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# Comparing Multiple Exciton Generation in Quantum Dots To Impact Ionization in Bulk Semiconductors: Implications for Enhancement of Solar Energy Conversion

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**ABSTRACT** Multiple exciton generation (MEG) in quantum dots (QDs) and impact ionization (II) in bulk semiconductors are processes that describe producing more than one electron–hole pair per absorbed photon. We derive expressions for the proper way to compare MEG in QDs with II in bulk semiconductors and argue that there are important differences in the photophysics between bulk semiconductors and QDs. Our analysis demonstrates that the fundamental unit of energy required to produce each electron–hole pair in a given QD is the band gap energy. We find that the efficiency of the multiplication process increases by at least 2 in PbSe QDs compared to bulk PbSe, while the competition between cooling and multiplication favors multiplication by a factor of 3 in QDs. We also demonstrate that power conversion efficiencies in QD solar cells exhibiting MEG can greatly exceed conversion efficiencies of their bulk counterparts, especially if the MEG threshold energy can be reduced toward twice the QD band gap energy, which requires a further increase in the MEG efficiency. Finally, we discuss the research challenges associated with achieving the maximum benefit of MEG in solar energy conversion since we show the threshold and efficiency are mathematically related.

**KEYWORDS** Multiple exciton generation, carrier multiplication, solar energy conversion, semiconductor nanocrystals, quantum dots

Electron–hole pair multiplication (EHPM) occurs when more than one electron–hole pair (EHP) is produced by absorption of one photon with energy at least twice the semiconductor band gap,  $E_g$ . In bulk semiconductors, EHPM is referred to as impact ionization (II), a well-known phenomenon,<sup>1,2</sup> while in semiconductor nanocrystals, or quantum dots (QDs), EHPM is referred to as multiple exciton generation, MEG,<sup>3</sup> carrier multiplication, CM,<sup>4</sup> or direct carrier multiplication, DCM,<sup>5</sup> to distinguish the phenomenon from II and highlight new proposed physics in quantum confined systems. In recent years, MEG has been reported in several QDs, such as PbSe,<sup>3,4,6–8</sup> PbS,<sup>3,9</sup> PbTe,<sup>10</sup> Si,<sup>11</sup> CdSe,<sup>12–14</sup> InAs,<sup>15,16</sup> InP,<sup>17</sup> and CdTe/CdSe core–shell QDs.<sup>18</sup> However, some authors report they cannot reproduce MEG in CdSe<sup>19</sup> and InAs<sup>20,21</sup> QDs, and for the lead chalcogenides, where MEG has been reported by all investigators, there is controversy concerning the value of the quantum yields (QYs) as well the significance of MEG for improving the performance of photovoltaic cells. Some authors report QYs  $\gg 1$  for exciton formation in PbSe and PbS QDs,<sup>3,4,6,7,22,23</sup> while others have reported only small QYs ( $<1.25$ ).<sup>8</sup> These variations have been attributed to effects of surface chemistry on the exciton relaxation

dynamics<sup>8,23</sup> and in some cases to long-lived charging of the QDs caused by trapping of a photoexcited electron or hole at the QD surface leaving a delocalized hole or electron residing in the core.<sup>22</sup> Extraneous effects such as charging can be reduced by flowing,<sup>24</sup> or stirring the sample<sup>22</sup> during the experiment and using low photon fluencies.

An enhancement in EHPM is expected in QDs over that achievable in bulk semiconductors due to beneficial quantum size effects, such as, relaxed momentum conservation, modified carrier-cooling rates, and enhanced Auger processes. In a recent report,<sup>25</sup> EHPM in bulk films of PbSe and PbS was measured using time-resolved terahertz spectroscopy, and the QYs, or number of electron–hole pairs produced per absorbed photon, were compared with previous reports of MEG in QDs of PbSe and PbS. The authors found that plots of the QYs of EHPM for the bulk semiconductors were equivalent or even larger than that reported for QDs for a given photon energy. From that comparison, the authors concluded that EHPM processes are not enhanced in QDs and EHPM processes are unlikely to significantly enhance solar energy conversion by boosting the photocurrent. In this report, we discuss what we claim is the appropriate way to compare MEG in QDs with II in bulk semiconductors. We show that plotting QY vs  $h\nu/E_g$  (where  $E_g$  is the band gap) provides information about the competition between producing multiple carriers and other energy

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Received for review: 04/27/2010

Published on Web: 07/26/2010



relaxation channels. We present a rigorous derivation of the efficiency of EHPM,  $\eta_{\text{EHPM}}$ , whether for bulk semiconductors or QD samples, that allows for meaningful comparisons and shows how  $\eta_{\text{EHPM}}$  is related to both the threshold energy needed to produce extra EHPs,  $h\nu_{\text{th}}$ , and the competition between EHPM and other relaxation channels. We find  $\eta_{\text{EHPM}}$  increases by  $\sim 2$  in PbSe QDs compared to bulk PbSe. We discuss differences in the photophysics between MEG and II. Finally, we present thermodynamic detailed balance calculations, following the Shockley–Queisser analysis,<sup>26–28</sup> that demonstrate power conversion efficiencies in QD solar cells can greatly exceed that of their bulk semiconductor counterparts.

The recent report<sup>25</sup> on EHPM in bulk PbS and PbSe and a previous report on MEG in PbS and PbSe QDs<sup>8</sup> compare EHPM for bulk semiconductors and QDs on plots of QY vs absolute photon energy ( $h\nu$ ). Such a comparison is misleading and incorrect, because for proper comparisons it is necessary to determine  $\eta_{\text{EHPM}}$ . The efficiency,  $\eta_{\text{EHPM}}$ , is defined as the minimum amount of energy required to produce an EHP (i.e., the band gap), divided by the actual amount of energy required to produce an additional EHP after the MEG threshold is passed; the latter quantity is referred to in the literature as the electron–hole pair creation energy  $\epsilon_{\text{EHPM}}$ .<sup>29,30</sup>  $\eta_{\text{EHPM}} = E_g/\epsilon_{\text{EHPM}}$ . The fact that measurements of MEG QYs for PbSe and PbS QDs are at best equal to that found in the recent II measurements<sup>20</sup> when compared using  $h\nu$  scaling, does not imply an absence of quantum confinement effects or that EHPM is the same for QDs and bulk. Furthermore, QY data plotted vs  $h\nu$  does not provide information about  $\eta_{\text{EHPM}}$ . When  $h\nu$  scaling is used, only the electron–hole pair creation energy,  $\epsilon_{\text{EHPM}}$ , can be ascertained from such a plot;  $\epsilon_{\text{EHPM}}$  is equal to the inverse of the slope of QY vs  $h\nu$ , [ $\epsilon_{\text{EHPM}} = (\Delta\text{QY}/\Delta h\nu)^{-1}$ ]. In contrast, as we will show below, the slope of QY vs  $h\nu/E_g$ , is equal to the EHPM efficiency,  $\eta_{\text{EHPM}} = [\Delta\text{QY}/\Delta(h\nu/E_g)]$ . Thus,  $\eta_{\text{EHPM}}$  is a measure of how well EHPM competes with other relaxation channels and provides a proper and meaningful comparison with respect to the photophysics of EHPM.

**EHPM Energy Considerations and Efficiency.** A fundamental constraint for EHPM processes is the conservation of energy, and for systems with translational symmetry (bulk crystals) the conservation of momentum must also be satisfied. An energetic electron–hole pair, EHP\*, produced by absorption of a photon with sufficient excess energy above the band gap can produce  $m$  EHPs. The EHPM process is described by the scheme



When an EHP\* is produced by absorption of a photon with energy,  $h\nu > E_g$ , conservation of energy dictates that the total number of EHPs created, multiplied by their energy, must

be less than or equal to the total input energy (energy of absorbed photons)

$$N(\text{EHP})\epsilon(e \cdot h) \leq h\nu N_{\text{photons}} \quad (2)$$

where  $\epsilon(e \cdot h)$  is defined as the thermalized energy of an EHP (i.e., the band gap). The inequality reflects the fact that some input energy is lost to heat. For photon energies greater than  $E_g$  and in the absence of EHPM, all the excess energy is lost as heat. The energy loss per absorbed photon is  $E_{\text{loss}} = \Delta E_{\text{tot}} = (h\nu - E_g)$ . For EHPM, the excess energy must be greater than the electron–hole pair creation energy,  $\Delta E_{\text{tot}} \geq \epsilon_{\text{EHPM}}$ . In the ideal case the efficiency equals 1,  $\eta_{\text{EHPM}} = 1$ , and the amount of energy needed to produce an additional EHP is the band gap energy,  $\epsilon_{\text{EHPM}} = E_g$ . Therefore, when the photon energy reaches  $2E_g$  one additional EHP can be created utilizing all excess energy, thus,  $E_{\text{loss}} = 0$  at  $h\nu = 2E_g$ . For photon energies exceeding  $2E_g$ , but less than  $3E_g$ , one additional EHP is formed and the rest is lost to heat, and  $E_{\text{loss}} = h\nu - 2E_g$ , which is the total lost energy after one EHPM event. At  $h\nu = 3E_g$ , two additional EHPs can be produced with  $E_{\text{loss}} = 0$ . Generalizing these observations, the total energy lost is  $E_{\text{loss}}^{(m)} = h\nu - mE_g$ , where  $m$  is the total number of EHPs allowed by energy conservation with a photon energy of  $h\nu$ , thus  $m = \lfloor h\nu/E_g \rfloor$ , where the operator,  $\lfloor \rfloor$ , denotes rounding down to the nearest integer.<sup>31</sup> In general, the amount of energy loss,  $E_{\text{loss}}$  is the total excess energy minus the number of EHPs multiplied by the energy needed to produce additional EHPs

$$E_{\text{loss}} = (h\nu - E_g) - (m - 1)E_g = (h\nu - mE_g) \quad (3)$$

for

$$mE_g \leq h\nu < (m + 1)E_g$$

where eq 3 is the energy loss for absorption of one photon. Solving for the quantum yield, we find  $\text{QY} = m = \lfloor h\nu/E_g \rfloor$  and resembles a staircase that is shown as trace  $M_{\text{max}}$ , in Figure 1b.

For nonideal cases, more energy than the band gap is needed to produce an additional EHP,  $\epsilon_{\text{EHPM}} > E_g$ , and this nonideality is reflected in EHPM efficiencies less than 1,  $\eta_{\text{EHPM}} < 1$ . Therefore,  $m = 1$  for photon energies less than  $E_g + \epsilon_{\text{EHPM}}$  and,  $m = 2$  for photon energies greater than  $E_g + \epsilon_{\text{EHPM}}$  but less than  $E_g + 2\epsilon_{\text{EHPM}}$ . This can be generalized as above to find the maximum number of EHPs at a given photon energy.

$$E_{\text{loss}} = (h\nu - E_g) - (m - 1)\epsilon_{\text{EHPM}} = h\nu - (E_g + (m - 1)\epsilon_{\text{EHPM}}) \quad (4)$$

for

$$E_g + (m + 1)\varepsilon_{\text{EHPM}} \leq h\nu \leq E_g + m\varepsilon_{\text{EHPM}}$$

where  $m$  is the total allowed EHPs for the nonideal case. Substituting  $\varepsilon_{\text{EHPM}} = E_g/\eta_{\text{EHPM}}$  and solving eq 4 when  $E_{\text{loss}} = 0$ , we find  $m = \lfloor (h\nu/E_g - 1)\eta_{\text{EHPM}} \rfloor + 1$ , and therefore the maximum QY is,

$$\text{QY}_{\text{max}} = \left\lfloor \left( \frac{h\nu}{E_g} - 1 \right) \eta_{\text{EHPM}} \right\rfloor + 1 \quad (5)$$

Typically, experimental QYs for EHPM start at some energy threshold,  $h\nu_{\text{th}}$ , and increase linearly, rather than exhibiting the staircase features described above that leads to eq 5. In these soft threshold cases, a phenomenological extension of eq 5 can be made by assuming that the energy loss is equal to  $E_{\text{loss}} = h\nu_{\text{th}} - E_g$  for photon energies greater than  $E_g + \varepsilon_{\text{EHPM}}$ . Substituting  $E_{\text{loss}} = (h\nu_{\text{th}} - E_g)$  into eq 4 and solving for  $m$  we find

$$\text{QY} = \left( \frac{h\nu}{E_g} - 1 \right) \eta_{\text{EHPM}} \quad (6)$$

By solving eq 5 or 6 for when the QY  $\geq 1$ , we find that the energy threshold,  $h\nu_{\text{th}}$ , is related to  $\eta_{\text{EHPM}}$ , and is

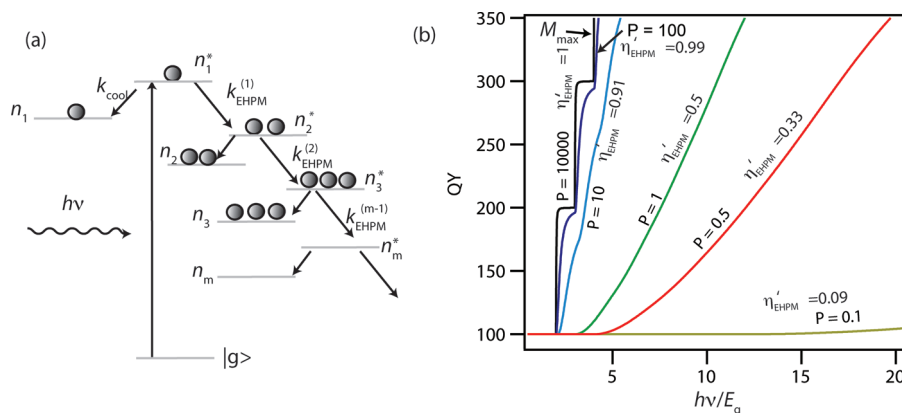
$$h\nu_{\text{th}} = E_g + E_g/\eta_{\text{EHPM}} \quad (7)$$

The total energy loss is  $E_{\text{loss}} = h\nu_{\text{th}} - E_g = E_g/\eta_{\text{EHPM}}$ . From the arguments above we conclude that  $\eta_{\text{EHPM}}$  is obtained from slope of QY vs  $h\nu/E_g$ .

**EHPM Rates vs Cooling Rate.** We also consider the competition between the rate of EHPM,  $k_{\text{EHPM}}$ , vs alternative energy relaxation channels, such as cooling via phonon emission. Figure 1a shows a cascading kinetic scheme where the high-energy exciton either cools directly to the lowest state or produces a hot biexciton state,  $n_2^*$ . That state can either cool or undergo another EHPM event. The initially excited exciton eventually loses all of its excess energy. We do not include decay processes of the relaxed excitons such as Auger recombination and radiative recombination that we assume occur on longer time scales. The set of differential equations that describe the cascaded scheme shown in Figure 1 are

$$\begin{aligned} \dot{n}_1^* &= k_{\text{cool}} n_1^* - k_{\text{EHPM}} n_1^* + I_0 \\ \dot{n}_1 &= k_{\text{cool}} n_1^* \\ \dot{n}_2^* &= k_{\text{EHPM}}^{(1)} n_1^* - k_{\text{cool}} n_2^* - k_{\text{EHPM}}^{(2)} n_2^* \\ \dot{n}_2 &= k_{\text{cool}} n_2^* \\ \dot{n}_3^* &= k_{\text{EHPM}}^{(2)} n_2^* - k_{\text{cool}} n_3^* - k_{\text{EHPM}}^{(3)} n_3^* \\ &\vdots \\ \dot{n}_m^* &= k_{\text{EHPM}}^{(m-1)} n_{m-1}^* - k_{\text{cool}} n_m^* - k_{\text{EHPM}}^{(m)} n_m^* \\ \dot{n}_m &= k_{\text{cool}} n_m^* \end{aligned} \quad (8)$$

where  $I_0$  is the photon fluence,  $n_1^*$  is the population of hot single exciton states,  $n_1$  is the population of relaxed single exciton states,  $n_2^*$  is the population of hot biexciton states,  $n_2$  is the population of relaxed biexciton states,  $n_3^*$  is the population of hot triexciton states, and  $n_3$  is the population of relaxed triexciton states. In general,  $n_m^*$  is the hot  $m$ -exciton state and  $n_m$  is the cooled  $m$ -exciton state. The cooling rate is denoted  $k_{\text{cool}}$ , and the EHPM rates are denoted  $k_{\text{EHPM}}^{(r)}$ , where  $r = m - 1$ . To find the QY, we solve eq 8 for the population of single, bi-, tri-, and higher exciton states at times longer than EHPM and cooling



**FIGURE 1.** (a) Cascade scheme for EHPM considered here. A high-energy photon creates an exciton with excess energy,  $n_1^*$ . The hot exciton can lose energy by cooling or EHPM to form either  $n_1$  or a hot biexciton,  $n_2^*$  and so on. (b) Plots of eq 9 for different values of  $P$ ,  $\eta'_{\text{EHPM}}$  is shown at each  $P$  value.

$$QY = \sum_{j=1}^m j n_j(t > \tau_{\text{EHPM}}, \tau_{\text{cool}}) = \sum_{j=1}^m j \frac{k_{\text{cool}} \prod_{i=1}^j k_{\text{EHPM}}^{(i-1)}}{\prod_{i=1}^j (k_{\text{cool}} + k_{\text{EHPM}}^{(i)})} \quad (9)$$

where  $k_{\text{EHPM}}^{(0)} = 1$ . To use eq 9 we need to know how  $k_{\text{EHPM}}$  and  $k_{\text{cool}}$  vary with excess energy. Keldysh found that for bulk semiconductors the EHPM rate follows<sup>32,33</sup>

$$k_{\text{EHPM}} = \left( \frac{e^2}{4\pi\epsilon} \right) \frac{m_e^*}{h^3} \frac{I_c^2 I_v^2}{(1 + 2\gamma)^{3/2}} \frac{(h\nu - h\nu_{\text{th}})^2}{h\nu_{\text{th}}^2} \quad (10)$$

where  $I_c$  and  $I_v$  are the overlap integrals between initial and final states in the conduction and valence bands and  $\gamma = m_e^*/m_h^*$  which are the effective masses in the conduction and valence bands. Now we need to know how  $k_{\text{cool}}$  varies with excess energy.

For bulk semiconductors, the most important cooling relaxation channel is hot carrier cooling via phonon emission,  $k_{\text{phonon}}$ . The ratio of rates,  $k_{\text{EHPM}}/k_{\text{phonon}}$  is proportional to the ratio of the mean free path for phonon scattering,  $\lambda_{\text{phonon}}$  and the mean free path for EHPM,  $\lambda_{\text{EHPM}}$ , i.e.,  $\lambda_{\text{EHPM}}/k_{\text{phonon}} \propto \lambda_{\text{phonon}}/\lambda_{\text{EHPM}}$ . We can get an idea of the length scales by considering the behavior of free charge carriers in bulk semiconductors. The average distance a charge carrier travels prior to phonon scattering is equal to the velocity of the carrier multiplied by the average time between collisions,  $\lambda_{\text{phonon}} = v\langle\tau\rangle$ .  $\lambda_{\text{phonon}}$  is relatively independent of the kinetic energy of the charged carrier because the length scale for phonon scattering is determined by the properties of the lattice, so as  $v$  increases it is offset by a shorter  $\langle\tau\rangle$ . For bulk PbSe,  $\lambda_{\text{phonon}}$  can be estimated from the carrier mobility, and we find  $\lambda_{\text{phonon}} \sim 67$  nm. In bulk semiconductors,  $\lambda_{\text{EHPM}}$  decreases with increasing carrier velocity (or excess kinetic energy),<sup>34</sup> corresponding to an increasing  $k_{\text{EHPM}}$ . In bulk PbSe,  $\lambda_{\text{EHPM}}$  has not been measured to our knowledge; however, for Si  $\lambda_{\text{EHPM}} \sim 10$  nm<sup>30</sup> at a few electronvolts above the band edge and for GaAs,  $\lambda_{\text{EHPM}} > 10$  nm for excess energies between 1 and 10 eV.<sup>34</sup> In accordance with the above observations, a Monte Carlo simulation of phonon cooling and impact ionization finds the phonon relaxation rate to be independent of excess energy, while the II rate increased with increasing excess energy.<sup>35</sup> The dimensions of QDs studied here are smaller than both  $\lambda_{\text{phonon}}$  and  $\lambda_{\text{EHPM}}$  of bulk materials indicating that EHPM and cooling in QDs are most likely different from bulk. Following Ridley<sup>32</sup> we parametrize  $k_{\text{EHPM}}/k_{\text{cool}}$  by the following expression

$$k_{\text{EHPM}} = k_{\text{cool}} P \left( \frac{h\nu - h\nu_{\text{th}}}{h\nu_{\text{th}}} \right)^s \quad (11)$$

where the factor  $P$  determines whether the EHPM onset is hard or soft, for  $P \gg 1$  the onset is hard, and for  $P < 1$  the onset is soft. The exponent  $s$  in eq 11 was found to be 2 in the original Keldysh treatment. However, that treatment was for an ideal semiconductor; in more detailed treatments,  $s$  can vary between 2 and 5. In our treatment we allow both  $s$  and  $P$  to be adjustable parameters. We now define an efficiency,  $\eta'_{\text{EHPM}}$ , based on the threshold parameter,  $P$ , that captures the competition between the  $k_{\text{EHPM}}$  and  $k_{\text{cool}}$

$$\eta'_{\text{EHPM}} = \frac{P}{1 + P} \quad (12)$$

where we use the prime to distinguish  $\eta'_{\text{EHPM}}$  from  $\eta_{\text{EHPM}}$  defined above in terms of  $\epsilon_{\text{EHPM}}$ . The relationship between  $\eta'_{\text{EHPM}}$  and the energy threshold is the same as we found before, but now each EHPM event has its own energy threshold given by

$$h\nu_{\text{th}}^{(m)} = E_g(1 + m/\eta'_{\text{EHPM}}) \quad (13)$$

where  $k_{\text{EHPM}}^{(m)}$  is zero below  $h\nu_{\text{th}}$  and therefore  $k_{\text{EHPM}}^{(m)} = k_{\text{cool}} P [(h\nu - h\nu_{\text{th}}^{(m)})/h\nu_{\text{th}}]^s \theta(h\nu - h\nu_{\text{th}}^{(m)})$  where  $\theta$  is the heavyside step function.

In Figure 1b we show plots of the QY from eq 9 for various values of  $P$  (with  $s = 2$ ) and note the values of  $\eta'_{\text{EHPM}}$ . We vary  $P$  from 10000 to 0.1, at  $P = 10000$ ,  $\eta'_{\text{EHPM}} = 1$ , and EHPM dominates over cooling. For this scenario, we recover the staircase behavior for an ideal behavior where eq 3 gives the total energy loss. At  $P = 1$ ,  $\eta'_{\text{EHPM}} = 0.5$ , we find a roughly linear increase of the QY with  $h\nu/E_g$ ; the onset, however, is not as sharp as that predicted from eq 6. For QY values less than  $\sim 150\%$  and for  $P < 10$ ,  $k_{\text{cool}} > k_{\text{EHPM}}$ , and QY increases  $\sim$  quadratically with  $h\nu/E_g$ . At a QY = 150%,  $k_{\text{cool}} \approx k_{\text{EHPM}}$ , this can be seen by substituting  $k_{\text{cool}} = k_{\text{EHPM}}$  and considering the first two terms of eq 9,  $QY = k_{\text{cool}}/(k_{\text{cool}} + k_{\text{EHPM}}^{(1)}) + 2k_{\text{EHPM}}^{(1)}/(k_{\text{cool}} + k_{\text{EHPM}}^{(1)})$ . The QY in this energy range increases approximately linear with  $h\nu/E_g$  with a slope determined by  $P$  and  $s$ .

**Data Analysis.** Figure 2a displays recent MEG QY data reported in ref 24 for three samples of different sizes of PbSe QDs (filled brown squares). We employ a 1 mm flow cell and flow our samples at 150 mL/min during the transient absorption experiment. We also plot recent data reported in ref 22 where the samples were stirred rather than flowed. The good agreement between these two data sets provides confidence in our reported results. EHPM QYs for bulk PbSe (filled black squares) and bulk PbS (open circles) are plotted



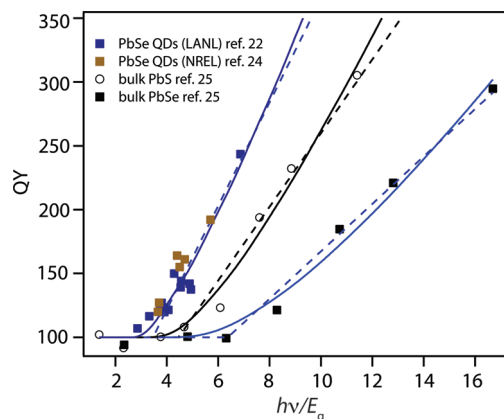


FIGURE 2. QY vs  $h\nu/E_g$  for PbSe QD samples measured at LANL and reported in ref 22 (blue squares), and PbSe QDs measured at NREL and reported in ref 24 (brown squares). EHPM QYs for bulk PbSe and bulk PbS are reproduced from ref 25. The dotted lines are a linear-least-squares best fit to eq 6 to the data, and the solid lines are eq 9. The best-fit parameters are reported in Table 1.

TABLE 1. Best-Fit Parameters for Lines Shown in Figure 2

	$\eta_{\text{EHPM}}$	$h\nu_{\text{th}}$	$\eta'_{\text{EHPM}}$	$P$	$s$	$h\nu'_{\text{th}}$
bulk PbSe	0.19	$6.5 E_g$	0.31	0.45	2.5	$4.22 E_g$
bulk PbS	0.29	$4.4 E_g$	0.45	0.83	2.6	$3.22 E_g$
QD samples						
PbSe QDs	0.41	$3.4 E_g$	0.6	1.5	2.2	$2.7 E_g$

and reproduced from ref 25. These data points were measured using a time-resolved terahertz experiment that is sensitive to the total number of carriers produced by the excitation pulse. Equation 6 was fit to each data set with only one adjustable parameter,  $\eta_{\text{EHPM}}$ , to obtain both the slope and  $h\nu_{\text{th}}$  and are shown as dotted lines. The solid lines are the best-fit lines using eq 9 where  $P$  and  $s$  are allowed to vary. The fits using eq 9 are slightly better because the predicted onset is not as abrupt. This appears to be more important for the QD samples than the bulk data. We report the best-fit parameters in Table 1 and tabulate  $\eta'_{\text{EHPM}}$ ,  $h\nu_{\text{th}}$ , and  $h\nu'_{\text{th}}$ .

The efficiency,  $\eta_{\text{EHPM}}$ , is clearly better for the PbSe QD samples than for the bulk PbSe. We find  $\eta_{\text{EHPM}}$  increases from 0.19 to 0.41 in the QD samples (a factor of  $>2$ ), while  $P$  increases from 0.45 to 1.5, an increase of  $>3$ . In accordance with our discussion above,  $h\nu_{\text{th}}$  decreases from  $4.2 E_g$  to  $2.7 E_g$ . Through the analysis presented here, comparing EHPM as a function of  $h\nu/E_g$  is more meaningful and correct than using  $h\nu$ . One of the reasons why there is confusion concerning  $h\nu$  vs  $h\nu/E_g$  scaling is because a proper definition of  $\eta_{\text{EHPM}}$  had not been clearly established. The assumption that the MEG efficiency is equal to the enhanced QY at a particular photon excitation energy leads to an erroneous conclusion that because the QY decreases at some fixed excitation energy for smaller QDs that  $\eta_{\text{EHPM}}$  is lower for QDs compared to bulk semiconductors. This leads an incorrect conclusion that EHPM is lower in QD than in bulk semiconductors. However, this definition of the efficiency neglects the energetics involved. The

excess energy available to produce an additional EHP decreases for smaller QD sizes because band gap energy increases for QDs compared to bulk. Therefore,  $h\nu/E_g$  scaling provides a clear way of comparing EHPM while the  $h\nu$  scaling does not. Furthermore, when considering data using the  $h\nu$  scaling, the relationship between the threshold values and  $\eta_{\text{EHPM}}$  is obscured because there does not appear to be any correlation between the slope (or the inverse of the electron–hole pair creation energy) and  $h\nu_{\text{th}}$ . However, the correlation is clearly visible with the  $h\nu/E_g$  scaling. For example, considering the bulk PbS data we see it takes  $\sim 4.3 E_g$  for EHPM to begin and each new EHP occurs at each additional  $3.3 E_g$ , in accordance with  $\eta_{\text{EHPM}} = 0.29$ . The recent report from Delerue et al.<sup>36</sup> also concluded that  $\eta_{\text{EHPM}}$  (defined in a similar fashion as we define here) is enhanced in QDs relative to bulk semiconductors.

**EHPM Energy Threshold Considerations.** In the above analysis, we find a relationship between  $\eta_{\text{EHPM}}$  and  $h\nu_{\text{th}}/E_g$ . This relationship implies that  $h\nu_{\text{th}}$  is inextricably linked to  $\eta_{\text{EHPM}}$ . However, the link between the  $\eta_{\text{EHPM}}$  and  $h\nu_{\text{th}}$  can be broken if other factors besides the efficiency help determine  $h\nu_{\text{th}}$ . For example, if the relationship between  $\epsilon_{\text{EHPM}}$  and the band gap energy is  $\epsilon_{\text{EHPM}} = A E_g + B$  where  $B$  is the related to  $h\nu_{\text{th}}$ .<sup>29,30,37</sup> We could also consider a scenario where  $\epsilon_{\text{EHPM}}$  is not a linear function but varies with the amount of excess energy so that  $\eta_{\text{EHPM}}$  increases with increasing energy, again plotting QY vs  $h\nu_{\text{th}}/E_g$  will provide  $\eta_{\text{EHPM}}$ .

There are at least three possible contributions to  $h\nu_{\text{th}}$ : (1) conservation of energy, (2) conservation of momentum, and (3)  $\eta_{\text{EHPM}}$ , as discussed above. Energy conservation dictates that  $h\nu_{\text{th}}/E_g \geq 2$ ; however, in a bulk semiconductor,  $\Delta k = 0$  absorption selection rules increases  $h\nu_{\text{th}}$ . The excess energy in the conduction band is  $\Delta E_e = (h\nu - E_g) (1 + m_e/m_h)$  and  $\Delta E_h = (h\nu - E_g) - \Delta E_e$ , where  $m_e$  is the effective mass of the electron and  $m_h$  is the effective mass of the hole. For parabolic bands,  $m_e \approx m_h$ , the situation for PbS and PbSe, and  $h\nu_{\text{th}}/E_g \approx 3$  on energy conservation arguments alone. However, the bands may not be parabolic;  $h\nu_{\text{th}}$  depends upon the detailed band structure and there is a distribution of excess energies populated by absorption.<sup>38</sup> There may also be weak second-order transitions involving a phonon that relaxes the  $\Delta k = 0$  selection rule.

Crystal momentum must be conserved for systems with translational symmetry and this additional constraint increases  $h\nu_{\text{th}}$  over the energy conservation limit for bulk semiconductors. The amount of increase in  $h\nu_{\text{th}}$  depends on the band structure, positions of split-off bands, indirect vs direct transitions, and other details that pertain to the semiconductor of interest. A review of the most common situations found in semiconductors has been tabulated in ref 2. For the case of isotropic bands the excess energy in the conduction or valence band is given by

$$\Delta E_e = \frac{(2m_e + m_h)}{m_e + m_h} E_g \quad (14)$$

where  $\Delta E_e$  is the excess kinetic energy necessary in the initiating electron. For PbS and PbSe the above condition results in an excess energy of  $3E_g/2$ ,  $E_g/2$  above the energy conservation limit. Therefore, energy and momentum constrain  $h\nu_{th}/E_g \approx 4$  for PbSe and PbS. In QDs, momentum is no longer a good quantum number since a crystal lattice only exists for a few nanometers and therefore the momentum conservation limit is relaxed, and for PbSe QDs,  $h\nu_{th}$  has been observed to be  $3\tilde{E}_g$  (reported here as  $2.7E_g$ ), well below the momentum conservation limit. Thus one major advantage of QDs is the possibility to decrease  $h\nu_{th}$  below the momentum conservation limit defined for bulk systems.

**Photophysics of Hot Electrons and Quantum Confinement Effects.** The analysis of  $\eta_{EHPM}$  presented above demonstrates that EHPM is more efficient in PbSe QDs than in bulk PbSe. In QDs there are at least three fundamental properties that are modified due to quantum confinement and affect the EHPM process.

(A) Crystal momentum is no longer a good quantum number. There are three factors that can affect  $h\nu_{th}$  related to crystal momentum: (1) absorption selection rules are modified; (2) conservation of crystal translational momentum is relaxed, allowing  $h\nu_{th}$  to be less than that required by momentum conservation. In fact, we find  $h\nu_{th}$  in QDs of PbSe is lower than that allowed by momentum conservation in bulk PbSe, and (3) single and multiexcitonic states can be coupled through the Coulomb operator to form a superposition of states.<sup>39</sup> Such coupling is not possible in bulk systems with well-defined momentum.

(B) The discrete structure of semiconductor QD energy bands, due to quantum confinement and intimate control over surface states and surface ligands can be used to modify carrier relaxation rates and thereby increase  $P$ . Intimate control over variable surfaces and interactions is a research challenge and opportunity rather than a priori a bad characteristic.

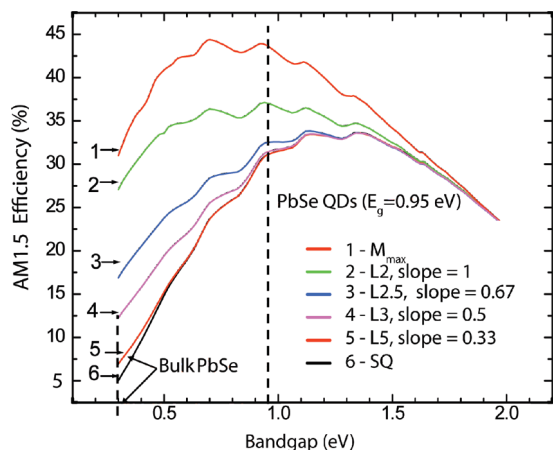
(C) Increased Coulombic coupling between excitons in QDs increases Auger-related processes like MEG.

The theoretical model for MEG developed by Efros, Shabaev, and Nozik<sup>39</sup> shows how the photophysics governing MEG in QDs is new and different from EHPM in bulk semiconductors. The strong Coulomb coupling of multiple excitons driving MEG in QDs is not present in the bulk. Other models for MEG/CM<sup>49,50</sup> also show different physics for bulk semiconductors compared to QDs. For example, in the Klimov model, CM occurs through excitation of virtual states that are transferred to biexciton states via intraband transitions.  $\eta_{EHPM}$  is higher in QDs because of enhanced intraband transition oscillator strengths in QDs vs bulk semiconductors. Zunger et al. use an impact ionization approach to

calculate enhancements in EHPM in QDs due to a higher density of final states.<sup>51</sup>

Our analysis of  $\eta_{EHPM}$  presented here does not consider whether  $k_{EHPM}$  is enhanced in QDs over bulk or whether  $k_{cool}$  decreases, and quantum confinement may effect both  $k_{cool}$  and  $k_{EHPM}$ . As we noted earlier the length scales for both EHPM and cooling in bulk PbSe are larger than the QD diameter; therefore we expect some dependence of these processes with size. If no new physical processes are invoked, then we would expect the surfaces of the QDs to dominate these relaxation pathways. The photoexcited carrier should reach the QD surface ballistically, and both  $k_{cool}$  and  $k_{EHPM}$  could increase. The resulting QY would depend on whether  $k_{EHPM}/k_{cool}$  increased, decreased, or remained constant. However, size effects do introduce new relaxation pathways that are not found in corresponding bulk semiconductors. One of the arguments for enhanced EHPM in QDs is the sparse density of states that can slow or inhibit phonon-mediated relaxation (referred as the phonon bottleneck).<sup>40,41</sup> The presence of the phonon bottleneck is masked by enhanced Coulombic coupling between the electron and hole wave functions providing an Auger-like relaxation channel<sup>42</sup> that relies on a large difference in  $m_e$  and  $m_h$ . Slowed cooling has been observed in QD systems where the electron and hole are separated,<sup>43</sup> the effective masses are similar,<sup>44</sup> or surface relaxation channels are suppressed,<sup>45</sup> combining these approaches, the 1P to 1S cooling was slowed to  $\sim 1$  ns.<sup>46</sup> However, the majority of hot carrier relaxation studies have used low excess energies, while MEG measurements are performed at high excess energies. One of the criticisms of enhanced MEG in QDs is that the density of states at these high excess energies is sufficiently dense to allow fast relaxation via phonon emission (the absorption spectra of QDs approach that of bulk at high excess energies<sup>47</sup>). However, we argue that it is the relative length scales that are important, and as we have shown, the ratio increases for QDs. It stands to reason that QD surfaces play a significant role in all carrier relaxation processes at these high energies. Recent theoretical treatments of QD–ligand interactions demonstrate that the QDs cannot be considered as isolated semiconductors within very high barrier confinement levels.<sup>48</sup> A significant research challenge is to better understand these high excess energy states and to determine what factors may influence MEG vs other relaxation channels and thereby learn how to further increase  $P$ . The majority of theoretical treatments of MEG to date have only considered enhancements in  $k_{EHPM}$  and not the ratio of  $k_{EHPM}/k_{cool}$ .

**Implications for Improved Solar Energy Conversion.** Concerning the issue of whether MEG can enhance solar power conversion efficiencies, we now demonstrate that solar cells produced from QDs can have much higher power conversion efficiencies than their bulk counterparts. The results are based on Shockley–Queisser (SQ) detailed balance calculations and are summarized in Figure 3. We<sup>28</sup> and



**FIGURE 3.** Photovoltaic power conversion efficiencies at AM1.5 vs band gap for various characteristics of MEG QY. Curve SQ is the Shockley–Queisser limit, and curves L2, L2.5, L3, L5, and  $M_{\max}$  are defined in the text.

Klimov<sup>52</sup> have previously conducted thermodynamic efficiency calculations comparing bulk semiconductors and QDs using the approach, and we extend these calculations for various values of  $h\nu_{\text{th}}$  and  $\eta_{\text{EHPM}}$ . In Figure 3, curve 6 (black solid line) is the conventional SQ calculation with just 1 EHP created per photon at the band gap; curve 1 (solid red curve) assumes the maximum multiplication energetically allowed and is based on  $M_{\max}$ . Curve 2 (solid green line) is based on  $h\nu_{\text{th}} = 2E_g$  followed by creation of one extra exciton created per  $E_g$  (defined as the L2 characteristic); curve 3 (solid blue line) is based on a threshold of  $2.5E_g$  with slope defined in eq 6, curve 4 is based on a threshold of  $3E_g$  (defined as the L3 characteristic); curve 5 is based on a threshold of  $4.5E_g$  with  $\eta_{\text{EHPM}} = 0.19$  (defined as the L5 characteristic and is the experimental bulk characteristic for PbSe, see Figure 2b). For each LX case  $E_g/\eta_{\text{EHPM}}$  is lost to heat as discussed above (eq 6). Our analysis suggests that the slope has a smaller effect on power conversion efficiency than does  $h\nu_{\text{th}}$ . Thus identifying QD systems where  $h\nu_{\text{th}}$  can be lowered (also implying a higher  $\eta_{\text{EHPM}}$ ) is imperative.

As seen in Figure 3, the maximum thermodynamic conversion efficiency of  $\sim 5\%$  for bulk PbSe is only marginally enhanced when the experimentally measured EHPM is included. Thus, EHPM in bulk PbSe cannot produce a significant enhancement of conversion efficiency. In contrast, for PbSe QDs with a quantized band gap of 0.95 eV, the maximum thermodynamic conversion efficiency is 31 % for the SQ calculation, 37 % for the L2 characteristic (solid green line), 32 % for the L3 characteristic (solid purple line), and 42 % for the  $M_{\max}$  characteristic (solid red line). These calculations show that PbSe QDs will always have a much higher theoretical conversion efficiency compared to bulk PbSe (by factors ranging from 2.7 (L3 characteristic) to 3.5 ( $M_{\max}$  characteristic)). The calculated conversion efficiencies also show that the maximum possible efficiency for present QDs (L3 characteristic) is barely enhanced compared to the SQ efficiency (32 % vs 31 %, respectively). However, if  $h\nu_{\text{th}}$

can be reduced to  $2E_g$  (L2 characteristic), the maximum efficiency is increased to 37 %, and if the MEG QY characteristic can become staircase-like ( $M_{\max}$ ), the maximum conversion efficiency increases further to 42 %. All these scenarios represent major increases of thermodynamic conversion efficiencies for PbSe QD solar cells compared to bulk PbSe solar cells. For MEG thresholds that are close to  $2E_g$  the maximum conversion efficiency can be greatly enhanced over the SQ limit (ca. a 19 % relative increase for L2 and ca. a 35 % relative increase for  $M_{\max}$ ). We note that an  $M_{\max}$  characteristic has been reported for MEG in the photocurrent measured in single single-walled carbon nanotubes (SWCNT), where after a photon energy threshold of  $2E_g$  was reached, stepwise increases in photocurrent were measured at each subsequent increase of one  $E_g$  of applied voltage to the SWCNT p–n junction.<sup>53</sup> The research challenge for MEG in QD-based solar cells is to find materials and conditions that produce L2 and ultimately  $M_{\max}$  MEG characteristics. Recent efforts toward producing efficient solar cells utilizing Pb–chalcogenide QDs as the active element show  $V_{\text{oc}}$  values that are higher than possible for a solar cell made from a bulk Pb–chalcogenide.<sup>54,55</sup> The higher band gap and resulting higher  $V_{\text{oc}}$  attainable with QDs results in a higher PCE as seen in Figure 3. The higher EHPM efficiency in QDs vs bulk semiconductors allows for a lower  $h\nu_{\text{th}}$  and thus drives the maximum possible PCE higher than the SQ limit for a bulk semiconductor of that given band gap.

**Conclusions.** We have shown that the correct way to compare EHPM processes between semiconductor QDs and bulk semiconductors is to plot the QY vs  $h\nu/E_g$  as this provides a direct determination of the EHPM efficiency,  $\eta_{\text{EHPM}}$ , and allows for determination of the relative contributions of EHPM and competing relaxation channels. We show that there are large increases in theoretical thermodynamic photovoltaic conversion efficiencies for solar cells based on QDs compared to those based on bulk semiconductors. In contrast to previous publications,<sup>8,25</sup> we present data and detailed analyses in support of our belief that there are fundamental differences in the photophysics between EHPM processes in QDs and bulk semiconductors, in addition to major differences in theoretical solar conversion efficiency. The largest benefit to solar energy conversion would be a lowering of the photon energy onset for MEG, producing a staircase characteristic of QY vs  $h\nu/E_g$ . For nonideal cases, the energy onset relative to the band gap must be between 2 and  $2.5E_g$  to have the greatest impact. We argue that the unique properties of QDs allow for lower threshold energy and higher  $\eta_{\text{EHPM}}$ . One theoretical study<sup>56</sup> surveyed 12 QD systems to determine which could produce an onset close to  $2E_g$ , and more such studies, both theoretical and experimental are needed along these lines.

**Acknowledgment.** We acknowledge helpful comments and discussion with Octavi Semonin and Justin Johnson. We



thank Randy Ellingson for careful reading of the manuscript and discussion. M.C.B. and A.G.M. gratefully acknowledge funding from the Solar Photochemistry program within the Division of Chemical Sciences, Geosciences, and Biosciences in the Office of Basic Energy Sciences of the Department of Energy. M.C.H., J.M.L., B.K.H., and A.J.N. were supported as part of the Center for Advanced Solar Photophysics, an Energy Frontier Research Center funded by U.S. Department of Energy, Office of Science, Office of Basic Energy Sciences. DOE funding was provided to NREL through Contract DE-AC36-086038308.

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