See discussions, stats, and author profiles for this publication at: https://www.researchgate.net/publication/236086331

Phosphorus As a Simultaneous Electron-Pair Acceptor in Intermolecular P···N Pnicogen Bonds and Electron-Pair Donor to Lewis Acids

ARTICLE *in* THE JOURNAL OF PHYSICAL CHEMISTRY A · MARCH 2013

Impact Factor: 2.69 · DOI: 10.1021/jp401480y · Source: PubMed

CITATIONS

33

READS

91

4 AUTHORS, INCLUDING:



Ibon Alkorta

Spanish National Research Council

680 PUBLICATIONS 12,430 CITATIONS

SEE PROFILE



Goar Sánchez

University College Dublin

69 PUBLICATIONS **905** CITATIONS

SEE PROFILE



José Elguero

Spanish National Research Council

1,502 PUBLICATIONS 22,206 CITATIONS

SEE PROFILE

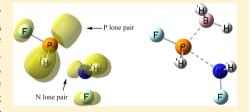


Phosphorus As a Simultaneous Electron-Pair Acceptor in Intermolecular P···N Pnicogen Bonds and Electron-Pair Donor to Lewis Acids

Janet E. Del Bene,*,† Ibon Alkorta,*,‡ Goar Sánchez-Sanz,§ and José Elguero‡

Supporting Information

ABSTRACT: Ab initio MP2/aug'-cc-pVTZ calculations have been performed to investigate the structures and energies of binary complexes LA:PH₂F and LA:PH₃ and of ternary complexes LA:H₂FP:NFH₂ and LA:H₃P:NH₃ in which the pnicogen-bonded P atom also acts as an electron-pair donor to a Lewis acid (LA), for LA = BH₃, NCH, ClH, FH, FCl, and HLi. Hydrogen bonds, halogen bonds, and dative covalent bonds are found at P in some cases, depending on the nature of the Lewis acid. HLi forms a lithium bond with P only in the binary complex HLi:PH₃. The binding energies of ternary complexes exhibit a classical synergistic



effect, although the computed cooperativity may be overestimated due to neglect of the interaction of the Lewis acid with NH₂F or NH₃ in some cases. The hydrogen-bonding Lewis acids appear to have little effect on the strength of the P···N bond, while the remaining Lewis acids strengthen the pnicogen bond. ³¹P absolute chemical shieldings increase in LA:H₂FP:NFH₂ complexes relative to the corresponding LA:PH₂F complexes as the positive charge on P decreases, while chemical shieldings decrease in LA:H₃P:NH₃ relative to the corresponding LA:PH₃ complexes as the positive charge increases. Absolute values of ^{1p}J(P-N) spin-spin coupling constants in complexes LA:H₂FP:NFH₂ decrease as the P-N distance decreases. It appears that this behavior is associated with the presence of a second intermolecular interaction, whether electron-donation by P or hydrogen bond formation at P-F.

■ INTRODUCTION

The pnicogen bond is a Lewis acid-Lewis base interaction in which a pnicogen atom (N, P, or As) acts as the Lewis acid. Although the pnicogen bond has been recognized for several decades, 1-5 it was not among those at the forefront of studies of intermolecular interactions until the landmark paper by Hey-Hawking et al. appeared in 2011. Since then, the pnicogen bond has received a great deal of attention in the literature.⁷

The pnicogen bond provides another example of the σ -hole concept proposed by Politzer and Murray.⁵ This term refers to the electron-deficient outer lobe of a p orbital, which can act as an electron-pair acceptor from a Lewis base. As with other types of intermolecular interactions, the pnicogen bond is stabilized in part by electrostatic and polarization contributions. However, the present authors and Scheiner in their recent papers have demonstrated that charge-transfer from the lone pair of an atom (Y) of the base to the antibonding σ^* P-X orbital of the acid, with X-P···Y approaching a linear alignment, is a very important component in the stabilization of complexes with pnicogen bonds. The pnicogen bond and its relationship to other types of intermolecular interactions has been discussed in recent review articles.²⁹⁻³¹

In a recent paper,³² we examined the effect of the formation of F-H···F hydrogen bonds at P-F and at N-F on the strength of P...N pnicogen bonds in complexes nFH: $(H_2FP:NFH_2)$, for n = 1-2, and a selected complex with n = 3.

We observed that the ELF representation of these complexes clearly indicates that the lone pair on the nitrogen is directed toward the P...N region, while the lone pair on phosphorus is not, as illustrated in Figure 1 for the parent complex H₂FP:NFH₂ and

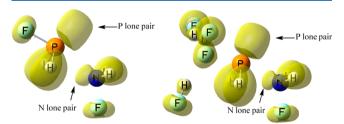


Figure 1. ELF representations at the 0.8 isosurface for H₂FP:NFH₂ and the same complex hydrogen bonded to three FH molecules at P-F, showing the P lone pairs and the N lone pairs in the P···N basins.

the complex having three FH molecules hydrogen-bonded at P-F. In that study, electrons in the intermolecular P-N region were assigned to the P-N basin only in complexes in which hydrogen bonding with FH occurred at P-F. When hydrogen bonding

Received: February 10, 2013 Revised: March 8, 2013

[†]Department of Chemistry, Youngstown State University, Youngstown, Ohio 44555, United States

[‡]Instituto de Química Médica (C.S.I.C.), Juan de la Cierva, 3, E-28006 Madrid, Spain

[§]Institute of Organic Chemistry and Biochemistry, Gilead Sciences Research Center & IOCB, Academy of Sciences of the Czech Republic, Flemingovo nám. 2, 166 10 Praha 6, Czech Republic

occurred at N-F, electrons in the P-N region were described as nitrogen lone pairs.

The existence of a diffuse and relatively exposed lone pair of electrons at P led us to ask to what extent the P atom could act as an electron-pair donor (a base) to a Lewis acid, while at the same time functioning as an electron-pair acceptor (an acid) for the P...N pnicogen bond. To answer this question, we have investigated two series of complexes LA:H2FP:NFH2 and LA:H₃P:NH₃, with LA representing the Lewis acids BH₃, NCH, ClH, FH, FCl, and HLi. In the present article, we present the structures of these complexes, as well as the energies for the reactions that form P...N and P...LA bonds. We investigate the ability of phosphorus to act as a Lewis electron-pair donor in various types of intermolecular interactions, including hydrogen bonds, halogen bonds, and lithium bonds as well as dative covalent bonds. We examine cooperative effects for ternary complexes LA:H₂FP:NFH₂ and LA:H₃P:NH₃ due to the presence of P···N and P···LA bonds and estimate the bond energies. We also investigate 31P and 15N absolute chemical shieldings and indirect P-N spin-spin coupling constants ^{1p}J(P-N) across the pnicogen bonds. In this article, we report the results of this investigation.

COMPUTATIONAL METHODS

The structures of isolated monomers, binary complexes LA:PH₂F and LA:PH₃, and ternary complexes LA:H₂FP:NFH₂ and LA:H₃P:NH₃ for the Lewis acids LA = BH₃, NCH, ClH, FH, FCl, and HLi, were optimized at second-order Møller–Plesset perturbation theory (MP2)^{33–36} with the aug'-cc-pVTZ basis set.³⁷ This basis set is derived from the Dunning aug-cc-pVTZ basis set^{38,39} by removing diffuse functions from H atoms. Frequencies were computed to establish that these optimized structures correspond to equilibrium structures on their potential surfaces. The binary complex HLi:PH₂F failed to optimize to a structure with a P···Li bond, undergoing an atom transfer reaction instead. This complex was then optimized under the constraint that P···Li—H must be linear. All optimization and frequency calculations were performed using the Gaussian 09 program.⁴⁰

The Natural Bond Orbital (NBO) method⁴¹ has been used to obtain atomic charges using the NBO-5 program⁴² within the Gamess program.⁴³ Absolute chemical shieldings have been calculated at MP2/aug'-cc-pVTZ using the GIAO approximation. 44 Coupling constants were evaluated using the equationof-motion coupled cluster singles and doubles (EOM-CCSD) method in the CI (configuration interaction)-like approximation, 45,46 with all electrons correlated. For these calculations, the Ahlrichs⁴⁷ qzp basis set was placed on ¹³C, ¹⁵N, and ¹⁹F, and the qz2p basis set on ³¹P, ³⁵Cl, and hydrogen-bonded ¹H atoms of Lewis acids. A previously developed basis set with the same number of basis functions as the qzp basis was placed on ⁷Li and ¹¹B. ⁴⁸ The Dunning cc-pVDZ basis set was placed on all other H atoms. Only ^{1p} J(P-N) coupling constants are reported in this article. The EOM-CCSD calculations were performed using ACES II⁴⁹ on the IBM Cluster 1350 (Glenn) at the Ohio Supercomputer Center.

■ RESULTS AND DISCUSSION

The energies and structures of the binary complexes LA:PFH₂ and LA:PH₃ and the ternary complexes LA:H₂FP:NFH₂ and LA:H₃P:NH₃ are reported in Tables S1 and S2, respectively, of the Supporting Information. The structures of the ternary

complexes LA:H₂FP:NFH₂ and LA:H₃P:NH₃ have C_s symmetry and are reported in Table 1 and illustrated in Figure 2.

Table 1. Distances (R, Å), Angles (\angle, deg) , and Reaction Energies for the P-N $[\Delta E(P-N)]$ and P-LA $[\Delta E(P-LA), \text{kJ mol}^{-1}]$ Reactions which Form the Ternary Complexes LA:H₂FP:NFH₂ and LA:H₃P:NH₃

LA:H ₂ FP:NFH ₂							
complex	R(P-N)	$\Delta E(P-N)$	R(P-LA)	_	$\Delta E(P-LA)$		
H ₂ FP:NFH ₂	2.524	-26.67					
$LA = BH_3$	2.413	-36.82	1.920^{a}	83 ^a	-144.75		
NCH	2.568	-42.55	3.564 ^b	75 ^b	-24.63		
ClH	2.541	-42.76	3.580^{c}	13 ^c	-28.52		
FH	2.503	-46.33	3.098^{d}	17^d	-38.14		
FCl	2.274	-58.96	4.019^{e}	1^e	-103.43		
HLi	2.378	-85.49 ^f	3.489 ^g	43 ^g	-92.22^{f}		
		LA:H ₃ P:N	$1H_3$				
complex	R(P-N)	$\Delta E(P-N)$	R(P-LA)	_	$\Delta E(\text{P-LA})$		
H ₃ P:NH ₃	3.292	-7.82					
$LA = BH_3$	3.098	-21.52	1.942 ^a	85 ^a	-120.89		
NCH	3.332	-18.39	3.730^{b}	16^{b}	-21.98		
ClH	3.192	-18.00	3.683 ^c	4 ^c	-25.03		
FH	3.194	-20.49	3.185^{d}	8^d	-34.06		
FCl	2.888	-35.01	4.035^{e}	0^e	-78.38		
HLi	4.325	-71.09	2.932^{g}	62^g	-103.82		

"The P-B distance and ∠N-P-B. ^bThe P-C distance and ∠H-C···P. ^cThe P-Cl distance and ∠H-Cl···P. ^dThe P-F distance and ∠H-F···P. ^eThe P-F distance and ∠Cl-F···P. ^fEnergies derived from a constrained optimized HLi:PFH₂ structure with H-Li-P linear. ^gThe P-H distance and ∠Li-H···P.

Complexes LA:PH₃ have $C_{3\nu}$ symmetry, with the lone pair of electrons of the sp³ hybridized P directed toward the acidic site of the Lewis acid. The complexes LA:PH₂F have reduced C_s symmetry due to the substitution of F for H but have structures that are similar to the corresponding LA:PH₃ complexes, as evident from Table 2. The P–N and P–LA reaction energies are given in Tables 1 and 2 as the energies for the following reactions, using complexes involving H₂FP:NFH₂ and PH₂F as examples. For ternary complexes:

$$\Delta E(P-N) = E(LA:H_2FP:NFH_2) - E(LA:PH_2F) - E(NH_2F)$$
(1)

$$\Delta E(P-LA) = E(LA:H_2FP:NFH_2) - E(H_2FP:NFH_2)$$
$$- E(LA)$$
(2)

For binary complexes:

$$\Delta E(P-N) = E(H_2FP:NFH_2) - E(PH_2F) - E(NH_2F)$$
(3)

$$\Delta E(P-LA) = E(LA:PH_2F) - E(PH_2F) - E(LA)$$
 (4)

It is important to note that eqs 1 and 2 for the formation of a ternary complex from a binary complex and an isolated monomer implicitly assume that the binding energy of the binary complex is unchanged in the ternary complex. Consequences of this assumption will be discussed below.

Structures of Complexes with Hydrogen Bonding Lewis Acids. X—H···P Hydrogen Bonds. Of the six Lewis acids considered in this study, three are possible proton donors for

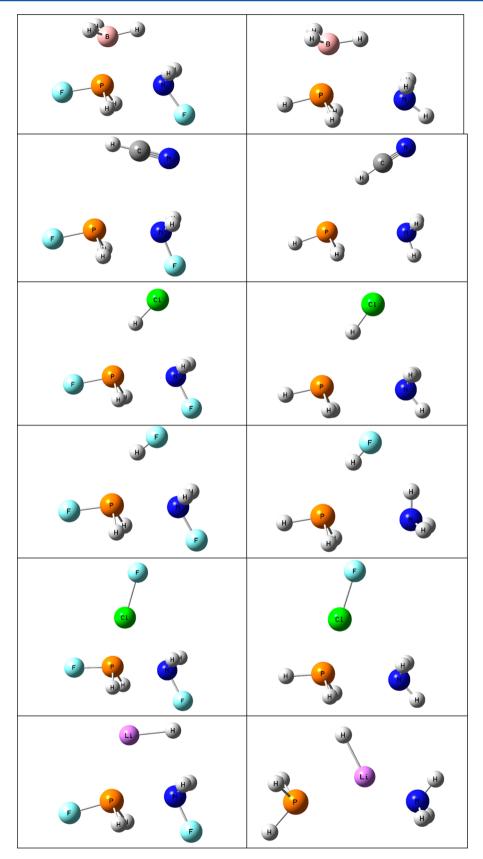


Figure 2. Complexes LA:H₂FP:NFH₂ and LA:H₃P:NH₃.

hydrogen bond formation: NCH, ClH, and FH. An ideal $X-H\cdots Y$ hydrogen bond is one in which these three atoms are arranged linearly, as measured by the angle H-X-Y, which has

a value of 0° when the hydrogen bond is linear. Figure 2 and the structural data of Table 1 suggest that the complex NCH:H₂FP:NFH₂ is not hydrogen-bonded at all since the

Table 2. Distances (R, Å), Angles (\angle, deg) , and P-LA Reaction Energies $[\Delta E(\text{P-LA}), \text{kJ mol}^{-1}]$ for the Formation of the Binary Complexes LA:PH₂F and LA:PH₃

LA:PH ₂ F						
complex	R(P-LA)	_	$\Delta E(P-LA)$			
$LA = BH_3$	1.865 ^a		-134.55			
NCH	3.936 ^b	3^b	-8.77			
ClH	3.836 ^c	3^c	-12.33			
FH	3.284^{d}	3^d	-18.48			
FCl	3.942^{e}	3^e	-71.11			
HLi	4.298^{f}	0^f	-33.40^{g}			
LA:PH ₃ ^h						
complex	R(P-LA	r)	$\Delta E(P-LA)$			
$LA = BH_3$	1.936		-107.18			
NCH	3.881		-11.41			
ClH	3.800		-14.86			
FH	3.271 -21.39					
FCl	4.034		-51.19			
HLi	4.270	-40.54				

^aThe P−B distance. ^bThe P−C distance and \angle H−C···P. ^cThe P−Cl distance and \angle H−Cl···P. ^dThe P−F distance and \angle H−F···P. ^eThe P−F distance and \angle Cl−F···P. ^fThe P−H distance and \angle Li−H···P. ^gEnergies derived from a constrained optimized HLi:PFH₂ structure with H−Li−P linear. ^hAll complexes have C_{3y} symmetry.

H–C···P angle is 75°. Rather, NCH appears to be almost parallel to the P···N bond. Moreover, both ClH and FH form distorted X–H···P hydrogen bonds with $H_2FP:NFH_2$, as indicate by the H–Cl–P and H–F–P angles of 13 and 17°, respectively. The nonlinearity of these bonds may be attributed to secondary interactions involving Cl and F with the positively charged H atoms of NH_2F . This interaction is particularly strong for NCH and is the primary interaction stabilizing this complex.

In contrast to the complexes with H₂FP:NFH₂, all three possible hydrogen-bonding Lewis acids form hydrogen bonds with H₃P:NH₃. This bond is distorted by 16° when NCH is the acid, a result of the interaction of N with the H atoms of NH₃. The deviation of hydrogen bonds from linearity by 4 and 8° for complexes with ClH and FH, respectively, indicates a weakening of the interaction of Cl and F with the H atoms of NH₃.

Intermolecular hydrogen bond distances in binary complexes with PH₃ are shorter than corresponding distances with PH₂F, a reflection of the electron-withdrawing effect of F. These distances in ternary complexes are shorter than those in the corresponding binary complexes, while those in the ternary complexes formed with H₂FP:NFH₂ are shorter than those in complexes with H₃P:NH₃. There is also an interesting structural difference between binary and ternary complexes. In all of the binary complexes, P acts as the electron-pair donor through an sp³ hybridized orbital. The P atom is four-coordinated, that is, the geometry around P is tetrahedral, with one intermolecular bond. The hydrogen-bonded LA:H₂FP:NFH₂ and LA:H₃P:NH₃ complexes may be viewed as involving a five-coordinated P, that is, they have a distorted trigonal bipyramidal geometry, with two intermolecular bonds.

P–*N Pnicogen Bonds*. Just as the reaction energies for the ternary complexes, which result in the formation of a bond between P and the Lewis acid, increase in going from the binary to the corresponding ternary complexes, so too do the reaction energies for NCH, ClH, and FH interacting at P lead to greater

P-N reaction energies in the ternary complexes relative to the corresponding binary complexes H₂FP:NFH₂ and H₃P:NH₃. However, the differences among these interaction energies in each series of ternary complexes are small.

What is interesting and puzzling at the same time is the variation of the P–N distances in these complexes. If the reaction energies are a measure of the strength of the P···N bond, then it would be expected that the strengthening of this bond in the ternary complexes should lead to a shortening of P–N distances, but this is not necessarily the case. For example, the P–N distance of 2.524 Å in the parent complexe $H_2FP:NFH_2$ lengthens to 2.568 and 2.541 Å in the complexes with NCH and ClH, but shortens to 2.503 Å in the complex with FH. Similarly, the P–N distance of 3.292 Å in $H_3P:NH_3$ increases to 3.332 Å in the complex with NCH, but decreases to 3.192 and 3.194 Å in the complexes with ClH and FH, respectively. These structural curiosities will be discussed below following a discussion of the reaction energies and their relationship to the strength of the P···N bond.

Structures of Complexes with a Halogen Bonding Lewis Acid. P···Cl-F Halogen Bonds. A P···Cl-F halogen bond may potentially form in binary complexes FCl:PH₂F and FCl:PH₃, and in ternary complexes FCl:H₂FP:NFH₂ and FCl:H₃P:NH₃. In the binary complexes FCl:PH₂F and FCl:PH₃, F-P distances are 3.942 and 4.034 Å, and the F-Cl distances are 1.903 and 1.852 Å, respectively, a rather significant elongation relative to the F-Cl distance of 1.638 Å in isolated FCl. The elongation of the F-Cl bond suggests that the P-Cl halogen bonds are quite strong. Moreover, the binding energies of the halogen bonds in the binary complexes FCl:PH2F and FCl:PH₃ are 71.1 and 51.2 kJ mol⁻¹, respectively, significantly stronger than the halogen bonds in the complexes $FCl:NH_2F$ and FCl:NH₃, which are 8.3 and 11.8 kJ mol⁻¹. The F-Cl distances in the nitrogen complexes are also much shorter at 1.688 and 1.713 Å, respectively. St

It is also not surprising to see that F–Cl distances elongate further to 1.930 and 1.898 Å, respectively, in the ternary complexes FCl:H₂FP:NFH₂ and FCl:H₃P:NH₃. These distance changes result in P–Cl distances of 2.089 and 2.137 Å, respectively, which are similar to the covalent P–Cl bond distances in PFClH and PH₂Cl of 2.057 and 2.076 Å, respectively, computed at the same level of theory. Thus, in both ternary complexes, but particularly in FCl:H₂FP:NFH₂, formation of a halogen bond results essentially in Cl transfer to P. A similar situation was found in binary FCl:CNH and some ternary FCl:CNH:Z complexes for Z an electron-donating substituent.⁵¹

P···N Pnicogen Bonds. The formation of a P–Cl bond with significant covalent character has a dramatic effect on the P···N bond. Thus, the P–N distance of 2.524 Å in $H_2FP:NFH_2$ decreases to 2.274 Å in $FCl:H_2FP:NFH_2$. This shortening is reminiscent of the effect of the formation of three F–H···F hydrogen bonds at P–F in $3FH:H_2FP:NFH_2$, a complex that has an even shorter P–N distance of 2.143 Å.³²

Structures of Complexes with a Lithium Bonding Lewis Acid. *P…Li—H Lithium Bonds*. HLi does not form a stable binary complex with an H–Li…P lithium bond with PH₂F since an atom-transfer reaction occurs. An optimized structure with H–Li…P constrained to be linear has an H–P distance of 4.298 Å. HLi does form a stable binary complex with PH₃ with an H–P distance of 4.270 Å.

The ternary complexes of HLi with H₂FP:NFH₂ and H₃P:NH₃ are equilibrium structures, but neither HLi:H₂FP:NFH₂ nor HLi:H₃P:NH₃ has an H–Li···P lithium bond, as can be seen from

Figure 2 and the data of Table 1. The Li–H···P angles for a lithium bond should also be near 0° but have values of 43 and 62° in these two complexes, respectively. Interaction of HLi with $H_2FP:NFH_2$ leads to a complex with a structure similar to that of the complex NCH:H $_2FP:NFH_2$, with HLi nearly parallel to the P···N bond. Thus, it would appear that there is a stabilizing electrostatic interaction between the hydridic H of HLi and the very positively charged H atoms of NH_2F . Interaction of HLi with $H_3P:NH_3$ leads to a complex in which HLi essentially inserts into the P···N bond and appears to interact more strongly with N than with P.

 $P\cdots N$ Bonds. The P-N distance in HLi:H₂FP:NFH₂ is short at 2.378 Å. In contrast, the P-N distance in HLi:H₃P:NH₃ is very long at 4.325 Å since the insertion of HLi essentially destroys the P-N bond.

Interaction with a Covalent Bonding Lewis Acid. P-B Bonds. Since BH₃ is an electron-deficient molecule, it may be anticipated that electron-pair donation by P results in a dative P-B covalent bond. This can be seen by comparing the computed P-B distances in the molecules H_2P-BH_2 (1.865 Å) and FHP-BFH (1.927 and 1.936 Å in the Z and E forms, respectively) with the distances in the binary complexes. The P-B distances in BH₃:PH₂F and BH₃:PH₃ are similar at 1.865 and 1.936 Å, respectively, with the shorter distance found in the complex with PH₂F. In contrast to the usual trend of decreasing distance in going from the binary to the ternary complexes, the B-P distances increase to 1.920 and 1.942 Å, respectively, in the complexes BH₃:H₂FP:NFH₂ and BH₃:H₃P:NH₃.

P···N Bonds. The formation of the P–B bond shortens the P–N distances in the ternary complexes. Thus, the P–N distances in the parent complexes H₂FP:NFH₂ and H₃P:NH₃ of 2.524 and 3.292 Å, respectively, decrease in BH₃:H₂FP:NFH₂ and BH₃:H₃P:NH₃ to 2.413 and 3.098 Å, respectively.

Energies. The energies reported in Table 1 are the reaction energies for the formation of ternary complexes from the corresponding binary complex and monomer. Thus, these are not the bond energies for either the P···N or P···LA bonds in the ternary complexes. Rather, the computed values are interdependent. Their interdependence can be derived and easily demonstrated by computing the change in the P–N and P–LA reaction energies in the ternary complexes relative to the corresponding binary complexes. Using H₂PF:NFH₂ and PH₂F as an example

$$\delta \Delta E(P-N) = \Delta E[(P-N), LA:H_2PF:NFH_2]$$
$$-\Delta E[(P-N), H_2PF:NFH_2]$$
(5)

$$\delta \Delta E(P-LA) = \Delta E[(P-LA), LA:H_2PF:NFH_2]$$
$$-\Delta E[(P-LA), LA:PFH_2]$$
(6)

For a given Lewis acid, $\delta\Delta E(P-N) = \delta\Delta E(P-LA)$. Thus, neither the reaction energies nor the change in the reaction energies for ternary complexes relative to the corresponding binary complexes provide information about the strengths of the P···N or P···LA bonds in these ternary complexes. What other approaches might provide some insight into the energetics of these complexes?

Cooperativity. As evident from Table 1, the formation of a ternary complex from the corresponding binary complex and monomer is an exothermic process. The classical cooperative effect, $\Delta E_{i\nu}$ computed as

$$\Delta E_{\rm i} = \Delta E(\text{ternary}) - \sum \Delta E(\text{binary})$$
 (7)

is always negative, as evident from Table 3. Thus, these data suggest that the formation of these two bonds has a synergistic effect.

Table 3. Classical (ΔE_i) Cooperativity (kJ mol⁻¹) for All Ternary Complexes and Estimated P···N $[\Delta E'(\text{P···N})]$ and P···LA $[\Delta E'(\text{P···LA}), \text{ kJ mol}^{-1}]$ Bond Energies for Complexes LA:H₂FP:NFH₂

LA:H ₂ FP:NFH ₂	$\Delta E_{\rm i}^{~a}$	$\Delta E'(P\cdots N)^b$	$\Delta E'(P\cdots LA)^c$		
$LA = BH_3$	-10.16	-31.9	-129.3		
NCH	-15.88	-23.8	-11.6		
ClH	-16.09	-24.9	-14.1		
FH	-19.67	-26.6	-18.5		
FCl	-32.29	-43.1	-54.7		
HLi	-58.88^{d}	-34.3	-25.8		
LA:H ₃ P:NH ₃		Δ	$E_{\rm i}$		
$LA = BH_3$		-13.70			
NCH		-10.57			
ClH		-10.18			
FH		-12.67			
FCl		-27.19			
HLi		-63	.27		
ПLI		-03	.4/		

^aComputed from eq 7. ^bEquation 8 gives a P···N bond energy of −25.6 kJ mol⁻¹ for H₂FP:NFH₂, which is about 1 kJ mol⁻¹ less than the energy of −26.7 kJ mol⁻¹ computed from eq 3. ^cComputed from eq 9. ^dBased on a constrained optimized HLi:PH₂F complex.

However, the nonadditivity may not be as large as computed since this calculation ignores any interaction of the Lewis acid with the $\mathrm{NH_2F}$ or $\mathrm{NH_3}$ molecules. These interactions appear to be significant in complexes of the Lewis acids NCH, ClH, FH, and HLi with $\mathrm{H_2FP:NFH_2}$, and even with $\mathrm{H_3P:NH_3}$, but to a less extent, as noted above.

Estimating P···N and P···LA Bond Energies in Complexes LA:H₂FP:NFH₂. Although we have computed second-order interaction energies employing the many-body interaction energy model of Stillinger et al.,⁵² in an attempt to assess the strength of all bonds (P···N, P···LA, and N···LA), this analysis is appropriate only for weak interactions⁵³ and not strong ones such as those involving the Lewis acids BH₃, FCl, and HLi. In addition, this analysis indicates that in each series the strongest P···N bond is found in the parent complexes H₂FP:NFH₂ and H₃P:NH₃, even though the P–N distance can be significantly shorter in complexes containing the Lewis acid. This result is contrary to distance—energy relationships in general.

In order to obtain more realistic P···N bond energies, we have estimated these energies for complexes LA:H₂FP:NFH₂ from distances and P···N energies of complexes nFH:H₂FP:NFH₂.³² These complexes have F–P···N–F linear as do the LA:H₂FP:NFH₂ complexes and are appropriate for comparison purposes. Figure 3 presents the plot of $\Delta E(P \cdot \cdot \cdot N)$ versus the P–N distance [R(P - N)] for these complexes. The equation of the trendline is

$$\Delta E'(P \cdot \cdot \cdot N) = -97.75R(P - N)^2 + 538.7R(P - N) - 762.6$$

$$n = 10, R^2 = 0.980$$
(8)

The P···N bond energies in complexes LA: H_2FP : NFH_2 estimated from this equation are given in Table 3. These energies are significantly less than the reaction energies computed from eq 1, as they should be. It is important to note the significant reduction in the P···N bond energies in complexes with the

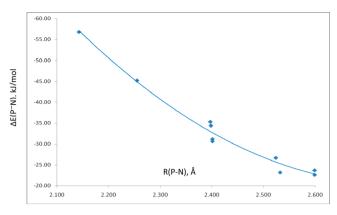


Figure 3. $\Delta E(P \dots N)$ versus R(P-N) for complexes nFH:H₂FP:NFH₂. Data taken from ref 32.

potential hydrogen-bonding Lewis acids, NCH, ClH, and FH. As noted above, NCH does not form a hydrogen bond with P, and both ClH and FH form very nonlinear hydrogen bonds due to interaction with NH₂F. Of these three acids, only FH strengthens the P···N bond relative to the parent, but by only 1 kJ mol⁻¹.

We have also estimated the strength of the bond between P and the Lewis acid using the equation

$$\Delta E'(\text{P···LA}) = \Delta E(\text{ternary}) - \Delta E_i - \Delta E'(\text{P···N})$$
 (9)

where $\Delta E(\text{ternary})$ is the total binding energy of the ternary complex relative to the corresponding isolated monomers, ΔE_i is the cooperativity, and $\Delta E'(P \cdots N)$ is the P-N bond energy estimated from eq 8. The $\Delta E'(P\cdots LA)$ values, which are also reported in Table 3, are overestimated since interaction between LA and the NH₂F molecule has been neglected. Nevertheless, it is interesting to note that for the hydrogenbonding Lewis acids, the order of interaction energies is NCH < ClH < FH, even though the interaction of NCH with P does not involve hydrogen-bond formation, and the hydrogen bonds in the complexes with ClH and FH are nonlinear due to interaction with NH₂F. The strongest interaction occurs with BH3 when a covalent bond forms between P and B. Next in order of bond energies is that between P and FCl, in which case partial Cl transfer occurs to form a P-Cl bond with significant covalent character. The interaction energy of HLi with P is also most probably overestimated, as implied by the structure of this complex.

Because complexes $LA:H_3P:NH_3$ have $H-P\cdots N-H$ linear and much longer P-N distances than found in Figure 3, eq 8 cannot be used to estimate $P\cdots N$ bond energies for these complexes. Unfortunately, we do not have other data that would suffice for this purpose.

Absolute Chemical Shieldings. The absolute chemical shieldings of ³¹P and ¹⁵N atoms are reported in Table 4. The presence or absence of a fluorine atom in the complexes determines the regions in which these NMR signals appear.

All ³¹P shieldings for the LA:H₂FP:NFH₂ ternary complexes are greater than shieldings for the LA:PH₂F binary complexes. In contrast, shieldings for ternary complexes LA:H₃P:NH₃ are reduced relative to the corresponding LA:PH₃ shieldings. These trends are consistent with the NBO charges on P in binary and ternary complexes. An increase in the positive charge on P leads to decreased shielding, while a decrease in the positive charge on P leads to an increased shielding. A linear correlation is found between the change in the ³¹P chemical shielding and the change in the positive charge on P in going from LA:PH₃ to LA:H₃P:NH₃,

Table 4. ³¹P and ¹⁵N Absolute Chemical Shieldings (ppm)

	LA:PH ₂ F	::PH ₂ F LA:H ₂ FP:NFH ₂		
	³¹ P	³¹ P	¹⁵ N	
parent		339.7	79.9	
$LA = BH_3$	285.8	330.8	84.1	
NCH	276.4	339.0	76.8	
ClH	278.5	353.1	66.3	
FH	278.7	349.0	80.7	
FCl	313.7	381.4	75.8	
	LA:PH ₃	LA:H ₃ P:NH ₃		
	³¹ P	³¹ P	¹⁵ N	
parent		623.9	271.6	
$LA = BH_3$	500.1	492.2	266.0	
NCH	625.4	614.5	267.1	
ClH	621.1	607.1	267.2	
FH	615.1	602.5	270.1	
FCl	515.3	466.0	250.3	

as illustrated in Figure 4. Although the shielding of ³¹P increases as the positive charge on P decreases in going from the binary

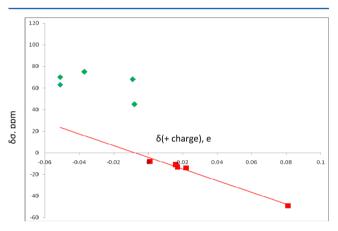


Figure 4. ³¹P chemical shielding in ternary complexes LA:H₂FP:NFH₂ and LA:H₃P:NH₃ minus that in the corresponding binary complexes LA:PH₂F and LA:PH₃ ($\delta\sigma$) versus the positive charge on P in the corresponding ternary complexes minus that in the corresponding binary complexes [δ (+ charge)]. •, LA:H₂FP:NFH₂; ■, LA:H₃P:NH₃ The correlation coefficient R^2 of the trendline for LA:H₃P:NH₃ complexes is 0.982.

complex LA:PH₂F to the corresponding ternary complex LA:H₂FP:NFH₂, Figure 4 indicates that these two variables are not well correlated for this series. Changes in ¹⁵N chemical shieldings do not correlate with changes in the negative charges on N in going from the binary to the corresponding ternary complexes.

Spin–Spin Coupling Constants $^{1p}J(P-N)$. Values of $^{1p}J(P-N)$ and its components for the binary parent complexes $H_2FP:NFH_2$ and $H_3P:NH_3$, the ternary complexes LA: $H_3P:NH_3$, and selected complexes LA: $H_2FP:NFH_2$, are reported in Table 5. These data indicate that the FC term is an excellent approximation to $^{1p}J(P-N)$ for these complexes. Therefore, only the FC terms have been computed for the remaining complexes LA: $H_2FP:NFH_2$. It is the FC terms that will be compared below.

Our previous studies of $^{1p}J(P-P)$ for complexes $(PH_2X)_2$ and $(PFHX)_2$ and $^{1p}J(P-N)$ for complexes $H_2XP:NXH_2$ with a variety of substituents X indicate that both of these coupling constants increase with decreasing P-P or P-N distance. This is a general relationship for two-bond coupling constants across

Table 5. ${}^{1p}J(P-N)$ and Its Components (Hz) and the P-N Distance $[R(P-N), (\mathring{A})]$ for Complexes LA:H₂FP:NFH₂ and LA:H₃P:NH₃^a

LA:H ₂ FP:NFH ₂ complexes						
	R(P-N)	PSO	DSO	FC	SD	¹ <i>pJ</i> (P−N)
parent	2.524	-0.1	-0.1	-113.5	0.0	-113.6
$LA = BH_3$	2.413	-0.2	-0.1	-42.7	-0.1	-43.1
NCH	2.568			-67.6		
ClH	2.541			-71.1		
FH	2.503	-0.1	-0.1	-79.9	0.1	-80.1
FCl	2.274			-1.3		
HLi	2.378			-44.4		

LA:H ₃ P:NH ₃ complexes						
	R(P-N)	PSO	DSO	FC	SD	¹ <i>pJ</i> (P−N)
parent	3.292	0.0	0.0	-117.5	0.0	-117.5
$LA = BH_3$	3.098	0.0	0.0	-112.6	0.1	-112.5
NCH	3.332	0.0	0.0	-112.8	0.1	-112.7
ClH	3.192	0.0	0.0	-119.4	0.1	-119.3
FH	3.194	0.0	0.0	-120.6	0.1	-120.5
FCl	2.888	-10.1	0.0	-113.7	0.1	-113.7
HLi	4.325	0.0	0.0	0.6	0.0	0.6

^aFor an optimized cationic complex $(H_2ClFP)^+:NH_2F$, the P-N distance is 2.117 Å, FC = 31.2 Hz, and total $^{1p}J(P-N)$ = 29.4 Hz.

intermolecular bonds in a related series of complexes, as extensively demonstrated for $^{2h}J(X-Y)$ versus the X-Y distance for coupling across X-H···Y hydrogen bonds. ⁵⁴ However, it is apparent from the data of Table 5 that this is not the case for the complexes LA:H₂FP:NFH₂ and LA:H₃P:NH₃. Figure 5 presents a plot of

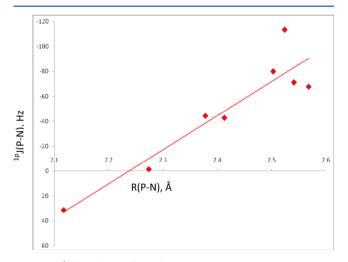


Figure 5. $^{1p}J(P-N)$ vs R(P-N) for complexes LA:H₂FP:NFH₂ and including (H₂ClFP)⁺:NFH₂. The correlation coefficient $R^2 = 0.857$.

 $^{1p}J(P-N)$ versus the P-N distance for complexes LA:H₂FP:NFH₂, clearly illustrating that $^{1p}J(P-N)$ decreases as the P-N distance decreases. The parent complex H₂FP:NFH₂ has one of the longer P-N distances but the largest absolute value (-114 Hz) of $^{1p}J(P-N)$, while FCl:H₂FP:NFH₂ has the shortest P-N distance but the smallest absolute value of $^{1p}J(P-N)$ (-1 Hz).

Some insight into this unusual behavior for coupling across these pnicogen bonds can be obtained from two previous studies in which $(PH_2F)_2$ and $H_2FP:NFH_2$ were hydrogenbonded to 1, 2, or 3 FH molecules at P–F or N–F. 26,32

For complexes nFH: $(PH_2F)_2$, $^{1p}J(P-P)$ decreased in absolute value and R(P-P) also decreased as the number of FH molecules bonded to the same P-F bond increased. In these complexes $^{1p}J(P-P)$ was shown to approach $^{1}J(P-P)$ for the covalent P-P bond in the molecule P_2H_4 . A similar situation occurred but to a lesser extent in 3FH: $(H_2FP:NFH_2)$ when all FH molecules were bonded to the same P-F bond. Once again, $^{1p}J(P-N)$ approaches $^{1}J(P-N)$ for H_2P-NH_3 .

The smallest absolute value of $^{1p}J(P-N)$ is found for the complex FCl:H₂FP:NFH₂, which has the shortest P-N distance. As noted above, the P-Cl bond in this complex has significant covalent character as indicated by its short P-Cl and long Cl-F distances of 2.089 and 4.019 Å, respectively. The computed NBO charge on F of FCl is -0.66e. To further investigate the small value of $^{1p}J(P-N)$ in this complex, we optimized the structure of the cation (H₂ClFP)⁺ and the cationic complex (H₂FClP)⁺:NH₂F. In these, the P-Cl distances are 1.930 and 1.979 Å, respectively. The P-N distance decreases to 2.117 Å in (H₂ClFP)⁺:NH₂F, and $^{1p}J(P-N)$ is +31.2 Hz with total J equal to 29.4 Hz. The data point for this cationic complex has been included in Figure 5. Thus, it appears that if H₂FP:NFH₂ acts as a Lewis base either at P-F or at P, the interaction tends to produce decreasing absolute values of $^{1p}J(P-N)$ with decreasing P-N distance.

^{1p}J(P-N) values have also been computed for complexes LA:H₃P:NH₃. In this series, ¹PJ(P-N) values vary by only 8 Hz if the complex HLi:H₃P:NH₃ is omitted since it does not have a P...N bond. There is no correlation between P-N distances and ^{1p}J(P-N) values in this series. FCl:H₃P:NH₃, which has the shortest P-N distance of 2.888 Å, has neither the largest nor the smallest coupling constant. The very different behavior of ${}^{1p}J(P-N)$ in these two series must be due in large part to the stabilizing effect of the linear F-P···N-F alignment in complexes LA:H₂FP:NFH₂ compared to the linear H-P···N-H alignment in LA:H₃P:NH₃. The F-P···N-F alignment promotes ground-state charge transfer from the N lone pair to the antibonding σ^* P–F orbital. This interaction influences the s electron densities on P and N both in the ground state and in those excited states which couple to it through the Fermi-contact operator.

CONCLUSIONS

In this study, we have carried out ab initio MP2/aug'-cc-pVTZ calculations to investigate the structures and energies of complexes LA:H₂FP:NFH₂ and LA:H₃P:NH₃ in which a pnicogen-bonded P also acts as an electron-pair donor to a Lewis acid (LA), for LA = BH₃, NCH, ClH, FH, FCl, and HLi. We have also examined the effect of interaction of P with the Lewis acid on 31 P and 15 N absolute chemical shieldings and spin—spin coupling constants $^{1p}J(P-N)$ across pnicogen bonds. These calculations support the following statements.

- (1) H₃P:NH₃ forms hydrogen bonds at P with the Lewis acids NCH, ClH, and FH. ClH and FH form distorted hydrogen bonds at P with H₂FP:NFH₂ due to interaction of these two acids with the positively charged H atoms of NFH₂. NCH does not form a hydrogen bond with H₂FP:NFH₂.
- (2) BH_3 interacts with the P atoms of $H_2FP:NFH_2$ and $H_3P:NH_3$ by forming a covalent bond. The interaction of FCl with these complexes leads to significant Cl transfer to P and a P-Cl bond with significant covalent character.
- (3) The geometries of these complexes change from tetrahedral about P in the binary complexes, to distorted trigonal bipyramidal about the P, which acts as the Lewis base in the ternary complexes.

- (4) Neither H₂FP:NFH₂ nor H₃P:NH₃ forms an H-Li···P lithium bond. Rather, in HLi:H₂FP:NFH₂, HLi is nearly parallel to the P-N bond, with the hydridic H interacting with the H atoms of NH₂F. HLi inserts into the P-N bond of H₃P:NH₃ and interacts more strongly with N.
- (5) The classical cooperativity indicates that the P···N and P···LA binding energies have a synergistic effect, although this effect is most probably overestimated due to the neglect of the interaction of the Lewis acid with NH₂F, which can be significant in some cases. It appears that the hydrogen-bonding acids NCH, ClH, and FH have little effect on the energy of the P···N bond in complexes LA:H₂FP:NFH₂, while interaction with the Lewis acids BH₃, FCl, and HLi strengthens the P···N bond.
- (6) The absolute chemical shieldings of ³¹P increase in going from binary LA:PH₂F to ternary LA:H₂FP:NFH₂ complexes as the positive charge on P decreases. In contrast, chemical shieldings decrease in ternary complexes LA:H₃P:NH₃ relative to LA:PH₃ as the positive charge on P increases. Changes in ¹⁵N chemical shieldings and changes in negative charges on N in going from binary to the corresponding ternary complexes do not correlate.
- (7) For complexes LA:H₂FP:NFH₂, ^{1p}J(P-N) coupling constants vary by more than 100 Hz and decrease as the P-N distance decreases. The smallest absolute value of ^{1p}J(P-N) is found for FCl:H₂FP:NFH₂, which has the shortest P-N distance. Its value approaches the value of ^{1p}J(P-N) for the cationic complex (H₂ClFP)⁺:NH₂F. These coupling constants decrease with distance in a manner similar to those of complexes in which intermolecular interactions occur through hydrogen-bond formation at P-F. There is little variation in ^{1p}J(P-N) for complexes LA:H₃P:NH₃ and no correlation between the values of this coupling constant and the P-N distance

ASSOCIATED CONTENT

S Supporting Information

MP2/aug'-cc-PVTZ structures and energies of binary and ternary complexes, and full refs 40, 43, and 49. This material is available free of charge via the Internet at http://pubs.acs.org.

AUTHOR INFORMATION

Corresponding Author

*E-mail: jedelbene@ysu.edu (J.E.D.B.); ibon@iqm.csic.es (I.A.).

Notes

The authors declare no competing financial interest.

ACKNOWLEDGMENTS

This work was carried out with financial support from the Ministerio de Economía y Competitividad (Project No. CTQ2012-35513-C02-02) and Comunidad Autónoma de Madrid (Project MADRISOLAR2, ref S2009/PPQ1533). Thanks are also given to the Ohio Supercomputer Center for its continued support and to the CTI (CSIC) for a grant of computer time.

■ REFERENCES

- (1) Widhalm, M.; Kratky, C. Chem. Ber. 1992, 125, 679-689.
- (2) Drago, R. S.; Wong, N.; Ferris, D. C. J. Am. Chem. Soc. 1991, 113, 1970–1977.
- (3) Carré, F.; Chuit, C.; Corriu, R. J. P.; Mongorte, P.; Nayyar, N. K.; Reyé, C. J. Organomet. Chem. 1995, 499, 147–154.
- (4) Murray, J. S.; Lane, P.; Politzer, P. Int. J. Quantum Chem. 2007, 107, 2286-2292.
- (5) Mohajeri, A.; Pakirai, A. H.; Bagheri, N. Chem. Phys. Lett. 2009, 467, 393-397.

- (6) Zahn, S.; Frank, R.; Hey-Hawkins, E.; Kirchner, B. Chem.—Eur. J. **2011**, *17*, 6034–6038.
- (7) Solimannejad, M.; Gharabaghi, M.; Scheiner, S. J. Chem. Phys. **2011**, 134, 024312–024316.
- (8) Scheiner, S. J. Chem. Phys. 2011, 134, 094315 (1-9).
- (9) Scheiner, S. J. Phys. Chem. A 2011, 115, 11202-11209.
- (10) Politzer, P.; Murray, J. Theor. Chem. Acc. 2012, 131, 1-10.
- (11) Adhikari, U.; Scheiner, S. J. Phys. Chem. A 2012, 116, 3487–3497.
- (12) Adhikari, U.; Scheiner, S. Chem. Phys. Lett. 2012, 532, 31-35.
- (13) Scheiner, S. Chem. Phys. Lett. 2011, 514, 32-35.
- (14) Scheiner, S. Chem. Phys. 2011, 387, 79-84.
- (15) Scheiner, S. J. Chem. Phys. 2011, 134, 164313 (1-9).
- (16) Adhikari, U.; Scheiner, S. J. Chem. Phys. **2011**, 135, 184306–184310.
- (17) Scheiner, S.; Adhikari, U. J. Phys. Chem. A 2011, 115, 11101–11110.
- (18) Scheiner, S. Phys. Chem. Chem. Phys. 2011, 13, 184306 (1-10).
- (19) Del Bene, J. E.; Alkorta, I.; Sánchez-Sanz, G.; Elguero, J. Chem. Phys. Lett. **2011**, *512*, 184–187.
- (20) Del Bene, J. E.; Alkorta, I.; Sánchez-Sanz, G.; Elguero, J. J. Phys. Chem. A **2011**, 115, 13724–13731.
- (21) Adhikari, U.; Scheiner, S. Chem. Phys. Lett. 2012, 536, 30-33.
- (22) Li, Q.-Z.; Li, R.; Liu, X.-F.; Li, W.-Z.; Cheng, J.-B. J. Phys. Chem. A 2012, 116, 2547–2553.
- (23) Li, Q.-Z.; Li, R.; Liu, X.-F.; Li, W.-Z.; Cheng, J.-B. ChemPhysChem **2012**, 13, 1205–1212.
- (24) Del Bene, J. E.; Alkorta, I.; Sánchez-Sanz, G.; Elguero, J. J. Phys. Chem. A 2012, 116, 3056–3060.
- (25) Del Bene, J. E.; Alkorta, I.; Sánchez-Sanz, G.; Elguero, J. Chem. Phys. Lett. **2012**, 538, 14–18.
- (26) Alkorta, I.; Sánchez-Sanz, G.; Elguero, J.; Del Bene, J. E. J. Chem. Theor. Comput. **2012**, *8*, 2320–2327.
- (27) An, X.-L.; Li, R.; Li, Q.-Z.; Liu, X.-F.; Li, W.-Z.; Cheng, J.-B. J. Mol. Model. 2012, 18, 4325–4332.
- (28) Alkorta, I.; Sánchez-Sanz, G.; Elguero, J.; Del Bene, J. E. J. Phys. Chem. A **2013**, 117, 183–191.
- (29) Politzer, P.; Riley, K. E.; Bulat, F. A.; Murray, J. S. Comput. Theor. Chem. **2012**, 998, 2–9.
- (30) Politzer, P.; Murray, J. S.; Clark, T. Phys. Chem. Chem. Phys. **2013**, DOI: 10.1039/c3cp00054k.
- (31) Scheiner, S. Acc. Chem. Res. 2013, 46, 280–288.
- (32) Del Bene, J. E.; Alkorta, I.; Sánchez-Sanz, G.; Elguero, J. J. Phys. Chem. A 2012, 116, 9205—9213.
- (33) Pople, J. A.; Binkley, J. S.; Seeger, R. Int. J. Quantum Chem., Quantum Chem. Symp. 1976, 10, 1-19.
- (34) Krishnan, R.; Pople, J. A. Int. J. Quantum Chem. 1978, 14, 91-
- (35) Bartlett, R. J.; Silver, D. M. J. Chem. Phys. 1975, 62, 3258-3268.
- (36) Bartlett, R. J.; Purvis, G. D. Int. J. Quantum Chem. 1978, 14, 561-581.
- (37) Del Bene, J. E. J. Phys. Chem. 1993, 97, 107-110.
- (38) Dunning, T. H. J. Chem. Phys. 1989, 90, 1007-1023.
- (39) Woon, D. E.; Dunning, T. H. J. Chem. Phys. 1995, 103, 4572–4585.
- (40) Frisch, M. J.; Trucks, G. W.; Schlegel, H. B.; Scuseria, G. E.; Robb, M. A.; Cheeseman, J. R.; Scalmani, G.; Barone, V.; Mennucci, B.; Petersson, G. A.; et al. *Gaussian 09*, revision A.01; Gaussian, Inc.: Wallingford, CT, 2009.
- (41) Reed, A. E.; Curtiss, L. A.; Weinhold, F. Chem. Rev. 1988, 88, 899–926.
- (42) Glendening, E. D.; Badenhoop, J. K.; Reed, A. E.; Carpenter, J. E.; Bohmann, J. A.; Morales, C. M.; Weinhold, F. *NBO 5.G*; University of Wisconsin: Madison, WI, 2004.
- (43) Schmidt, M. W.; Baldridge, K. K.; Boatz, J. A.; Elbert, S. T.; Gordon, M. S.; Jensen, J. H.; Koseki, S.; Matsunaga, N.; Nguyen, K. A.; Su, S. J.; et al. *Gamess*, version 11; Iowa State University: Ames, IA, 2008.
- (44) Ditchfield, R. Mol. Phys. 1974, 27, 789-807.

- (45) Perera, S. A.; Nooijen, M.; Bartlett, R. J. J. Chem. Phys. 1996, 104, 3290-3305.
- (46) Perera, S. A.; Sekino, H.; Bartlett, R. J. J. Chem. Phys. 1994, 101, 2186–2196.
- (47) Schäfer, A.; Horn, H.; Ahlrichs, R. J. Chem. Phys. 1992, 97, 2571–2577.
- (48) Del Bene, J. E.; Elguero, J.; Alkorta, I.; Yañez, M.; Mó, O. *J. Phys. Chem. A* **2006**, *110*, 9959–9966.
- (49) Stanton, J. F.; Gauss, J.; Watts, J. D.; Nooijen, M.; Oliphant, N.; Perera, S. A.; Szalay, P. S.; Lauderdale, W. J.; Gwaltney, S. R.; Beck, S.; et al. *ACES II*; University of Florida: Gainesville, Fl.
- (50) Del Bene, J. E.; Alkorta, I.; Elguero, J. J. Phys. Chem. A 2008, 112, 7925–7929.
- (S1) Del Bene, J. E.; Alkorta, I.; Elguero, J. Phys. Chem. Chem. Phys. **2011**, 13, 13951–13961.
- (52) Hankins, D.; Moskowitz, J. W.; Stillinger, F. H. J. Chem. Phys. 1970, 53, 4544–4554.
- (53) Xantheas, S. J. Chem. Phys. 1994, 100, 7523-7534.
- (54) Del Bene, J. E. In *Calculation of NMR and EPR Parameters*; Kaupp, M., Bühl, M., Malkin, V., Eds.; Wiley-VCH: Weinheim, Germany, 2004; pp 353–370.