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How amino and nitro substituents direct electrophilic aromatic substitution in benzene: an explanation with Kohn–Sham molecular orbital theory and Voronoi deformation density analysis†

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The substituent effect of the amino and nitro groups on the electronic system of benzene has been investigated quantum chemically using quantitative Kohn–Sham molecular orbital theory and a corresponding energy decomposition analysis (EDA). The directionality of electrophilic substitution in aniline can accurately be explained with the amount of contribution of the $2p_z$ orbitals on the unsubstituted carbon atoms to the highest occupied π orbital. For nitrobenzene, the molecular π orbitals cannot explain the regioselectivity of electrophilic substitution as there are two almost degenerate π orbitals with nearly the same $2p_z$ contributions on the unsubstituted carbon atoms. The Voronoi deformation density analysis has been applied to aniline and nitrobenzene to obtain an insight into the charge rearrangements due to the substituent. This analysis method identified the orbitals involved in the C–N bond formation of the π system as the cause for the π charge accumulation at the *ortho* and *para* positions in the case of the NH_2 group and the largest charge depletion at these same positions for the NO_2 substituent. Furthermore, we showed that it is the repulsive interaction between the π_{HOMO} of the phenyl radical and the π_{HOMO} of the NH_2 radical that is responsible for pushing up the π_{HOMO} of aniline and therefore activating this π orbital of the phenyl ring towards electrophilic substitution.

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Introduction

In modern organic chemistry textbooks an explanation of the chemical reactivity of the benzene ring in electrophilic aromatic substitution is directly connected with electron-donating or electron-withdrawing influence of substituents on the electronic system. The explanation is not relying on modern quantitative computational techniques, but quite often on the concepts of Lewis from 1916,^{1e} where the electrons are thought to be at an intermediate state between different resonance structures (see Scheme 1).¹ This, however, does not describe what happens quantum chemically in the electronic system. The effect of the substituent on the reactivity of the benzene ring can be divided

into the field/inductive effect and the resonance (or mesomeric) effect.¹ The main problem is to determine individual contributions of each effect for a particular substituent.² When the resonance and field effects act in the same direction, their separation becomes even more difficult. Undoubtedly, the classical Hammett approach³ (proposed in 1937) expressed by the σ substituent constants has been the first attempt of a quantitative description of the substituent effects. Also this approach, based on experimental data on benzoic acid derivatives, is still widely used in chemistry. To date, different quantitative characteristics are also used to estimate contributions of inductive and resonance effects but they are not general and usually depend on the kind of studied systems.⁴ It is known that the inductive effect operates through σ -bonds, while the resonance effect is transmitted through π -electrons. Lewis structures, which can be seen as a qualitative application of the valence bond theory, are used to explain activating or deactivating substituent properties and also to predict a favored product of the electrophilic attack. A more rigorous way to describe a relationship between molecular structure and electron density is the analysis using qualitative molecular orbitals.^{1a,d,5}

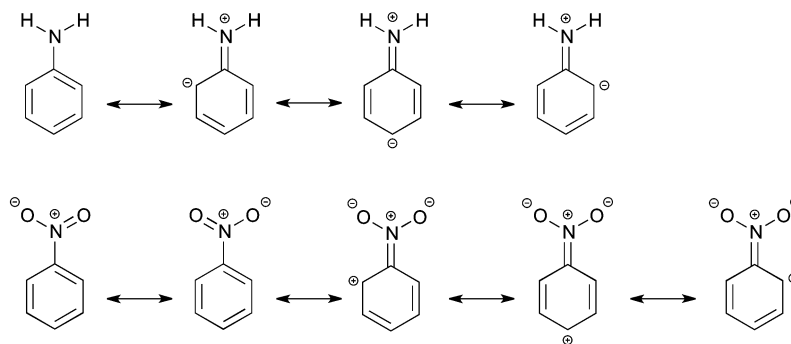
In this work, we would like to study the substituent effects of NH_2 and NO_2 groups on benzene using Kohn–Sham density functional theory. As is known, these two substituents have

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Scheme 1 Resonance structures of aniline and nitrobenzene.

completely opposite electronic properties and therefore, opposite effects on the electrophilic substitution reactions of benzene.¹ The amino group is activating and *ortho*- and *para*-directing, whereas the nitro substituent is known to be deactivating and *meta*-directing. This difference in reactivity can be made plausible by the Lewis structures of aniline and nitrobenzene (Scheme 1), but it does not give an explanation of the influence of the substituent on the molecular σ and π orbitals located on the phenyl ring. The resonance structures suggest that the amino group increases the electron density only at *ortho*- and *para*-positions of the ring, making them more preferred to the electrophilic attack. In turn, the nitro group, according to the resonance structures, promotes the formation of a *meta*-product by decreasing the π -electron density at the *ortho* and *para* positions (Scheme 1). The field effect was deduced to be also important for the nitro substituent and to explain its deactivating properties.^{1a,6a} In previous studies,^{6b-d} some attempts were done to separate the total substituent effect of the nitro group into σ - and π -contributions. However, the outcome was not conclusive, in particular about an importance of the resonance effect, that is the directing effect, in nitrobenzene.

In this study, the resonance and inductive effects of the substituents on the benzene ring are analyzed and separated using Kohn–Sham Molecular Orbital (KS-MO) theory and the accompanying Energy Decomposition Analysis⁷ (EDA). The quantitative KS-MO model together with the EDA have proven to be able to elucidate the nature of different types of bonds: the nature of resonance-assisted hydrogen bonding⁸ and halogen bonding⁹ has been defined. Moreover, the KS-MO model was successfully used for explaining the organic reaction mechanism,¹⁰ the concept of aromaticity and other properties of chemical compounds.¹¹ This method uses symmetry which allows separating the interactions into σ - and π -electronic systems of the benzene ring and the substituents. Previously, Fernandez *et al.*^{11d} found a correlation between the Hammett constants and the π electronic energy term. We will also use the Voronoi Deformation Density (VDD) charge analysis, which enables us to track the reorganization in the σ and π electron densities of the phenyl ring due to the substituent and to determine the resonance and inductive effects on the ring. Based on frontier molecular orbital theory to explain chemical reactivity, our quantitative KS-MO results together with the VDD charges clarify the orientation of the electrophilic aromatic

substitution and the change in reactivity of the benzene ring caused by the NH_2 or NO_2 substituents.

Methodology

General procedure

All calculations were carried out using the Amsterdam Density Functional (ADF) program.¹² Geometries and energies were calculated using the generalized gradient approximation (GGA) with the BLYP functional.^{12c,d} The MOs were expanded in uncontracted sets of Slater type orbitals (STOs) containing diffuse functions with two sets of polarization functions (TZ2P).^{12e} The 1s core shells of carbon, nitrogen and oxygen were treated by the frozen-core approximation. Geometries were optimized in the gas phase assuming C_{2v} symmetry (the difference in energy of the amino group between planar and pyramidal geometries is only 0.3 kcal mol^{−1}, see also ref. 13).

Energy decomposition analysis

To analyze the effect of the substituent on the benzene ring, we defined two fragments consisting of two radicals with opposite spins, which are combined into aniline or nitrobenzene (see Scheme 2). The fragments are treated in the KS open-shell restricted formalism as proposed in ref. 7a.

The interaction energy is examined in the substituted benzene in the framework of the KS-MO model using a quantitative energy decomposition analysis (EDA)^{7a} into electrostatic interactions, Pauli repulsive orbital interactions and attractive orbital interactions:

$$\Delta E_{\text{int}} = \Delta V_{\text{elstat}} + \Delta E_{\text{Pauli}} + \Delta E_{\text{oi}} \quad (1)$$

The term ΔV_{elstat} corresponds to the classical electrostatic interaction between the unperturbed charge distributions of the distorted fragments and is usually attractive. The Pauli repulsion energy, ΔE_{Pauli} , comprises the destabilizing interactions between the occupied orbitals and is responsible for the steric repulsion. The orbital interaction energy, ΔE_{oi} , represents the donor–acceptor



Scheme 2 Fragment decomposition of substituted benzenes (X = O, H).

interactions between the occupied molecular orbitals on one fragment with the unoccupied molecular orbitals of the other fragment, the electron-pair bond formation, as well as the mixing of occupied and virtual orbitals within the same fragment.

The orbital interaction energy can be further decomposed into the contributions from each irreducible representation Γ of the interacting system (eqn (2)):⁷

$$\Delta E_{\text{oi}} = \Delta E_{\sigma} + \Delta E_{\pi} \quad (2)$$

Both nitrobenzene and aniline have C_{2v} symmetry, which decomposes ΔE_{σ} into $\Delta E_{A1} + \Delta E_{B2}$ and ΔE_{π} into $\Delta E_{A2} + \Delta E_{B1}$ components.

Analysis of the charge distribution

The Voronoi Deformation Density¹⁴ (VDD) atomic charges for aniline and nitrobenzene have also been computed. The VDD charge Q_A is computed as the (numerical) integral of the deformation density $\Delta\rho(\mathbf{r})$ associated with the formation of the molecule from its atoms in the volume of the Voronoi cell of atom A (eqn (3)). The Voronoi cell of an atom A is defined as the compartment of space bound by the bond midplanes on and perpendicular to all bond axes between the nucleus A and its neighboring nuclei.

$$Q_A = - \int_{\text{Voronoi cell of A}} \left(\rho(\mathbf{r}) - \sum_B \rho_B(\mathbf{r}) \right) d\mathbf{r} \quad (3)$$

Here, $\rho(\mathbf{r})$ is the electron density of the molecule and the sum over $\rho_B(\mathbf{r})$ is the superposition of atomic densities ρ_B of a fictitious promolecule without chemical interactions that is associated with the situation in which all atoms are neutral. Q_A directly monitors how much charge flows, due to chemical interactions, out of ($Q_A > 0$) or into ($Q_A < 0$) the Voronoi cell of atom A, that is, the region of space that is closer to nucleus A than to any other nucleus.

The VDD method also allows us to analyze the electronic redistributions within two polyatomic fragments when a chemical bond is formed between these two molecular fragments. Previously, we have shown that this method is most informative to analyze resonance-assisted hydrogen bonding appropriately as it allows decomposition of the total changes into σ and π electronic rearrangements.^{8a,b} The change in VDD atomic charges ΔQ_A is defined by eqn (4), which relates this quantity directly to the deformation density $\rho_{\text{Ph-NX}_2}(\mathbf{r}) - \rho_{\text{Ph}\cdot}(\mathbf{r}) - \rho_{\cdot\text{NX}_2}(\mathbf{r})$ associated with the formation of the overall molecule from the two fragments $\text{Ph}\cdot$ and $\cdot\text{NX}_2$ (with X = H or O).^{8a,b,14}

$$\Delta Q_A = - \int_{\text{Voronoi cell of A in Ph-NX}_2} \left(\rho_{\text{Ph-NX}_2}(\mathbf{r}) - \rho_{\text{Ph}\cdot}(\mathbf{r}) - \rho_{\cdot\text{NX}_2}(\mathbf{r}) \right) d\mathbf{r} \quad (4)$$

ΔQ_A monitors how much charge flows out of ($\Delta Q_A > 0$) or into ($\Delta Q_A < 0$) the Voronoi cell of atom A as a result of the chemical bond formation between fragments $\text{Ph}\cdot$ and $\cdot\text{NX}_2$ in the substituted benzene.

This functionality is extended by the decomposition into σ and π components (for the planar, C_s symmetric molecules):

$$\begin{aligned} \Delta Q_A^{\sigma/\pi} &= - \int_{\text{Voronoi cell of A in Ph-NX}_2} \left(\rho_{\text{Ph-NX}_2}^{\sigma/\pi}(\mathbf{r}) - \rho_{\text{Ph}\cdot}^{\sigma/\pi}(\mathbf{r}) - \rho_{\cdot\text{NX}_2}^{\sigma/\pi}(\mathbf{r}) \right) d\mathbf{r} \end{aligned} \quad (5)$$

For the π system, this functionality is additionally extended by the decomposition of the electronic redistribution per atom ΔQ_A into a component associated with the Pauli repulsion ΔE_{Pauli} and a component associated with the bonding orbital interactions ΔE_{oi} .

$$\Delta Q_A^{\pi} = \Delta Q_{A,\text{Pauli}}^{\pi} + \Delta Q_{A,\text{oi}}^{\pi} \quad (6)$$

This π charge decomposition constitutes a bond analysis tool that mirrors the π term of the ΔE_{Pauli} and ΔE_{oi} terms occurring in the bond energy decomposition of eqn (1) and (2) (note that ΔV_{elstat} is not associated with any charge redistribution). This can be obtained by writing the deformation density of π electronic systems as follows:

$$\Delta\rho^{\pi}(\mathbf{r}) = \Delta\rho_{\text{Pauli}}^{\pi}(\mathbf{r}) + \Delta\rho_{\text{oi}}^{\pi}(\mathbf{r}) \quad (7)$$

The change in π atomic charge caused by Pauli repulsion between the monomers in the complex is defined by eqn (8), and the corresponding change caused by charge transfer and polarization is given by eqn (9).

$$\begin{aligned} \Delta Q_{A,\text{Pauli}}^{\pi} &= - \int_{\text{Voronoi cell of A in Ph-NX}_2} \left(\rho_{\text{Ph-NX}_2}^{0,\pi}(\mathbf{r}) - \rho_{\text{Ph}\cdot}^{\pi}(\mathbf{r}) - \rho_{\cdot\text{NX}_2}^{\pi}(\mathbf{r}) \right) d\mathbf{r} \end{aligned} \quad (8)$$

$$\Delta Q_{A,\text{oi}}^{\pi} = - \int_{\text{Voronoi cell of A in Ph-NX}_2} \left(\rho_{\text{Ph-NX}_2}^{\pi}(\mathbf{r}) - \rho_{\text{Ph-NX}_2}^{0,\pi}(\mathbf{r}) \right) d\mathbf{r} \quad (9)$$

The ρ^0 density is obtained from $\Psi_{\text{Ph-NX}_2}^0 = N\hat{A}[\Psi_{\text{Ph}\cdot}\Psi_{\cdot\text{NX}_2}]$ through explicit anti-symmetrization (\hat{A} operator) and renormalization (N constant) of the product of monomer wave functions when the unperturbed monomer densities $\rho_{\text{Ph}\cdot} + \rho_{\cdot\text{NX}_2}$ are superimposed. The π density ρ^{π} is obtained as the sum of orbital densities of the occupied molecular orbitals belonging to the A'' irreducible representation (in C_s symmetry). As the molecular symmetry of aniline and nitrobenzene is C_{2v} , thus of higher symmetry than C_s , the changes in the atomic charge can be split further into A2 and B1.

$$\Delta Q_{A,\text{Pauli}}^{\pi} = \Delta Q_{A,\text{Pauli}}^{A2} + \Delta Q_{A,\text{Pauli}}^{B1} \quad (10)$$

$$\Delta Q_{A,\text{oi}}^{\pi} = \Delta Q_{A,\text{oi}}^{A2} + \Delta Q_{A,\text{oi}}^{B1} \quad (11)$$

Results and discussion

Energy decomposition analysis and bonding mechanism

The energy decomposition analysis and the molecular orbital diagrams of the bonding mechanism in nitrobenzene and

Table 1 Energy decomposition analysis (in kcal mol^{−1}) of the C–N bond for substituted benzenes from Ph• and •NX₂ (with X = H and O)

NX ₂		<i>d</i> (CN)/Å	Δ <i>V</i> _{elstat}	Δ <i>E</i> _{Pauli}	Δ <i>E</i> _σ ^a	Δ <i>E</i> _{A1}	Δ <i>E</i> _{B2}	Δ <i>E</i> _π ^a	Δ <i>E</i> _{A2}	Δ <i>E</i> _{B1}	Δ <i>E</i> _{oi}	Δ <i>E</i> _{int}
•NH ₂	0	1.389	−160.0	288.5	−247.0	−239.5	−7.5	−25.1	−0.2	−24.9	−272.1	−143.6
•NH ₂	90	1.389	−165.5	292.3	−249.5	−238.0	−11.5	−11.0	−0.1	−9.2	−260.5	−133.7
•NH ₂	0	1.492	−124.2	211.0	−208.9	−204.1	−4.8	−17.3	−0.1	−17.2	−226.2	−139.4
•NO ₂	0	1.492	−161.2	330.0	−224.4	−217.7	−6.7	−18.5	−0.7	−17.8	−242.9	−74.1
•NO ₂	90	1.492	−159.5	330.3	−229.6	−219.9	−9.7	−11.0	−0.7	−9.1	−239.6	−68.8
•NO ₂	0	1.389	−211.6	445.0	−276.0	−265.9	−10.1	−27.9	−1.0	−26.9	−303.9	−70.5

^a Δ*E*_σ = Δ*E*_{A1} + Δ*E*_{B2} and Δ*E*_π = Δ*E*_{A2} + Δ*E*_{B1}.

aniline between Ph• and •NX₂, obtained at the KS-DFT BLYP/TZ2P level of theory, are displayed in Table 1 and Fig. 1 and 2 (only the most important interactions are represented).

The energy decomposition analysis of the electron-pair bond formation between Ph• and the substituent •NX₂ shows that interaction energy for the formation of nitrobenzene is about half of the formation of aniline (−74.1 kcal mol^{−1} and −143.6 kcal mol^{−1}, respectively) and the C–N bond is also shorter in aniline than in nitrobenzene (1.389 Å and 1.492 Å, respectively). The longer C–N distance in nitrobenzene is caused by the larger Pauli repulsion (330.0 kcal mol^{−1} for Ph–NO₂ and 288.5 for Ph–NH₂). Compression of the C–N distance in nitrobenzene to the distance in aniline makes the Pauli repulsion go up from 330.0 kcal mol^{−1} to 445.0 kcal mol^{−1}, whereas in aniline the Pauli repulsion is only 288.5 kcal mol^{−1} at

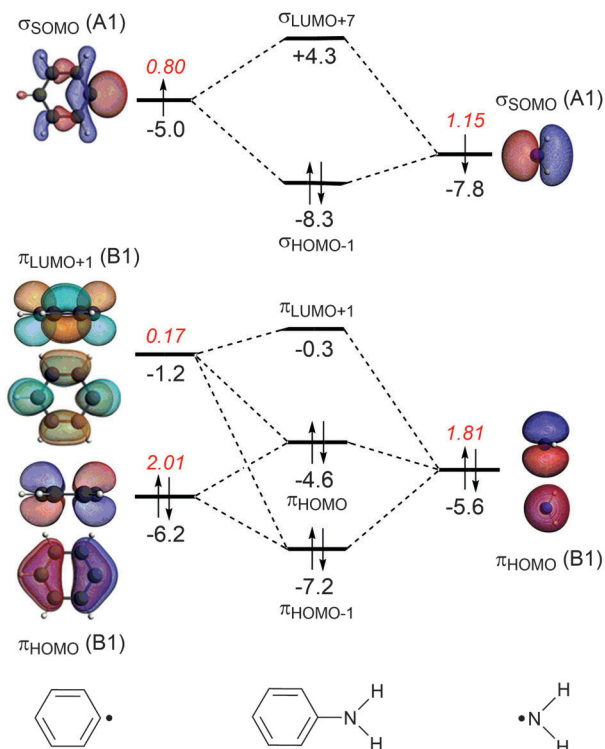


Fig. 1 MO diagrams for the C–N bond formation from Ph• and •NH₂ into aniline with the electron-pair formation in the σ system (only A1 orbitals) at the top and the donor–acceptor interactions in the π system (only B1 orbitals) at the bottom. The energies (eV) of the molecular or fragment orbitals are given in black and the gross electron population of the fragment orbitals in red.

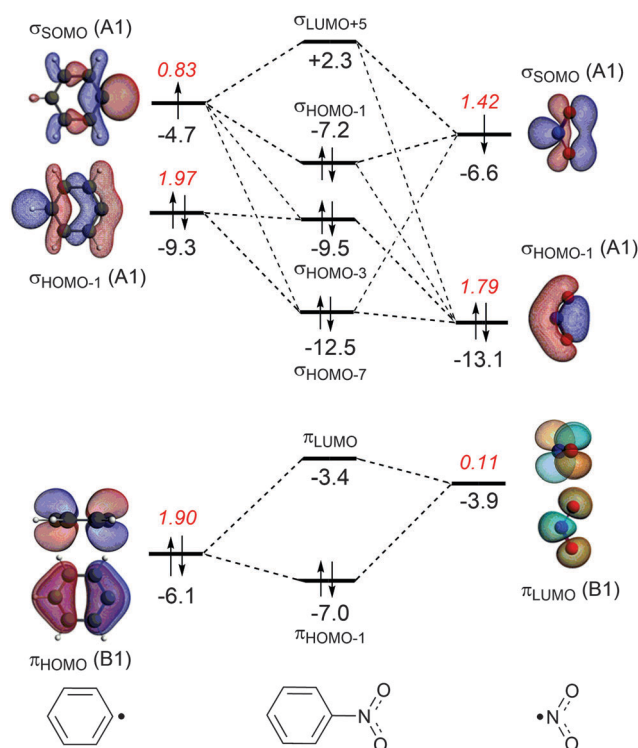


Fig. 2 MO diagrams for the C–N bond formation from Ph• and •NO₂ into nitrobenzene with the electron-pair formation in the σ system (only A1 orbitals) at the top and the donor–acceptor interactions in the π system (only B1 orbitals) at the bottom. The energies (eV) of the molecular or fragment orbitals are given in black and the gross electron population of the fragment orbitals in red. (The σ_{HOMO} on both fragments are of B2 orbitals, which do not overlap.)

1.389 Å. The shortening of the C–N distance in nitrobenzene results in an increase of 115.0 kcal of the Pauli repulsion and only in an extra attraction of −111.4 kcal mol^{−1} of the bonding components (electrostatic and orbital interaction). The σ MO diagram shows the repulsive interaction between the occupied σ_{HOMO−1} of Ph• and σ_{HOMO−1} of •NO₂, which is absent in the σ MO diagram of aniline (see Fig. 1 and 2). The largest bonding contribution to the interaction energy is the A1 component of the orbital interaction (that is the formation of the electron-pair bond), which amounts to −239.5 kcal mol^{−1} for aniline and −217.7 kcal mol^{−1} for nitrobenzene. The electrostatic interaction is of similar strength for both systems: −160.0 kcal mol^{−1} for aniline and −161.2 kcal mol^{−1} for nitrobenzene. Note that the Δ*E*_{A2} and Δ*E*_{B2} only account for polarization within each fragment

as the A2 and B2 orbitals have no amplitude on the atoms located on the C_2 rotation axis and therefore do not overlap.

The stabilization caused by the donor–acceptor interactions in the B1 irreducible representation (that is in the π electronic system) is larger for aniline ($-24.9 \text{ kcal mol}^{-1}$) than for nitrobenzene ($-17.8 \text{ kcal mol}^{-1}$). Compression of the C–N bond in Ph–NO₂ to the distance of Ph–NH₂ enlarges the ΔE_{B1} to $-26.9 \text{ kcal mol}^{-1}$.

For both substituents, NH₂ and NO₂, the formation of the electron-pair bond in the σ electronic system causes the singly occupied molecular orbital (SOMO) of the phenyl radical to donate 0.2 electrons to the SOMO of the substituent accounting for the inductive effect of the substituent. In the case of nitrobenzene, the bond formation is accompanied by the Pauli repulsive interaction between occupied orbitals on the Ph• and •NO₂ fragments (see Fig. 2).

The donor–acceptor interactions in the π electronic system of aniline and nitrobenzene have an opposite effect on the phenyl radical: NH₂ is electron donating and NO₂ is electron-withdrawing. The MO diagrams illustrate this clearly. For aniline, the π -orbital of the NH₂ group donates 0.17 electrons to the π_{LUMO+1} orbital of the benzene ring (see Fig. 1). This counteracts the charge-flow in the σ system. There is also Pauli repulsion between the π_{HOMO} on Ph• and •NH₂, which pushes up the energy of the π_{HOMO} of aniline to -4.6 eV and accounts for the activation towards electrophilic substitution and not the donor–acceptor interactions. This mechanism has also been encountered in the study of the substituent effects on the optical properties of naphthalene diimides.^{11c}

In the case of nitrobenzene, the electron transfer goes in the opposite direction. The π_{LUMO} of the NO₂ group accepts 0.11 electrons from the π -system of the benzene ring increasing the deactivation for electrophilic substitution (see Fig. 2). The π_{HOMO} of nitrobenzene lies at -7.0 eV , which is 2.4 eV lower than the same orbital in aniline and explains the lower reactivity of nitrobenzene.

Another way to investigate the effect of the substituents is to rotate the substituents by 90 degrees, that is, perpendicular to the plane of the benzene ring and analyze the capability of the substituents to participate in the π -electron delocalization of the ring. The donor–acceptor interactions are either lost as in the nitrobenzene or become negligible as in aniline (the amino group donates only 0.03 electrons, see Fig. S1 and S2, ESI†). Rotation of the substituent NX₂ (the rotation barriers are given in Table S1, ESI†) switches off the donor–acceptor interactions in the π electronic system, however the energetic loss is quite small in both cases. For nitrobenzene, ΔE_{π} goes from $-18.5 \text{ kcal mol}^{-1}$ to $-11.0 \text{ kcal mol}^{-1}$ and for aniline from $-25.1 \text{ kcal mol}^{-1}$ to $-11.0 \text{ kcal mol}^{-1}$. Clearly, the π orbitals of the phenyl ring can also interact with the perpendicular substituent and the π delocalization is therefore not switched off completely (see Fig. S1 and S2 in the ESI† for the MO diagrams for the perpendicular conformation).

After this explanation of the activating and deactivating effects of the NH₂ and NO₂ substituents on the benzene ring based on the MO diagrams, we would also like to understand

the directionality of the electrophilic attack. Recently, Fievez *et al.*^{10c} showed that the orbital interaction is the driving force towards selectivity in electrophilic aromatic substitution for activating substituents, but it is not the main factor for the NO₂ substituent. They studied the interaction energy and its components (eqn (1)) between monosubstituted benzene derivatives and a model electrophile at the onset of the reaction in a plane parallel to the molecular plane.

Here, we would like to analyze the molecular orbitals of the substituted benzenes in terms of the contribution of the $2p_z$ orbitals on the carbon, nitrogen and oxygen atoms to the molecular π orbitals, allowing us to explain the directionality from the molecular orbital perspective (see Fig. 3). The high contribution of a $2p_z$ orbital on a certain carbon atom to the π_{HOMO} of the substituted benzene will direct the electrophilic attack towards that atom because of the larger overlap between the accepting orbital of the electrophile and the π_{HOMO} of the substituted benzene. The most favorable interaction occurs at the atom with the highest $2p_z$ contribution to the π_{HOMO} .

Aniline has only one highest occupied π orbital at -4.6 eV with the largest gross Mulliken contributions on the *meta* (14%) and the *para* (22%) positions. The electrophilic attack will therefore occur at these positions. Nitrobenzene has two almost degenerate highest occupied π orbitals at -6.9 eV and -7.0 eV . The π_{HOMO} directs the electrophilic attack towards *ortho* and *meta* positions with $2p_z$ contributions of 23% on these two positions, and the π_{HOMO-1} towards the *para* position with a $2p_z$ contribution of 31% on the *para* (contributions on the *ortho* and *meta* positions are small, 5% and 8% respectively). Thus, the π orbitals of nitrobenzene are deactivated (because they are low-lying) and the experimentally observed *meta* directing effect of the nitro substituent for electrophilic aromatic substitution cannot be explained from the character of the π_{HOMO} and π_{HOMO-1} .

VDD charge analysis

Complementary to the KS-MO analysis and the EDA, we have also investigated the VDD atomic charges (eqn (3)) and charge rearrangements (eqn (4)) on the phenyl ring due to the substituent effects to predict the regioselectivity of electrophilic substitution and explain the reactivity of the aromatic ring. Fig. 4 displays the VDD atomic charges (eqn (3)) for benzene, nitrobenzene and aniline, which are the differences between the final density and the density of the promolecule (the sum over spherical atomic densities). The comparison of the VDD atomic charges shows that aniline has a more negative charge than benzene at the *ortho* and *para* positions, -78 and -74 milli-electrons, respectively, compared to only -48 milli-electrons in benzene. This is in line with the large amplitudes of the π_{HOMO} on the *ortho* and *para* carbon atoms. Nitrobenzene has at all positions a less negative charge than benzene, which is in line with the deactivating properties of the nitro group. The *meta* position in nitrobenzene is slightly more negative (-41 milli-electrons) than the *ortho* and *para* positions (-34 and -28 milli-electrons). Note that the differences in aniline are larger than in nitrobenzene.

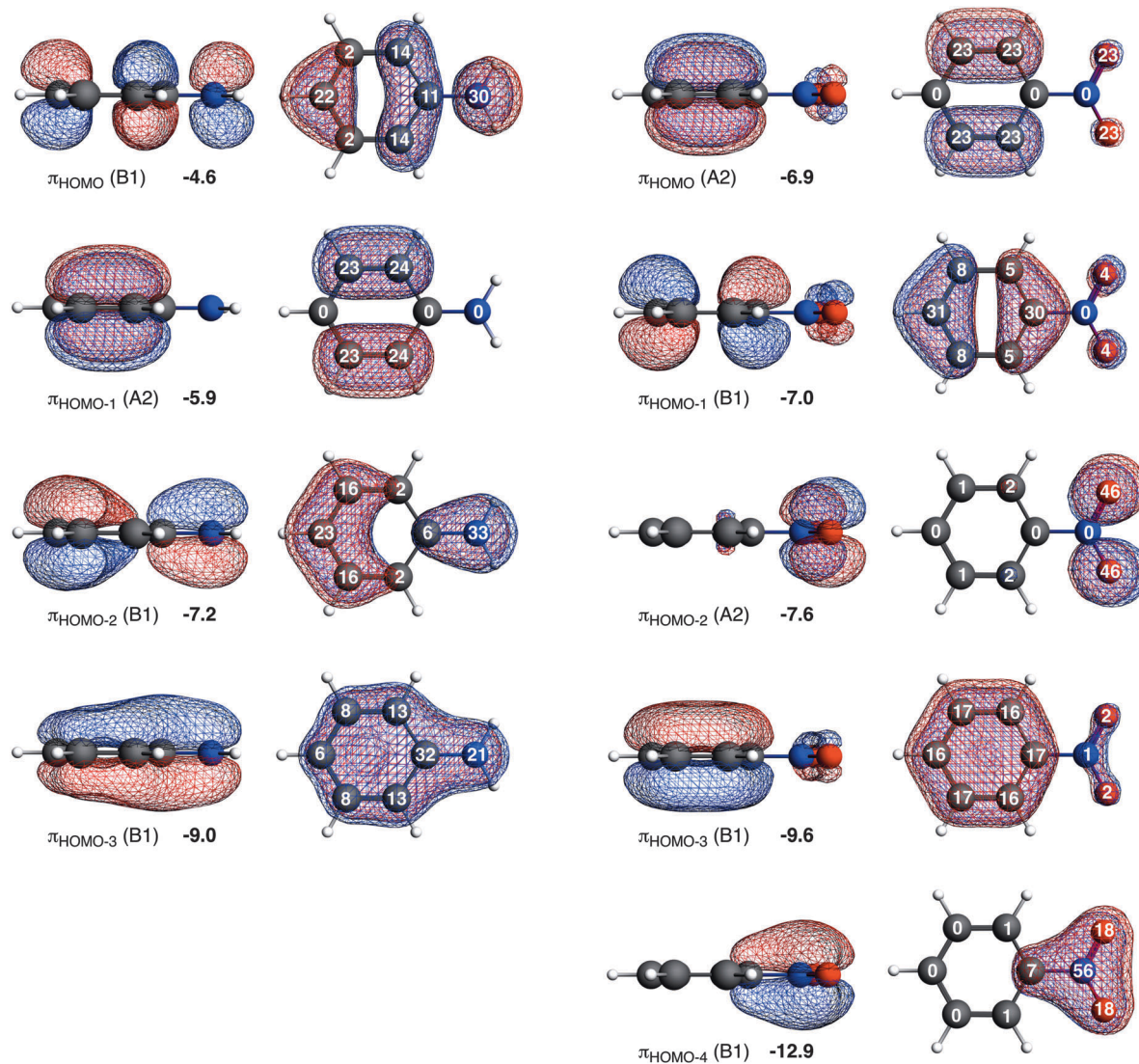


Fig. 3 The π orbitals of aniline (left) and nitrobenzene (right) in A2 and B1 representation. The energies of the molecular orbitals are given in eV (black) and the gross Mulliken $2p_z$ contributions to MO are given in white on the atom (in percentages).

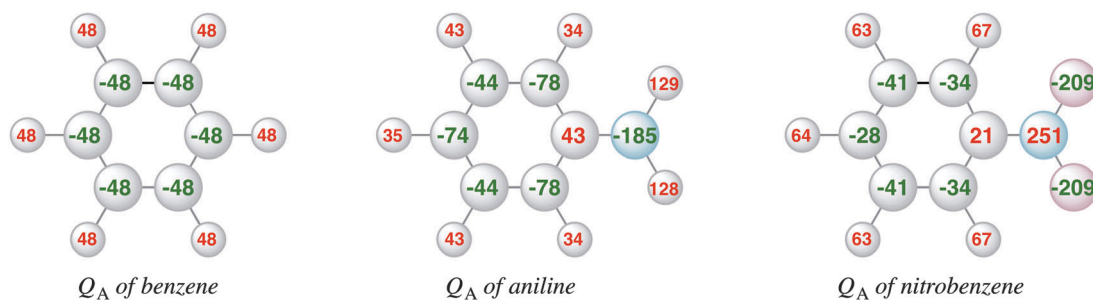


Fig. 4 VDD atomic charges (milli-electrons) of benzene, aniline and nitrobenzene (eqn (3)).

The VDD charge rearrangements, as defined in eqn (4), allows analysis of the charge redistributions within two poly-atomic fragments when a chemical bond is formed between these two molecular fragments. Furthermore, it allows

decomposition of the total changes into the components of different irreducible representations. In Fig. 5, the VDD charge rearrangements (ΔQ) due to the formation of the C–N bond in aniline and nitrobenzene are given. The bond formation causes

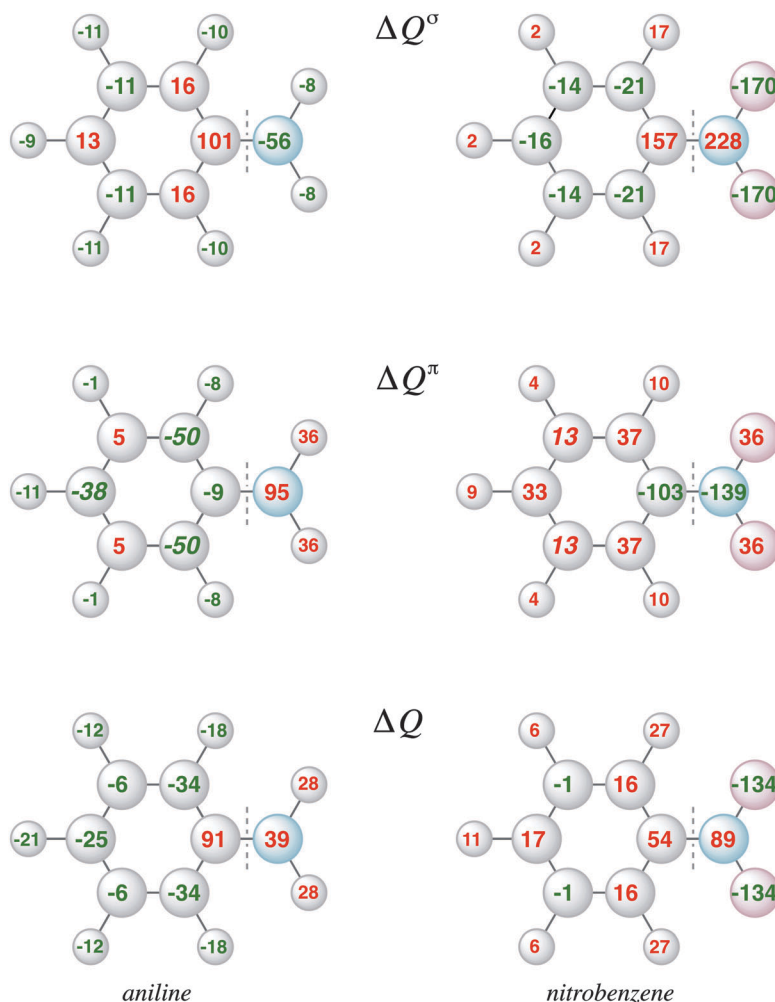


Fig. 5 VDD electronic redistribution (ΔQ) and the partitioning in the ΔQ^σ and ΔQ^π components caused by the formation of the C–N bond in aniline (left) and nitrobenzene (right) from the fragments Ph^\bullet and $^\bullet\text{NH}_2$ and $^\bullet\text{NO}_2$ respectively.

the phenyl ring of aniline to be activated with the largest electronic charge accumulations on the *ortho* and *para* positions, and the phenyl ring of nitrobenzene to be deactivated with the smallest electronic charge depletions at the *meta* positions. Decomposition into σ and π charge rearrangements, shown in Fig. 5, reveals that the π electronic system, and thus the π bond formation, is responsible for the regioselectivity of electrophilic substitution, which is in line with previous research.^{6c} Negative numbers on the atoms mean an accumulation of π -electron density on those atoms and positive numbers mean a depletion of π -electron density at atoms. The π C–N bond formation in aniline causes ΔQ^π to become more negative at the *ortho* and *para* positions (–50 and –38 milli-electrons) experimentally leading to a mixture of *ortho* and *para* products, and in nitrobenzene to become more positive at all positions, but less positive at the *meta* position (only 13 millielectrons are lost at the *meta* position), thus the nitro group is a deactivating *meta*-directing substituent.^{15,16} The VDD electronic rearrangements are in line with the experimentally observed regioselectivity of electrophilic aromatic substitution. To determine

which factor is more important, orbital interactions or charge redistribution, an additional investigation of the transition state of an electrophile with the substituted benzene is necessary.

Moreover, the VDD charge rearrangements allow for decomposition into the charge rearrangements caused by the Pauli repulsion and orbital interactions. As aniline and nitrobenzene are C_{2v} symmetric molecules, we decomposed the π charge rearrangements into the A2 and B1 contributions. Only the B1 charge rearrangements are caused by the C–N bond formation, whereas the A2 charge rearrangements are only due to polarization (no A2 orbital has amplitude on the atoms lying on the C_2 symmetry axis). Fig. 6 and 7 clearly show that the directionality of the electrophilic substitution is caused by the B1 charge rearrangements in the orbital interactions, $\Delta Q_{\text{oi}}^{\text{B1}}$. The largest charge accumulations of $\Delta Q_{\text{oi}}^{\text{B1}}$ are at the *ortho* and *para* positions for aniline and the largest charge depletions of $\Delta Q_{\text{oi}}^{\text{B1}}$ are at the *ortho* and *para* positions for nitrobenzene. For aniline, this finding confirms our results from the molecular orbital analysis, whereas for nitrobenzene the VDD charge

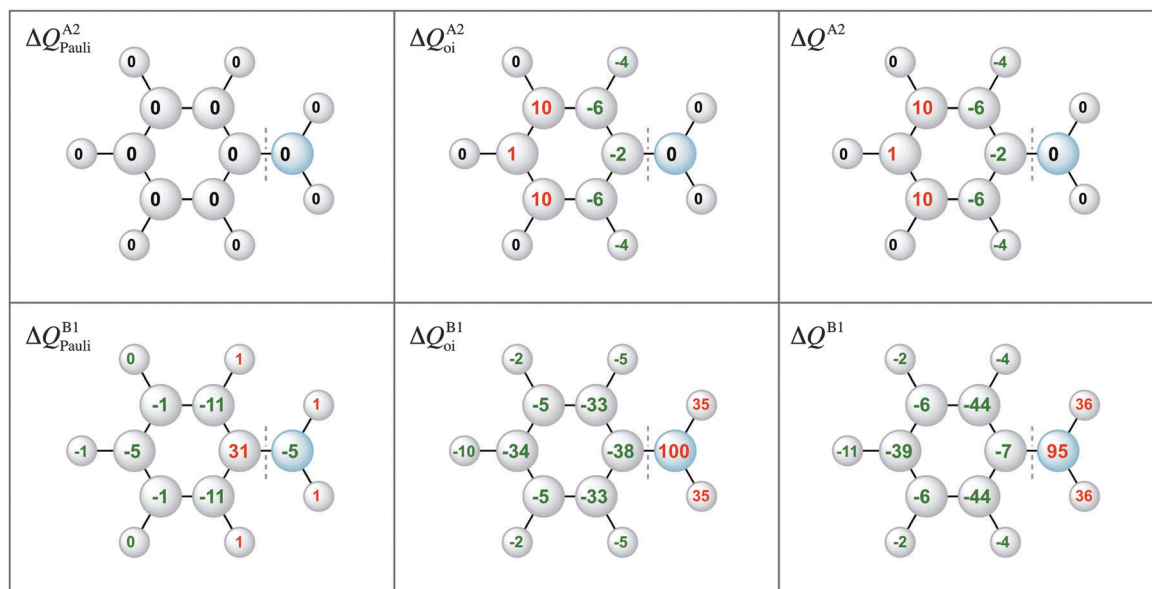
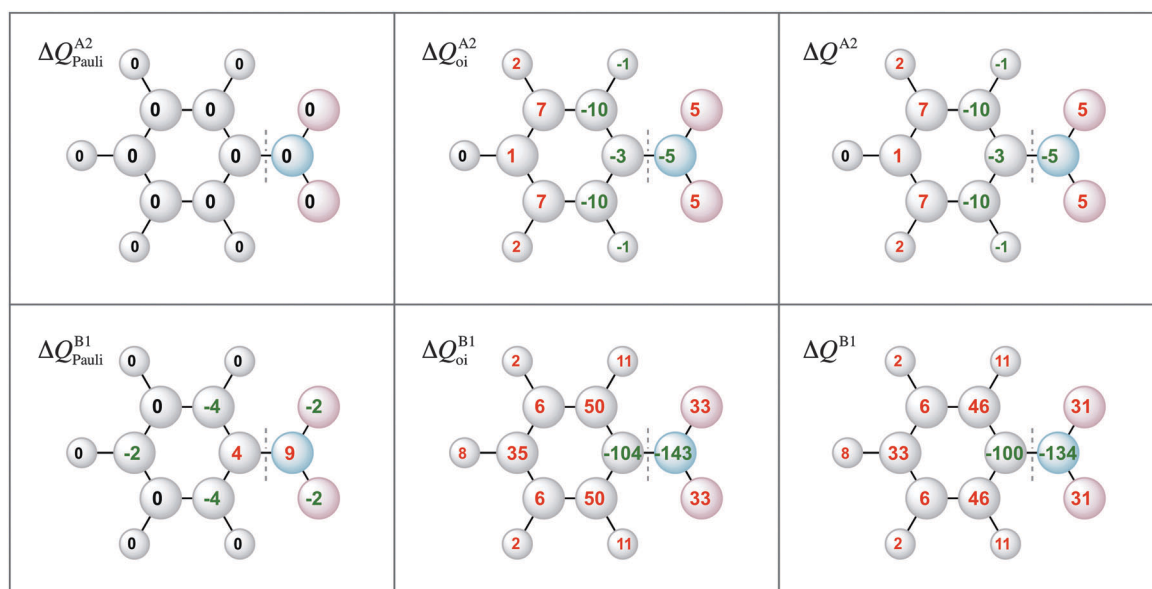


Fig. 7 VDD electronic redistribution (ΔQ) in the A2, B1 irreducible representations of the π system due to Pauli repulsion and the orbital interaction for nitrobenzene caused by the formation of the C–N bond from the fragments Ph^\bullet and $^\bullet\text{NO}_2$.



system of benzene caused by the formation of the C–N bond. The computations revealed that the C–N bond in aniline is stronger and shorter than in nitrobenzene. With our quantitative Kohn–Sham molecular orbital (KS-MO) model and the corresponding energy decomposition analysis (EDA) we explained that the NH₂ group can approach the phenyl ring closer than the NO₂ group because there is less Pauli repulsion between the hydrogen atoms of NH₂ and the hydrogen atoms of the phenyl radical at the *ortho* positions, whereas these

In this paper, we studied using density functional theory the substituent effect of NH₂ and NO₂ groups on the electronic

hydrogen atoms experience Pauli repulsion with the lone pairs of the oxygen atoms of NO₂. We separated the inductive and resonance effects. The σ component of the C–N bond formation shows for both substituents the inductive effect whereby the phenyl ring donates electronic density to the substituent. In the π electronic system, the effects of the substituents are opposite: NH₂ donates the electronic charge, whereas NO₂ accepts the electronic charge from the π system of the phenyl radical.

The donor–acceptor interactions from the π_{HOMO} of $\bullet\text{NH}_2$ to the π_{LUMO} of the phenyl radical for the C–N bond formation in aniline are accompanied by the repulsive interaction between the two π HOMOs on the two fragments. It is this repulsive interaction between the occupied orbitals, which pushes up the π_{HOMO} on the phenyl ring of aniline and activates it to electrophilic substitution. The directionality of aniline can be understood from the 2p_z contributions (located on the unsubstituted carbon atoms) to the π_{HOMO} of aniline, which have the largest amplitude at the *ortho* and *para* positions.

In the case of nitrobenzene, the donor–acceptor interactions lead to a lowering of the π_{HOMO} on the phenyl ring, which deactivates this orbital. Further inspection of the π_{HOMO} and $\pi_{\text{HOMO}-1}$ orbitals does not explain the directionality of nitrobenzene clearly. It is the VDD charge analysis which shows that the π electronic rearrangements due to C–N bond formation in nitrobenzene are responsible for the largest deactivation at the *ortho* and *para* positions of nitrobenzene, making the nitro group *meta* directing for electrophilic aromatic substitution.

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