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# Dynamic Modeling of Biogas Upgrading in Hollow Fiber Membrane Contactors

Yunfei Yan,\*\*,† Zhien Zhang,† Li Zhang, Yanrong Chen, and Qiang Tang

Key Laboratory of Low-Grade Energy Utilization Technologies and Systems, Ministry of Education, Chongqing University, Chongqing 400044, People's Republic of China

ABSTRACT: Membrane absorption is a novel method for acid gas removal compared to conventional separation techniques. The current study presents the simulation results using a computational fluid dynamics (CFD) method for biogas purification. A comprehensive two-dimensional (2D) mass-transfer model was developed and solved in a hollow fiber membrane contactor (HFMC) under a non-wetted condition.  $H_2O$ , triethanolamine (TEA), diethanolamine (DEA), monoethamolamine (MEA), and potassium argininate (PA) were used as the absorbent liquids. The effects of gas—liquid parameters and membrane characteristics on the  $CO_2$  removal efficiency and absorption flux and  $CH_4$  recovery were systematically examined and evaluated. The comparisons between model predictions and experimental data with various gas—liquid parameters were in good agreement. An increase of gas velocity and  $CO_2$  content caused an increase of  $CO_2$  flux and a decrease of  $CO_2$  removal efficiency and  $CH_4$  recovery; however, an increase of absorbent velocity and concentration caused an increase in the above three values. In addition, a smaller fiber inner diameter and membrane thickness and a longer module were good for the biogas upgrading process. It should be noted that the highest  $CO_2$  flux coincided with the original module dimensions. The simulation predictions also showed that PA provided better membrane module performance than other absorbents. The order for  $CO_2$  absorption efficiency and  $CH_4$  recovery was  $PA > MEA > DEA > TEA > H_2O$ . Overall, the developed model provides the guidelines for selecting the optimum module properties and fluid conditions. The membrane gas absorption technique has shown great potential in biogas upgrading.

### 1. INTRODUCTION

With the rapid development of technology, there is an increasing demand for fuels. Natural gas is an environmentally friendly, renewable, and clean energy source. It is also the third largest proportion in energy structure throughout the world after coal and oil. Biogas production and utilization is an additional available energy. The upgraded biogas in the form of a natural gas candidate can be supplied to the developed natural gas grids and delivered to industry and households. Particularly, it can be used as a vehicle fuel, of which the demand has dramatically increased over the past few decades. <sup>1,2</sup> The separation of CH<sub>4</sub> and CO<sub>2</sub> is a key issue in the natural gas industry. Generally, there are several techniques for CO<sub>2</sub> capture from biogas, i.e., physical and chemical absorption, pressure swing adsorption, membrane separation, etc.<sup>3</sup> Among them, the membrane gas absorption (MGA) has been introduced to be a high-efficiency technique and promising alternative for conventional separation methods for acid gas removal.<sup>4-6</sup> This process combines the advantages of both chemical absorption and membrane separation methods, including no channeling, flooding, entraining, and foaming issues, less capital investment, much bigger gas-liquid interfacial area, and ease to scale up.4

The main CO<sub>2</sub> emission is produced from fossil fuel combustion and other industrial processes. There are various sources of CO<sub>2</sub> emissions worldwide, which result in global warming. With regard to pure CO<sub>2</sub>, Boributh et al.<sup>7</sup> investigated the physical absorption of CO<sub>2</sub> considering pore size distribution and wetting ratio in a hollow fiber membrane module. Zhang et al.<sup>8</sup> reported that the CO<sub>2</sub> removal efficiency for single gas reached around 95% when monoethamolamine (MEA) solution was used as the absorbent. These investigations indicated that the membrane gas absorption method for pure CO<sub>2</sub> capture was feasible when using the appropriate absorbent. In terms of flue gas,

CO<sub>2</sub> accounts for about 10-20% in the gas mixture. Mehdipour et al.  $^{9}$  studied flue gas containing 20%  $\mathrm{CO}_{2}$  and 80%  $\mathrm{N}_{2}$  as the research object. The CO<sub>2</sub> capture process reached complete removal using 2 M K<sub>2</sub>CO<sub>3</sub> solution at 298 K. Furthermore, Masoumi et al.<sup>6</sup> analyzed CO<sub>2</sub> absorption from gas mixtures containing 10% CO<sub>2</sub> into MEA/diethanolamine (DEA)/N-methyldiethanolamine (MDEA)-promoted potassium carbonate solutions in a membrane contactor. They showed that the CO<sub>2</sub> flux increased considerably using promoted solutions in comparison to non-promoted solutions. In the case of natural gas, CO<sub>2</sub> also accounts for a major proportion. Keshavarz et al. 10 simulated a feed gas mixture of 15% CO<sub>2</sub>, 5% H<sub>2</sub>S, and 80% N<sub>2</sub> absorption in a membrane module. They successfully conducted the simultaneous absorption of CO<sub>2</sub> and H<sub>2</sub>S in a masstransfer model. For the first time, Marzouk et al. 11,112 carried out experiments on CO<sub>2</sub> removal from a gas mixture containing 90.5% CH<sub>4</sub> and 9.5% CO<sub>2</sub> into water and amine solvents at high pressures up to 50 MPa in a hollow fiber membrane contactor (HFMC). Thus, plenty of researchers have paid close attention to the applications of membrane contactors for CO<sub>2</sub> capture from pure CO<sub>2</sub>, flue gas, or natural gas. Typically, there is 25-50% CO<sub>2</sub> in the composition of biogas. However, CO<sub>2</sub> absorption from biogas in a HFMC is rarely reported in the published literature.<sup>3</sup>

Lately, a variety of aqueous solvents, including physical and chemical solutions, have been widely investigated experimentally and theoretically. Choosing an appropriate absorbent liquid is a significant factor influencing the membrane performance. Physical solvent has low capital compared to the expensive

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Figure 1. Molecular structures for different liquid absorbents used in this simulation.

chemical solvent for CO<sub>2</sub> absorption. Porcheron and Drozdz<sup>13</sup> carried out experiments and modeling of the gas-liquid contact process using H<sub>2</sub>O as the solvent in a polypropylene (PP) HFMC. However, the CO<sub>2</sub> absorption effect under these conditions was not obvious. Rangwala<sup>14</sup> compared the CO<sub>2</sub> absorption performance of three absorbents: aqueous H<sub>2</sub>O<sub>2</sub> NaOH, and DEA solvents using HFMCs. The mass-transfer rate for absorption of CO<sub>2</sub> in the HFMC was examined. The results showed that the removal process was significantly enhanced in the case of chemical absorption compared to physical absorption. This was due to the reason that the amine solutions were weak basic compounds and the chemical bonds between amine and CO<sub>2</sub> were easily broken under high temperatures. To improve the reaction rate constant, the mixed solutions using activators into the absorbent have gained wide attention. Lin et al. 15 investigated blended solutions of piperazine (PZ) and 2-amino-2-methyl-1-propanol (AMP) in the gas absorption membrane process. They found that increasing the PZ concentration showed an increase of the CO<sub>2</sub> absorption rate. Furthermore, Munoz et al. 16 tested new liquid absorbents consisting of water solutions of CO<sub>2</sub>-complexing agents, and the absorbents showed outstanding absorption capacities, superior to MEA or any other amino acid. However, it is necessary to find a novel aqueous absorbent with higher surface tension and lower reaction heat, because the alkanolamine solutions result in membrane wetting issues. It was noted that amino acid salts were good substitutes for conventional solutions because they had higher surface tension, which reduced the risk of membrane wetting. The solvents based on amino acid salts were also suitable for stable and long-term gas-liquid reaction in the membrane module. 17,18

Recently, a number of simulation works have been accomplished to explore the behaviors of gas transport in the membranes. Keshavarz et al. 10,19 developed a steady-state model and numerical scheme for CO2 separation in a HFMC under non-wetted and partially wetted modes. The reversible chemical reactions in the liquid phase as well as wetted parts of the pores were considered in the diffusion-reaction models. They indicated that the membrane performance was deteriorated with a high wetting ratio of the membrane. Additionally, a general two-dimensional (2D) mathematical model for calculation of the CO<sub>2</sub> concentration in polymeric membrane modules was established, which took into account axial and radial diffusion in the tube, membrane, and shell compartments of the contactor. The simulated predictions were in excellent consistency with the available experimental values for various liquid velocities.<sup>20</sup> Al-Marzouqi et al. 21,22 used a mass-transfer model to simulate the transport process of gas and liquid in the membrane contactor under the non-wetted conditions. Additionally, they found increasing the absorbent concentration and velocity or decreasing the gas velocity increased the  $\mathrm{CO}_2$  removal efficiency. Later, Jung et al.  $^{23}$  used two models, including the explicit model and the multilayer perceptron neural network model for the  $\mathrm{CO}_2$  capture process using HFMCs. They stated that the explicit model for the single-stage module could be extended to the multistage module, and these models could be applied in  $\mathrm{CO}_2$  absorption in a HFMC. However, in most previous literature, there is no simulation work that simultaneously reported the effects of the fluid properties and module structure on the biogas purification efficiency in the HFMC. Also, from the above observations, the computational fluid dynamics (CFD) technique is a feasible method to predict acid gas removal in the contactor.

In the present study, a 2D mass-transfer model for simulation of CO<sub>2</sub> separation from biogas at atmospheric pressure was developed. The effects of gas and liquid properties and membrane structure were investigated by a simulated biogas containing 40% CO<sub>2</sub> and 60% CH<sub>4</sub>. In the simulations, biogas and liquid flow countercurrently in a non-wetting condition. Physical solvent (H2O) and chemical absorbents [triethanolamine (TEA), DEA, MEA, and potassium argininate (PA)] were used for CO<sub>2</sub> absorption. Among them, PA shows better absorption performance compared to other conventional absorbents because of several amino groups in the molecular structure (see Figure 1). It also provides the advantages of low volatility, ionic property, and resistance to oxidative and thermal degradation. It is the first time the aqueous PA solution was used as an absorbent in a HFMC. The governing equations including the tube, membrane, and shell regions are solved in the material balance. The validation of the developed model was verified with the experimental data by Yan et al.,<sup>3</sup> where the non-wetting condition was assumed.

### 2. THEORY

In this study, a numerical analysis of  $\mathrm{CO}_2$  separation from biogas in a HFMC is conducted by means of deriving and solving the continuity equations, including three domains: the gas, porous membrane, and absorbent sections. The schematic diagram of the gas—liquid membrane contactor is depicted in Figure 2. As can be seen, the biogas is fed into the shell side, passing through the membrane pores, and then is absorbed by aqueous liquid. Only the gas phase diffuses in the membrane because of operation in a non-wetted condition. In this case, the absorbent is passed into the tube in a countercurrent flow.

Specifications of the module used in this numerical analysis are shown in Table 1. The membrane module was provided by Hangzhou Jeffel Membrane Technology, Ltd. in China. The following assumptions are made in this simulation work: (1) steady state and isothermal conditions, (2) ideal gas behavior, (3) applicability of Henry's law for the gas—liquid interface,

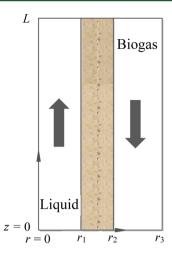


Figure 2. Schematic of a gas-liquid HFMC.

Table 1. Specifications of the Membrane Module<sup>4</sup>

parameter	value
membrane material	polypropylene (PP)
fiber inner diameter ( $\mu$ m)	360
membrane thickness ( $\mu$ m)	45
Happel's free surface model radius $(\mu m)$	402
module inner diameter (m)	3.6
membrane length (cm)	320
number of fibers	500
porosity	0.45
tortuosity	$(2-\varepsilon)/\varepsilon$
packing density	0.3125
membrane area (m²)	0.176

- (4) non-wetted mode for the membrane contactor, (5) laminar flow for gas and absorbent flow in the HFMC, and (6) a fully developed laminar parabolic velocity profile in the fibers.
- **2.1.** Governing Equations Inside the Tube. Considering diffusion, reaction, and convection, the steady-state material balance equation for each species i (CO<sub>2</sub> or absorbent) in the tube side may be expressed below

$$D_{i\text{-tube}} \left[ \frac{\partial C_{i\text{-tube}}}{\partial r} + \frac{1}{r} \frac{\partial C_{i\text{-tube}}}{\partial r} + \frac{\partial^2 C_{i\text{-tube}}}{\partial z^2} \right]$$

$$= U_{z\text{-tube}} \frac{\partial C_{i\text{-tube}}}{\partial z} - R_i$$
(1)

where  $D_{i\text{-tube}}$ ,  $C_{i\text{-tube}}$ ,  $U_{z\text{-tube}}$ , and  $R_i$  are the diffusion coefficient and the concentration of species i inside the tube, the velocity in the axial direction, and the reaction rate, respectively. When physical

absorption is considered in the membrane contactor, the reaction term in eq 1 is negligible. The axial velocity distribution in the tube is assumed to follow Newtonian laminar flow  $^{24}$ 

$$U_{z\text{-tube}} = 2\bar{U}_{\text{tube}} \left[ 1 - \left( \frac{r}{r_1} \right)^2 \right]$$
 (2)

where  $\overline{U}_{\text{tube}}$  denotes the average velocity in the tube side, r is the radial coordinate, and  $r_1$  is the inner fiber radius.

**2.2. Governing Equations Inside the Membrane.** In the case of the non-wetted mode, the steady-state governing equation for CO<sub>2</sub> transport can be expressed as

$$D_{\text{CO}_2\text{-mem}} \left[ \frac{\partial C_{\text{CO}_2\text{-mem}}}{\partial r} + \frac{1}{r} \frac{\partial C_{\text{CO}_2\text{-mem}}}{\partial r} + \frac{\partial^2 C_{\text{CO}_2\text{-mem}}}{\partial z^2} \right] = 0$$
(3)

where  $D_{\text{CO}_2\text{-mem}}$  and  $C_{\text{CO}_2\text{-mem}}$  are the diffusion coefficient and the concentration of  $\text{CO}_2$  across the membrane, respectively.

The diffusion coefficient of  $CO_2$  in the membrane considering the effect of porosity and tortuosity can be written as

$$D_{\text{CO}_2\text{-mem}} = \frac{\varepsilon}{\tau} D_{\text{CO}_2\text{-shell}} \tag{4}$$

where  $\varepsilon$ ,  $\tau$ , and  $D_{\text{CO}_2\text{-shell}}$  denote the membrane porosity, the membrane tortuosity, and the diffusion coefficient of  $\text{CO}_2$  inside the shell, respectively.

**2.3. Governing Equations Inside the Shell.** The differential mass-transfer balance for CO<sub>2</sub> transport in the shell is given by

$$\begin{split} D_{\text{CO}_2\text{-shell}} & \left[ \frac{\partial C_{\text{CO}_2\text{-shell}}}{\partial r} + \frac{1}{r} \frac{\partial C_{\text{CO}_2\text{-shell}}}{\partial r} + \frac{\partial^2 C_{\text{CO}_2\text{-shell}}}{\partial z^2} \right] \\ & = U_{z\text{-shell}} \frac{\partial C_{\text{CO}_2\text{-shell}}}{\partial z} \end{split} \tag{5}$$

where  $U_{z\text{-shell}}$  represents the axial velocity in the shell and  $C_{\text{CO}_2\text{-shell}}$  is the CO<sub>2</sub> concentration inside the shell.

The gas flow in the shell side is always very complicated. Assuming Happel's free surface theory, the axial velocity inside the shell may be estimated as<sup>25</sup>

$$U_{z-\text{shell}} = 2\bar{U}_{\text{shell}} \left[ 1 - \left( \frac{r_2}{r_3} \right)^2 \right]$$

$$\times \left[ \frac{(r/r_3)^2 - (r_2/r_3)^2 + 2\ln(r_2/r)}{3 + (r_2/r_3)^4 - 4(r_2/r_3)^2 + 4\ln(r_2/r_3)} \right]$$
(6)

Table 2. Boundary Conditions of Governing Equations

boundary	tube	membrane	shell
<i>z</i> = 0	$C_{\text{CO}_2\text{-tube}} = 0$	insulated	$\frac{\partial C_{\text{CO}_2\text{-shell}}}{\partial r} = 0$
z = L		insulated	$C_{1\text{-tube}} = C_0$
<i>r</i> = 0	$\frac{\partial C_{\text{CO}_2\text{-tube}}}{\partial r} = 0$		
$r = r_1$	$C_{\text{CO}_2\text{-tube}} = mC_{\text{CO}_2\text{-mem}}$ $\frac{\partial C_{\text{1-tube}}}{\partial r} = 0$	$C_{\text{CO}_2\text{-mem}} = \frac{C_{\text{CO}_2\text{-tube}}}{m}$	
$r = r_2$		$C_{\rm CO_2\text{-mem}} = C_{\rm CO_2\text{-shell}}$	$C_{\text{CO}_2\text{-shell}} = C_{\text{CO}_2\text{-mem}}$

Table 3. Physicochemical Properties Used in This Study

parameter	value/expression	reference
$R (m^3 atm mol^{-1} K^{-1})$	8.314	26
$D_{\rm CO_2}  ({\rm m^2  s^{-1}})$	$1.8 \times 10^{-5}$	27
$D_{\mathrm{CO}_2}^{\mathrm{mem}} \left( \mathrm{m}^2  \mathrm{s}^{-1} \right)$	$1.8 \times 10^{-5} (\varepsilon/\tau)$	27
	CO <sub>2</sub> -H <sub>2</sub> O	
<i>m</i> <sub>H<sub>2</sub>O</sub>	0.83	28
$D_{\rm CO_2}^{\rm H_2O}~({ m m^2~s^{-1}})$	$2.35 \times 10^{-6} \exp(-2199/T)$	29
$D_{ m H_{2O}}^{ m l}~({ m m^2~s^{-1}})$	$0.5D_{\mathrm{CO}_2}^{\mathrm{H}_2\mathrm{O}}$	30
	CO <sub>2</sub> -MEA	
$m_{ m MEA}$	0.86	6
$k_{\text{MEA}} \left( \text{m}^3 \text{ mol}^{-1} \text{ s}^{-1} \right)$	$10^{(10.99-2152/T)}/1000$	31
$D_{\mathrm{CO}_2}^{\mathrm{MEA}} \ (\mathrm{m^2} \ \mathrm{s^{-1}})$	$1.4 \times 10^{-9}$	30
$D_{ m MEA}^{ m l}~({ m m}^2~{ m s}^{-1})$	$7.7 \times 10^{-10}$	30
$R_{ m MEA}$	$k_{\mathrm{MEA}}C_{\mathrm{CO}_2}C_{\mathrm{MEA}}$	30
	CO <sub>2</sub> -TEA	
$m_{\text{TEA}}$	0.602	32
$k_{\text{TEA}}  (\text{m}^3  \text{mol}^{-1}  \text{s}^{-1})$	$4.52 \times 10^4 \exp(-2688/T)$	33
$D_{\mathrm{CO}_2}^{\mathrm{TEA}} \left( \mathrm{m}^2  \mathrm{s}^{-1} \right)$	$1.95 \times 10^{-9}$	34
$D^{\mathrm{l}}_{\mathrm{TEA}}~(\mathrm{m^2~s^{-1}})$	$7.11 \times 10^{-10}$	34
$R_{\text{TEA}}$	$k_{\mathrm{TEA}}C_{\mathrm{CO_2}}C_{\mathrm{TEA}}$	34
	CO <sub>2</sub> -DEA	
$m_{\text{DEA}}$	0.8	30
$k_2  (\text{m}^3  \text{mol}^{-1}  \text{s}^{-1})$	$2.375 \\ 2.2 \times 10^{-6}$	35
$k_2 k_{\rm H_2O} / k_{-1}$		35
$k_2k_{\text{DEA}}/k_{-1}$	$4.37 \times 10^{-4}$	35
$H_2O$ concentration (mol m <sup>-3</sup> ) $D_{CO_2}^{DEA}$ (m <sup>2</sup> s <sup>-1</sup> )	$50$ $1.05 \times 10^{-9}$	36 30
$D_{\text{CO}_2}^{\text{I}}$ (m <sup>2</sup> s <sup>-1</sup> )	$4.97 \times 10^{-10}$	
$D_{ m DEA}$ (m s ) $R_{ m DEA}$		30 35
NDEA	$\frac{C_{\text{CO}_2}C_{\text{DEA}}}{\frac{1}{k_2} + \frac{1}{(k_2k_{\text{H}_2\text{O}}/k_{-1})C_{\text{H}_2\text{O}} + (k_2k_{\text{DEA}}/k_{-1})C_{\text{DEA}}}}$	33
	$\frac{1}{k_2} + \frac{1}{(k_2 k_{\text{H2O}} / k_{-1}) C_{\text{H2O}} + (k_2 k_{\text{DEA}} / k_{-1}) C_{\text{DEA}}}$	
	CO <sub>2</sub> –PA	
$m_{ m PA}$	0.66	37
$k_{\rm PA}  ({\rm m}^3  {\rm mol}^{-1}  {\rm s}^{-1})$	$(2.58 \times 10^{16} \exp(-8654/T)C_{Arg} + 4.32 \times 10^{13} \exp(-6666/T)C_{OH}^{-})C_{CO_2}$	38
OH <sup>-</sup> concentration (mol m <sup>-3</sup> )	$K_{\rm w}/K_{\rm p}((1-m_{\rm pA})/m_{\rm pA})$	39 and 40
$D_{\rm CO_2}^{\rm PA}  ({\rm m}^2  {\rm s}^{-1})$	$D_{ m CO_2}^{ m H_2O}(\mu_{ m H_2O}/\mu_{ m PA})^{0.82}$	38
$D_{\rm PA}^{ m l}~({ m m^2~s^{-1}})$	$0.5D_{\mathrm{CO_2}}^{\mathrm{PA}}$	30
$D_{\rm CO_2}^{\rm H_2O}~({ m m^2~s^{-1}})$	$2.35 \times 10^{-6} \exp(-2199/T)$	38
$\mu_{\rm H_2O}~({\rm mPa~s^{-1}})$	$1.86 \times 10^{-6} \exp(16400/RT)$	38
$\mu_{\rm PA}~({\rm mPa~s^{-1}})$	1.276	37
$R_{\mathrm{PA}}$	$k_{\mathrm{PA}}C_{\mathrm{CO}_2}C_{\mathrm{PA}}$	38

where  $\overline{U}_{\text{shell}}$ ,  $r_2$ , and  $r_3$  are the average velocity in the shell, the outer fiber radius, and Happel's free surface model radius, respectively.

The boundary conditions for solving the developed masstransfer model are listed in Table 2.

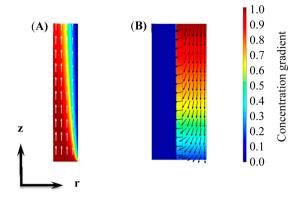
### 3. NUMERICAL SCHEME

The physical and chemical parameters used in this model are shown in Table 3. The finite difference element method is used for numerical solution of the governing equations (eqs 1, 3, and 5) using COMSOL Multiphysics software, version 4.4. The material balance error control and adaptive meshing are applied using a numerical solver of PARDISO, which is thread-safe, high-efficiency, robust, memory efficient, and easy to use for solving large sparse symmetric linear systems of equations on shared- and distributed-memory multiprocessors. A computational platform with the characteristics of RAM 4.00 GB and Intel Core i5-4200U CPU at 1.60 GHz and 64-bit operating system was used to

solve the coupled partial differential equations. The computational time for solving the model equations was about  $3\,\mathrm{min}$ .

### 4. RESULTS AND DISCUSSION

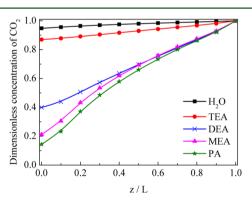
# **4.1. Concentration Distribution of Phases.** Figure 3 shows the concentration gradients and flux vectors of $CO_2$ and liquid in the membrane contactor using 10 wt % PA solution as the absorbent while considering the non-wetting condition. The biogas is fed into the shell from the inlet of the shell (z = L), where the concentration of the gas mixture is maximum, while the absorbent flows from the inlet of the tube (z = 0), where the $CO_2$ concentration is assumed to be zero. It can be seen from Figure 3A that the concentration gradient and flux vectors of solvent in the center of the fiber are higher than those at the gas—liquid interface because of the absence of $CO_2$ . The concentration gradient of liquid gradually decreases from the



**Figure 3.** Two-dimensional concentration distribution of (A) absorbent and (B) CO<sub>2</sub> in the HFMC (liquid concentration, 10 wt %; T, 303 K;  $U_b$  0.06 m s<sup>-1</sup>; and  $U_{g^{\prime}}$  0.32 m s<sup>-1</sup>).

inlet to the outlet of the tube side. It is also indicated from Figure 3B that  $CO_2$  flows across the membrane because of the large concentration difference between the feed and tube side and then is absorbed by the solvent inside the tube. The  $CO_2$  flux vectors are in both r and z directions in the tube and shell sections because of diffusion and convection. In addition, the concentration gradient of  $CO_2$  inside the tube is much smaller than that inside the shell and membrane domains because of the lower diffusion coefficient in the solvent than that in the gas phase. It is clearly seen that the  $CO_2$  dimensionless concentration distribution is more uniform when the solvent passes through the tube side.

**4.2.** Concentration Profile in the Axial Direction. The axial  $CO_2$  concentration profile at the membrane—shell interface of the membrane contactor with different solvents is depicted in Figure 4. It is obvious that the  $CO_2$  concentration is maximum at



**Figure 4.** Concentration profile for CO<sub>2</sub> with various absorbents along the membrane module (liquid concentration, 10 wt %; T, 303 K;  $U_{\nu}$  0.06 m s<sup>-1</sup>; and  $U_{gr}$  0.32 m s<sup>-1</sup>).

z=L and then declined to the minimum at the outlet (z=0) along the membrane module in the shell side. The amount of  $\mathrm{CO}_2$  in the gas mixture is increasingly absorbed by the aqueous solvent. It is also noted that PA solution is the best solvent for  $\mathrm{CO}_2$  separation, and the value of the dimensionless concentration at z=0 is around 0.1. This contributed to the highest reaction rate with  $\mathrm{CO}_2$ . In addition, water and TEA show bad absorption performance. The sequence of absorption performance for all of the solvents is  $\mathrm{H}_2\mathrm{O} < \mathrm{TEA} < \mathrm{DEA} < \mathrm{MEA} < \mathrm{PA}$ .

**4.3. Effect of Gas–Liquid Properties (Model Validation).** *4.3.1. Effect of the Gas Velocity.* To characterize the capture process, the  $CO_2$  removal efficiency and flux can be calculated using the equations below

$$\eta = \left(1 - \frac{C_{\text{out}}}{C_0}\right) \times 100\% \tag{7}$$

$$J_{\text{CO}_2} = \frac{273.15(C_0 Q_0 - C_{\text{out}} Q_{\text{out}})}{22.4TS} \tag{8}$$

where  $\eta$  is the removal efficiency of CO<sub>2</sub>,  $C_{\text{out}}$  is the outlet concentration of CO<sub>2</sub>,  $C_0$  denotes the inlet concentration of CO<sub>2</sub>,  $J_{\text{CO}_2}$  is the CO<sub>2</sub> flux,  $Q_0$  is the inlet volumetric flow rate,  $Q_{\text{out}}$  is the outlet volumetric flow rate, T is the operating temperature, and S is the membrane area, respectively.  $C_{\text{out}}$  is obtained by integrating the local concentration at the outlet of the shell side

$$C_{\text{out}} = \frac{\iint_{z=0} C(\mathbf{r}) \, dA}{\iint_{z=0} dA}$$
(9)

The gas velocity is a key factor for CO2 absorption using a HFMC. As illustrated in Figure 5, the effects of gas velocity on membrane performance are investigated. The removal efficiencies of CO2 for five absorbents have a downward trend in Figure 5A. This is due to the reason that the residence time shortens with increasing gas velocity, which is unfavorable for the CO<sub>2</sub> capture process.<sup>35</sup> Additionally, the CO<sub>2</sub> removal efficiencies of H<sub>2</sub>O and TEA are much lower than those of the other three solutions. Figure 5B illustrates that the flux of CO<sub>2</sub> increases with increasing gas velocity. This can be explained by the enhancement of the mass-transfer process in the HFMC. The mass-transfer resistance increases and the layer of the gas phase reduces with increasing the velocity of the gas mixture. In addition, it can be seen from Figure 5C that all of the five absorbents show similar behaviors in the purified CH<sub>4</sub> percentage. A lower gas velocity has a positive effect on the biogas purification. The CH<sub>4</sub> concentrations of PA and MEA reach 100% at the gas velocity of 0.19 m s<sup>-1</sup>. Figure 5 also reveals that the simulation results are in good accordance with the available experimental data.

4.3.2. Effect of the Liquid Velocity. The effects of the liquid velocity on the membrane performance are illustrated in the velocity range of 0.046–0.08 m s<sup>-1</sup> in Figure 6. With the increase in solvent velocity, the CO<sub>2</sub> removal process is enhanced. In this case, the CO<sub>2</sub> concentration gradient between the tube side and shell side increases with increasing liquid velocity. As plotted in Figure 6A, the separation efficiencies of H<sub>2</sub>O and TEA have a slight change because of physical absorption and a low chemical reaction rate. On the other hand, a smaller liquid velocity reduces the liquid phase layer and the total resistance for mass transfer.8 Therefore, the CO<sub>2</sub> flux increases for all absorbents with an increase of absorbent velocity. The reported phenomenon can be observed from Figure 6B. With respect to this figure, it can be concluded that a higher liquid velocity is good for CO<sub>2</sub> capture. For CO<sub>2</sub> flux, the comparison between modeling results and experimental data is also investigated using four chemical solutions as absorbents in Figure 6B.

4.3.3. Effect of the  $CO_2$  Content. The changes of fermenting materials always cause the variation of the components of biogas in industrial applications. The effect of the  $CO_2$  content from 30 to 50% on the HFMC performance in the presence of different aqueous solutions is shown in Figure 7. It is clearly seen that the removal efficiency of  $CO_2$  decreases when the  $CO_2$  content increases in Figure 7A. This is due to the fact that more unreacted  $CO_2$  flows out of the module with a higher content of  $CO_2$  in the gas mixture. <sup>41</sup> Moreover, PA solution shows better  $CO_2$  capture

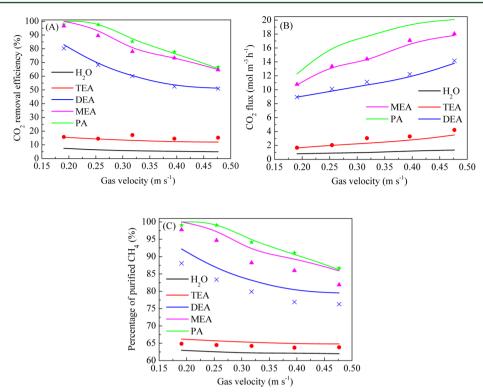


Figure 5. Effect of the gas velocity on the membrane performance (lines, simulation results, symbols, experimental data;  $^4$  liquid concentration, 10 wt %; T, 303 K; and  $U_0$ , 0.06 m s<sup>-1</sup>).

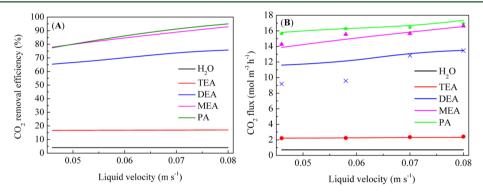


Figure 6. Effect of the liquid velocity on the membrane performance (lines, simulation results, symbols, experimental data;  $^4$  liquid concentration, 20 wt %; T, 303 K; and  $U_e$ , 0.32 m s<sup>-1</sup>).

efficiency within the scope of the  $\mathrm{CO}_2$  content. Even at a high  $\mathrm{CO}_2$  content of 50%, the corresponding  $\mathrm{CO}_2$  removal efficiency is 86.4%, which shows good membrane performance. In the meantime, it turns out that the  $\mathrm{CH}_2$  concentration declines, while the  $\mathrm{CO}_2$  content increases. As demonstrated in Figure 7B, the  $\mathrm{CO}_2$  flux grows up with the augment of the  $\mathrm{CO}_2$  concentration in the feed gas. This is due to the reason that a higher  $\mathrm{CO}_2$  concentration improves the driving force for the mass-transfer process of gas. As observed, there is a good agreement between the reported experimental data<sup>4</sup> and simulation results.

4.3.4. Effect of the Liquid Concentration. Figure 8 presents the influence of the solvent concentration (5, 10, 20, and 30 wt %) on the membrane performance. Chemical absorbents show better membrane performance, and the absorption performance of physical solution remains the same with the increase in the liquid concentration. As shown in panels A and C of Figure 8, both CO<sub>2</sub> absorption efficiency and CH<sub>4</sub> concentration after purification reach about 90% when using

30 wt % DEA, MEA, and PA solutions. Also, the  $\rm CO_2$  flux gradually increases with an increase of the liquid concentration because of a higher chemical reaction rate. The numerical observation is in perfect agreement with experimental data. As observed, the change in the liquid concentration has a major positive effect on the biogas purification for solutions of MEA, MEA, and PA. For instance, when considering PA as the absorbent, the simulated percentage of  $\rm CO_2$  removal,  $\rm CO_2$  flux, and percentage of purified  $\rm CH_4$  increase from 61.6%, 11.58 mol m<sup>-3</sup> h<sup>-1</sup>, and 84.6% to 97.4%, 18.4 mol m<sup>-3</sup> h<sup>-1</sup>, and 99.0%, respectively.

**4.4. Effect of the Membrane Structure.** *4.4.1. Effect of the Fiber Diameter.* Figure 9 shows the effect of the fiber diameter on the contactor performance. As seen, bigger fibers provide better absorption performance. Under this condition, more solutions react with  $CO_2$  in the tube side, which benefits the  $CO_2$  capture. <sup>43</sup> As illustrated in Figure 9A, the  $CO_2$  capture efficiencies of 240  $\mu$ m fiber are about twice of those of 400  $\mu$ m fiber. At the same time, the purified  $CH_4$  concentration

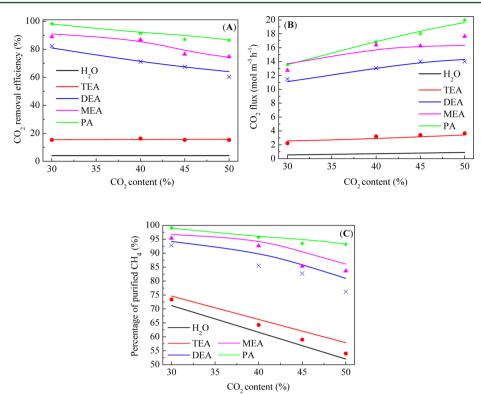
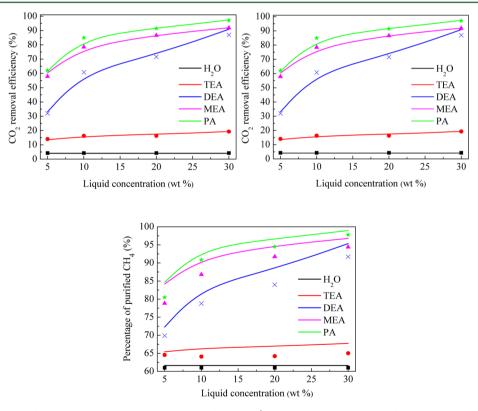


Figure 7. Effect of the CO<sub>2</sub> content on the membrane performance (lines, simulation results, symbols, experimental data; <sup>4</sup> liquid concentration, 20 wt %; T, 303 K;  $U_{\rm b}$  0.06 m s<sup>-1</sup>; and  $U_{\rm ev}$  0.32 m s<sup>-1</sup>).



**Figure 8.** Effect of the liquid concentration on the membrane performance (lines, simulation results, symbols, experimental data;  $^4$  T, 303 K;  $U_{\rm b}$  0.06 m s $^{-1}$ ; and  $U_{\rm g}$  0.32 m s $^{-1}$ ).

significantly increases with an increase in the diameter of the membrane fiber. On the other hand, the liquid velocity increases when a hollow fiber membrane with a smaller inner diameter is considered. As demonstrated in panels B and C of Figure 9, the  ${\rm CO_2}$  flux and  ${\rm CH_4}$  concentration after biogas upgrading also considerably increase.

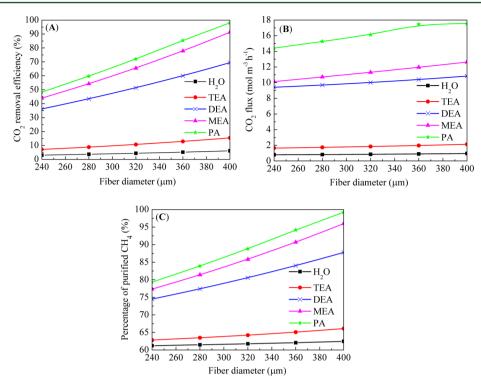


Figure 9. Effect of the fiber diameter on the membrane performance (liquid concentration, 10 wt %; T, 303 K; U<sub>1</sub>, 0.06 m s<sup>-1</sup>; and U<sub>2</sub>, 0.32 m s<sup>-1</sup>).

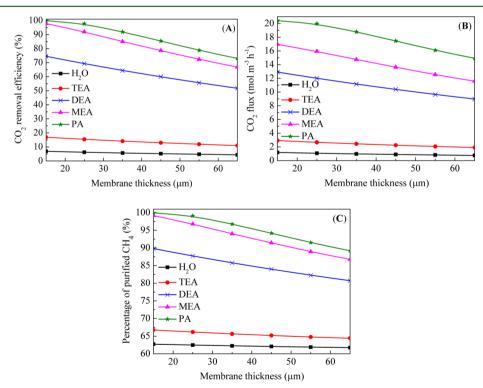


Figure 10. Effect of the membrane thickness on the membrane performance (liquid concentration, 10 wt %; T, 303 K;  $U_{\nu}$  0.06 m s<sup>-1</sup>; and  $U_{g^{\prime}}$  0.32 m s<sup>-1</sup>).

4.4.2. Effect of the Membrane Thickness. Figure 10 depicts the absorption performance of the membrane as a function of the membrane thickness. The thickness in the range from 15 to 65  $\mu$ m is observed. Considering this figure, CO<sub>2</sub> removal efficiency and flux and CH<sub>4</sub> concentration at given conditions have a downward trend with increasing the thickness of the membrane. This is attributed to the increase of resistance along the pores with a

thicker membrane. <sup>43</sup> With thinner thicknesses of membrane, the HFMC achieves a higher contactor performance. As observed in panels A and B of Figure 10, the percentages of captured  $CO_2$  and purified  $CH_4$  are higher than 97 and 99% using MEA and PA solutions in the hollow fiber module, respectively.

4.4.3. Effect of the Fiber Length. It is noted that the increase in the membrane module length enhances the biogas upgrading

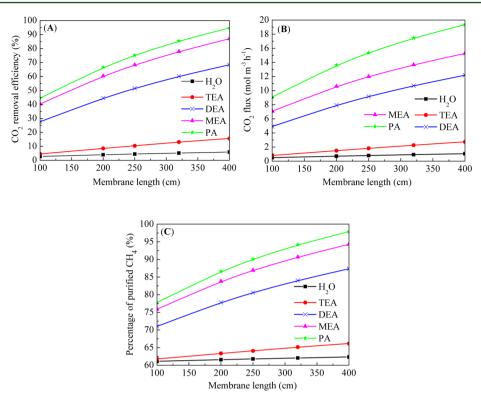


Figure 11. Effect of the fiber length on the membrane performance (liquid concentration, 10 wt %; T, 303 K;  $U_{\nu}$  0.06 m s<sup>-1</sup>; and  $U_{\nu}$ , 0.32 m s<sup>-1</sup>).

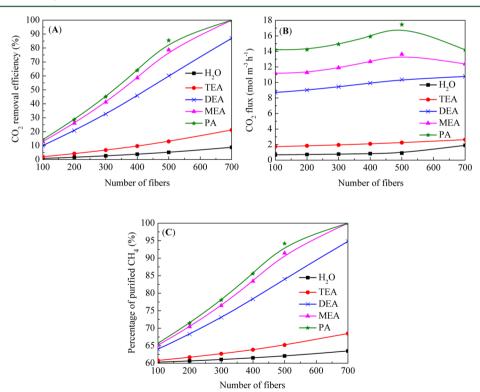


Figure 12. Effect of the number of fibers on the membrane performance (liquid concentration, 10 wt %; T, 303 K; U<sub>b</sub> 0.06 m s<sup>-1</sup>; and U<sub>w</sub> 0.32 m s<sup>-1</sup>).

process in Figure 11. The concentrations and velocities of gas and liquid are kept constant in this simulation. For a long fiber module, it offers more space for reaction between  $CO_2$  and solution. The reacting time for gas and liquid is high enough, resulting in saturated aqueous solutions at the outlet of the contactor.<sup>44</sup> For example, when using PA solution as the

absorbent, the  $\mathrm{CO}_2$  absorption efficiency and flux significantly increase by 50.2% and 10.3 mol m<sup>-3</sup> h<sup>-1</sup> with the increment of the hollow fiber module length in the range of 100–400 cm, respectively. In the meantime, the  $\mathrm{CH}_4$  content in the production of upgrading biogas also remarkably increases by 20.1%. Although increasing the module length improves the removal

performance, the costs on the fabrication of membrane contactors simultaneously increase. Thus, the absorption performance and economy should be taken into consideration in the design and selection of optimum module dimensions.

4.4.4. Effect of the Number of Fibers. Figure 12 reveals the effect of the number of fibers on the HFMC performance. As the number of fibers increases from 100 to 700, both the CO<sub>2</sub> removal efficiency and CH<sub>4</sub> concentration increase. Especially for these solvents that have a high reaction rate with CO2, the two values increase roughly 90 and 35%, respectively. This is due to the fact that increasing the number of fibers results in a higher gas-liquid contact area and residence time inside the module. In addition, it is noted that the maximum of CO<sub>2</sub> flux coincides with the initial fiber dimensions of 500 fibers when using MEA and PA as absorbents. This can be explained by the simultaneous effect of the increased amount of absorbed CO2 and the growth of the mass-transfer interface, which is illustrated by S in eq 8. Further, this phenomenon occurs also because the two solvents have a higher reaction rate with CO<sub>2</sub>. However, the amount of fibers is limited and could be perfectly embedded in the module.

### 5. CONCLUSION

The aim of the present study was to study the potential interest of a membrane absorption process for CO<sub>2</sub> capture in biogas. A comprehensive 2D mass-transfer model was developed and solved considering non-wetted conditions for a countercurrent gas-liquid flow arrangement in the HFMC. Five kinds of absorbents (H<sub>2</sub>O, TEA, DEA, MEA, and PA) were performed in the simulations. The established model showed excellent predictions, with experimental data reporting the influences of different gas and liquid parameters on the performance of the membrane contactor. Thus, the proposed model was capable of predicting the CO<sub>2</sub> absorption and CH<sub>4</sub> recovery processes in a hollow fiber membrane module. The key findings in this study are listed as follows: (1) The influences of gas and absorbent solution parameters on the membrane performance have been thoroughly investigated. One of the key results provided that increasing the gas velocity and CO<sub>2</sub> content decreased CO<sub>2</sub> removal efficiency and CH<sub>4</sub> recovery and increased CO<sub>2</sub> flux; in contrast, the increases in the absorbent velocity and concentration enhanced the membrane performance. (2) According to the results from the simulations, a smaller fiber inner diameter and membrane thickness and a longer module length were good for the biogas upgrading process. Particularly, it was found that the highest CO<sub>2</sub> flux coincided with the original fiber dimensions of 500 fibers when using MEA and PA as absorbents. This was due to the simultaneous effect of the increased amount of absorbed CO<sub>2</sub> and growth of the mass-transfer interface. (3) It was also indicated that PA provided better purification performance of the contactor than other absorbents. The order for CO<sub>2</sub> absorption efficiency and CH<sub>4</sub> recovery was PA > MEA > DEA > TEA >  $H_2O$ . Therefore, PA solution was proven as an advantageous aqueous solvent for capturing CO<sub>2</sub>. (4) Among all of the factors of membrane properties, the fiber number, contactor length, and inner fiber diameter had a significant effect on the biogas upgrading process compared to the membrane thickness. This was due to the reason that the mass-transfer process of gas and absorbent dramatically enhanced. With regard to the parameters of the fluid, the liquid concentration and gas velocity were the major influences under these testing conditions. To obtain higher CH<sub>4</sub> production purity, the experiment should be operated at lower velocity of the gas phase and higher liquid concentration, which were beneficial to the absorption of CO<sub>2</sub>.

### AUTHOR INFORMATION

### **Corresponding Author**

\*Telephone: +862365103114. Fax: +862365111832. E-mail: yunfeiyan@cqu.edu.cn.

### **Author Contributions**

<sup>†</sup>Yunfei Yan and Zhien Zhang contributed equally to this study and share first authorship.

### **Notes**

The authors declare no competing financial interest.

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### ■ NOMENCLATURE

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C = \text{concentration (mol m}^{-3})
D = \text{diffusion coefficient (m}^2 \text{ s}^{-1})
J = \text{flux (mol m}^{-2} \text{ h}^{-1})
k = \text{reaction rate constant (m}^3 \text{ mol}^{-1} \text{ s}^{-1})
L = \text{fiber length (cm)}
n = \text{number of fibers}
Q = \text{volumetric flow rate (m}^3 \text{ s}^{-1})
r = \text{radial coordinate } (\mu \text{m})
R = \text{gas constant (m}^3 \text{ atm mol}^{-1} \text{ K}^{-1})
R_i = \text{overall reaction rate of any species (mol m}^{-3} \text{ s}^{-1})
T = \text{temperature (K)}
U = \text{velocity (m s}^{-1})
\overline{U} = \text{average velocity (m s}^{-1})
```

### **Greek Letters**

```
 \begin{split} \varepsilon &= \text{porosity} \\ \tau &= \text{tortuosity} \\ \theta &= \text{packing density} \\ \delta &= \text{membrane thickness (m)} \\ \eta &= \text{CO}_2 \text{ removal efficiency (\%)} \end{split}
```

### Subscripts

```
g = gas
l = liquid
mem = membrane
out = outlet
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