trimer, tetramer, and polymer  $(CH_3OH)_n$   $(n \ge 4)$  were identified by matrix-isolation infrared (IR) spectroscopy.<sup>6–8</sup> The small clusters with n < 5 were also found by IR spectroscopy in a pulsed supersonic slit-jet expansion system<sup>14</sup> and IR cavity ring-down spectroscopy.<sup>15</sup> However, the interpretation of the broad  $\nu_{OH}$  envelope for methanol in the pure liquid and concentrated solutions is still the subject of much discussion because of its structureless feature. Several researchers pointed out that the  $\nu_{OH}$  envelope of liquid methanol seems to be represented by one Gaussian function. 10 Because methanol molecules can form a percolated network through hydrogen bonding in condensed phase, the analytical model based on the limit size clusters may not be

The broadening of the  $\nu_{\rm OH}$  envelope of methanol may arise not only from the presence of various aggregates but also from the cooperativity of hydrogen bonding. <sup>17–19</sup> The cooperativity plays an important role in the formation of hydrogen-bonded aggregates; the strength of a newly formed hydrogen bond is

significantly influenced by the presence of already formed hydrogen bonds. Because the  $\nu_{OH}$  wavenumber correlates with the strength of hydrogen bond, the cooperativity should significantly affect the feature of the  $v_{OH}$  band of methanol. To link spectral information to microscopic information on hydrogen bonds, therefore, we must consider both the hydrogenbonding patterns and the cooperativity. In this paper, we propose a novel method to analyze the broad  $\nu_{OH}$  envelope of methanol observed in condensed phase. The purpose here is not to clarify what kind of methanol clusters exist in the solution and pure liquid but to interpret what kind of hydrogen-bonding patterns are dominant. First, we modify the notation of hydrogen-bonding patterns for investigating the  $\nu_{\rm OH}$  envelope of water, <sup>20</sup> in which the cooperativity of hydrogen bonding is estimated by considering the nearest and next-nearest neighbor interactions. For the methanol system, 12 hydrogen-bonding patterns can be distinguished. Second, we employ the quantum chemical calculation to link the  $\nu_{OH}$  wavenumbers with the hydrogen-bonding patterns incorporated into the methanol clusters. As a result, the  $\nu_{\rm OH}$ wavenumbers of the 12 patterns can be categorized into five. This method enables us to investigate the change in the broad and structureless  $v_{OH}$  envelope of methanol in condensed phase in terms of the variation in the hydrogen-bonding patterns.

#### 2. Quantum Chemical Calculation

Quantum chemical calculations were performed by using the Gaussian 03 program. Pottimal geometries, harmonic wavenumbers, and IR intensities of methanol clusters (CH<sub>3</sub>OH)<sub>n</sub> with n=1-7 were obtained by the density functional theory (DFT) by using the 6-311++G(d,p) basis set. PFT calculations, we used Becke's three-parameter exchange functional together with correlation functional of Lee-Yang-Parr (B3LYP). Harmonic wavenumbers  $\nu_{\rm harm}$  obtained by DFT calculations were scaled by the formula  $\nu_{\rm OH}$  =  $\nu_{\rm harm}$  (1.2155 – 0.00007 $\nu_{\rm harm}$ ). The normal vibrations were calculated for two types of isotope

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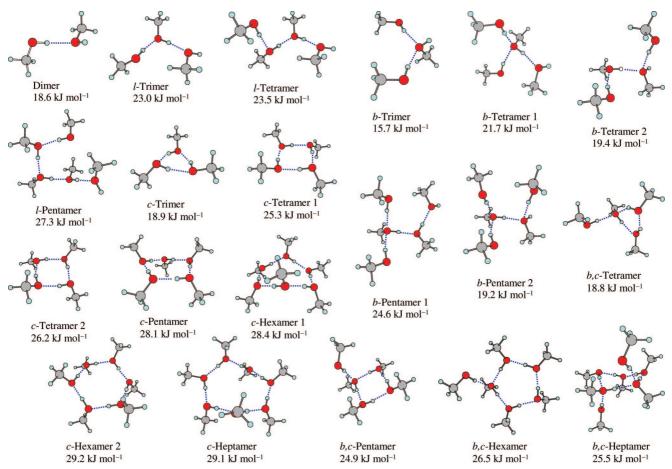


Figure 1. Geometries of methanol clusters  $(CH_3OH)_n$  with n = 2-7 optimized at the B3LYP/6-311++G(d,p) level. The linear, cyclic, and branched structures are indicated by l-, c-, and b-, respectively. The average hydrogen-bonding energy for each structure,  $\Delta \bar{E}_{hb}$ , is indicated below the structure (see text for the definition). The dotted line represents the OH···O hydrogen bond.

clusters. The coupled  $\nu_{OH}$  wavenumbers were calculated for methanol (CH<sub>3</sub>OH) embedded in clusters constituted of CH<sub>3</sub>OH molecules. The uncoupled  $\nu_{\rm OH}$  wavenumbers were calculated for CH<sub>3</sub>OH surrounded by deuterated methanol (CH<sub>3</sub>OD) molecules in the same clusters. 28,29 The total and average energy of hydrogen bonding,  $\Delta E_{\rm hb}$  and  $\Delta \bar{E}_{\rm hb}$ , are defined by the following equations

$$\Delta E_{\rm hb} = nE({\rm monomer}) - E({\rm n-mer})$$
 (1a)

$$\Delta \bar{E}_{hb} = \frac{\Delta E_{hb}}{m} \tag{1b}$$

where E(monomer) is the electronic energy for the monomer, E(n-mer) is the electronic energy for the n-mer, n is the number of methanol molecules participating in the cluster, and m is the number of hydrogen bonds in the cluster. The zero-point energy correction was carried out for E(monomer) and E(n-mer) of the undeuterated systems.

## 3. Experimental Section

The CH<sub>3</sub>OD was obtained from Aldrich. The purity of the sample is ca. 98% (the isotopic purity is higher than 99%). The CH<sub>3</sub>OH and carbon tetrachloride (CCl<sub>4</sub>) were purchased from Wako (∞ pure grade, the purity is 99.8%). All chemicals were used without further purification. IR spectra were recorded on a Bruker IFS66V vacuum spectrophotometer equipped with a deuterated triglycine sulfate (DTGS) detector by coaddition of 256 scans at a resolution of 2 cm<sup>-1</sup>. To measure the uncoupled  $\nu_{\rm OH}$  band, we prepared an isotope mixture that contained 1 wt% of CH<sub>3</sub>OH in CH<sub>3</sub>OD as the pure liquid of methanol. A CCl<sub>4</sub> solution of methanol with the isotope mixture was also prepared, in which the total methanol concentration was 0.10 mol dm<sup>-3</sup>. We used the quartz cell with 10 mm of path length for the CCl<sub>4</sub> solution and the CaF<sub>2</sub> cell with 0.1 mm of path length for the pure liquid. The sample cells were placed in a homemade holder temperature-regulated by a Peltier device.

Nonlinear curve fittings and principal-component analysis (PCA) were performed by a software written by one of the authors (Y.K.). 30 The Levenberg-Marquardt algorithm 31 for a nonlinear least-squares method was used for the curve-fitting procedure. The position and number of the peaks used in the curve fitting were estimated by third derivative, and the shape of the decomposed band was assumed to be a linear combination of Gaussian and Lorentzian functions. Third derivatives were calculated by the Savitzky-Golay method.32 PCA was performed by finding eigenvalues and eigenvectors of a tridiagonal matrix calculated from the experimental IR spectra.<sup>33</sup> The Householder method was used to obtain the tridiagonal form of data matrix. The QL algorithm with implicit shifts was employed to determine the eigenvalues and eigenvectors.<sup>31</sup>

### 4. Results and Discussion

4.1. Relationship between the  $v_{OH}$  Wavenumbers and Hydrogen-Bonding Patterns for Methanol Clusters. Figure 1 shows the optimized geometries for methanol clusters, together with  $\Delta \bar{E}_{hb}$ . The coupled and uncoupled  $\nu_{OH}$  wavenumbers of methanol clusters are given in Table 1. All the free OH-bond lengths are calculated to be  $0.962 \pm 0.02 \text{ Å}$  (1 Å =  $10^{-10} \text{ m}$ ).<sup>34</sup>

TABLE 1: Calculated  $v_{OH}$  Wavenumbers of Methanol Clusters  $(CH_3OH)_n$  with n = 1-7

	coupled $\nu_{\rm OH}/{\rm cm}^{-1}$	(absorbance	e/km mol <sup>-1</sup> )	uncoupled $\nu_{\mathrm{OH}}$	cm <sup>-1</sup>		assignment	
monomer	dimer	<i>l</i> -trime	ar	<i>l</i> -tetramer		<i>l</i> -pentamer	$a_{\mathrm{D}}\mathrm{DA}d_{\mathrm{A}}a_{\mathrm{A}}$	$M_{\rm O}$
						1		
	3639 (44) 3639	3644 (43)	3644	3645 (47) 364	5	3643 (44) 3642	Free	
	3533 (508) 3533	3483 (683)	2175	3478 (600) 34	76	3448 (646) 3449	0DA00 1DA00	
		3450 (583)		3471 (621) 34		3415 (682) 3408	0DA10	
		3430 (363)	3400	3362 (959) 33		3365 (1314) 3359	1DA10	
				3302 (737) 33	0)	3309 (942) 3327	1DA10	
<i>b</i> -trimer	<i>b</i> -tetramer 1	<i>b</i> -1	tetramer 2	<i>b</i> -pen	tamer 1	<i>b</i> -pentamer 2		
3626 (53) 3626	3641 (50) 3642	3631	(55) 3630	3643 (4:	5) 3643	3631 (59) 3630	Free	
3558 (299) 3553	` /		(341) 3565	5015 (1.	3) 3013	3585 (256) 3589	0DA01	_
3547 (526) 3553		2202	(5.1) 5565			2202 (220) 220)	0DA01	_
(0=0)	3515 (378) 3507			3498 (4	49) 3493	3544 (447) 3538	0DA11	0
	3494 (702) 3500			*	026) 3464	, ,	0DA11	0
	( )		(596) 3500	2.02 (0	,	0011 (010) 0013	1DA01	0
			(521) 3474				0DA10	1
			(- )	3451 (4:	34) 3449		1DA00	1
				`	,	3446 (663) 3447	2DA01	1
	3392 (853) 3397						2DA00	2
	(111)			3247 (12	219) 3255		2DA10	3
c-trimer	c-tetramer	1	c-tetran	ner 2	c-p€	entamer		
3478 (790) 3468	8 3395 (0) 336	8	3384 (174	) 3350	3367 (1	41) 3341	1DA10	2
3471 (832) 3460	3394 (1807)	3368	3357 (184	7) 3350	3357 (3	396) 3331	1DA10	2
3433 (27) 3453	3365 (1951)	3361	3357 (185	5) 3350	3326 (2	2391) 3322	1DA10	2
	3308 (0) 336	1	3292 (1) 3	351	3318 (2	2516) 3320	1DA10	2
					3261 (5	57) 3319	1DA10	2
c-hexamer 1	c-hex	amer 2		c-heptamer				
3367 (136) 334	40 3354 (74	19) 3313	336	67 (324) 3342			1DA10	2
3358 (524) 333	39 3339 (0)	3312	336	52 (846) 3328			1DA10	2
3350 (467) 332			334	16 (91) 3324			1DA10	2
3314 (2725) 33	322 3296 (3)	156) 3312	333	39 (108) 3324			1DA10	2
3307 (2902) 33	,	151) 3311		03 (3258) 3323			1DA10	2
3260 (24) 3319	9 3241 (0)	3312		00 (3461) 3322			1DA10	2
			325	58 (25) 3320			1DA10	2
b,c-tetramer	b,c-pentam	ier	b,c-hex	amer	b,c-h	eptamer		
3521 (423) 3513	3 3507 (472) 3	502	3502 (542	3498	,	530) 3503	0DA11	(
2505 (620) 2511	0.460.460.5	461	2421 (552	2420	*	133) 3493	0DA11	(
3505 (630) 3510			3431 (579	*	`	196) 3443	1DA11	1
3481 (474) 3481	,		3358 (551	,	,	1385) 3353	1DA10	2
	3320 (779) 3	320	3323 (193		3260 (8	328) 3251	1DA10	2
			3292 (142	U) <i>3</i> 296	2261 /1	120) 2250	1DA10	2
2257 (601) 227	2050 (000) 2	272	2217 (070	2240	*	120) 3359	2DA11	2
3357 (691) 3370	3250 (996) 3	213	3216 (960	) 3240	31/4 (1	1265) 3201	2DA10	3

The OH-bond length  $(r_{OH})$  of the hydrogen donor in cyclic clusters is elongated from 0.974 to 0.986 Å with increasing n from 3 to 6. For the same size cluster,  $\Delta E_{\rm hb}$  falls in the following order: cyclic > branched cyclic > linear chain > branched chain. It is worth noting that the number of hydrogen bonds in the cyclic structure is always greater by one than that in the same size cluster with the chain. As seen in Figure 1, the  $\Delta \bar{E}_{hb}$ value calculated for methanol clusters does not exceed 30 kJ  $\text{mol}^{-1}$ . The  $\Delta \bar{E}_{\text{hb}}$  of 25–30 kJ  $\text{mol}^{-1}$  is very close to the largest value of hydrogen bonding for several monohydric alcohols in condensed phase estimated by quantum chemical calculations, 17,35 Monte Carlo simulation study,36 and by Raman and IR spectroscopy.<sup>37</sup> This value also corresponds to the average hydrogenbond energy of monohydric alcohols in the pure liquid deduced by thermodynamic consideration.<sup>38</sup> Several researchers pointed out that the average hydrogen-bond energy of monohydric alcohols reaches a limiting value of ca. 30 kJ mol<sup>-1</sup> even if the size of clusters keeps increasing in the system.<sup>37</sup> It is therefore likely that the upper limit value of the cooperative hydrogenbond energy for methanol is around 30 kJ mol<sup>-1</sup>.

To link the  $\nu_{OH}$  wavenumber with the hydrogen-bonding pattern of monohydric alcohols, we expand the notation used for the hydrogen-bonding pattern of water. 20 First, the OH···O hydrogen bond between donor (D) and acceptor (A) alcohols is denoted as DA. When another alcohol molecule newly participates into the DA hydrogen bond, the bond strength is changed (the so-called cooperativity of hydrogen bonding). Both D and A are capable of forming hydrogen bonds with the other methanol molecules; D can accept two protons, whereas A can donate and/or accept one proton. To consider the cooperativity of hydrogen bonding, the hydrogen-bonding pattern of monohydric alcohols is represented as  $a_D DAd_A a_A$ , where a is the number of protons accepted by D  $(a_D)$  or A  $(a_A)$ , and  $d_A$  is the number of protons donated by A. The  $d_A$  and  $a_A$  vary from 0 to 1, and  $a_D$  ranges from 0 to 2. In this method, therefore, the cooperative of hydrogen bonding is estimated by considering

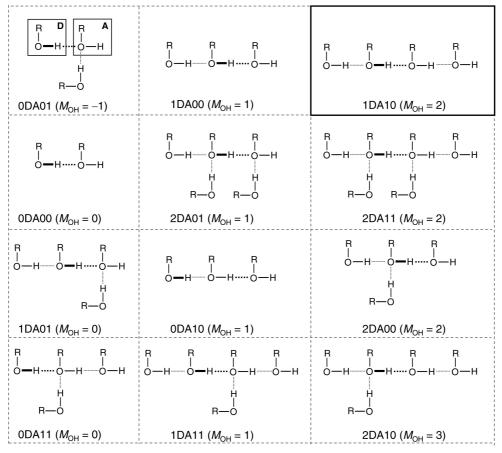


Figure 2. Schematic images of possible hydrogen-bonding patterns  $a_D DA d_A a_A$  for monohydric alcohol clusters (see text for details). The  $M_{OH}$ value is also given for each pattern. The two-coordinate methanol chain is indicated in the square with solid line.

the interactions of nearest and next-nearest neighbors. The hydrogen-bonding patterns found in the methanol clusters are listed in Table 1, together with their  $\nu_{OH}$  wavenumbers.

The DA strength changes depending upon the hydrogenbonding pattern  $a_DDAd_Aa_A$ . To classify the hydrogen-bond strength of methanol, we introduce the indicator  $M_{\rm OH} = a_{\rm D} +$  $d_A - a_A$ . The DA is strengthened with increasing  $a_D$  and/or  $d_A$ but weakened with increasing  $a_A$ . As a result, the  $M_{OH}$  value ranges from -1 to 3. Figure 2 shows schematic images for the relationship between  $M_{\rm OH}$  and the possible hydrogen-bonding patterns of monohydric alcohols. When DA is isolated, the hydrogen-bonding pattern is represented by 0DA00 with  $M_{\rm OH}$ = 0. A positive value of  $M_{\rm OH}$  indicates that the DA strength increases compared with that for the pattern with  $M_{\rm OH}=0$ . In the case where  $M_{\rm OH}$  is negative, the DA strength decreases. It is worth reminding that the 1DA01 and 0DA11 patterns also give  $M_{\rm OH}=0$ . By using the  $M_{\rm OH}$  value, one can predict that the 2DA10 pattern with  $M_{\rm OH} = 3$  causes the most strengthened DA. The  $\nu_{OH}$  band due to the methanol molecule that is not the proton donor appears at the highest wavenumber region. These bands are represented as Free in this paper.

In Figure 3, the uncoupled and coupled  $\nu_{OH}$  wavenumbers are plotted as a function of  $r_{OH}$ . Figure 3A reveals a linear relationship between the uncoupled  $\nu_{\rm OH}$  wavenumber and  $r_{\rm OH}$ . A similar tendency was previously reported.<sup>39,40</sup> As shown in Figure 3A, the  $\nu_{OH}$  wavenumbers of the hydrogen-bonding patterns with the same  $M_{\rm OH}$  are close to each other. In other words, the  $\nu_{\rm OH}$  wavenumber region of methanol is separated into six regions characterized by  $M_{OH}$ , although there is overlap. The width of the wavenumber region for each  $M_{OH}$  reflects the variety of the hydrogen-bonding geometries of the  $a_DDAd_Aa_A$ 

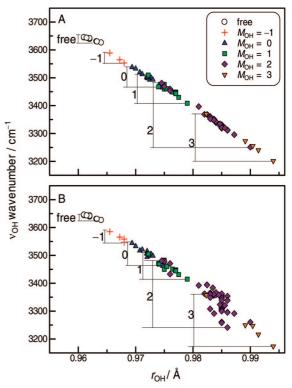
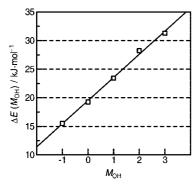


Figure 3. Relationship between the  $v_{\rm OH}$  wavenumbers and  $r_{\rm OH}$ calculated for methanol clusters  $(CH_3OH)_n$  with n = 1-7 in the uncoupled (A) and coupled (B) systems.

patterns. When the hydrogen bond is formed under constrained geometries, the  $\nu_{OH}$  wavenumber appears far from a moderate



**Figure 4.** The hydrogen-bonding energy of the hydrogen-bonding pattern with  $M_{\rm OH}$ ,  $\Delta E(M_{\rm OH})$ , plotted against the  $M_{\rm OH}$  index.

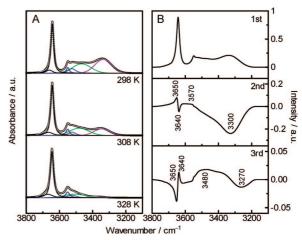
position. For example, the  $\nu_{\rm OH}$  wavenumbers (ca. 3470 cm<sup>-1</sup>) for the cyclic trimer are much higher than those (3360–3320 cm<sup>-1</sup>) for the cyclic tetramer, pentamer, and hexamer because of the strained O–H···O angle (see Table 1 and Table S1 in the Supporting Information),<sup>34</sup> even if all of the hydrogenbonding patterns are 1DA10 ( $M_{\rm OH}=2$ ) in the cyclic cluster. In Figure 3B, we found that several points are deviated from the linear correlation line, especially in the wavenumber region of  $M_{\rm OH}=2$ . The deviation may be caused by the coupling among the OH stretching modes.<sup>28,29</sup> By comparing panels A and B of Figure 3, we can conclude that the  $\nu_{\rm OH}$  wavenumber due to the  $a_{\rm D}{\rm DA}d_{\rm A}a_{\rm A}$  pattern can be characterized by  $M_{\rm OH}$  for both uncoupled and coupled systems, although the vibrational coupling changes the width of the wavenumber region.

It is very interesting to establish the correlation between  $M_{\rm OH}$  and the hydrogen-bond energy of the  $a_{\rm D}{\rm DA}d_{\rm A}a_{\rm A}$  patterns. Because this kind of information cannot be directly extracted from the calculation results, we employed the multiple linear regression (MLR) analysis<sup>31</sup> on  $\Delta E_{\rm hb}$  by assuming following equation:

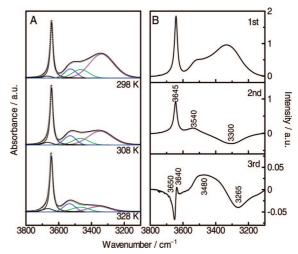
$$\Delta E_{\rm hb} = \sum_{M_{\rm OH}=-1}^{3} n_{M_{\rm OH}} \Delta E(M_{\rm OH}) \tag{2}$$

where  $n_{M_{\rm OH}}$  is the number of the hydrogen-bonding patterns with  $M_{\rm OH}$  involved in one cluster and  $\Delta E(M_{\rm OH})$  is the hydrogen-bonding energy allocated to each  $M_{\rm OH}$  value. In the eq 2, it is assumed that  $\Delta E_{\rm hb}$  of each cluster is equal to the sum of the energies of the hydrogen-bonding patterns with  $M_{\rm OH}$  involved in the cluster. The MLR analysis was carried out to determine the five variables of  $\Delta E(M_{\rm OH})$  ( $-1 < M_{\rm OH} < 3$ ) by using the calculation results for the methanol clusters illustrated in Figure 1. Note that the data for c-trimer and b,c-tetramer is not used in the MLR analysis, because their hydrogen bonds are formed under significant constrained conditions. Figure 4 shows the result of the MLR analysis, and a linear correlation between  $\Delta E(M_{\rm OH})$  and  $M_{\rm OH}$  was found. Thus, we concluded that the  $M_{\rm OH}$  index corresponds to the hydrogen-bond strength of DA.

**4.2.** Temperature Dependence of the  $\nu_{OH}$  Envelope of Methanol in a CCl<sub>4</sub> Solution. The uncoupled and coupled  $\nu_{OH}$  bands of methanol in CCl<sub>4</sub> at a concentration of 0.10 mol dm<sup>-3</sup> were measured with varying temperature from 283 to 333 K with increments of 5 K. Figure 5 depicts the uncoupled  $\nu_{OH}$  envelope of methanol in the CCl<sub>4</sub> solution at 298, 308, and 328 K, together with the curve-fitting and PCA results. Figure 6 shows the temperature dependence of the coupled  $\nu_{OH}$  envelope. The first PCA eigenvector represents the invariant component through the entire temperature region. The second and third PCA eigenvectors suggest that the  $\nu_{OH}$  envelope of methanol contains



**Figure 5.** (A) Uncoupled  $\nu_{OH}$  envelopes of methanol measured in the 0.10 mol dm<sup>-3</sup> CCl<sub>4</sub> solution at 298, 308, and 328 K and their curve fitting results. (B) PCA results for the temperature dependence of the IR spectra of methanol in CCl<sub>4</sub>.



**Figure 6.** (A) Coupled  $\nu_{OH}$  envelope of methanol measured in the 0.10 mol dm<sup>-3</sup> CCl<sub>4</sub> solution at 298, 308, and 328 K and their curve fitting results. (B) PCA results for the temperature dependence of the IR spectra of methanol in CCl<sub>4</sub>.

several independent bands, which change their relative intensities with rising temperature. By comparing Figure 5 with Figure 6, one can remark that the overlap of the coupled  $\nu_{\rm OH}$  bands is more severe than that of the uncoupled bands. According to PCA and third-derivative calculations, the uncoupled and coupled  $\nu_{\rm OH}$  envelopes were reasonably decomposed into six and five components by curve fitting, respectively. The marked difference between uncoupled and couple  $\nu_{\rm OH}$  envelopes is found in the 3600–3400 cm<sup>-1</sup> region; three bands around 3550, 3525, and 3475 cm<sup>-1</sup> were identified for the uncoupled system, whereas two bands around 3540 and 3470 cm<sup>-1</sup> were obtained for the coupled one. The uncoupled  $\nu_{\rm OH}$  band at 3550 cm<sup>-1</sup> may arise from the methanol dimer, which cannot be identified under the coupled condition.

According to Figure 3, the uncoupled and coupled  $\nu_{\rm OH}$  bands observed for methanol in CCl<sub>4</sub> can be associated with  $M_{\rm OH}$ ; Free (3670–3640 cm<sup>-1</sup>),  $M_{\rm OH}$  = 0 (3550–3520 cm<sup>-1</sup>),  $M_{\rm OH}$  = 1 (3520–3440 cm<sup>-1</sup>), and  $M_{\rm OH}$  = 2 (3360–3320 cm<sup>-1</sup>). Figure 7 shows the changes in the relative intensity of the  $\nu_{\rm OH}$  bands decomposed by the curve fitting. For both the uncoupled and coupled systems, a similar tendency was obtained. It should be noted that the relationship between the relative IR intensity and the population functions of the hydrogen-bonding patterns

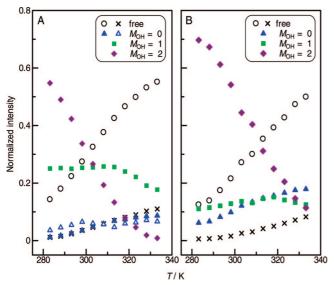
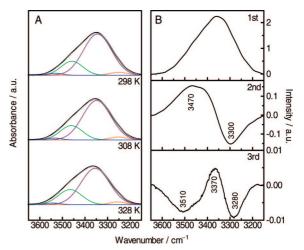


Figure 7. Temperature dependence of the normalized integral intensities for the uncoupled (A) and coupled (B)  $\nu_{OH}$  bands of methanol in the 0.10 mol dm<sup>-3</sup> CCl<sub>4</sub> solution estimated by curve fitting.

is not straightforward because of the dependence of the IR intensities on the hydrogen bond (see also Table 1). The relative intensity of the band due to  $M_{\rm OH}=2$  decreases with increasing temperature, whereas the bands due to Free and  $M_{\rm OH}=0$ increase. The result may be related to the recombination of the patterns 1DA10 (2), 2DA11 (2), 2DA00 (2), 0DA00 (0), 1DA01 (0), and 0DA11 (0). The numbers in parentheses corresponds to the  $M_{\rm OH}$  index. Several research groups have shown by simulation that methanol molecules in condensed phase prefer to form the hydrogen bond with the two-coordinate chain structures (1DA10) rather than the branched ones (2DA11 or 2DA00).41-44 In a dilute CCl<sub>4</sub> solution, the linear chain and cyclic clusters may also exist. 38,45 The linear chain structures consist of the 1DA00(1), 0DA10 (1), and 1DA10 (2) patterns, whereas the cyclic clusters exclusively contain the 1DA10 (2) pattern. For methanol in the CCl<sub>4</sub> solution, therefore, the following interpretation is also possible: the changes in relative intensity of the  $\nu_{OH}$  bands are attributed to the thermal dissociation of the linear chain and cyclic structures.

4.3. Temperature Dependence of the  $v_{OH}$  Envelope of Methanol in the Pure Liquid. Figure 8 shows the uncoupled  $\nu_{\rm OH}$  envelope for the pure methanol liquid at 298, 308, and 328 K and the PCA result. The second and third PCA eigenvectors suggest the existence of the bands around 3510, 3470, 3370, 3300, and 3280 cm<sup>-1</sup>. Therefore, the  $v_{\rm OH}$  envelope for the pure methanol liquid was decomposed into four bands at 3540, 3460, 3340, and 3250 cm<sup>-1</sup> as shown in Figure 8A. It should be emphasized that no Free  $\nu_{\rm OH}$  band of methanol was observed for the pure liquid. The band at 3540 cm<sup>-1</sup> is assignable to  $M_{\rm OH}$ = 0. Because the  $\nu_{\rm OH}$  band due to Free is not observed, the  $M_{\rm OH} = 0$  band should be directly associated with the 0DA11 pattern.46 The 0DA11 pattern is related to the existence of an end-donor methanol molecule in the pure liquid. The band at 3460 cm<sup>-1</sup> is assigned to  $M_{\rm OH} = 1$ , which is associated with the 0DA10 and 1DA11 patterns. The 1DA00 (1) and 2DA01 (1) can be neglected, because no Free band is observed. The band at 3340 cm<sup>-1</sup> is due to  $M_{\rm OH}=2$ , which arises from the 1DA10 and 2DA11 patterns (2DA00 can be ignored). The twocoordinate network, which has often been reported for the hydrogen bonding of methanol in the pure liquid,41-44 is represented by 1DA10 (2). The band at 3250 cm<sup>-1</sup> is linked to  $M_{\rm OH}=3$ , which is related to the 2DA10 pattern. The bands at



**Figure 8.** (A) Uncoupled  $\nu_{OH}$  envelopes of methanol measured in the pure liquid at 298, 308, and 328 K and their curve fitting results. (B) PCA results for the temperature dependence of IR spectra of the pure liquid methanol.

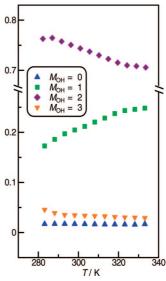


Figure 9. Temperature dependence of the normalized integral intensities for the uncoupled  $\nu_{OH}$  bands of methanol in the pure liquid estimated by curve fitting.

3540 (0) and 3250 (3) cm<sup>-1</sup> may arise from the branched networks of methanol in the pure liquid.

Figure 9 represents the thermal changes in the relative intensity of the bands due to  $M_{\rm OH}=0,\,1,\,2,\,{\rm and}\,3.$  The  $M_{\rm OH}=$ 2 band is dominant throughout the entire temperature range investigated. The relative intensity of the  $M_{\rm OH}=1$  band increases as the temperature goes up, whereas the  $M_{\rm OH}=2$ band decreases in relative intensity. On the other hand, the temperature dependences of the  $M_{\rm OH}=0$  and 3 bands are very small. Because  $M_{\rm OH}$  is correlated with the hydrogen-bond strength as shown in Figure 4, the spectral change reflects that the hydrogen-bonding patterns of methanol shift from strengthened patterns to weakened ones as the temperature rises. In the case where methanol molecules prefer to form the twocoordinate network in condensed phase as reported previously,41-44 the thermal changes in the IR spectra of the pure methanol liquid may arise from the thermal dissociation of the two-coordinate network and the increase in the branched chain structures.

#### 5. Conclusion

In the present paper, we proposed a method for analyzing the broad  $v_{OH}$  band of methanol in condensed phase. Because methanol molecules can form a percolated network through hydrogen bonding in condensed phase, the analytical model based on the limit size clusters may not be appropriate. The spectral simulation of methanol clusters revealed that the  $\nu_{\rm OH}$ wavenumbers are reasonably approximated by considering nearest and next-nearest neighbor interactions. The strength of the OH···O hydrogen bond between D and A, which is denoted as DA, is cooperatively increased or decreased by a newly formed hydrogen bond at D and/or A. To consider the cooperativity of hydrogen bond, we represented the hydrogenbonding pattern as  $a_D DAd_A a_A$ , where a is the number of protons accepted by D  $(a_D)$  or A  $(a_A)$ , and  $d_A$  is the number of protons donated by A. The  $M_{\rm OH}$  index, which is defined as  $M_{\rm OH}=a_{\rm D}$  $+ d_{\rm A} - a_{\rm A}$ , reflects the DA strength and the  $v_{\rm OH}$  wavenumber of D. As a result, the  $\nu_{OH}$  wavenumber region of methanol is classified into six regions (Free and  $M_{\rm OH} = -1, 0, 1, 2, \text{ and } 3$ ). The  $\nu_{\rm OH}$  band due to the methanol that is not the proton donor is represented as Free.

The  $\nu_{\rm OH}$  envelope of methanol in the CCl<sub>4</sub> solution and pure liquid was successfully analyzed by using the  $a_DDAd_Aa_A$ patterns and  $M_{\rm OH}$ . The temperature dependence of the  $\nu_{\rm OH}$  band for methanol in CCl<sub>4</sub> indicated that the relative intensity of the band due to  $M_{\rm OH}=2$  decreases with increasing temperature, whereas the bands due to Free and  $M_{\rm OH}=0$  increase. The result is related to the recombination of the patterns 1DA10 (2), 2DA11 (2), 2DA00 (2), 0DA00 (0), 1DA01 (0), and 0DA11 (0). For the pure liquid of methanol, the band due to  $M_{\rm OH}=2$ (1DA10 and 2DA11 patterns) is dominant throughout the entire temperature range investigated. The relative intensity of the  $M_{\rm OH}$ = 1 (0DA10 and 1DA11 patterns) band increases as the temperature goes up, whereas that of the  $M_{\rm OH}=2$  band decreases. On the other hand, the temperature dependence of the  $M_{\rm OH}=0$  (0DA11 pattern) and 3 (2DA10 pattern) bands are very small. Because  $M_{\rm OH}$  is correlated with the hydrogenbond strength, the spectral change reflects that the hydrogenbonding patterns of methanol shift from strengthened patterns to weakened ones as the temperature rises.

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**Supporting Information Available:** Structural parameters of optimized structures for methanol clusters. This material is available free of charge via the Internet at http://pubs.acs.org.

### **References and Notes**

- (1) Glew, D. N.; Rath, N. S. Can. J. Chem. 1971, 49, 837.
- (2) Van Ness, H. C.; Van Winkle, J.; Richtol, H. H.; Hollinger, H. B. J. Phys. Chem. 1967, 71, 1483.
- (3) Dixon, J. R.; George, W. O.; Hossain, Md.F.; Lewis, R.; Price, J. M. J. Chem. Soc. Faraday Trans. 1997, 93, 3611.
- (4) Pimentel, G. C.; McClellan, A. L. The Hydrogen Bond; W.H. Freeman and Co.: San Francisco, 1960; pp 67-141.
  - (5) Buck, U.; Huisken, F. Chem. Rev. 2000, 100, 3863.
- (6) Van Thiel, M.; Becker, E. D.; Pimentel, G. C. J. Chem. Phys. 1957,
  - (7) Han, S. W.; Kim, K. J. Phys. Chem. 1996, 100, 17124.
  - (8) Perchard, J. P.; Mielke, Z. Chem. Phys. 2001, 264, 221.
- (9) Coussan, S.; Loutellier, A.; Perchard, J. P.; Racine, S.; Peremans, A.; Tadjeddine, A.; Zheng, W. Q. J. Chem. Phys. 1997, 107, 6526.(10) Kristiansson, O. J. Mol. Struct. 1999, 477, 105.
- (11) Huisken, F.; Kulcke, A.; Laush, C.; Lisy, J. M. J. Chem. Phys. 1991, 95, 3924.

- (12) Huisken, F.; Kaloudis, M.; Koch, M.; Werhahn, O. J. Chem. Phys. 1996, 105, 8965.
  - (13) Buck, U.; Ettischer, I. J. Chem. Phys. 1998, 108, 33.
- (14) Häber, T.; Schmitt, U.; Suhm, M. A. Phys. Chem. Chem. Phys. 1999, 1, 5573.
- (15) Provencal, R. A.; Paul, J. B.; Roth, K.; Chapo, C.; Casaes, R. N.; Saykally, R. J.; Tschumper, G. S.; Schaefer, H. F., III J. Chem. Phys. 1999, 110, 4258.
- (16) Pribble, R. N.; Hagemeister, F. C.; Zwier, T. S. J. Chem. Phys. **1997**, 106, 2145.
- (17) Hagemeister, F. C.; Gruenloh, C. J.; Zwier, T. S. J. Phys. Chem. A **1998**, 102, 82,
  - (18) Luck, W. A. P. J. Mol. Struct. 1998, 448, 131.
  - (19) Akiyama, M.; Torii, H. Spectrochim. Acta. 2000, A56, 137.
- (20) Ohno, K.; Okimura, M.; Akai, N.; Katsumoto, Y. Phys. Chem. Chem. Phys. 2005, 7, 3005.
- (21) Frisch, M. J.; Trucks, G. W.; Schlegel, H. B.; Scuseria, G. E.; Robb, M. A.; Cheeseman, J. R.; Montgomery, J. A., Jr.; Vreven, T.; Kudin, K. N.; Burant, J. C.; Millam, J. M.; Iyengar, S. S.; Tomasi, J.; Barone, V.; Mennucci, B.; Cossi, M.; Scalmani, G.; Rega, N.; Petersson, G. A.; Nakatsuji, H.; Hada, M.; Ehara, M.; Toyota, K.; Fukuda, R.; Hasegawa, J.; Ishida, M.; Nakajima, T.; Honda, Y.; Kitao, O.; Nakai, H.; Klene, M.; Li, X.; Knox, J. E.; Hratchian, H. P.; Cross, J. B.; Bakken, V.; Adamo, C.; Jaramillo, J.; Gomperts, R.; Stratmann, R. E.; Yazyev, O.; Austin, A. J.; Cammi, R.; Pomelli, C.; Ochterski, J. W.; Ayala, P. Y.; Morokuma, K.; Voth, G. A.; Salvador, P.; Dannenberg, J. J.; Zakrzewski, V. G.; Dapprich, S.; Daniels, A. D.; Strain, M. C.; Farkas, O.; Malick, D. K.; Rabuck, A. D.; Raghavachari, K.; Foresman, J. B.; Ortiz, J. V.; Cui, Q.; Baboul, A. G.; Clifford, S.; Cioslowski, J.; Stefanov, B. B.; Liu, G.; Liashenko, A.; Piskorz, P.; Komaromi, I.; Martin, R. L.; Fox, D. J.; Keith, T.; Al-Laham, M. A.; Peng, C. Y.; Nanayakkara, A.; Challacombe, M.; Gill, P. M. W.; Johnson, B.; Chen, W.; Wong, M. W.; Gonzalez, C.; Pople, J. A. Gaussian 03; Gaussian, Inc.: Wallingford, CT, 2004.
- (22) El Firdoussi, A.; Esseffar, M.; Bouab, W.; Abboud, J.-L. M.; Mó, O.; Yáñez, M.; Ruasse, M. F. J. Phys. Chem. A 2005, 109, 9141.
  - (23) Becke, A. D. J. Chem. Phys. 1993, 98, 5648.
  - (24) Lee, C.; Yang, W.; Parr, G. R. Phys. Rev. B 1988, 37, 785.
- (25) Yoshida, H.; Ehara, A.; Matsuura, H. Chem. Phys. Lett. 2000, 325,
- (26) Matsuura, H.; Yoshida, H. In Handbook of Vibrational Spectroscopy; Chalmers, J. M., Griffiths, P. R., Eds; John Wiley & Sons Inc.: New York, 2001; Vol 3, p S4203.
- (27) Yoshida, H.; Takeda, K.; Okamura, J.; Ehara, A.; Matsuura, H. J. Phys. Chem. 2002, 106, 3580.
- (28) Hermansson, K.; Ojamäe, L. Intern. J. Quantum Chem. 1992, 42,
- (29) Hermansson, K.; Lidgren, J.; Probst, M. M. Chem. Phys. Lett. 1995, 233, 371.
- (30) The software, named SPINA, can be downloaded from the following website: http://home.hiroshima-u.ac.jp/katsumot/spina.html
- (31) Press, W. H.; Flannery, B. P.; Teukolsky, S. A.; Vetterling, W. T. Numerical Recipes in C; Cambridge University Press: Cambridge, U.K.,
  - (32) Savitzky, A.; Golay, M. J. E. Anal. Chem. 1964, 36, 1627.
- (33) Ozaki, Y.; Katsumoto, Y.; Jiang, J-H.; Liang, Y. In Spectral analysis in the NIR region in Useful and Advanced Information in the Field of Near Infrared Spectroscopy; Tsuchikawa, S., Ed.; Research Signpost: Trivandrum India, 2003.
- (34) Structural parameters of optimized structures for methanol clusters are listed in Table S1 of the Supporting Information.
  - (35) Sum, A. K.; Sandler, S. I. J. Phys. Chem. A 2000, 104, 1121.
  - (36) Stubbs, J. M.; Siepmann, J. I. J. Phys. Chem. B 2002, 106, 3968.
- (37) Palombo, F.; Sassi, P.; Paolantoni, M.; Morresi, A.; Cataliotti, R. S. J. Phys. Chem. B 2006, 110, 18017.
- (38) Benson, S. W. J. Am. Chem. Soc. 1996, 118, 10645.
- (39) Kurita, E.; Matsuura, H.; Ohno, K. Spectrochim. Acta 2004, A60, 3013.
  - (40) Badger, R. M. J. Chem. Phys. 1934, 2, 128.
  - (41) Jorgensen, W. L. J. Am. Chem. Soc. 1981, 103, 341
  - (42) Matsumoto, M.; Gubbins, K. E. J. Chem. Phys. 1990, 93, 1981.
- (43) Kosztolányi, T.; Bakó, I.; Pálinkás, G. J. Chem. Phys. 2003, 118, 4546.
- (44) Pagliai, M.; Cardini, G.; Righini, R.; Schettino, U. J. Chem. Phys. 2003, 119, 6655
  - (45) Sarker, S.; Joarder, R. N. J. Chem. Phys. 1993, 99, 2032.
- (46) The 0DA00 and 1DA01 patterns should coexist with the Free band. See also Figure 2.

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