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# Modeling Gas Solubilities in the Aqueous Solution of Methyldiethanolamine

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**ABSTRACT:** A thermodynamically consistent model recently developed for representing CO<sub>2</sub> solubility in aqueous solutions of methyldiethanolamine is extended to include H<sub>2</sub>S and lower hydrocarbons. The electrolyte–nonrandom two-liquid (NRTL) activity coefficient model and the PC-SAFT equation of state are used to represent the liquid phase and the vapor phase nonideality, respectively. The Henry's constant of H<sub>2</sub>S in water is fitted to the total pressure data of the H<sub>2</sub>S–H<sub>2</sub>O binary system. The NRTL binary interaction parameters of the solvent–electrolyte binaries are regressed with the VLE data of the H<sub>2</sub>S–H<sub>2</sub>O–MDEA ternary system. The differential heat of H<sub>2</sub>S absorption of the H<sub>2</sub>S–H<sub>2</sub>O–MDEA ternary system and the partial pressures of H<sub>2</sub>S and CO<sub>2</sub> of the H<sub>2</sub>S–CO<sub>2</sub>–H<sub>2</sub>O–MDEA quaternary system are predicted and compared favorably to the experimental data. The Henry's constants of light hydrocarbons in water and MDEA are also determined by fitting the total pressure data of the hydrocarbon–H<sub>2</sub>O binary and the hydrocarbon–H<sub>2</sub>O–MDEA ternary systems.

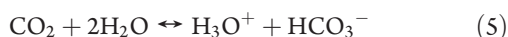
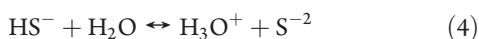
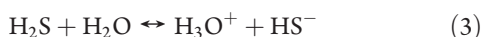
## 1. INTRODUCTION

Aqueous methyldiethanolamine (MDEA) solutions are widely used in the natural gas industry to strip acid gases (CO<sub>2</sub> and H<sub>2</sub>S) from natural gas. Design of gas treating processes with aqueous MDEA solutions requires accurate vapor–liquid equilibrium (VLE) and enthalpy calculations for the acid gas–H<sub>2</sub>O–MDEA system. Solubilities of light hydrocarbons in aqueous MDEA solutions are also important as they determine the magnitude of loss of hydrocarbon in the gas treating process. In this work, we extend our recent modeling work on the CO<sub>2</sub>–H<sub>2</sub>O–MDEA system<sup>1</sup> to H<sub>2</sub>S and hydrocarbons in aqueous MDEA solutions. This extended model should provide accurate VLE and enthalpy calculations for process modeling and simulation of natural gas treating processes with aqueous MDEA solutions.

## 2. THERMODYNAMIC MODEL

The acid gas solubility in aqueous amine solutions is determined by both its physical solubility and the chemical equilibrium of the aqueous phase ionic reactions among the acid gases, water, and amines.

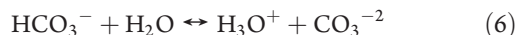
In aqueous solutions, acid gases H<sub>2</sub>S and CO<sub>2</sub> react with MDEA. The ionic equilibrium reactions are expressed as



**Table 1. Parameters for the PC-SAFT Equation of State<sup>a</sup>**

	<i>m</i>	$\epsilon$ (K)	$\sigma$ (Å)	$\epsilon^{AB}$ (K)	$k^{AB}$ (Å <sup>3</sup> )	source
H <sub>2</sub> S	1.6631	229.3	3.0404	0	0	Aspen databank <sup>7</sup>
H <sub>2</sub> O	1.0656	366.51	3.0007	2500.7	0.034868	Gross and Sadowski <sup>6</sup>
MDEA	3.3044	237.44	3.5975	3709.9	0.066454	Zhang and Chen <sup>1</sup>
CO <sub>2</sub>	2.5692	152.10	2.5637	0	0	Aspen databank <sup>7</sup>
CH <sub>4</sub>	1.0	150.03	3.7039	0	0	Aspen databank <sup>7</sup>
C <sub>2</sub> H <sub>6</sub>	1.6069	191.42	3.5206	0	0	Aspen databank <sup>7</sup>
C <sub>3</sub> H <sub>8</sub>	2.0020	208.11	3.6184	0	0	Aspen databank <sup>7</sup>
C <sub>4</sub> H <sub>10</sub>	2.3316	222.88	3.7086	0	0	Aspen databank <sup>7</sup>

<sup>a</sup> Definitions: *m*, segment number parameter;  $\epsilon$ , segment energy parameter;  $\sigma$ , segment size parameter;  $\epsilon^{AB}$ , association energy parameter;  $k^{AB}$ , effective association volume parameter.



The liquid phase compositions must satisfy the chemical equilibrium relationships:

$$K_j = \frac{\prod_i (x_i \gamma_i)^{\nu_i}}{\prod_i (x_i \gamma_i)^{\nu_i}} \quad (7)$$

where  $K_j$  is the chemical equilibrium constant of reaction *j*;  $x_i$  is the mole fraction of reactant component *i* in reaction *j*;  $x_{i'}$  is the mole fraction of product component *i'* in reaction *j*;  $\gamma_i$  and  $\gamma_{i'}$  are the symmetric activity coefficients of solvents, that is, water and amines,

**Received:** October 23, 2010

**Accepted:** March 30, 2011

**Revised:** March 24, 2011

Table 2. Summary of Model Parameters for the H<sub>2</sub>S–H<sub>2</sub>O–MDEA System

parameters	component	source
Antoine equation parameter	MDEA	Zhang and Chen <sup>1</sup>
heat of vaporization, $\Delta_{\text{vap}}H$	MDEA	Zhang and Chen <sup>1</sup>
dielectric constant, $\epsilon$	MDEA	Aspen Databank <sup>7</sup>
ideal gas Gibbs energy of formation at 298.15 K, $\Delta_f G_{298.15}^{\text{ig}}$	H <sub>2</sub> O, MDEA, H <sub>2</sub> S	Aspen Databank <sup>7</sup>
ideal gas enthalpy of formation at 298.15 K, $\Delta_f H_{298.15}^{\text{ig}}$	H <sub>2</sub> O, MDEA, H <sub>2</sub> S	Aspen Databank <sup>7</sup>
ideal gas heat capacity, $C_p^{\text{ig}}$	H <sub>2</sub> O, H <sub>2</sub> S	Aspen Databank <sup>7</sup>
	MDEA	Zhang and Chen <sup>1</sup>
molality scale Gibbs energy of formation in aqueous phase infinite dilution at 298.15 K, $\Delta_f G_{298.15}^{\infty, \text{aq}}$	H <sub>3</sub> O <sup>+</sup> , OH <sup>−</sup> , HS <sup>−</sup> , S <sup>−2</sup>	Aspen Databank <sup>7</sup> and Wagman et al. <sup>8</sup>
	MDEAH <sup>+</sup>	Zhang and Chen <sup>1</sup>
enthalpy of formation in aqueous phase infinite dilution at 298.15 K, $\Delta_f H_{298.15}^{\infty, \text{aq}}$	H <sub>3</sub> O <sup>+</sup> , OH <sup>−</sup> , HS <sup>−</sup> , S <sup>−2</sup>	Aspen Databank <sup>7</sup> and Wagman et al. <sup>8</sup>
	MDEAH <sup>+</sup>	Zhang and Chen <sup>1</sup>
heat capacity in aqueous phase infinite dilution, $C_p^{\infty, \text{aq}}$	H <sub>3</sub> O <sup>+</sup> , OH <sup>−</sup>	Aspen Databank <sup>7</sup>
	HS <sup>−</sup> , S <sup>−2</sup>	Criss and Cobble <sup>9</sup>
	MDEAH <sup>+</sup>	Zhang and Chen <sup>1</sup>
PC-SAFT parameters, $m$ , $\epsilon$ , $\sigma$ , $\epsilon^{\text{AB}}$ , $k^{\text{AB}}$ for the pure component and $k^{ij}$ for binary	H <sub>2</sub> O	Gross and Sadowski <sup>6</sup>
	MDEA	Zhang and Chen <sup>1</sup>
	H <sub>2</sub> S	Aspen databank <sup>7</sup>
	H <sub>2</sub> O–MDEA binary, H <sub>2</sub> S–H <sub>2</sub> O binary, H <sub>2</sub> S–MDEA binary	set to zero
Henry's constant parameter	H <sub>2</sub> S in H <sub>2</sub> O	regression <sup>a</sup>
	H <sub>2</sub> S in MDEA	this work
Brelvi–O'Connell characteristic volume, $V^{\text{BO}}$	H <sub>2</sub> O, MDEA, H <sub>2</sub> S,	Aspen databank <sup>7</sup>
NRTL binary parameters	H <sub>2</sub> S–H <sub>2</sub> O binary	set to zero
	MDEA–H <sub>2</sub> O binary	Zhang and Chen <sup>1</sup>
	H <sub>2</sub> O–(MDEAH <sup>+</sup> , HS <sup>−</sup> ) binary, MDEA–(MDEAH <sup>+</sup> , HS <sup>−</sup> ) binary	regression <sup>b</sup>

<sup>a</sup> Data used for regression: VLE data of H<sub>2</sub>S–H<sub>2</sub>O binary. <sup>b</sup> Data used for regression: VLE data of H<sub>2</sub>S–H<sub>2</sub>O–MDEA ternary.

Table 3. Parameters for Reference State Properties (in J kmol<sup>−1</sup>)

property	$\Delta_f G_{298.15}^{\text{ig}}$	$\Delta_f H_{298.15}^{\text{ig}}$	$\Delta_f G_{298.15}^{\infty, \text{aq}}$	$\Delta_f H_{298.15}^{\infty, \text{aq}}$	source
H <sub>2</sub> S	$-3.3440 \times 10^7$	$-2.0630 \times 10^7$			Aspen Databank <sup>7</sup>
H <sub>2</sub> O	$-2.2859 \times 10^8$	$-2.4181 \times 10^8$			Aspen Databank <sup>7</sup>
MDEA	$-1.6900 \times 10^8$	$-3.8000 \times 10^8$			Aspen Databank <sup>7</sup>
CO <sub>2</sub>	$-3.9437 \times 10^8$	$-3.9351 \times 10^8$			Aspen Databank <sup>7</sup>
HS <sup>−</sup>			$1.2080 \times 10^7$	$-1.7600 \times 10^7$	Wagman et al. <sup>8</sup>
S <sup>−2</sup>			$8.5800 \times 10^7$	$3.3100 \times 10^7$	Wagman et al. <sup>8</sup>
H <sub>3</sub> O <sup>+</sup>			$-2.3713 \times 10^8$	$-2.8583 \times 10^8$	Aspen Databank <sup>7</sup>
OH <sup>−</sup>			$-1.5724 \times 10^8$	$-2.2999 \times 10^8$	Wagman et al. <sup>8</sup>
MDEAH <sup>+</sup>			$-2.5952 \times 10^8$	$-5.1095 \times 10^8$	Zhang and Chen <sup>1</sup>
HCO <sub>3</sub> <sup>−</sup>			$-5.8677 \times 10^8$	$-6.9199 \times 10^8$	Wagman et al. <sup>8</sup>
CO <sub>3</sub> <sup>−2</sup>			$-5.2781 \times 10^8$	$-6.7714 \times 10^8$	Wagman et al. <sup>8</sup>

Table 4. Antoine Equation Parameters for Pure MDEA<sup>a</sup>

	$C_{1i}$	$C_{2i}$	$C_{3i}$	$C_{4i}$	source
MDEA	$1.2276 \times 10^2$	$-1.3253 \times 10^4$	$-1.3839 \times 10^1$	$3.20 \times 10^{-6}$	Aspen Databank <sup>7</sup>

<sup>a</sup> Correlation for Antoine equation,  $\ln(P_i^*/Pa) = C_{1i} + (C_{2i})/(T(K)) + C_{3i} \ln(T(K)) + C_{4i}(T(K))^2$ .

41 and the unsymmetric activity coefficients of molecular or ionic  
42 solutes  $i$  and  $i'$  in aqueous solution and are normalized to the

aqueous phase infinite dilution reference state; and  $\nu_i$  and  $\nu_{i'}$  are the  
stoichiometric coefficients of reactants and products, respectively.

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44

Chemical equilibrium constants for the ionic reactions can be calculated from the reference state Gibbs energies of the participating species:

$$-RT \ln K_j = \Delta G_j^\circ(T) \quad (8)$$

where  $\Delta G_j^\circ(T)$  is the reference state Gibbs energy change for reaction  $j$  at temperature  $T$ ,  $R$  is the universal gas constant, and  $T$  is the system temperature.

**Table 5. Parameters for Heat of Vaporization<sup>a</sup>**

	$C_{1i}$	$C_{2i}$	$T_{ci}$	source
MDEA	$9.7381 \times 10^7$	$4.6391 \times 10^{-1}$	741.9	Aspen Databank <sup>7</sup>

<sup>a</sup>DIPPR equation for heat of vaporization,  $\Delta_{\text{vap}}H_i/\text{J kmol}^{-1} = C_{1i}(1 - T_{ri})^{C_{2i}}$ ,  $T_{ri} = (T(\text{K}))/T_{ci}(\text{K})$ ,  $T_{ci}$  is critical temperature of component  $i$ .

**Table 6. Parameters for Dielectric Constant<sup>a</sup>**

	$A_i$	$B_i$	$C_i$	source
MDEA	21.9957	8992.68	298.15	Aspen Databank <sup>7</sup>

<sup>a</sup>Correlation for dielectric constant,  $\epsilon_i = A_i + B_i(1/(T(\text{K})) - 1/(C_i))$

**Table 7. Parameters for Henry's constant<sup>a</sup>**

solute	solvent	$a_{ij}$	$b_{ij}$	$c_{ij}$	$d_{ij}$	source
$i$	$j$					
H <sub>2</sub> S	H <sub>2</sub> O	151.031	-6415.26	-20.3806	0.01476	this work
H <sub>2</sub> S	MDEA	151.031	-6415.26	-20.3806	0.01476	this work <sup>b</sup>
CO <sub>2</sub>	H <sub>2</sub> O	100.65	-6147.7	-10.191	-0.010	Yan and Chen <sup>10</sup>
CO <sub>2</sub>	MDEA	19.8933	-1072.7	0.0	0.0	Zhang and Chen <sup>1</sup>
CH <sub>4</sub>	H <sub>2</sub> O	188.529	-8720.4	-24.072	0	this work
CH <sub>4</sub>	MDEA	-19.586	-2401.0	-5.765	0	this work
C <sub>2</sub> H <sub>6</sub>	H <sub>2</sub> O	247.809	-11988.3	-32.592	0	this work
C <sub>2</sub> H <sub>6</sub>	MDEA	-23.905	2435.5	6.111	0	this work
C <sub>3</sub> H <sub>8</sub>	H <sub>2</sub> O	350.878	-17129.0	-47.638	0	this work
C <sub>3</sub> H <sub>8</sub>	MDEA	-216.864	12221.1	34.167	0	this work
C <sub>4</sub> H <sub>10</sub>	H <sub>2</sub> O	898.953	-44053.7	-127.985	0	this work
C <sub>4</sub> H <sub>10</sub>	MDEA	-345.518	20003.5	52.064	0	this work

<sup>a</sup>Correlation for Henry's constant,  $\ln(H_{ij}/P_a) = a_{ij} + b_{ij}/(T(\text{K})) + c_{ij}/(T(\text{K}))^2 + d_{ij}/(T(\text{K}))^3$ . <sup>b</sup>Henry's constant of H<sub>2</sub>S in MDEA is set to be same as that of H<sub>2</sub>S in water.

**Table 8. Parameters for Ideal Gas Heat Capacity (in J kmol<sup>-1</sup>·K<sup>-1</sup>)<sup>a</sup>**

	H <sub>2</sub> S <sup>b</sup>	MDEA	H <sub>2</sub> O	CO <sub>2</sub>
source	Aspen Databank <sup>7</sup>	Zhang and Chen <sup>1</sup>	Aspen Databank <sup>7</sup>	Aspen Databank <sup>7</sup>
$C_{1i}$	$3.3288 \times 10^4$	$2.7303 \times 10^4$	$3.3738 \times 10^4$	$1.9795 \times 10^4$
$C_{2i}$	$2.6086 \times 10^4$	$5.4087 \times 10^2$	-7.0176	$7.3437 \times 10^1$
$C_{3i}$	$9.134 \times 10^2$	0	$2.7296 \times 10^{-2}$	$-5.6019 \times 10^{-2}$
$C_{4i}$	$-1.7979 \times 10^4$	0	$-1.6647 \times 10^{-5}$	$1.7153 \times 10^{-5}$
$C_{5i}$	$9.494 \times 10^2$	0	$4.2976 \times 10^{-9}$	0
$C_{6i}$	0	0	$-4.1696 \times 10^{-13}$	0
$C_{7i}$	100	278	200	300
$C_{8i}$	1500	397	3000	1088.6

<sup>a</sup>Correlation for ideal gas heat capacity,  $C_p^{\text{ig}}/\text{J kmol}^{-1}\text{K}^{-1} = C_{1i} + C_{2i}(T(\text{K})) + C_{3i}(T(\text{K}))^2 + C_{4i}(T(\text{K}))^3 + C_{5i}(T(\text{K}))^4 + C_{6i}(T(\text{K}))^5$ ,  $C_{7i} < T < C_{8i}$ . <sup>b</sup>Correlation for ideal gas heat capacity of H<sub>2</sub>S,  $C_p^{\text{ig}}/\text{J kmol}^{-1}\text{K}^{-1} = C_{1i} + C_{2i}((C_{3i}/(T(\text{K}))) / (\sinh(C_{3i}/(T(\text{K}))))^2 + C_{4i}((C_{5i}/(T(\text{K}))) / (\cosh(C_{5i}/(T(\text{K}))))^2$ ,  $C_{7i} < T < C_{8i}$

**Table 9. Parameters for Aqueous Phase Infinite Dilution Heat Capacity<sup>a</sup>**

	$C_1$	Source
HS <sup>-</sup>	$-1.5884 \times 10^5$	this work
S <sup>-2</sup>	$-4.0061 \times 10^4$	this work
H <sub>3</sub> O <sup>+</sup>	$7.5291 \times 10^4$	Aspen Databank <sup>7</sup>
OH <sup>-</sup>	$-1.4845 \times 10^5$	Aspen Databank <sup>7</sup>
MDEAH <sup>+</sup>	$3.3206 \times 10^5$	Zhang and Chen <sup>1</sup>
HCO <sub>3</sub> <sup>-</sup>	$-2.9260 \times 10^4$	Zhang and Chen <sup>1</sup>
CO <sub>3</sub> <sup>-2</sup>	$-3.9710 \times 10^5$	Zhang and Chen <sup>1</sup>

<sup>a</sup>Correlation for aqueous phase infinite dilution heat capacity,  $C_{p,i}^{\text{aq}}/\text{J kmol}^{-1}\text{K}^{-1} = C_1$ . <sup>b</sup> $C_{p,i}^{\text{aq}}$  value of HS<sup>-</sup> is the average value of heat capacity between 298 and 473 K taken from Criss and Cobble (1968),<sup>9</sup> and that of S<sup>-2</sup> is calculated from the Criss-Cobble correlation<sup>9</sup> with the entropy value from Wagman et al. (1982).<sup>8</sup>

**Table 10. Parameters of the Characteristic Volume (in m<sup>3</sup> kmol<sup>-1</sup>) for the Brelvi-O'Connell Model<sup>a</sup>**

	$v_1$	$v_2$	source
H <sub>2</sub> S	0.0985	0	Aspen Databank <sup>7</sup>
H <sub>2</sub> O	0.464	0	Aspen Databank <sup>7</sup>
MDEA	0.369	0	Aspen Databank <sup>7</sup>
CO <sub>2</sub>	0.177	$-3.42 \times 10^{-4}$	Yan and Chen <sup>10</sup>
CH <sub>4</sub>	0.0736	0	this work
C <sub>2</sub> H <sub>6</sub>	0.1393	0	this work
C <sub>3</sub> H <sub>8</sub>	0.2000	0	Aspen Databank <sup>7</sup>
C <sub>4</sub> H <sub>10</sub>	0.2550	0	Aspen Databank <sup>7</sup>

<sup>a</sup>Correlation for the characteristic volume parameters,  $V_i^{\text{BO}}(\text{m}^3 \text{ kmol}^{-1}) = v_1 + v_2(T(\text{K}))$ .

**Table 11. NRTL parameters  $\tau_{ij}$ <sup>a</sup> for MDEA-H<sub>2</sub>O Binary with  $\alpha = 0.2$**

parameter	component i	component j	value	source
$a_{ij}$	H <sub>2</sub> O	MDEA	8.5092	Zhang and Chen <sup>1</sup>
$a_{ij}$	MDEA	H <sub>2</sub> O	-1.7141	
$b_{ij}$	H <sub>2</sub> O	MDEA	-1573.9	
$b_{ij}$	MDEA	H <sub>2</sub> O	-261.85	

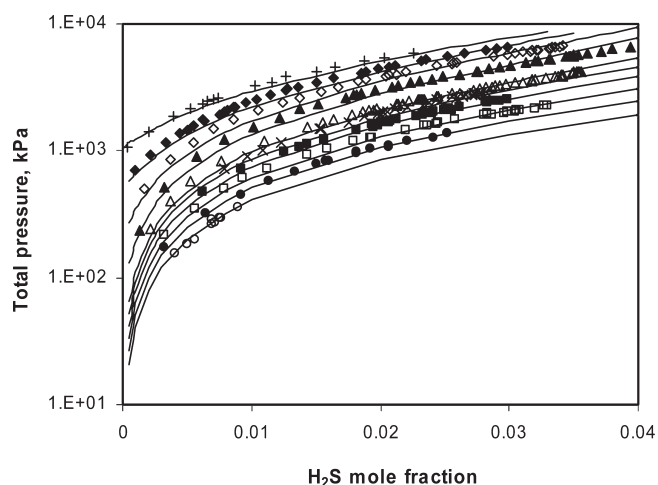
<sup>a</sup>Correlation for the NRTL parameters,  $\tau_{ij} = a_{ij} + b_{ij}/(T(\text{K}))$

**Table 12. NRTL Parameters  $\tau_{ij}$  for Molecule-Electrolyte Binaries with  $\alpha = 0.2$**

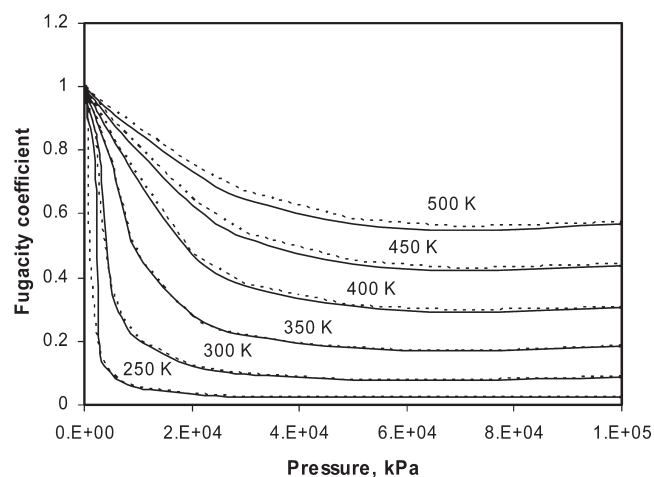
component i	component j	value	source
H <sub>2</sub> O	(MDEAH <sup>+</sup> , HCO <sub>3</sub> <sup>-</sup> )	8.7170	Zhang and Chen <sup>1</sup>
(MDEAH <sup>+</sup> , HCO <sub>3</sub> <sup>-</sup> )	H <sub>2</sub> O	-4.2995	
H <sub>2</sub> O	(MDEAH <sup>+</sup> , CO <sub>3</sub> <sup>-2</sup> )	10.4032	
(MDEAH <sup>+</sup> , CO <sub>3</sub> <sup>-2</sup> )	H <sub>2</sub> O	-4.9252	
MDEA	(MDEAH <sup>+</sup> , HCO <sub>3</sub> <sup>-</sup> )	5.2964	
(MDEAH <sup>+</sup> , HCO <sub>3</sub> <sup>-</sup> )	MDEA	-0.8253	
H <sub>2</sub> O	(MDEAH <sup>+</sup> , HS <sup>-</sup> )	4.0564	this work
(MDEAH <sup>+</sup> , HS <sup>-</sup> )	H <sub>2</sub> O	-1.7522	
MDEA	(MDEAH <sup>+</sup> , HS <sup>-</sup> )	7.4499	
(MDEAH <sup>+</sup> , HS <sup>-</sup> )	MDEA	-1.9446	

Table 13. Experimental Data Used in the Regression for the H<sub>2</sub>S–H<sub>2</sub>O System

data type	T (K)	P (kPa)	H <sub>2</sub> S mole fraction	data points	average relative deviation, $ \Delta P/P $ (%)	reference
VLE, TPx, total pressure	278–333	37–494	0.0006–0.007	34	7.1	Wright and Maass <sup>11</sup>
VLE, TPx, total pressure	303–316	1720	0.019–0.025	15	5.4	Pohl <sup>12</sup>
VLE, TPx, total pressure	303–443	1720–2340	0.005–0.03	39	9.8	Burgess and Germann <sup>13</sup>
VLE, TPx, total pressure	273–323	47–96	0.0005–0.003	36	5.8	Clarke and Glew <sup>14</sup>
VLE, TPx, total pressure	283–453	155–6670	0.0003–0.037	325	5.5	Lee and Mather <sup>15</sup>
VLE, TPx, total pressure	311–478	345–10300	0.004–0.041	12	7.6	Gillespie and Wilson <sup>16</sup>
VLE, TPx, total pressure	294–594	222–13900	0.002–0.016	49	10.5	Suleimenov and Krupp <sup>17</sup>
VLE, TPx, total pressure	313	470–2490	0.006–0.03	9	4.2	Kuranov et al. <sup>18</sup>



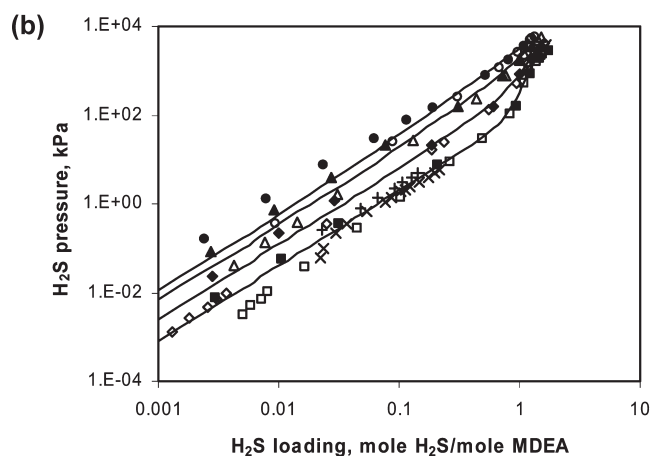
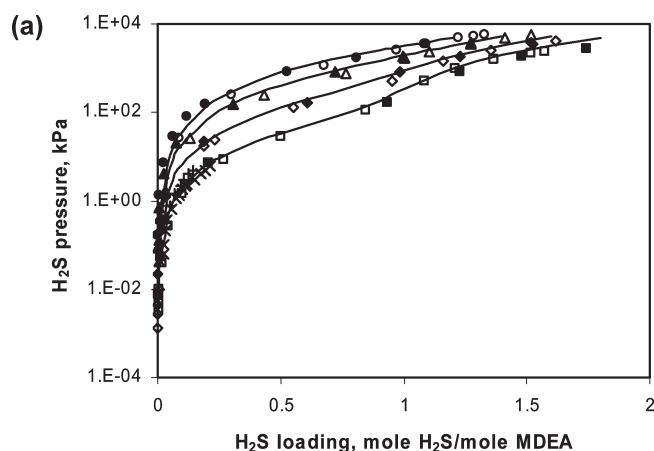
**Figure 1.** Comparison of the experimental data from Lee and Mather<sup>15</sup> (symbols) for total pressure of binary H<sub>2</sub>S–H<sub>2</sub>O solution and the model results (lines): (○)  $T = 283$ , (●)  $T = 293$ , (□)  $T = 303$ , (■)  $T = 313$ , (×)  $T = 323$ , (△)  $T = 333$ , (▲)  $T = 363$ , (◇)  $T = 393$ , (◆)  $T = 423$ , (+)  $T = 453$  K.



**Figure 2.** Vapor phase fugacity coefficient for pure H<sub>2</sub>S: (solid line) PC-SAFT results, (dotted line) GERG2008 results.

The physical solubility of the acid gas is calculated from Henry's law:

$$P \cdot y_i \cdot \phi_i = H_i \cdot x_i \cdot \gamma_i^* \quad (9)$$



**Figure 3.** Comparison of the experimental data (symbols) and the model results (lines) for H<sub>2</sub>S partial pressure of H<sub>2</sub>S–H<sub>2</sub>O–MDEA solution. MDEA mole fraction is 0.13. The empty symbols represent the experimental data from Jou et al.<sup>20</sup> (□)  $T = 313$ , (◇)  $T = 343$ , (△)  $T = 373$ , (○)  $T = 393$  K; the full symbols represent the experimental data from Huang and Ng,<sup>26</sup> (■)  $T = 313$ , (◆)  $T = 343$ , (▲)  $T = 373$ , (●)  $T = 393$  K; (×) experimental data of Jou et al.<sup>24</sup> at 313 K; (+) experimental data of ter Maat et al.<sup>22</sup> at 313 K.

where  $P$  is the system pressure,  $y_i$  is the mole fraction of component  $i$  in the vapor phase,  $\phi_i$  is the fugacity coefficient of component  $i$  in the vapor phase,  $H_i$  is the Henry's law constant of component  $i$  in the mixed solvent of water and amine,  $x_i$  is the equilibrium mole fraction of component  $i$  in the liquid phase, and  $\gamma_i^*$  is the unsymmetric activity coefficient of component  $i$  in the mixed solvent solution of water and amine

Table 14. Experimental Data Used in the Regression for the H<sub>2</sub>S–H<sub>2</sub>O–MDEA System

data type	T (K)	P (kPa)	MDEA mole fraction	H <sub>2</sub> S loading	data points	average relative deviation, $ \Delta P/P $ (%)	reference
VLE, $TP_x$ , H <sub>2</sub> S pressure	298–393	0.13–5900	0.02–0.13	0.0076–3.2	108	31.9	Jou et al. <sup>20</sup>
VLE, $TP_x$ , H <sub>2</sub> S pressure	298–389	13–1500	0.02–0.036	0.18–2.17	49	13.0	Maddox et al. <sup>21</sup>
VLE, $TP_x$ , H <sub>2</sub> S pressure	283–313	0.14–19	0.075–0.131	0.02–0.57	37	29.5	ter Maat et al. <sup>22</sup>

Table 15. Comparison between Experimental Data and Model Predictions for Total Pressure or H<sub>2</sub>S Partial Pressure of the H<sub>2</sub>S–H<sub>2</sub>O–MDEA System

data type	T (K)	P (kPa)	MDEA mole fraction	H <sub>2</sub> S loading	data points	average relative deviation, $ \Delta P/P $ (%)	reference
VLE, $TP_x$ , H <sub>2</sub> S pressure	313	0.5–1600	0.045	0.13–1.73	27	64.7	Macgregor and Mather <sup>23</sup>
VLE, $TP_x$ , H <sub>2</sub> S pressure	313–373	0.002–310	0.075–0.13	0.004–1.08	50	34.5	Jou et al. <sup>24</sup>
VLE, $TP_x$ , H <sub>2</sub> S pressure	313–373	1.5–450	0.062	0.08–0.90	43	45.1	Li and Shen <sup>25</sup>
VLE, $TP_x$ , total pressure	313–413	170–4900	0.034–0.067	0.48–1.93	71	9.4	Kuranov et al. <sup>18</sup>
VLE, $TP_x$ , H <sub>2</sub> S pressure	298–393	0.0013–5900	0.02–0.13	0.0013–3.2	150	27.9	Huang and Ng <sup>26</sup>
VLE, $TP_x$ , H <sub>2</sub> S pressure	298–313	0.03–1.6	0.020–0.045	0.01–0.26	29	30.4	Lemoine et al. <sup>27</sup>
VLE, $TP_x$ , total pressure	313–393	200–6000	0.126	0.15–1.43	26	12.4	Pérez-Salado Kamps et al. <sup>28</sup>
VLE, $TP_x$ , total pressure	313–373	6–1000	0.117	0–0.12	27	12.1	Sidi-Boumedine et al. <sup>29</sup>

and is normalized to the mixed solvent infinite dilution reference state.

The Henry's law constant in the mixed solvent can be calculated from those in the pure solvents:<sup>1</sup>

$$\ln\left(\frac{H_i}{\gamma_i^\infty}\right) = \sum_A w_A \ln\left(\frac{H_{iA}}{\gamma_{iA}^\infty}\right) \quad (10)$$

where  $H_i$  is the Henry's constant of molecular solute  $i$  in the mixed solvent,  $H_{iA}$  is the Henry's constant of solute  $i$  in pure solvent  $A$ ,  $\gamma_i^\infty$  is the infinite dilution activity coefficient of solute  $i$  in the mixed solvent,  $\gamma_{iA}^\infty$  is the infinite dilution activity coefficient of solute  $i$  in pure solvent  $A$ , and  $w_A$  is a weighting factor calculated by eq 11:

$$w_A = \frac{x_A(V_{iA}^\infty)^{2/3}}{\sum_B x_B(V_{iB}^\infty)^{2/3}} \quad (11)$$

where  $V_{iA}^\infty$  is the partial molar volume of solute  $i$  at infinite dilution in pure solvent  $A$ , and is calculated from the Brelvi–O'Connell model<sup>2</sup> with the characteristic volume for the solute ( $V_i^{\text{BO}}$ ) and solvent ( $V_s^{\text{BO}}$ ).

The Henry's constant of solute  $i$  in solvent  $A$  is further corrected with the Poynting term for pressure:

$$H_{iA}(T, P) = H_{iA}(T, p_A^{o,l}) \exp\left(\frac{1}{RT} \int_{p_A^{o,l}}^P V_{iA}^\infty dp\right) \quad (12)$$

where  $H_{iA}(T, P)$  is the Henry's constant of solute  $i$  in solvent  $A$  at system temperature and pressure,  $H_{iA}(T, p_A^{o,l})$  is the Henry's constant of solute  $i$  in solvent  $A$  at system temperature and the solvent vapor pressure, and  $V_{iA}^\infty$  is the partial molar volume of solute  $i$  at infinite dilution in solvent  $A$  calculated from the Brelvi–O'Connell model.

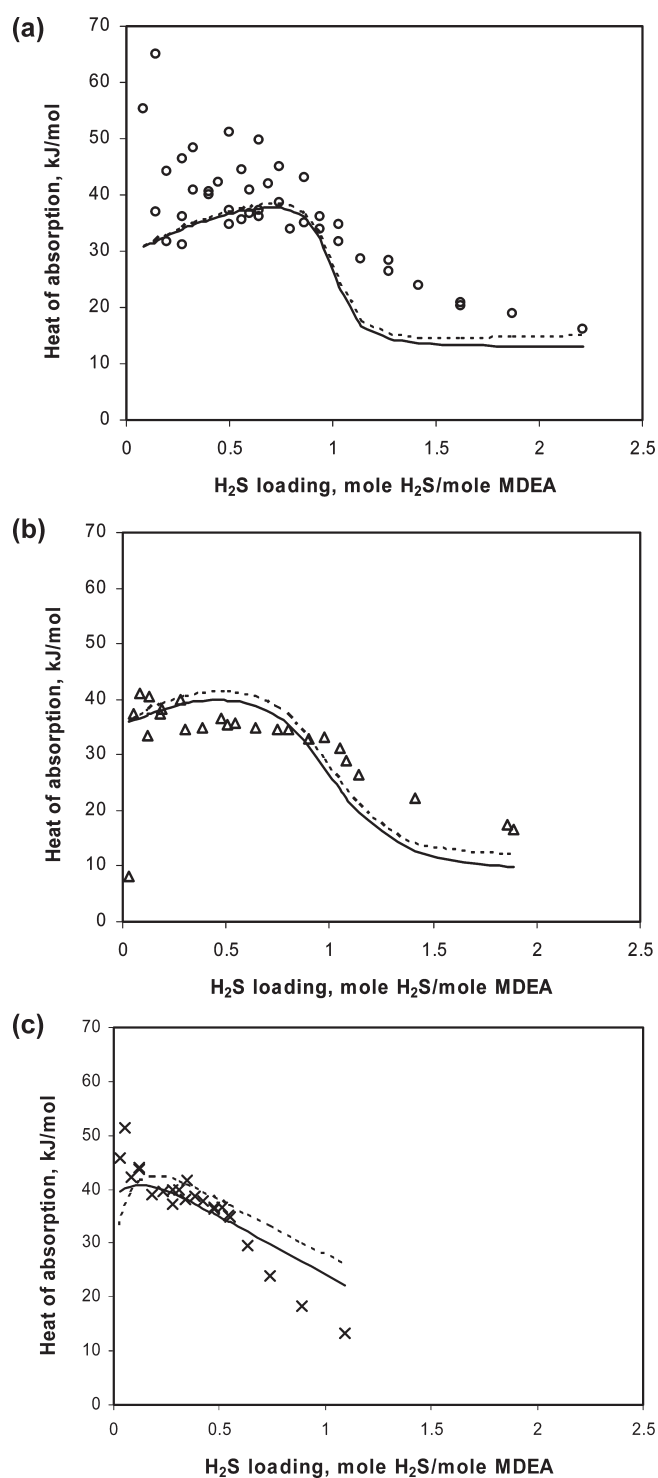
The detailed thermodynamic model for the CO<sub>2</sub>–H<sub>2</sub>O–MDEA system has been presented in an earlier work.<sup>1</sup>

We do not repeat the equations for the thermodynamic framework in this paper. The 2009 version of the electrolyte–nonrandom two-liquid (NRTL) model<sup>3,4</sup> is used to calculate activity coefficients required in the aqueous phase chemical equilibrium calculations and the mixed solvent phase equilibrium calculations. Unless specified otherwise, all molecule–molecule binary parameters and electrolyte–electrolyte binary parameters are defaulted to zero, and all molecule–electrolyte binary parameters are defaulted to (8, –4), the average values of the parameters as reported for the electrolyte NRTL model.<sup>4</sup> The nonrandomness factor,  $\alpha$ , is fixed at 0.2.

The PC-SAFT<sup>5,6</sup> equation of state (EOS) is used to calculate the vapor phase fugacity coefficients. Reported in Table 1, the PC-SAFT EOS pure component parameters are taken from our earlier work for the CO<sub>2</sub>–H<sub>2</sub>O–MDEA system,<sup>1</sup> Gross and Sadowski (2002),<sup>6</sup> and the Aspen Plus databank.<sup>7</sup> The binary PC-SAFT interaction parameters are all set to 0.

Table 2 summarizes the model parameters and the sources of the parameters used in the H<sub>2</sub>S–H<sub>2</sub>O–MDEA thermodynamic model. The model parameters include pure component parameters and thermodynamic constants for the molecular and ionic species, PC-SAFT EOS parameters, Henry's constant and Brelvi–O'Connell characteristic volume parameters, and binary interaction parameters associated with the electrolyte NRTL model. Most of the parameters can be obtained from our earlier work<sup>1</sup> and the literature;<sup>6–9</sup> the remaining parameters are determined by fitting to the experimental data. Note that while the model parameters and the sources of the parameters used in the CO<sub>2</sub>–H<sub>2</sub>O–MDEA model have been summarized in our previous work,<sup>1,10</sup> we present in this work all the model parameters required for modeling the solubilities of CO<sub>2</sub>, H<sub>2</sub>S, and light hydrocarbons in aqueous MDEA solution for completeness. In addition to the PC-SAFT parameters reported in Table 1, values of the remaining parameters are summarized in Tables 3–12.





**Figure 4.** Comparison of the experimental data from Oscarson and Izatt<sup>31</sup> (symbols) and the model results (lines) for differential heat of  $\text{H}_2\text{S}$  absorption in aqueous MDEA solution. MDEA mole fraction is 0.13. (○)  $T = 300$ , (△)  $T = 350$ , (×)  $T = 400$  K; (solid line) prediction according to enthalpy balance; (dotted line) prediction according to Gibbs–Helmholtz equation.

### 3. MODELING RESULTS

We first extend the thermodynamic model for the  $\text{CO}_2\text{--H}_2\text{O--MDEA}$  system to cover the  $\text{H}_2\text{S--H}_2\text{O--MDEA}$

system. We then predict the partial pressures of the acid gases for the  $\text{H}_2\text{S--CO}_2\text{--H}_2\text{O--MDEA}$  system based on the  $\text{CO}_2\text{--H}_2\text{O--MDEA}$  and  $\text{H}_2\text{S--H}_2\text{O--MDEA}$  models. For the hydrocarbon– $\text{H}_2\text{O--MDEA}$  system, we consider their physical solubility and fit the VLE data with the Henry's constants.

**3.1.  $\text{H}_2\text{S--H}_2\text{O}$  System.** Summarized in Table 13 are the extensive experimental total pressure data available for the  $\text{H}_2\text{S--H}_2\text{O}$  system.<sup>11–18</sup> These data cover temperature from 273 to 594 K and pressure from 37 to 13900 kPa. We use these data in the regression to determine the Henry's constant of  $\text{H}_2\text{S}$  in water. Also given in Table 13 are the excellent correlation results with average relative deviations of less than 10% for all data sets. As an example, Figure 1 shows that the total pressure data of Lee and Mather (1977)<sup>15</sup> for the  $\text{H}_2\text{S--H}_2\text{O}$  binary are represented well. The regressed parameters for the Henry's constant are given in Table 7.

To check reliability of the model predictions for  $\text{H}_2\text{S}$  solubility above 13900 kPa, we show in Figure 2 the vapor fugacity coefficients of pure  $\text{H}_2\text{S}$  calculated with the PC-SAFT EOS up to 100000 kPa and those calculated with the GERG2008 EOS.<sup>19</sup> As the GERG2008 EOS provides a high fidelity representation of the  $\text{H}_2\text{S}$  PVT data, the satisfactory match between the results of the PC-SAFT EOS and those from the GERG2008 EOS suggests the extrapolation of  $\text{H}_2\text{S}$  fugacity to high pressure with PC-SAFT is reliable.

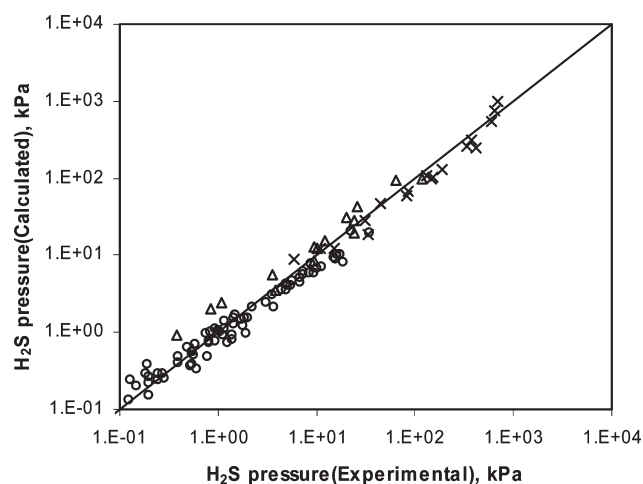
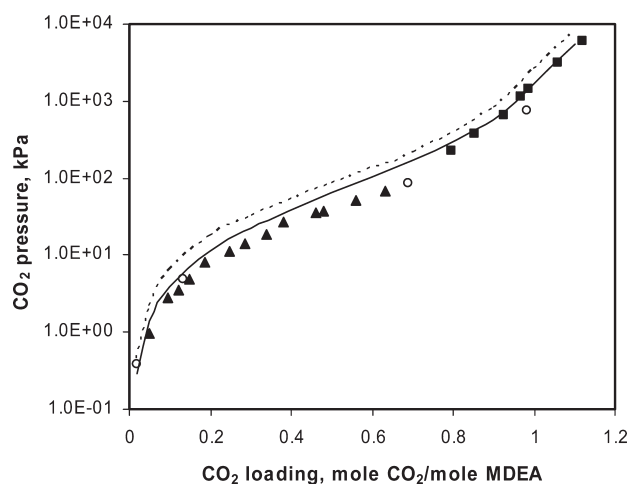
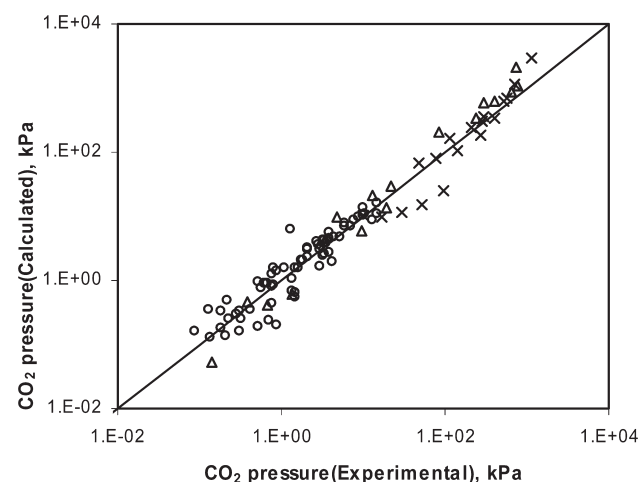
**3.2.  $\text{H}_2\text{S--H}_2\text{O--MDEA}$  System.** Extensive VLE data are available for the  $\text{H}_2\text{S--H}_2\text{O--MDEA}$  ternary system.<sup>18,20–29</sup> We select the data of Jou et al. (1982),<sup>20</sup> Maddox et al. (1987),<sup>21</sup> and ter Maat et al. (2004)<sup>22</sup> to minimize the impact of data inconsistency and to cover the wide ranges for temperature from 283 to 393 K, pressure from 0.13 to 5900 kPa, MDEA mole fraction from 0.02 to 0.13, and  $\text{H}_2\text{S}$  loading from 0.0076 to 3.2. The remaining literature data are used for model validation only.

Figure 3 panels a and b show that, as the  $\text{H}_2\text{S}$  loading decreases, scattering on the reported  $\text{H}_2\text{S}$  partial pressures increases. The Jou et al.<sup>20</sup> data deviate from the others<sup>22,24,26</sup> especially at low pressures. Therefore, the data set of Jou et al.<sup>20</sup> is limited to the data with  $\text{H}_2\text{S}$  pressure above 0.1 kPa in the regression. The VLE data of Huang and Ng (1998)<sup>26</sup> also cover wide ranges for temperature, pressure, MDEA concentration, and  $\text{H}_2\text{S}$  loading. However, as shown in Figure 3, panels a and b, the high temperature data of Huang and Ng<sup>26</sup> are found to be severely inconsistent with those from Jou et al.<sup>20</sup> Specifically, the  $\text{H}_2\text{S}$  partial pressures at temperatures of 373 K and 393 K reported by Huang and Ng<sup>26</sup> are almost 1 order of magnitude higher than those reported by Jou et al.<sup>20</sup> We further find that the VLE predictions for the  $\text{H}_2\text{S--CO}_2\text{--H}_2\text{O--MDEA}$  quaternary system are highly sensitive to whether Huang and Ng's data<sup>26</sup> are used in the regression of the molecule–electrolyte NRTL binary parameters. Specifically, the VLE predictions from the model for the  $\text{H}_2\text{S--CO}_2\text{--H}_2\text{O--MDEA}$  system show strong deviations from the experimental data<sup>22,25,30</sup> when Huang and Ng's VLE data for the  $\text{H}_2\text{S--H}_2\text{O--MDEA}$  system are included in the regression. Therefore the VLE data of Huang and Ng<sup>26</sup> are not used in regression.

The selected experimental data are correlated with the model by adjusting the four NRTL binary interaction parameters for the two major molecule–electrolyte binaries, that is, the  $\text{H}_2\text{O--(MDEAH}^+, \text{HS}^-)$  binary and the  $\text{MDEA--(MDEAH}^+, \text{HS}^-)$

**Table 16.** Comparison between Experimental Data and Model Predictions for H<sub>2</sub>S Partial Pressure and CO<sub>2</sub> Partial Pressure of the H<sub>2</sub>S–CO<sub>2</sub>–H<sub>2</sub>O–MDEA System

data type	VLE, <i>TPx</i> , partial pressures	VLE, <i>TPx</i> , partial pressures	VLE, <i>TPx</i> , partial pressures
<i>T</i> (K)	283–298	311–373	323
<i>P</i> (kPa), H <sub>2</sub> S pressure	0.12–35	0.38–65	6–680
<i>P</i> (kPa), CO <sub>2</sub> pressure	0.08–15	0.14–770	10–1150
MDEA mole fraction	0.075–0.13	0.13	0.13
H <sub>2</sub> S loading	0.02–0.59	0.01–0.30	0.11–0.88
CO <sub>2</sub> loading	0.05–0.40	0.002–0.64	0.09–0.71
data points	73	16	18
average relative deviation of H <sub>2</sub> S partial pressure, $ \Delta P/P $ , %	26.2	49.5	25.1
average relative deviation of CO <sub>2</sub> partial pressure, $ \Delta P/P $ , %	37.3	66.6	42.5
reference	ter Maat et al. <sup>22</sup>	Huang and Ng <sup>26</sup>	Dicko et al. <sup>30</sup>

**Figure 5.** Parity plot for H<sub>2</sub>S partial pressure of H<sub>2</sub>S–CO<sub>2</sub>–H<sub>2</sub>O–MDEA system. Experimental data vs model predictions: (○) ter Maat et al.,<sup>22</sup> (Δ) Huang and Ng,<sup>26</sup> (×) Dicko et al.<sup>30</sup>**Figure 7.** Comparison of the experimental data (symbols) and the model results (lines) for CO<sub>2</sub> partial pressure in aqueous MDEA solution. MDEA mole fraction is 0.13, *T* = 313 K. (▲) CO<sub>2</sub> pressure data of the CO<sub>2</sub>–H<sub>2</sub>O–MDEA system from Ermatchkov et al.,<sup>33</sup> (■) CO<sub>2</sub> pressure data of the CO<sub>2</sub>–H<sub>2</sub>O–MDEA system from Pérez-Salado Kamps et al.,<sup>28</sup> (○) CO<sub>2</sub> pressure data of the H<sub>2</sub>S–CO<sub>2</sub>–H<sub>2</sub>O–MDEA system from Huang and Ng,<sup>26</sup> H<sub>2</sub>S loading is fixed to 0.04, (solid line) predicted CO<sub>2</sub> pressure of the ternary CO<sub>2</sub>–H<sub>2</sub>O–MDEA system, (dotted line) predicted CO<sub>2</sub> pressure of the quaternary H<sub>2</sub>S–CO<sub>2</sub>–H<sub>2</sub>O–MDEA system, H<sub>2</sub>S loading is fixed to 0.04.**Figure 6.** Parity plot for CO<sub>2</sub> partial pressure of H<sub>2</sub>S–CO<sub>2</sub>–H<sub>2</sub>O–MDEA system. Experimental data vs model predictions: (○) ter Maat et al.,<sup>22</sup> (Δ) Huang and Ng,<sup>26</sup> (×) Dicko et al.<sup>30</sup>

binary. Table 14 shows the correlation results. The average relative deviations on H<sub>2</sub>S partial pressures for the three data sets are less than 32%. The regressed NRTL parameters are given in

Table 12. Note that these NRTL parameters are assumed to be temperature-independent. Furthermore, the Henry's constant of H<sub>2</sub>S in MDEA is set to be same as that of H<sub>2</sub>S in water. Figure 3 shows the comparison between the model results and the experimental data for H<sub>2</sub>S partial pressures at MDEA mole fractions of 0.13. The model results at other MDEA concentrations are similar. It is evident from Table 14 and Figure 3 that the experimental data are fitted well across all temperatures, pressures, MDEA concentrations, and H<sub>2</sub>S loadings. To highlight the results especially at extreme H<sub>2</sub>S loadings, Figure 3 panels a and b are shown in linear scale in H<sub>2</sub>S loading and logarithmic scale in H<sub>2</sub>S loading, respectively.

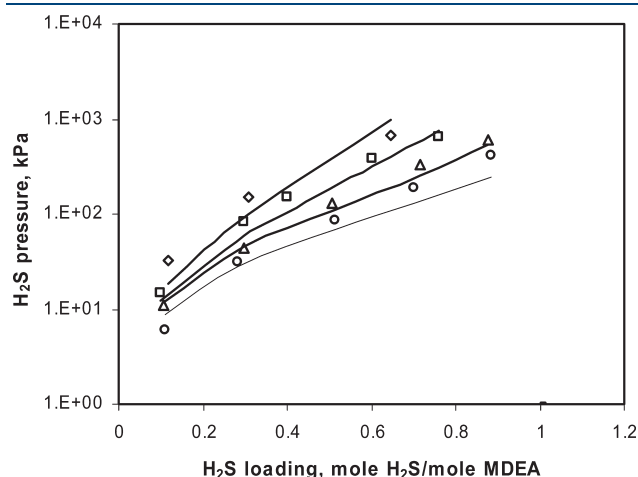
Table 15 shows the comparison between the model predictions and the experimental VLE data from sources not included in the regression. The results highlight the fact that we cannot match all the VLE data because the experimental data from different sources can be inconsistent. For example, the model



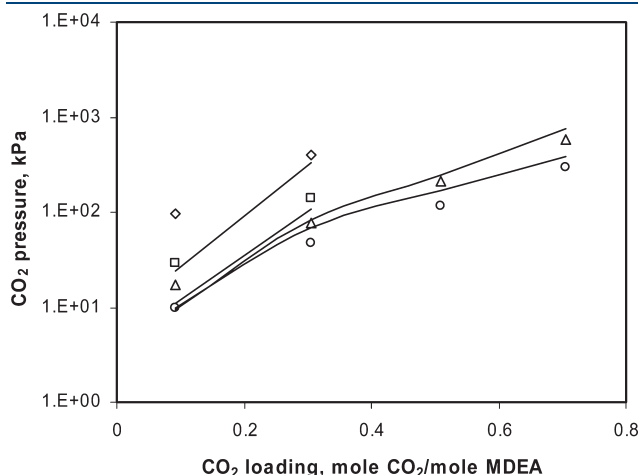
predictions deviate by almost 65% against the  $\text{H}_2\text{S}$  partial pressure data from Macgregor and Mather (1991).<sup>23</sup> It is also interesting that, although no total pressure data are used in the regression, the model predictions match very well with the three total pressure measurements of Kuranov et al. (1996),<sup>18</sup> Pérez-Salado Kamps et al. (2001),<sup>28</sup> and Sidi-Boumedine et al. (2004).<sup>29</sup> The average relative deviations on these three total

pressure data sets are merely 9.4%, 12.4%, and 12.1%, respectively.

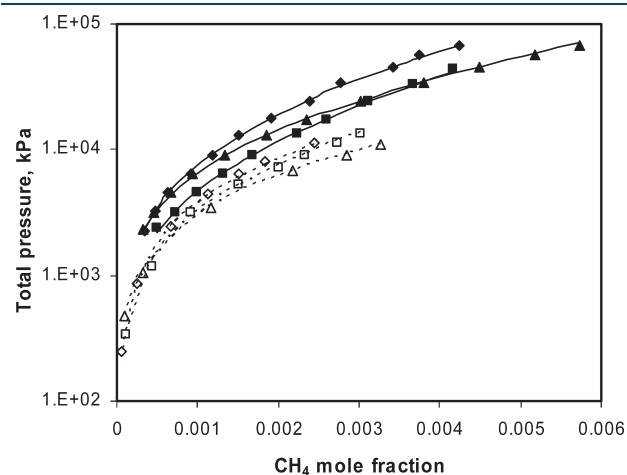
Figure 4 shows that the predicted differential heats of  $\text{H}_2\text{S}$  absorption are compared favorably to the experimental data of Oscarson and Izatt (1990)<sup>31</sup> at MDEA mole fraction of 0.13.



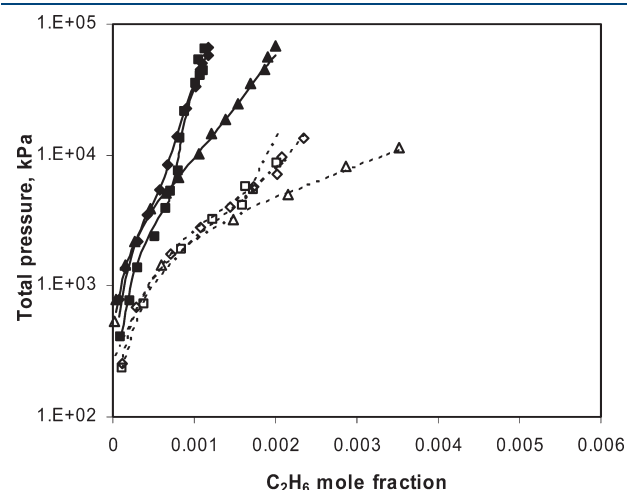
**Figure 8.** Comparison of the experimental data from Dicko et al.<sup>30</sup> (symbols) and the model results (lines) for  $\text{H}_2\text{S}$  partial pressure of  $\text{H}_2\text{S}-\text{CO}_2-\text{H}_2\text{O}-\text{MDEA}$  solution. MDEA mole fraction is 0.13,  $T = 323$  K: (○)  $\text{CO}_2$  loading is 0.1, (△)  $\text{CO}_2$  loading is 0.3, (□)  $\text{CO}_2$  loading is 0.5, (◇)  $\text{CO}_2$  loading is 0.8.



**Figure 9.** Comparison of the experimental data from Dicko et al.<sup>30</sup> (symbols) and the model results (lines) for  $\text{CO}_2$  partial pressure of  $\text{H}_2\text{S}-\text{CO}_2-\text{H}_2\text{O}-\text{MDEA}$  solution. MDEA mole fraction is 0.13,  $T = 323$  K: (○)  $\text{H}_2\text{S}$  loading is 0.1, (△)  $\text{H}_2\text{S}$  loading is 0.3, (□)  $\text{H}_2\text{S}$  loading is 0.5, (◇)  $\text{H}_2\text{S}$  loading is 0.7.



**Figure 10.** Comparison of the experimental data from Culberson and McKetta<sup>34</sup> (full symbols) and Jou et al.<sup>38</sup> (empty symbols) for  $\text{CH}_4$  solubility and the model results (lines): (■)  $T = 298$ , (◆)  $T = 344$ , (▲)  $T = 410$ , (□)  $T = 298$ , (◇)  $T = 343$ , (△)  $T = 403$  K; (solid line) predicted total pressure of the  $\text{CH}_4-\text{H}_2\text{O}$  solution; (dotted line) predicted total pressure of the  $\text{CH}_4-\text{H}_2\text{O}-\text{MDEA}$  solution.

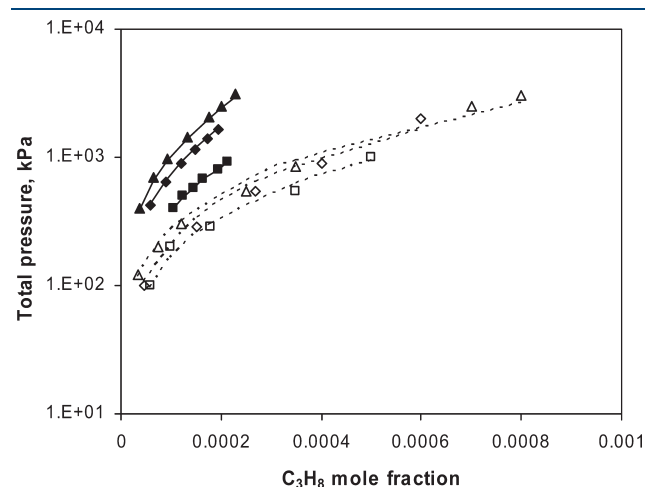


**Figure 11.** Comparison of the experimental data from Culberson and McKetta<sup>35</sup> (full symbols) and Jou et al.<sup>38</sup> (empty symbols) for  $\text{C}_2\text{H}_6$  solubility and the model results (lines): (■)  $T = 311$ , (◆)  $T = 344$ , (▲)  $T = 411$ , (□)  $T = 313$ , (◇)  $T = 343$ , (△)  $T = 403$  K; (solid line) predicted total pressure of the  $\text{C}_2\text{H}_6-\text{H}_2\text{O}$  solution; (dotted line) predicted total pressure of the  $\text{C}_2\text{H}_6-\text{H}_2\text{O}-\text{MDEA}$  solution.

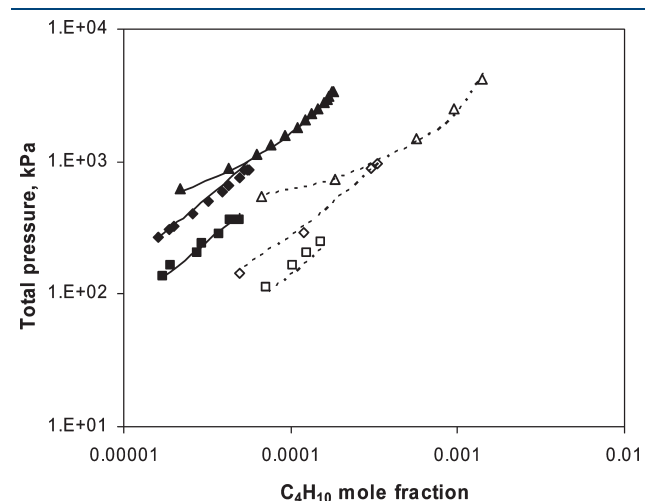
**Table 17.** Experimental Data Used in the Regression for the Hydrocarbon– $\text{H}_2\text{O}$  Systems

hydrocarbon	$T$ (K)	$P$ (kPa)	hydrocarbon mole fraction	data points	average relative deviation, $ \Delta P/P $ (%)	reference
$\text{CH}_4$	298–444	2200–69000	0.00032–0.0078	71	2.9	Culberson and McKetta <sup>34</sup>
$\text{C}_2\text{H}_6$	311–444	410–69000	0.000048–0.0032	71	9.8	Culberson and McKetta <sup>35</sup>
$\text{C}_3\text{H}_8$	293–368	400–3900	0.000032–0.00026	44	3.8	Chapoy et al. <sup>36</sup>
$\text{C}_4\text{H}_{10}$	311–411	135–3400	0.000016–0.00018	63	8.9	Le Breton and McKetta <sup>37</sup>

Note that no data on heat of H<sub>2</sub>S absorption are included in the regression of the model parameters.



**Figure 12.** Comparison of the experimental data from Chapoy et al.<sup>36</sup> (full symbols) and Carroll et al.<sup>39</sup> (empty symbols) for C<sub>3</sub>H<sub>8</sub> solubility and the model results (lines): (■)  $T = 298$ , (◆)  $T = 323$ , (▲)  $T = 353$ , (□)  $T = 298$ , (◇)  $T = 323$ , (△)  $T = 348$  K; (solid lines) predicted total pressure of the C<sub>3</sub>H<sub>8</sub>–H<sub>2</sub>O solution; (dashed lines) predicted total pressure of the C<sub>3</sub>H<sub>8</sub>–H<sub>2</sub>O–MDEA solution.



**Figure 13.** Comparison of the experimental data from Le Breton and McKetta<sup>37</sup> (full symbols) and Jou et al.<sup>40</sup> (empty symbols) for C<sub>4</sub>H<sub>10</sub> solubility and the model results (lines): (■)  $T = 311$ , (◆)  $T = 344$ , (▲)  $T = 411$ , (□)  $T = 298$ , (◇)  $T = 348$ , (△)  $T = 423$  K; (solid lines) predicted total pressure of the C<sub>4</sub>H<sub>10</sub>–H<sub>2</sub>O solution; (dotted lines) predicted total pressure of the C<sub>4</sub>H<sub>10</sub>–H<sub>2</sub>O–MDEA solution.

The solid lines in Figure 4 are the results determined according to enthalpy balance of the absorption process:

$$\Delta H_{\text{abs}} = \frac{n_{\text{final}} H_{\text{final}}^l - n_{\text{initial}} H_{\text{initial}}^l - n_{\text{H}_2\text{S}} H_{\text{H}_2\text{S}}^v}{n_{\text{H}_2\text{S}}} \quad (13)$$

$\Delta H_{\text{abs}}$  is the heat of absorption,  $H_{\text{final}}^l$  is the molar enthalpy of the final H<sub>2</sub>S–H<sub>2</sub>O–MDEA solution,  $H_{\text{initial}}^l$  is the molar enthalpy of the initial H<sub>2</sub>S–H<sub>2</sub>O–MDEA solution,  $H_{\text{H}_2\text{S}}^v$  is the molar enthalpy of gaseous H<sub>2</sub>S absorbed,  $n_{\text{final}}$ ,  $n_{\text{initial}}$ , and  $n_{\text{H}_2\text{S}}$  are the numbers of moles of the final H<sub>2</sub>S–H<sub>2</sub>O–MDEA solution, the initial H<sub>2</sub>S–H<sub>2</sub>O–MDEA solution, and the H<sub>2</sub>S absorbed, respectively. The differential heat of absorption means the heat effect per unit mole of H<sub>2</sub>S when an infinitesimal amount of H<sub>2</sub>S is absorbed by the H<sub>2</sub>S–H<sub>2</sub>O–MDEA solution.

The dashed lines are the differential heats calculated from the Gibbs–Helmholtz equation:<sup>32</sup>

$$\Delta H_{\text{abs}} = -RT^2 \left[ \frac{\partial \ln f_{\text{H}_2\text{S}}}{\partial T} \right]_{P,x} \quad (14)$$

where  $f_{\text{H}_2\text{S}}$  is the fugacity of H<sub>2</sub>S.

The heats calculated from enthalpy balance are differential in loading and constant in temperature, while those calculated from the Gibbs–Helmholtz equation are constant in loading but differential in temperature. Figure 4 shows a very small discrepancy between these two calculations. The discrepancy increases slightly with the increases in temperature and the H<sub>2</sub>S loading.

**3.3. H<sub>2</sub>S–CO<sub>2</sub>–H<sub>2</sub>O–MDEA System.** The available VLE data<sup>22,26,30</sup> for the H<sub>2</sub>S–CO<sub>2</sub>–H<sub>2</sub>O–MDEA quaternary system are summarized in Table 16. To properly model the quaternary system, the model requires additional NRTL binary parameters on top of the binary parameters established for the subsystems of H<sub>2</sub>S–H<sub>2</sub>O–MDEA and CO<sub>2</sub>–H<sub>2</sub>O–MDEA. Examples are the binary parameters for the H<sub>2</sub>S–electrolyte binaries where electrolytes are derived from the ionic reactions between MDEA and CO<sub>2</sub>, or the binary parameters for the CO<sub>2</sub>–electrolyte binaries where electrolytes are derived from the ionic reactions between MDEA and H<sub>2</sub>S. These additional parameters are set to the default values. The acid gas solubility predictions for the H<sub>2</sub>S–CO<sub>2</sub>–H<sub>2</sub>O–MDEA quaternary system based on the parameters with the default values are found to be in satisfactory agreement with the experimental data. Figure 5 and 6 show the parity plots for the model predictions versus the experimental data on H<sub>2</sub>S and CO<sub>2</sub> partial pressures, respectively. The corresponding relative average deviations between the model predictions and the experimental data for the CO<sub>2</sub> and H<sub>2</sub>S partial pressures of the quaternary system are summarized in Table 16. The results show the quality of model predictions for the quaternary system does not degenerate significantly from those for the ternary subsystems. The

**Table 18.** Experimental Data Used in the Regression for the Hydrocarbon–H<sub>2</sub>O–MDEA Systems

hydrocarbon	$T$ (K)	$P$ (kPa)	MDEA mole fraction	hydrocarbon mole fraction	data points	average relative deviation, $ \Delta P/P $ (%)	reference
CH <sub>4</sub>	298–403	95–13000	0.0765	0.000042–0.0033	44	6.5	Jou et al. <sup>38</sup>
C <sub>2</sub> H <sub>6</sub>	298–403	96–13500	0.0765	0.000015–0.0035	45	10.8	Jou et al. <sup>38</sup>
C <sub>3</sub> H <sub>8</sub>	273–348	100–3000	0.0765	0.000035–0.0008	25	10.3	Carroll et al. <sup>39</sup>
C <sub>4</sub> H <sub>10</sub>	298–423	110–4200	0.0765	0.000049–0.0014	25	11.1	Jou et al. <sup>40</sup>

results also show relatively large discrepancies between the model predictions and the experimental data of Huang and Ng.<sup>26</sup> Figure 7 shows the predicted CO<sub>2</sub> partial pressures of the ternary CO<sub>2</sub>–H<sub>2</sub>O–MDEA system match the data of Pérez-Salado Kamps et al. (2001)<sup>28</sup> and Ermatchkov et al. (2006)<sup>33</sup> well. For the quaternary H<sub>2</sub>S–CO<sub>2</sub>–H<sub>2</sub>O–MDEA system, the predicted CO<sub>2</sub> partial pressures increase as H<sub>2</sub>S loading increases from 0 to 0.04. However, the CO<sub>2</sub> partial pressures with H<sub>2</sub>S loading of 0.04 as reported by Huang and Ng<sup>26</sup> for the quaternary system are much lower than the predictions. In fact, the Huang and Ng data are close to or even lower than the experimental CO<sub>2</sub> partial pressure data reported for the CO<sub>2</sub>–H<sub>2</sub>O–MDEA ternary system.<sup>28,33</sup> The H<sub>2</sub>S partial pressure data of Huang and Ng<sup>26</sup> for the quaternary system show similar behaviors. In addition, Figures 8 and 9 show the comparisons of the model predictions and the experimental data of Dicko et al. (2010)<sup>30</sup> for H<sub>2</sub>S and CO<sub>2</sub> partial pressures as one of the CO<sub>2</sub> and H<sub>2</sub>S loadings is fixed and the other loading is varied. The model predictions exhibit the trends that H<sub>2</sub>S and CO<sub>2</sub> partial pressures increase as the loading of the other solute increases, in line with those of the experimental data.

**3.4. Hydrocarbon–H<sub>2</sub>O and Hydrocarbon–H<sub>2</sub>O–MDEA systems.** The Henry's constants for four light hydrocarbons in water are fitted to the total pressure data of the hydrocarbon–water systems. The experimental data<sup>34–37</sup> used in the regression are shown in Table 17. For the CH<sub>4</sub>–H<sub>2</sub>O and C<sub>2</sub>H<sub>6</sub>–H<sub>2</sub>O systems, the characteristic volume parameters of hydrocarbons and the Henry's constants are regressed together from the gas solubility data with pressure up to 69000 kPa. For the C<sub>3</sub>H<sub>8</sub>–H<sub>2</sub>O and C<sub>4</sub>H<sub>10</sub>–H<sub>2</sub>O systems, only the Henry's constants are fitted to the low and mid pressure data up to 3900 kPa. The regressed parameters are summarized in Tables 7 and 10. Figures 10–13 illustrate that the model satisfactorily captures the system nonideality and that the calculated total pressures match the experimental data well. The average relative deviations are less than 10%.

The Henry's constants of the hydrocarbons in MDEA are fitted to the total pressure data of the hydrocarbon–H<sub>2</sub>O–MDEA ternary systems. The experimental data<sup>38–40</sup> used in the regression are shown in Table 18. The regressed parameters are given in Table 7. Figures 10–13 show that the calculated total pressures are in good agreement with the experimental data. The average relative deviations are around 10%. Figures 10–13 also show that the hydrocarbon solubilities in the aqueous MDEA solutions increase significantly compared to those in pure water.

## 4. CONCLUSION

To support process modeling and simulation of the natural gas treating processes with MDEA, the recently developed CO<sub>2</sub>–H<sub>2</sub>O–MDEA model has been successfully extended to correlate the available experimental solubility data of H<sub>2</sub>S and four light hydrocarbons in the aqueous MDEA solutions. The model has been validated for VLE and enthalpy calculations of the H<sub>2</sub>S–H<sub>2</sub>O–MDEA system with temperature from 283 to 393 K, pressure up to 6000 kPa, MDEA concentration up to 8 m (~50 wt %) and H<sub>2</sub>S loading up to 3.2. The model predictions for H<sub>2</sub>S and CO<sub>2</sub> partial pressures of the H<sub>2</sub>S–CO<sub>2</sub>–H<sub>2</sub>O–MDEA quaternary system are found to be satisfactory. The model should be a useful tool for accurate calculations of gas solubilities in aqueous MDEA solutions.

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## ACKNOWLEDGMENT

We thank our colleagues Joe DeVincentis and Yuhua Song for their extensive reviews and helpful comments on this manuscript.

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